

Dynamics of strongly interacting parton-hadron matter

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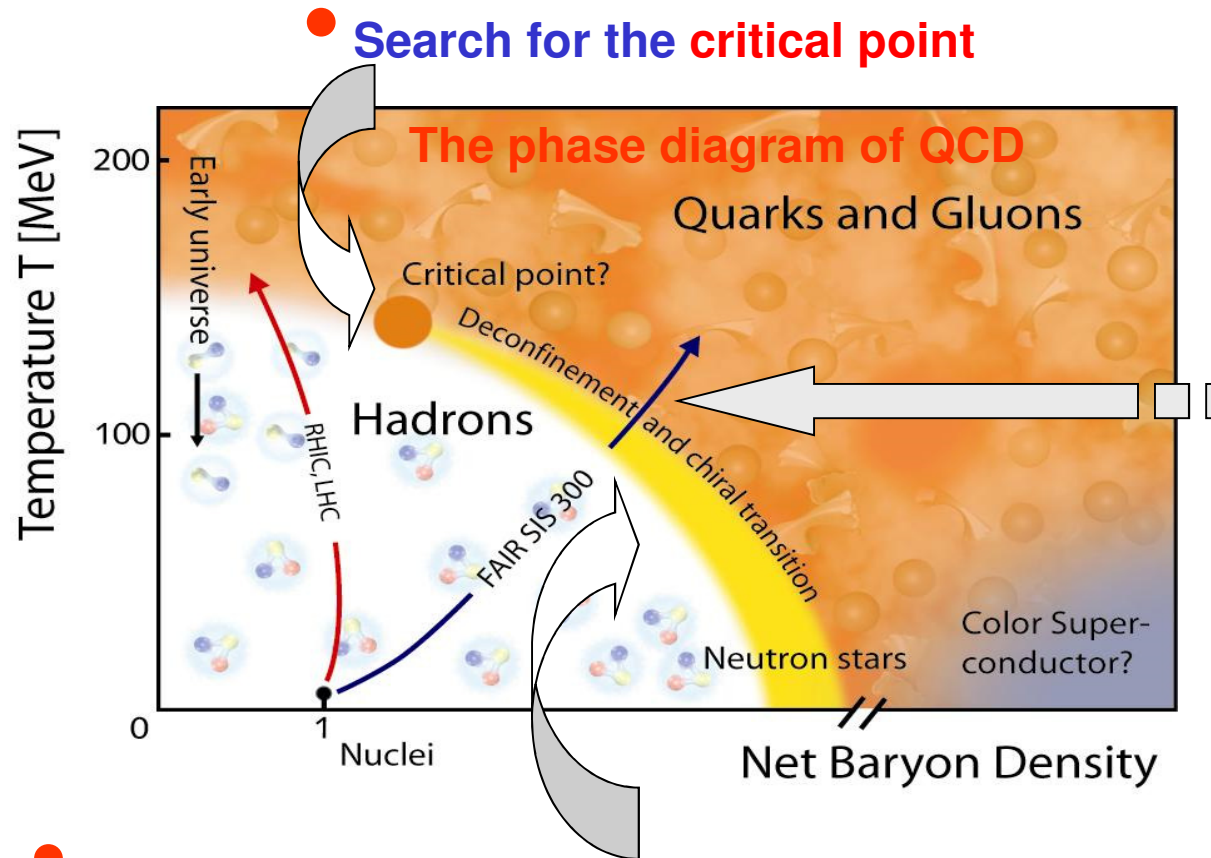
for the PHSD group



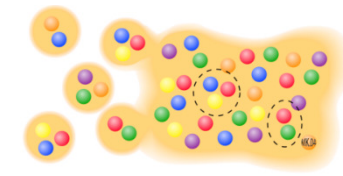
EMMI - NQM seminar
20 April 2016



The ,holy grail‘ of heavy-ion physics:

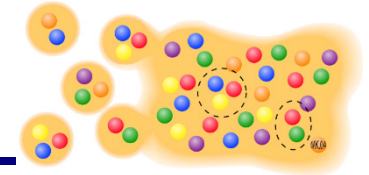


- Study of the **phase transition** from hadronic to partonic matter – **Quark-Gluon-Plasma**



- Study of the **in-medium** properties of hadrons at high baryon density and temperature
- Search for the signals of **chiral symmetry restoration**

From SIS to LHC: from hadrons to partons



The goal: to study of the phase transition from hadronic to partonic matter and properties of the Quark-Gluon-Plasma on a **microscopic level**

→ need a **consistent non-equilibrium transport model**

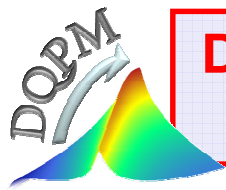
- ❑ with explicit **parton-parton interactions** (i.e. between quarks and gluons)
- ❑ explicit **phase transition** from hadronic to partonic degrees of freedom
- ❑ **IQCD EoS** for partonic phase (‘cross over’ at $\mu_q=0$)

❑ **Transport theory for strongly interacting systems:** off-shell Kadanoff-Baym equations for the Green-functions $S_h^<(x,p)$ in phase-space representation for the **partonic** and **hadronic phase**



Parton-Hadron-String-Dynamics (PHSD)

QGP phase is described by



**Dynamical QuasiParticle Model
(DQPM)**

W. Cassing, E. Bratkovskaya, PRC 78 (2008) 034919;
NPA831 (2009) 215;
W. Cassing, EPJ ST 168 (2009) 3

A. Peshier, W. Cassing, PRL 94 (2005) 172301;
Cassing, NPA 791 (2007) 365; NPA 793 (2007)

Interacting quasiparticles

- Entropy density of interacting bosons and fermions in quasiparticle limit (G. Baym 1998):

$$\begin{aligned}
 s^{dqp} = & -d_g \int \frac{d\omega}{2\pi} \frac{d^3 p}{(2\pi)^3} \frac{\partial n_B}{\partial T} (\text{Im} \ln(-\Delta^{-1}) + \text{Im} \Pi \text{Re} \Delta) && \text{gluons} \\
 & -d_q \int \frac{d\omega}{2\pi} \frac{d^3 p}{(2\pi)^3} \frac{\partial n_F((\omega - \mu_q)/T)}{\partial T} (\text{Im} \ln(-S_q^{-1}) + \text{Im} \Sigma_q \text{Re} S_q) && \text{quarks} \\
 & -d_{\bar{q}} \int \frac{d\omega}{2\pi} \frac{d^3 p}{(2\pi)^3} \frac{\partial n_F((\omega + \mu_q)/T)}{\partial T} (\text{Im} \ln(-S_{\bar{q}}^{-1}) + \text{Im} \Sigma_{\bar{q}} \text{Re} S_{\bar{q}}) && \text{antiquarks}
 \end{aligned}$$

with $d_g = 16$ for 8 transverse gluons and $d_q = 18$ for quarks with 3 colors, 3 flavors and 2 spin projections

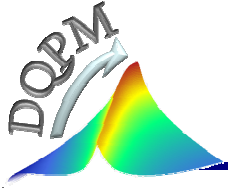
$$\begin{aligned}
 \text{Bose distribution function:} & \quad n_B(\omega/T) = (\exp(\omega/T) - 1)^{-1} \\
 \text{Fermi distribution function:} & \quad n_F((\omega - \mu_q)/T) = (\exp((\omega - \mu_q)/T) + 1)^{-1}
 \end{aligned}$$

- Gluon propagator: $\Delta^{-1} = P^2 - \Pi$ & Quark propagator $S_q^{-1} = P^2 - \Sigma_q$ ($P^2 = \omega^2 - \vec{p}^2$)

→ Properties of a system in many-body theory are defined by the complex self-energies, i.e. for QGP - quark self-energy Σ_q and gluon self-energy Π
 How to model Σ_q and Π ?!

e.g.: nonperturbative Dyson-Schwinger Bethe-Salpeter approaches

Simple approximation → DQPM



Dynamical QuasiParticle Model (DQPM) - Basic ideas:

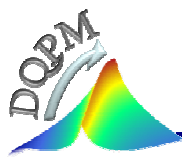
DQPM describes QCD properties in terms of ,resummed' single-particle Green's functions (propagators) – in the sense of a two-particle irreducible (2PI) approach:

$$\begin{aligned} \text{gluon propagator: } \Delta^{-1} &= P^2 - \Pi & \& \quad \text{quark propagator } S_q^{-1} &= P^2 - \Sigma_q \\ \text{gluon self-energy: } \Pi &= M_g^2 - i2\Gamma_g\omega & \& \quad \text{quark self-energy: } \Sigma_q &= M_q^2 - i2\Gamma_q\omega \end{aligned}$$

(scalar approximation)

- the resummed properties are specified by complex (retarded) self-energies which depend on temperature:
 - the real part of self-energies (Σ_q, Π) describes a dynamically generated mass (M_q, M_g);
 - the imaginary part describes the interaction width of partons (Γ_q, Γ_g)
- space-like part of energy-momentum tensor $T_{\mu\nu}$ defines the potential energy density and the mean-field potential (1PI) for quarks and gluons (U_q, U_g)
- 2PI framework guaranties a consistent description of the system in- and out-off equilibrium on the basis of Kadanoff-Baym equations with proper states in equilibrium

A. Peshier, W. Cassing, PRL 94 (2005) 172301;
Cassing, NPA 791 (2007) 365; NPA 793 (2007)



The Dynamical QuasiParticle Model (DQPM) – v.1 (as in PHSD)

Properties of interacting quasi-particles:
massive quarks and gluons (q, \bar{q}, g)
with **Lorentzian spectral functions**:

$$A_i(\omega, T) = \frac{4\omega\Gamma_i(T)}{(\omega^2 - \vec{p}^2 - M_i^2(T))^2 + 4\omega^2\Gamma_i^2(T)}$$

$(i = q, \bar{q}, g)$

■ Modeling of the quark/gluon masses and widths → **HTL limit at high T**

■ **quarks:**

mass: $M_{q(\bar{q})}^2(T) = \frac{N_c^2 - 1}{8N_c} g^2 \left(T^2 + \frac{\mu_q^2}{\pi^2} \right)$

width: $\Gamma_{q(\bar{q})}(T) = \frac{1}{3} \frac{N_c^2 - 1}{2N_c} \frac{g^2 T}{8\pi} \ln\left(\frac{2c}{g^2} + 1\right)$

■ **gluons:**

$$M_g^2(T) = \frac{g^2}{6} \left(\left(N_c + \frac{N_f}{2} \right) T^2 + \frac{N_c}{2} \sum_q \frac{\mu_q^2}{\pi^2} \right)$$

$$\Gamma_g(T) = \frac{1}{3} N_c \frac{g^2 T}{8\pi} \ln\left(\frac{2c}{g^2} + 1\right)$$

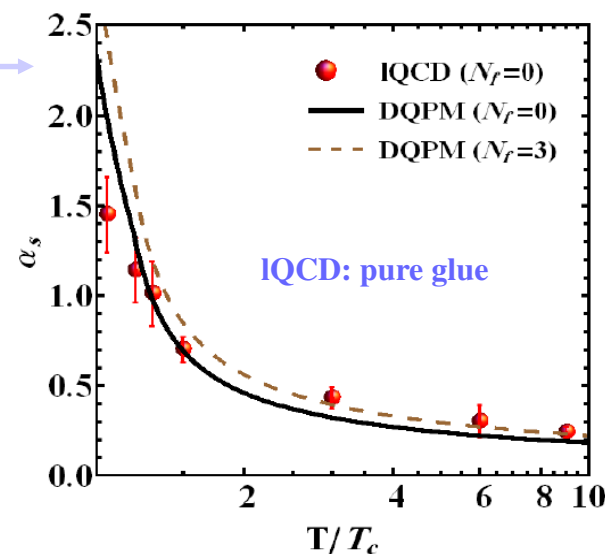
$N_c = 3, N_f = 3$

■ **running coupling: T-dependent $\alpha_s(T)$**

$$\alpha_s(T) = \frac{g^2(T)}{4\pi} = \frac{12\pi}{(11N_c - 2N_f) \ln[\lambda^2(T/T_c - T_s/T_c)^2]}$$

□ **fit to lattice (IQCD) results** (e.g. entropy density)

with 3 parameters: $T_s/T_c = 0.46$; $c = 28.8$; $\lambda = 2.42$
(for pure glue $N_f = 0$)



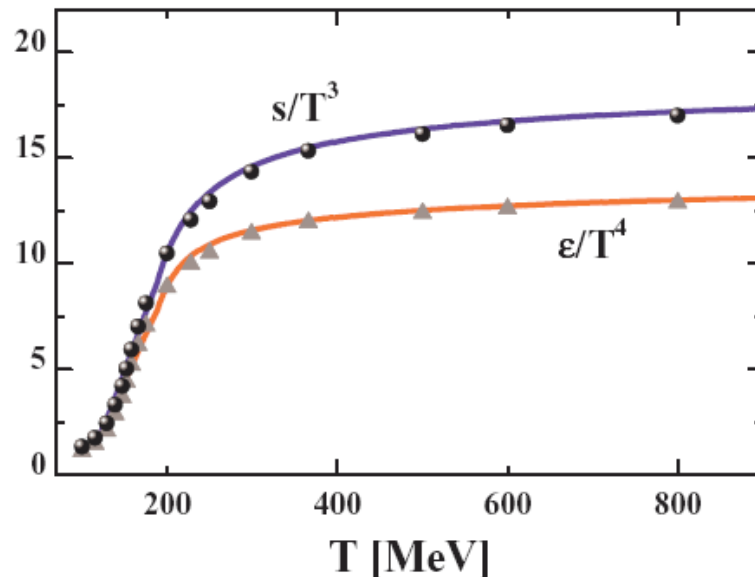
DQPM: Peshier, Cassing, PRL 94 (2005) 172301;
Cassing, NPA 791 (2007) 365; NPA 793 (2007)

DQPM thermodynamics ($N_f=3$) and IQCD

entropy $s = \frac{\partial P}{\partial T} \rightarrow$ pressure P

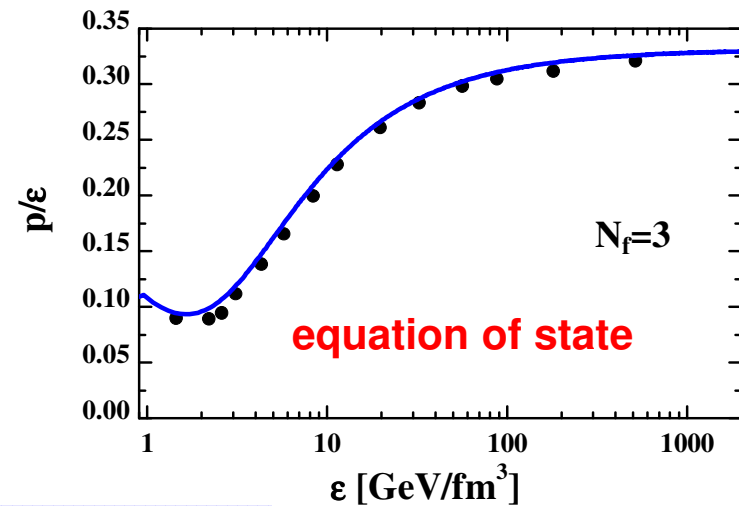
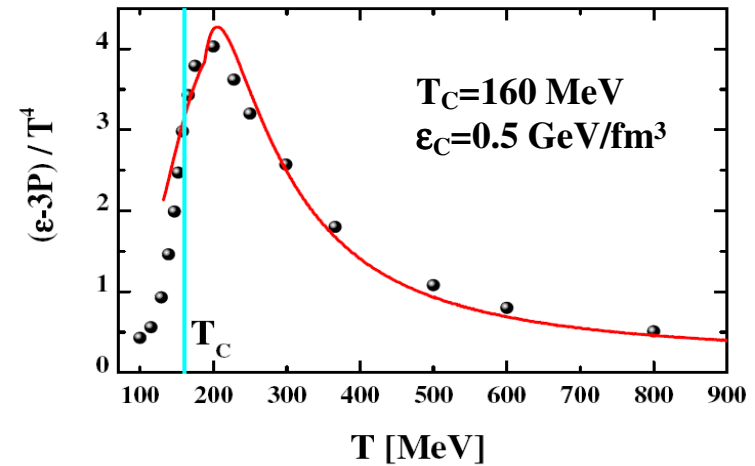
energy density: $\epsilon = Ts - P$

IQCD: Wuppertal-Budapest group
Y. Aoki et al., JHEP 0906 (2009) 088.



interaction measure:

$$W(T) := \epsilon(T) - 3P(T) = Ts - 4P$$



DQPM gives a good description of IQCD results !

Time-like and space-like quantities

Separate time-like and space-like single-particle quantities by $\Theta(+P^2)$, $\Theta(-P^2)$:

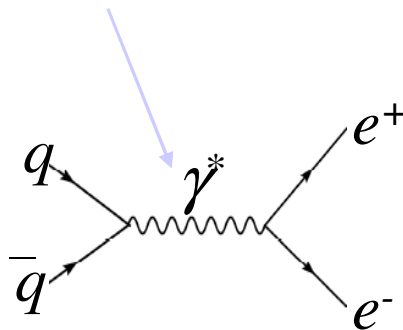
$$\tilde{\text{Tr}}_g^\pm \dots = d_g \int \frac{d\omega}{2\pi} \frac{d^3p}{(2\pi)^3} 2\omega \rho_g(\omega) \Theta(\omega) n_B(\omega/T) \underline{\Theta(\pm P^2)} \dots \quad \text{gluons}$$

$$\tilde{\text{Tr}}_q^\pm \dots = d_q \int \frac{d\omega}{2\pi} \frac{d^3p}{(2\pi)^3} 2\omega \rho_q(\omega) \Theta(\omega) n_F((\omega - \mu_q)/T) \underline{\Theta(\pm P^2)} \dots \quad \text{quarks}$$

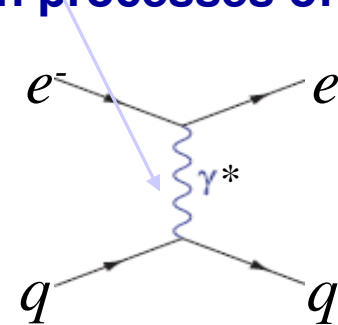
$$\tilde{\text{Tr}}_{\bar{q}}^\pm \dots = d_{\bar{q}} \int \frac{d\omega}{2\pi} \frac{d^3p}{(2\pi)^3} 2\omega \rho_{\bar{q}}(\omega) \Theta(\omega) n_F((\omega + \mu_q)/T) \underline{\Theta(\pm P^2)} \dots \quad \text{antiquarks}$$

Time-like: $\Theta(+P^2)$: particles may decay to **real particles** or interact

Examples:



Space-like: $\Theta(-P^2)$: particles are **virtuell** and appear as **exchange quanta** in interaction processes of real particles

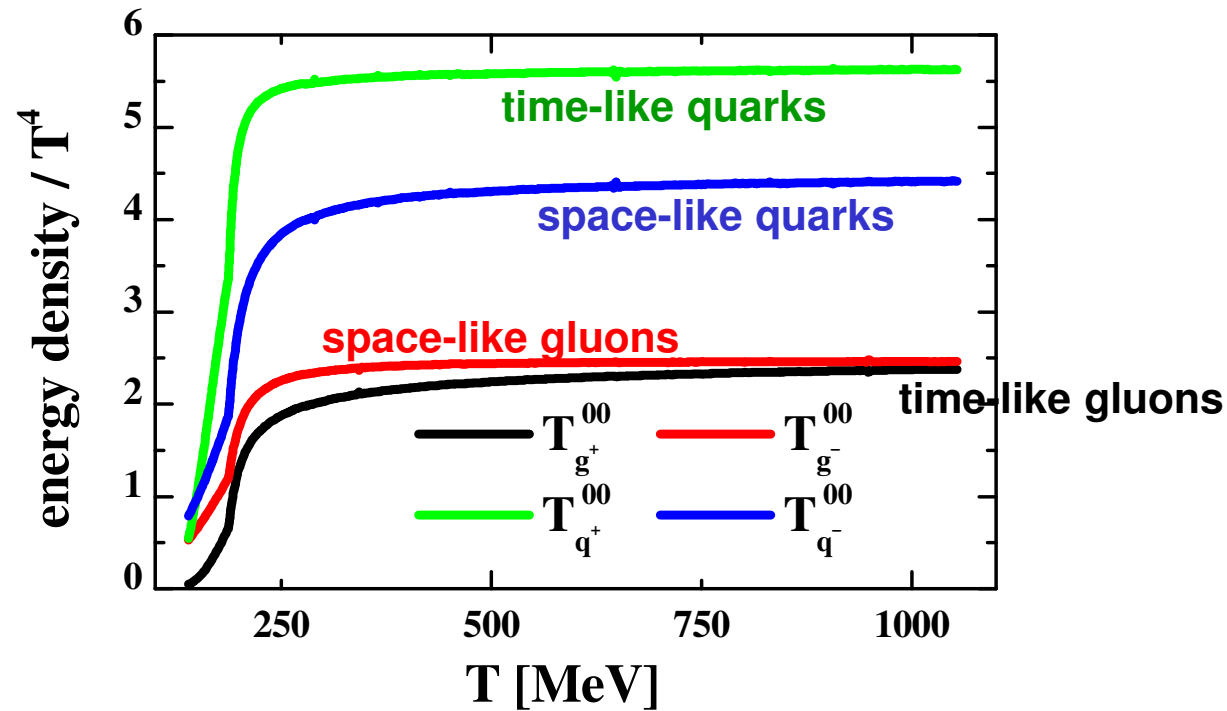


Time-like and 'space-like' energy densities

Time/space-like part of energy-momentum tensor $T_{\mu\nu}$ for quarks and gluons:

$$T_{00,x}^{\pm}(T) = \tilde{T}r_x^{\pm} \omega$$

x: gluons, quarks, antiquarks



- space-like energy density of quarks and gluons = ~1/3 of total energy density
- space-like energy density dominates for gluons
- space-like parts are identified with potential energy densities

Mean-field potential for quasiparticles

- Space-like part of energy-momentum tensor $T_{\mu\nu}$ defines the **potential energy density**:

$$V_p(T, \mu_q) = T_{g-}^{00}(T, \mu_q) + T_{q-}^{00}(T, \mu_q) + T_{\bar{q}-}^{00}(T, \mu_q)$$

space-like gluons **space-like quarks+antiquarks**

→ **mean-field scalar potential (1PI) for quarks and gluons (U_q, U_g) vs scalar density ρ_s** :

$$U_s(\rho_s) = \frac{dV_p(\rho_s)}{d\rho_s}$$

$$U_q = U_s, \quad U_g \sim 2U_s$$

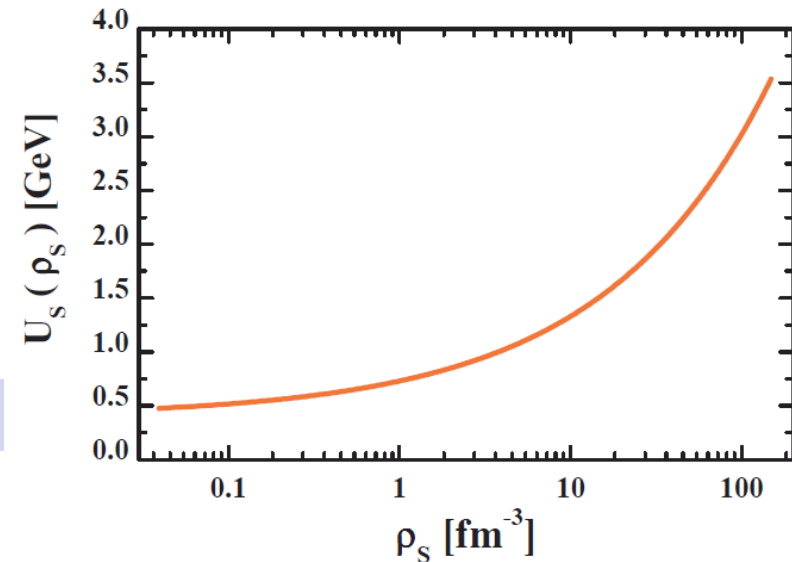
Quasiparticle potentials (U_q, U_g) are repulsive !

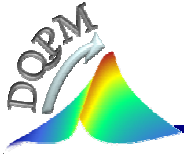
→ **the force acting on a quasiparticle j :**

$$F \sim M_j/E_j \nabla U_s(x) = M_j/E_j dU_s/d\rho_s \nabla \rho_s(x)$$

$$j = g, q, \bar{q}$$

→ **accelerates particles**





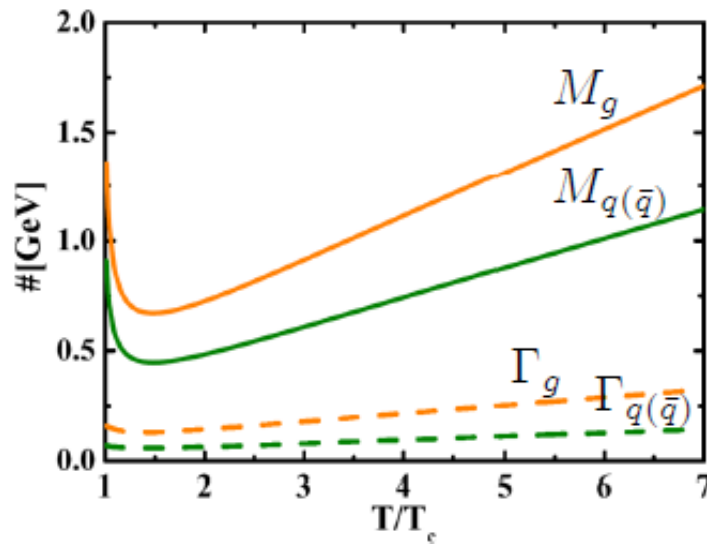
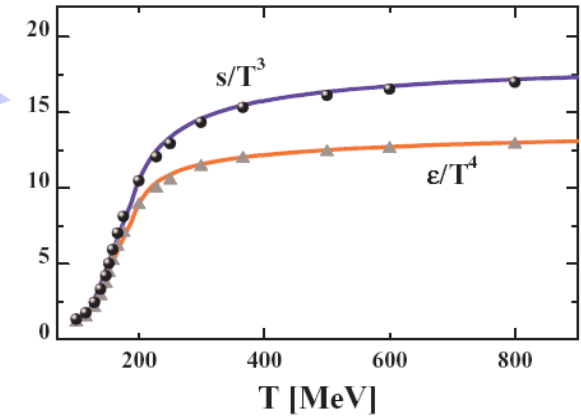
The Dynamical QuasiParticle Model (DQPM)

➤ fit to lattice (IQCD) results (e.g. entropy density)

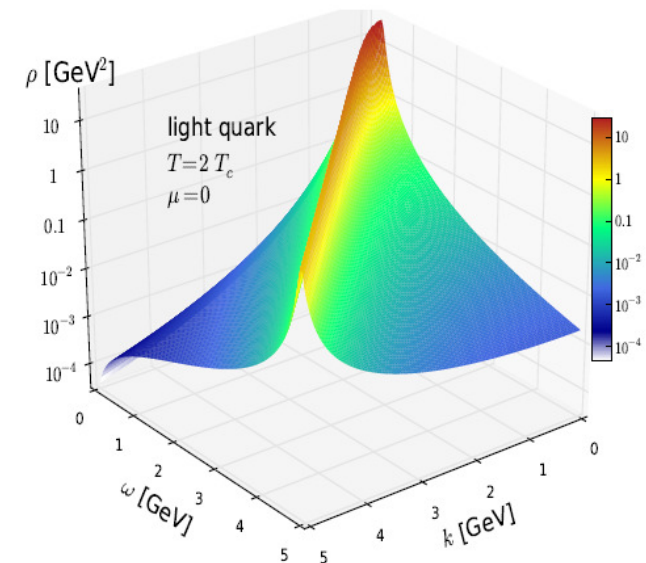
* BMW IQCD data S. Borsanyi et al., JHEP 1009 (2010) 073

➔ Quasiparticle properties:

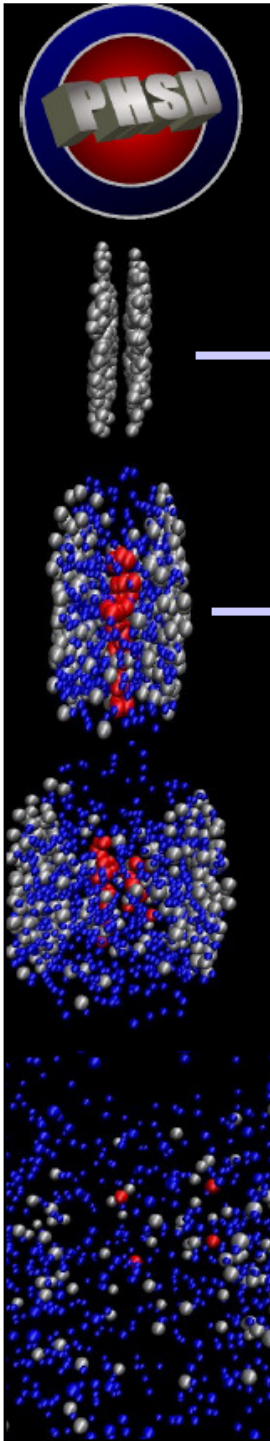
■ large width and mass for gluons and quarks



$T_c = 158 \text{ MeV}$
 $\epsilon_c = 0.5 \text{ GeV/fm}^3$

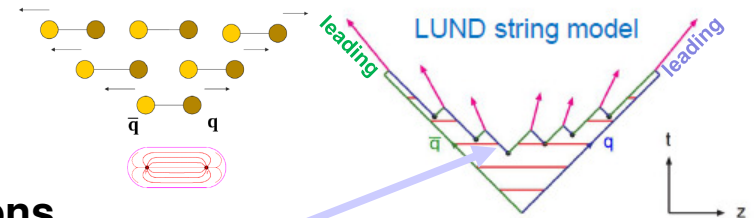


- DQPM matches well lattice QCD
- DQPM provides mean-fields (1PI) for gluons and quarks as well as effective 2-body interactions (2PI)
- DQPM gives transition rates for the formation of hadrons → PHSD



I. PHSD - basic concept

I. From hadrons to QGP:



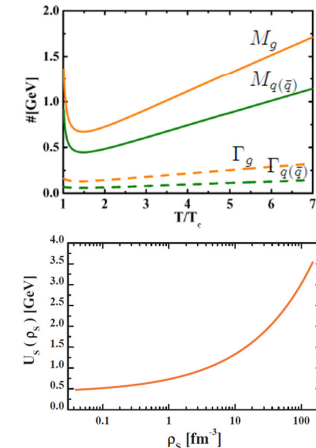
□ Initial A+A collisions – as in HSD:

- string formation in primary NN collisions
- string decay to pre-hadrons (= new produced secondary hadrons: B - baryons, m - mesons) → ,**flavor chemistry**‘ from strings

□ Formation of initial QGP stage - if local energy density $\varepsilon > \varepsilon_c = 0.5 \text{ GeV/fm}^3$:

I. Dynamical Quasi-Particle Model (DQPM) defines:

- 1) properties of quasiparticles in equilibrium, i.e. masses $M_q(T)$ and widths $\Gamma_q(T)$ ($T \rightarrow \varepsilon$ by IQCD EoS)
- 2) ,chemistry‘ of ,initial state‘ of QGP: number of q , $q\bar{q}$, g
- 3) ,energy balance‘, i.e. the fraction of mean-field quark and gluon potentials U_q , U_g from the energy density ε

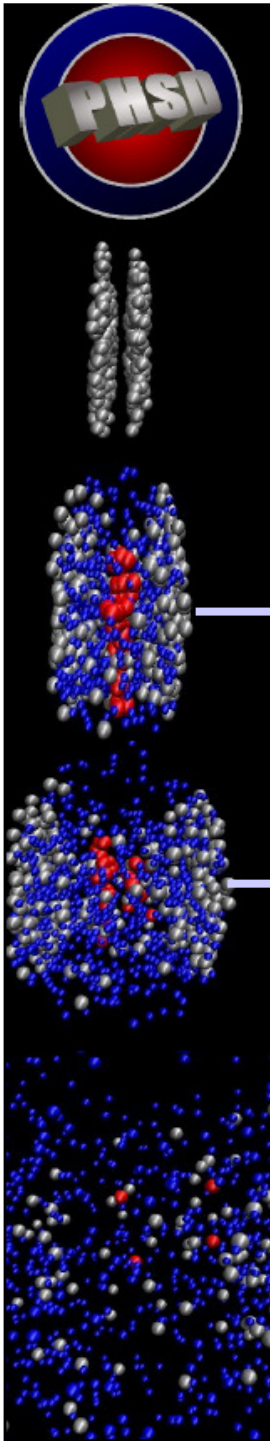


II. Realization of the initial QGP stage from DQPM in the PHSD:

by dissolution of pre-hadrons (keep ,leading‘ hadrons!) into massive colored quarks (and gluons) + mean-field energy

$$B \rightarrow qqq, \quad \tilde{m} \rightarrow q\bar{q}, \quad (q\bar{q}) \Rightarrow g \quad \forall U_q, U_g$$

→ allows to keep initial non-equilibrium momentum anisotropy !



II. PHSD - basic concept

II. Partonic phase - QGP:

- Propagation of quarks and gluons (= ‚dynamical quasiparticles‘) with off-shell spectral functions (width, mass) defined by the DQPM in **self-generated mean-field potential** for quarks and gluons U_q, U_g
- EoS of partonic phase: ‚crossover‘ from lattice QCD (fitted by DQPM)
- (quasi-) elastic and inelastic parton-parton interactions: using the effective cross sections from the DQPM

- (quasi-) elastic collisions:

$$q + q \rightarrow q + q \quad g + q \rightarrow g + q$$

$$q + \bar{q} \rightarrow q + \bar{q} \quad g + \bar{q} \rightarrow g + \bar{q}$$

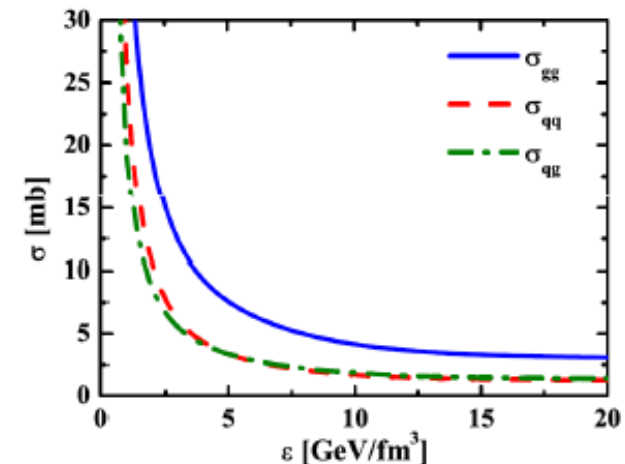
$$\bar{q} + \bar{q} \rightarrow \bar{q} + \bar{q} \quad g + g \rightarrow g + g$$

- inelastic collisions:

(Breit-Wigner cross sections)

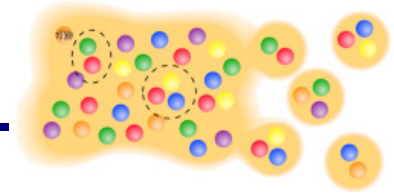
$$\left\{ \begin{array}{l} q + \bar{q} \rightarrow g \\ g \rightarrow q + \bar{q} \end{array} \right.$$

$$\left\{ \begin{array}{l} q + \bar{q} \rightarrow g + g \\ g \rightarrow g + g \end{array} \right. \text{ suppressed (<1\%)} \\ \text{due to the large mass of gluons}$$





III. PHSD - basic concept

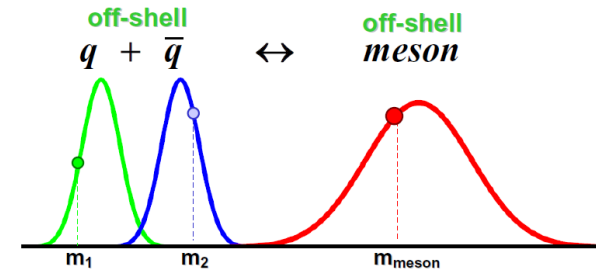


III. Hadronization (based on DQPM):

- massive, off-shell (anti-)quarks with broad spectral functions hadronize to off-shell mesons and baryons or color neutral excited states - 'strings' (strings act as 'doorway states' for hadrons)

$$g \rightarrow q + \bar{q}, \quad q + \bar{q} \leftrightarrow \text{meson ('string')}$$

$$q + q + q \leftrightarrow \text{baryon ('string')}$$



- Local covariant off-shell transition rate for q+qbar fusion

→ meson formation:

$$Tr_j = \sum_j \int d^4 x_j d^4 p_j / (2\pi)^4$$

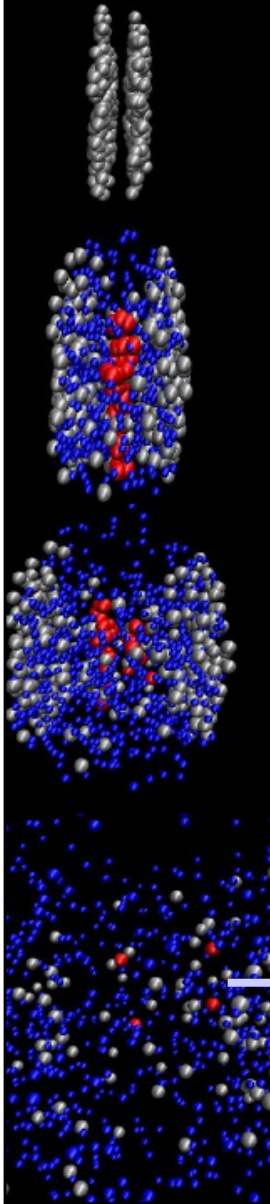
$$\frac{dN^{q+\bar{q} \rightarrow m}}{d^4 x d^4 p} = Tr_q Tr_{\bar{q}} \delta^4(p - p_q - p_{\bar{q}}) \delta^4\left(\frac{x_q + x_{\bar{q}}}{2} - x\right) \delta(\text{flavor, color})$$

$$\cdot N_q(x_q, p_q) N_{\bar{q}}(x_{\bar{q}}, p_{\bar{q}}) \cdot \omega_q \rho_q(p_q) \cdot \omega_{\bar{q}} \rho_{\bar{q}}(p_{\bar{q}}) \cdot |M_{q\bar{q}}|^2 W_m(x_q - x_{\bar{q}}, p_q - p_{\bar{q}})$$

- $N_j(x, p)$ is the phase-space density of parton j at space-time position x and 4-momentum p
- W_m is the phase-space distribution of the formed 'pre-hadrons' (Gaussian in phase space)
- $|M_{q\bar{q}}|^2$ is the effective quark-antiquark interaction from the DQPM

→ Strict 4-momentum and quantum number (flavour, color) conservation

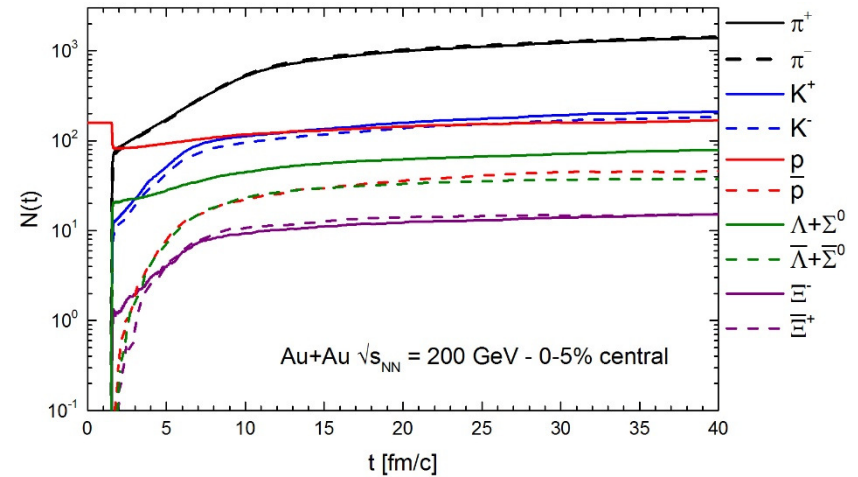
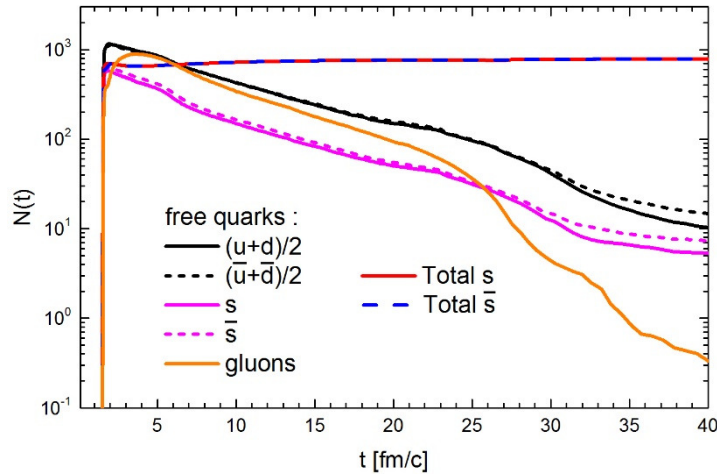
IV. Hadronic phase: hadron-string interactions – off-shell HSD





Time evolution of a central Au+Au collision at 200 GeV

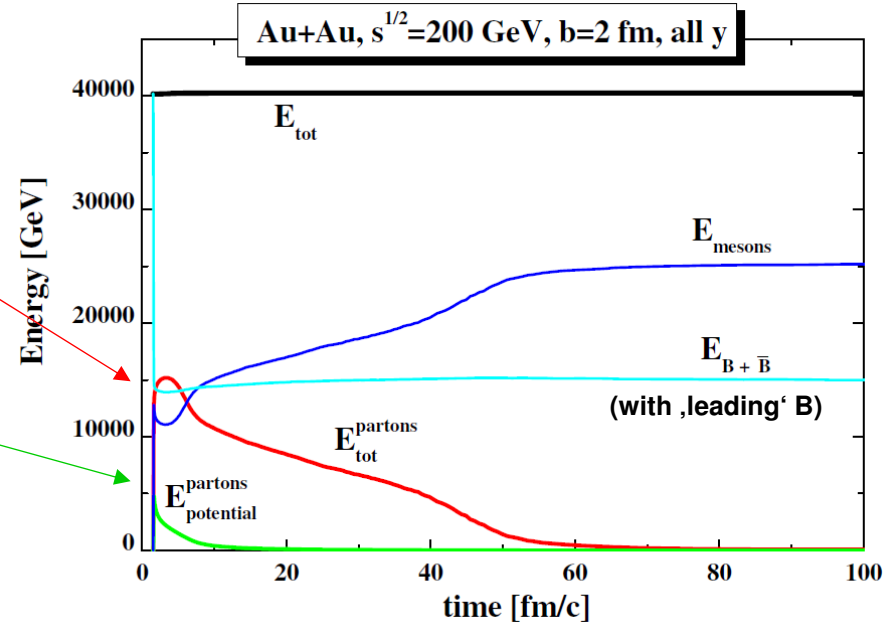
Number of partons and hadrons as a function of time:



Energy distribution vs. time:

Energy balance in the PHSD:

- ~1/3 of the total energy in central Au+Au at 200 GeV goes to the QGP
- ~1/3 of the total QGP energy is potential energy



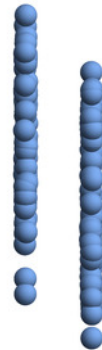
Au+Au at 200 A GeV, b=2.2 fm






t = 0.1 fm/c



Au + Au $\sqrt{s_{NN}} = 200$ GeV

b = 2.2 fm – Section view



-  Baryons (394)
-  Antibaryons (0)
-  Mesons (0)
-  Quarks (0)
-  Gluons (0)

Au+Au at 200 A GeV, b=2.2 fm






t = 1.63549 fm/c



Au + Au $\sqrt{s_{NN}} = 200$ GeV

b = 2.2 fm – Section view



-  Baryons (394)
-  Antibaryons (0)
-  Mesons (1598)
-  Quarks (4383)
-  Gluons (344)

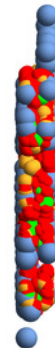
Au+Au at 200 A GeV, b=2.2 fm






t = 2.06543 fm/c



Au + Au $\sqrt{s_{NN}} = 200$ GeV

b = 2.2 fm – Section view



-  Baryons (396)
-  Antibaryons (2)
-  Mesons (1136)
-  Quarks (5066)
-  Gluons (516)

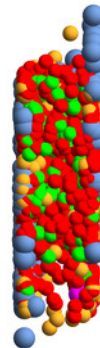
Au+Au at 200 A GeV, b=2.2 fm






t = 3.20258 fm/c



Au + Au $\sqrt{s_{NN}} = 200$ GeV

b = 2.2 fm – Section view



-  Baryons (413)
-  Antibaryons (13)
-  Mesons (1080)
-  Quarks (4708)
-  Gluons (761)

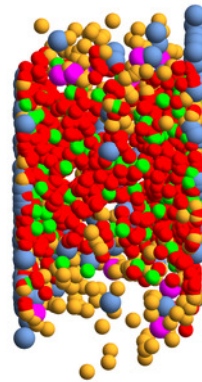
Au+Au at 200 A GeV, b=2.2 fm






t = 5.56921 fm/c



Au + Au $\sqrt{s_{NN}} = 200$ GeV

b = 2.2 fm – Section view



-  Baryons (472)
-  Antibaryons (70)
-  Mesons (1724)
-  Quarks (3843)
-  Gluons (652)

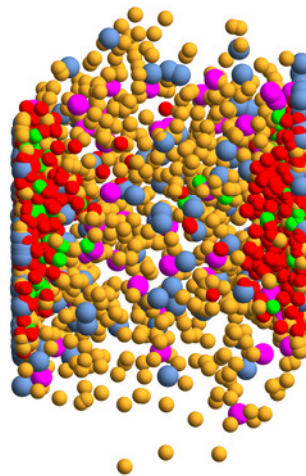
Au+Au at 200 A GeV, b=2.2 fm






t = 8.06922 fm/c



Au + Au $\sqrt{s_{NN}} = 200$ GeV

b = 2.2 fm – Section view



-  Baryons (559)
-  Antibaryons (139)
-  Mesons (2686)
-  Quarks (2628)
-  Gluons (442)

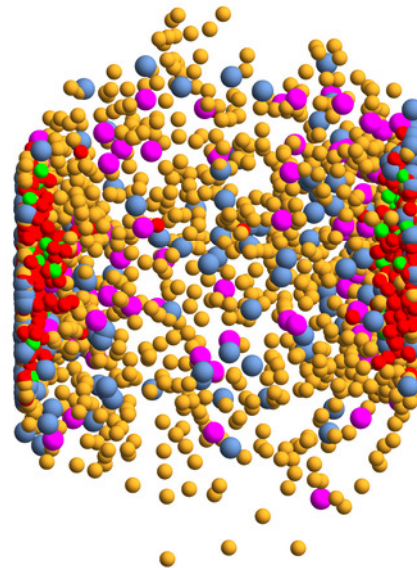
Au+Au at 200 A GeV, b=2.2 fm






t = 10.5692 fm/c



Au + Au $\sqrt{s_{NN}} = 200$ GeV

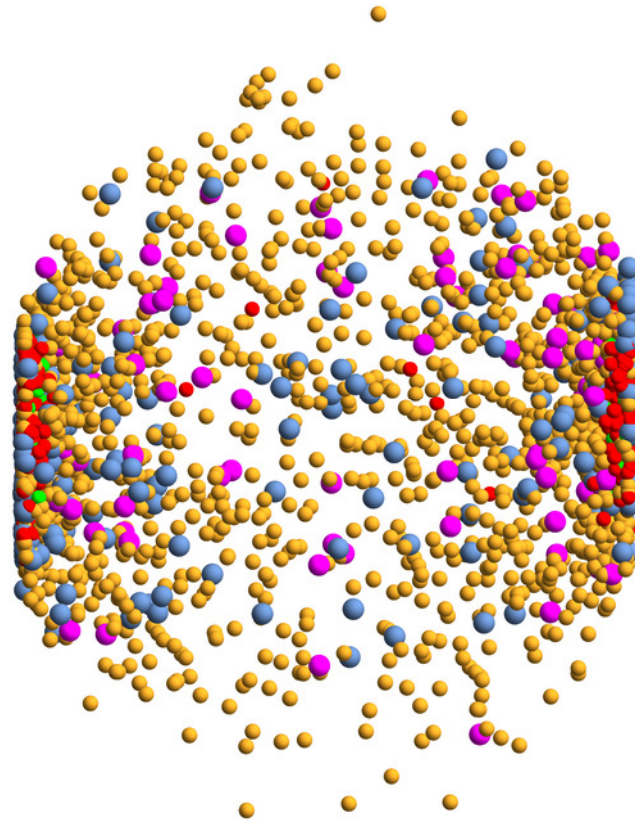
b = 2.2 fm – Section view



-  Baryons (604)
-  Antibaryons (187)
-  Mesons (3169)
-  Quarks (2076)
-  Gluons (319)






Au+Au at 200 A GeV, b=2.2 fm

t = 15.5692 fm/c



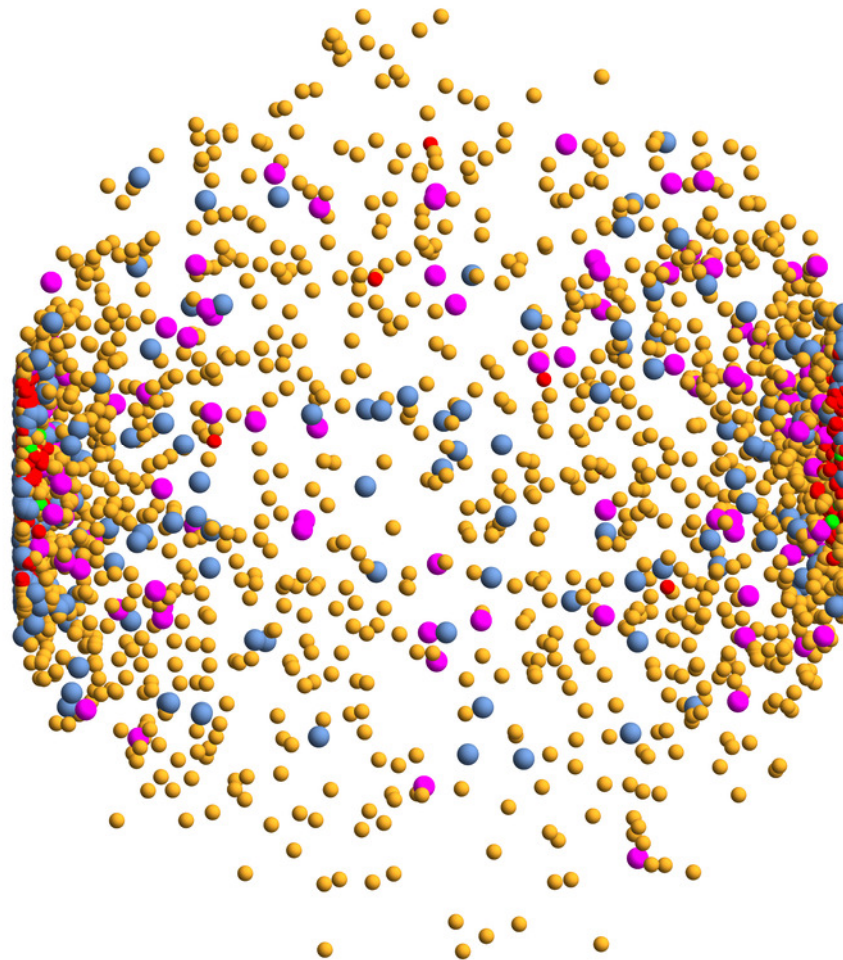
Au + Au $\sqrt{s_{NN}} = 200$ GeV

b = 2.2 fm – Section view

-  Baryons (662)
-  Antibaryons (229)
-  Mesons (3661)
-  Quarks (1499)
-  Gluons (175)






Au+Au at 200 A GeV, b=2.2 fm

t = 20.5692 fm/c



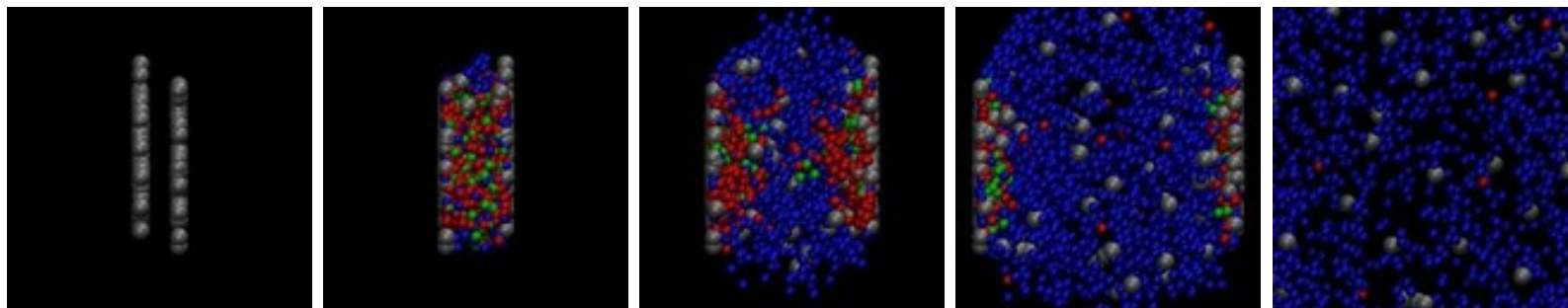
Au + Au $\sqrt{s_{NN}} = 200$ GeV

b = 2.2 fm - Section view

-  Baryons (692)
-  Antibaryons (266)
-  Mesons (4022)
-  Quarks (1184)
-  Gluons (90)

P.Moreau

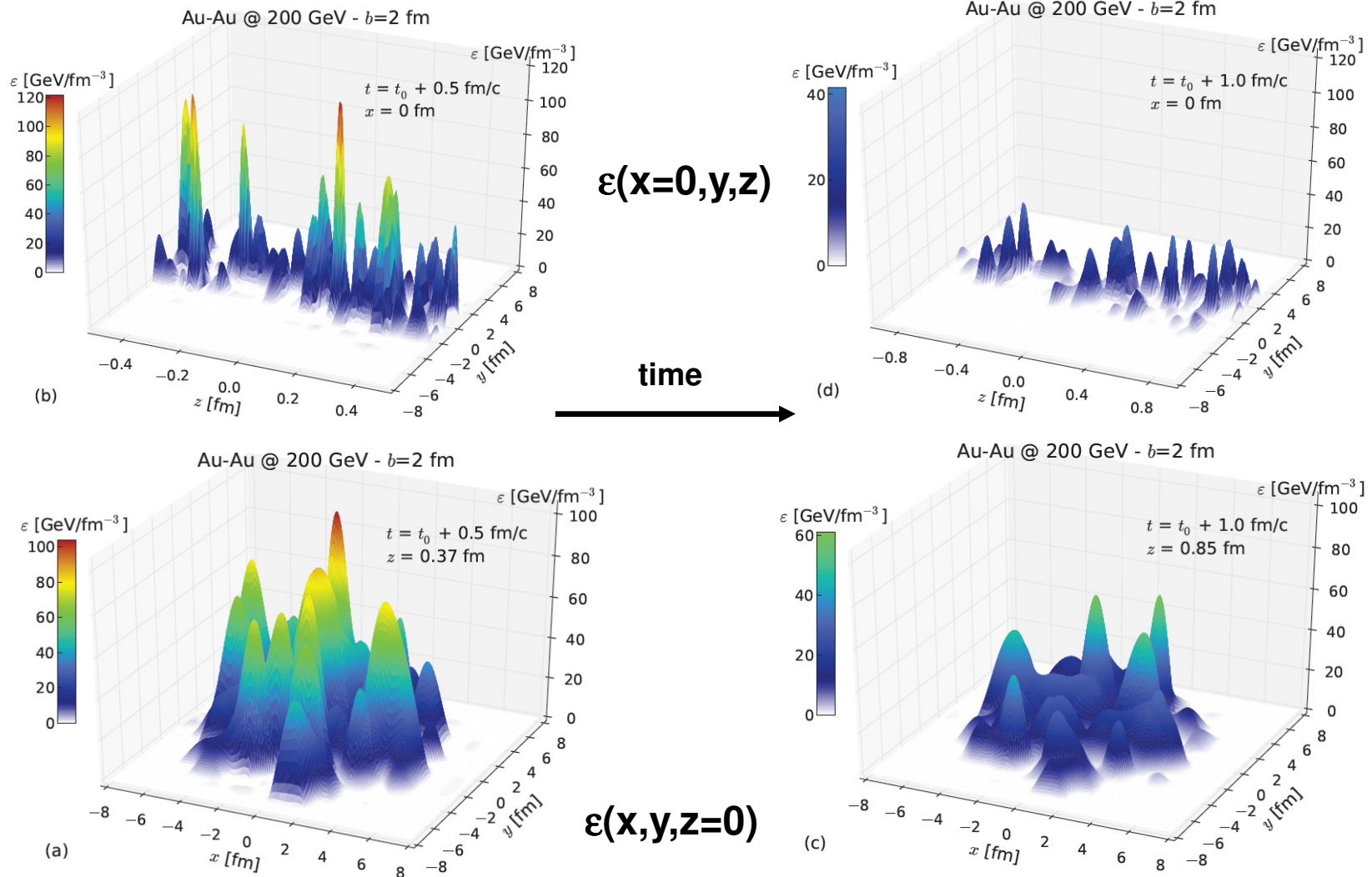
„Bulk“ properties in Au+Au





Time evolution of energy density

PHSD: 1 event Au+Au, 200 GeV, $b = 2$ fm



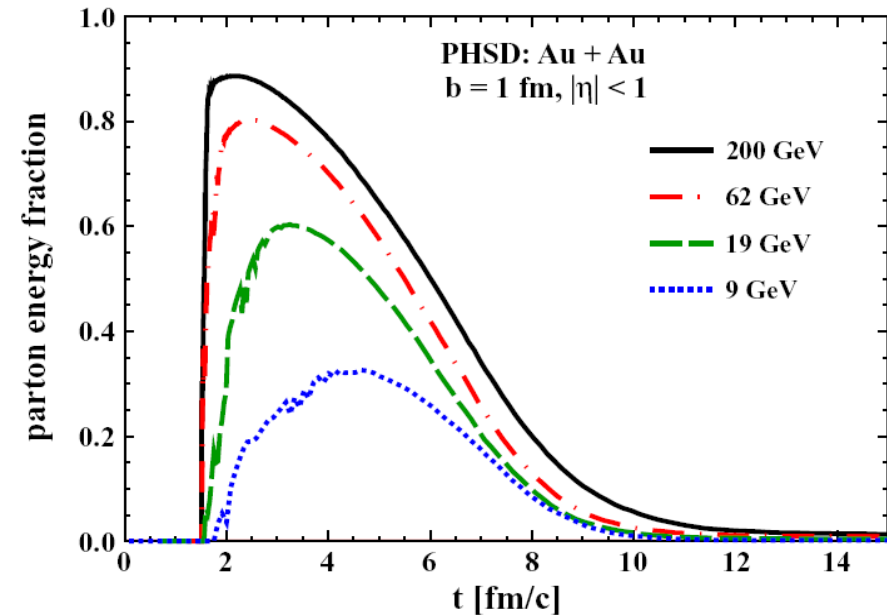
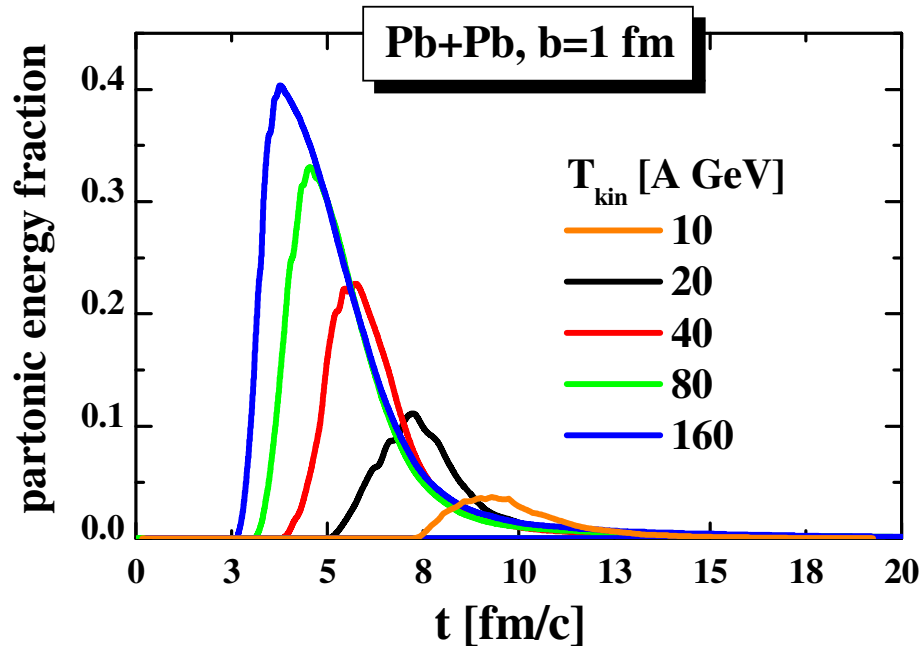
ΔV : $\Delta x = \Delta y = 1$ fm, $\Delta z = 1/\gamma$ fm

R. Marty et al, PRC92 (2015) 015201



Partonic energy fraction in central A+A

Time evolution of the partonic energy fraction vs energy



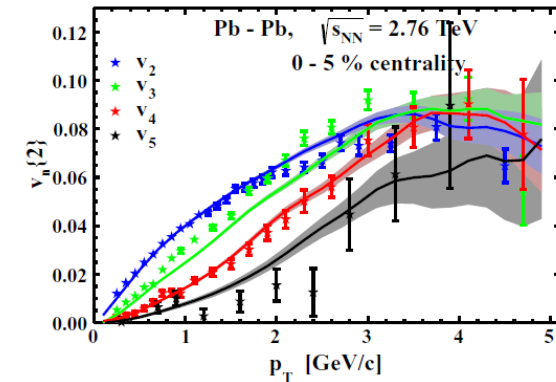
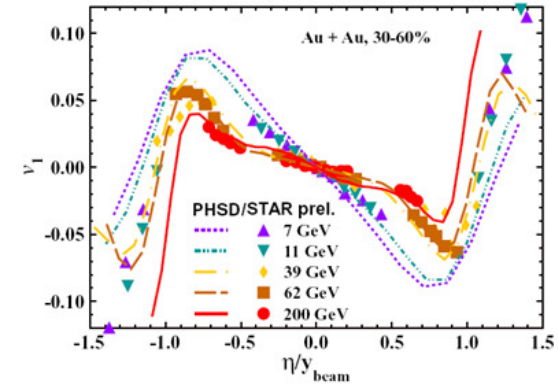
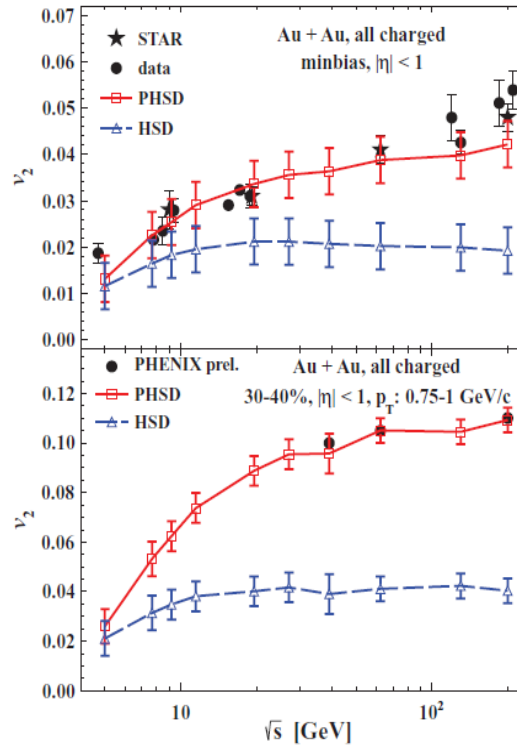
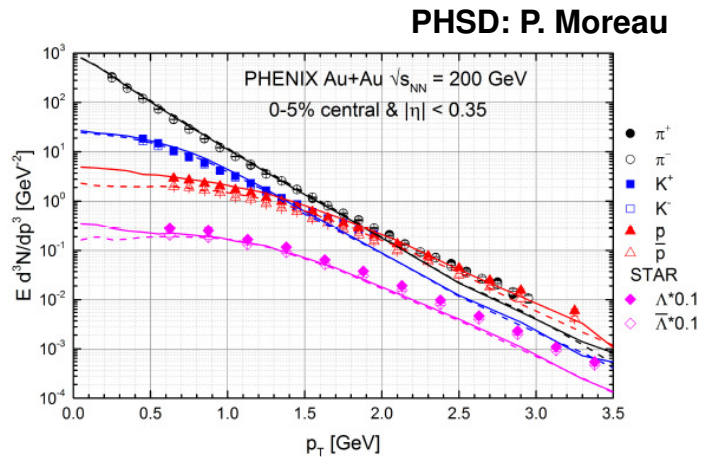
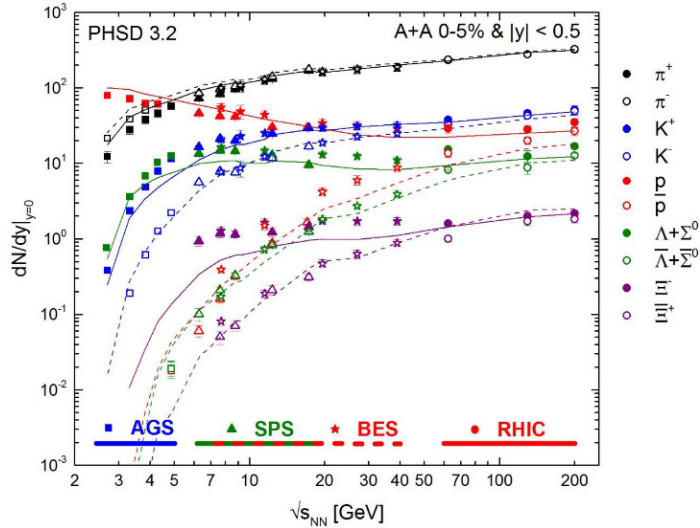
- Strong increase of partonic phase with energy from AGS to RHIC
- SPS: Pb+Pb, 160 A GeV: only about 40% of the converted energy goes to partons; the rest is contained in the large hadronic corona and leading particles
- RHIC: Au+Au, 21.3 A TeV: up to 90% - QGP

W. Cassing & E. Bratkovskaya, NPA 831 (2009) 215
V. Konchakovski et al., Phys. Rev. C 85 (2012) 011902



Non-equilibrium dynamics: description of A+A with PHSD

PHSD: highlights

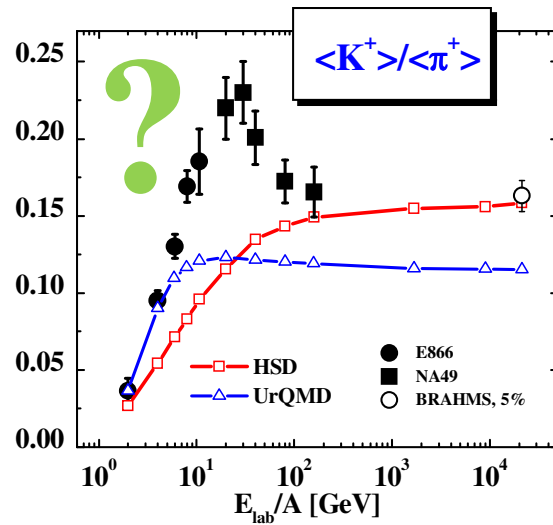


V. Konchakovski et al.,
PRC 85 (2012) 011902; JPG42 (2015) 055106

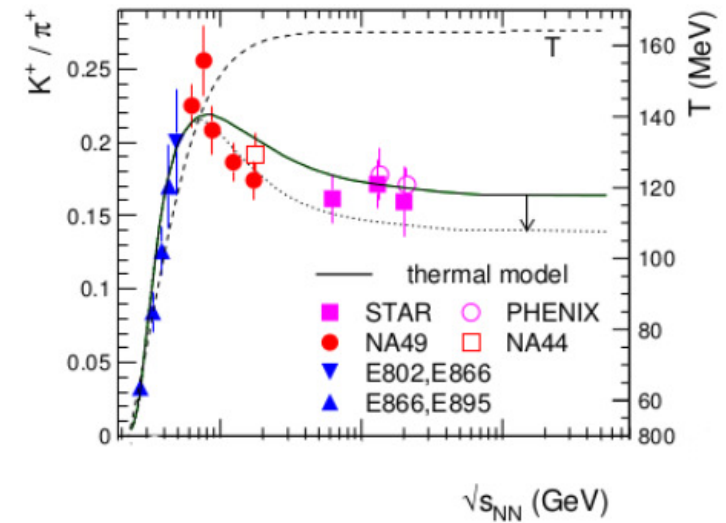
PHSD provides a good description of 'bulk' observables (y -, p_T -distributions, flow coefficients v_n , ...) from SPS to LHC

Strangeness in A+A

HSD, UrQMD, PRC 69 (2004) 032302



Thermal model: A. Andronic et al., NPA 834 (2010)



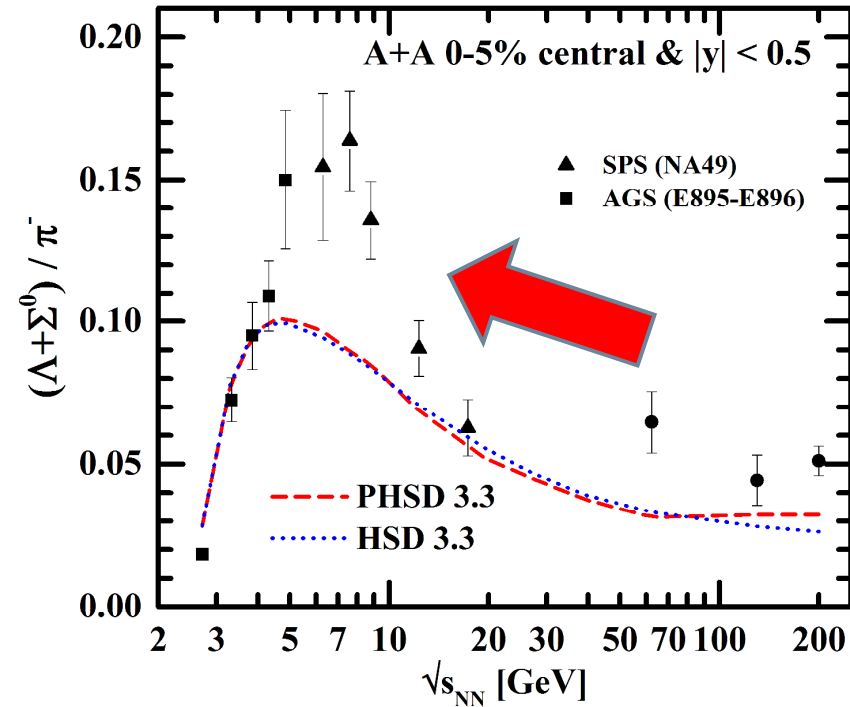
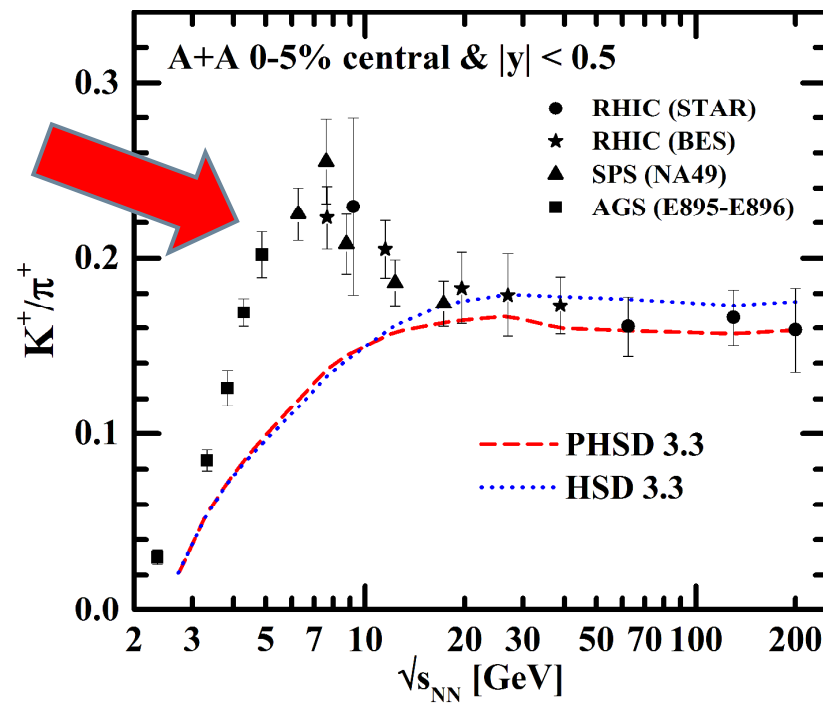
Thanks to Alessia Palmese, Pierre Moreau



K^+/π^+ ,horn'

PHSD: even when considering the creation of a QGP phase, the **strangeness enhancement** seen experimentally by NA49 and STAR at a bombarding energy ~ 20 A GeV (FAIR/NICA energies!) **remains unexplained**

→ 'Horn' is not traced back to deconfinement ?!

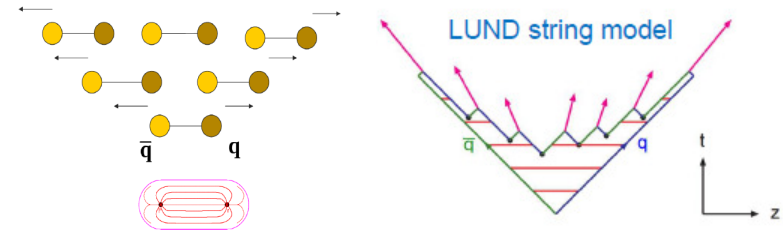




‘Quark flavor chemistry’ in the LUND string model

□ In PHSD:

the ‘flavor chemistry’ of the final hadrons is mainly defined by the LUND string model



□ LUND model:

1) ‘quark flavor chemistry’ is determined by the Schwinger-formula

According to the Schwinger-formula, the probability to form a massive $s\bar{s}$ in a string-decay is suppressed in comparison to light flavor ($u\bar{u}, d\bar{d}$):

$$\frac{P(s\bar{s})}{P(u\bar{u})} = \frac{P(s\bar{s})}{P(d\bar{d})} = \gamma_s = \exp\left(-\pi \frac{m_s^2 - m_q^2}{2\kappa}\right)$$

with κ - string tension;

in vacuum: $\kappa \sim 0.9 \text{ GeV/fm} = 0.176 \text{ GeV}^2$

The relative production factors in PHSD/HSD are:

$u : d : s : uu$	$\left\{ \begin{array}{l} 1 : 1 : 0.3 : 0.07 \\ 1 : 1 : 0.4 : 0.07 \end{array} \right.$	at SPS to RHIC; at AGS energies.
------------------	---	-------------------------------------

m_s, m_q ($q=u,d$) – constituent (‘dressed’) quark masses

2) ‘Kinematics’ is determined by the fragmentation function $f(x, m_T)$

$$f(x, m_T) \approx \frac{1}{x} (1 - x^a) \exp(-bm_T^2/x)$$



Schwinger mechanism in vacuum

I. In vacuum (e.g. p+p collisions) :

- 'dressing' of bare quark masses is due to the coupling to the vacuum scalar quark condensate (cf. Dyson-Schwinger Bethe-Salpeter approaches)

$$m_q^V = m_q^0 - g_s \langle q\bar{q} \rangle_V$$

bare quark masses:

$$m_u^0 = m_d^0 \approx 7 \text{ MeV}, \quad m_s^0 \approx 100 \text{ MeV}$$

- vacuum scalar quark condensate is fixed by Gell-Mann-Oakes-Renner relation:

$$f_\pi^2 m_\pi^2 = -\frac{1}{2}(m_u^0 + m_d^0) \langle \bar{q}q \rangle_V \quad \Rightarrow \quad \langle \bar{q}q \rangle_V \approx -3.2 \text{ fm}^{-3}$$

f_π and m_π are the pion decay constant and pion mass

→ Constituent quark masses in vacuum : $m_q \equiv m_q^V$

$$m_u^V = m_d^V \approx 0.35 \text{ GeV}, \quad m_s^V \approx 0.5 \text{ GeV}$$



Schwinger mechanism in medium

II. In medium (e.g. A+A collisions) :

- In the presence of a **hot and dense hadronic medium**, the degrees of freedom modify their properties, e.g. **the in-medium constituent masses**:

$$m_s^* = m_s^0 + (m_s^v - m_s^0) \frac{\langle q\bar{q} \rangle}{\langle q\bar{q} \rangle_V} \quad m_q^* = m_q^0 + (m_q^v - m_q^0) \frac{\langle q\bar{q} \rangle}{\langle q\bar{q} \rangle_V}$$

- **The scalar quark condensate $\langle q\bar{q} \rangle$** is viewed as an **order parameter for the restoration of chiral symmetry**:

$$\langle \bar{q}q \rangle = \begin{cases} \neq 0 & \text{chiral non-symmetric phase;} \\ = 0 & \text{chiral symmetric phase.} \end{cases}$$

- The behavior of the scalar quark condensate $\langle q\bar{q} \rangle$ in the **hadronic medium** (baryons + mesons) can be obtained e.g. from the **non-linear $\sigma - \omega$ model**

$$\frac{\langle q\bar{q} \rangle}{\langle q\bar{q} \rangle_V} = 1 - \frac{\Sigma_\pi}{f_\pi^2 m_\pi^2} \rho_S - \sum_h \frac{\sigma_h \rho_S^h}{f_\pi^2 m_\pi^2}$$

baryonic
medium

mesonic
medium

where ρ_s is the **scalar nucleon density** (depends on EoS)

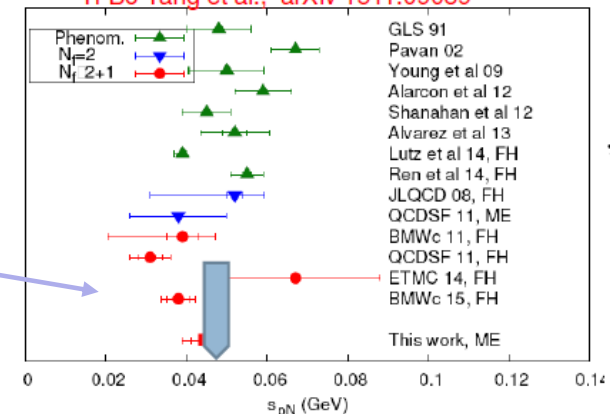
$\Sigma_\pi \approx 45 \text{ MeV}$ is the **pion-nucleon Σ -term**

$\sigma_h = m_\pi/2$ for light mesons; $=m_\pi/4$ - strange mesons

See B. Friman et al., Eur. Phys. J. A 3, 165, 1998

□ **pion-nucleon Σ -term : 45 MeV**

Yi-Bo Yang et al., arXiv 1511.09089





Scalar density in PHSD

1) ρ_s is the **scalar density of baryonic matter**:

$d = 4$ in case of isospin symmetric nuclear matter

$$\rho_s = d \int \frac{d^3 p}{(2\pi)^3} \frac{m_N^*(x)}{\sqrt{p^2 + m_N^{*2}}} f_N(x, \mathbf{p})$$

where **in-medium nucleon mass** is

$$m_N^*(x) = m_N^V - g_s \sigma(x)$$

with m_N^V denoting **the nucleon mass in vacuum**

Scalar field $\sigma(x)$ mediates the scalar interaction with the surrounding medium with g_s coupling.

$\sigma(x)$ is defined determined locally by the **nonlinear gap equation**:

$$m_\sigma^2 \sigma(x) + B \sigma^2(x) + C \sigma^3(x) = g_s \rho_s = g_s d \int \frac{d^3 p}{(2\pi)^3} \frac{m_N^*(x)}{\sqrt{p^2 + m_N^{*2}}} f_N(x, \mathbf{p})$$

Within the **non-linear $\sigma - \omega$ model** for nuclear matter, the **parameters g_s, m_σ, B, C** can be **fixed** in order to reproduce the main nuclear matter quantities at **saturation**, i.e. saturation density, binding energy per nucleon, compression modulus and the effective nucleon mass.

2) ρ_s^h is the **scalar density of mesons** of type h (from PHSD):

$$\rho_s^h(x) = \frac{(2s+1)(2t+1)}{(2\pi)^3} \int d^3 \mathbf{p} \frac{m_h}{\sqrt{\mathbf{p}^2 + m_h^2}} f_h(x, \mathbf{p})$$



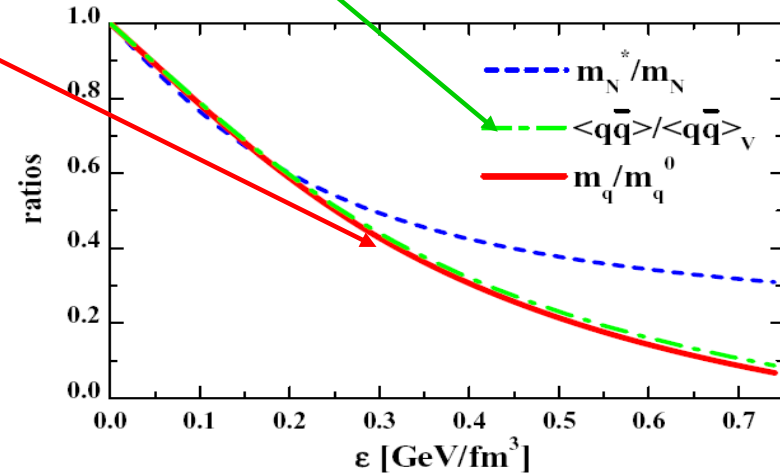
Modeling of the chiral symmetry restoration in PHSD

- In the Schwinger formula the in-medium constituent masses $m_{q;s}^* \rightarrow m_{q;s}$ have to be considered:

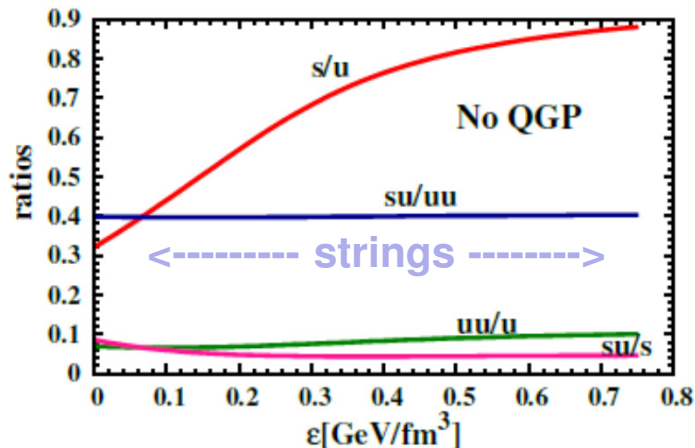
$$\frac{P(s\bar{s})}{P(u\bar{u})} = \frac{P(s\bar{s})}{P(d\bar{d})} = \gamma_s = \exp\left(-\pi \frac{m_s^2 - m_q^2}{2\kappa}\right)$$

- As a consequence of the chiral symmetry restoration (CSR), the strangeness production probability increases with the energy density ε .

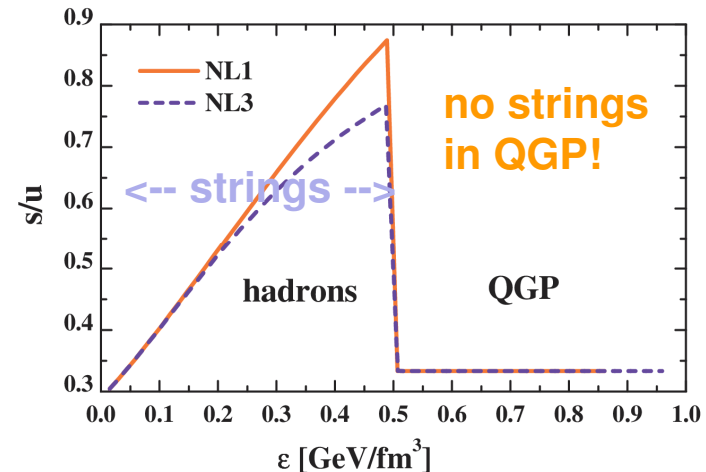
scalar quark condensate $\langle q\bar{q} \rangle$ for NL3



1) Scenario 'HSD' – assume NO QGP:



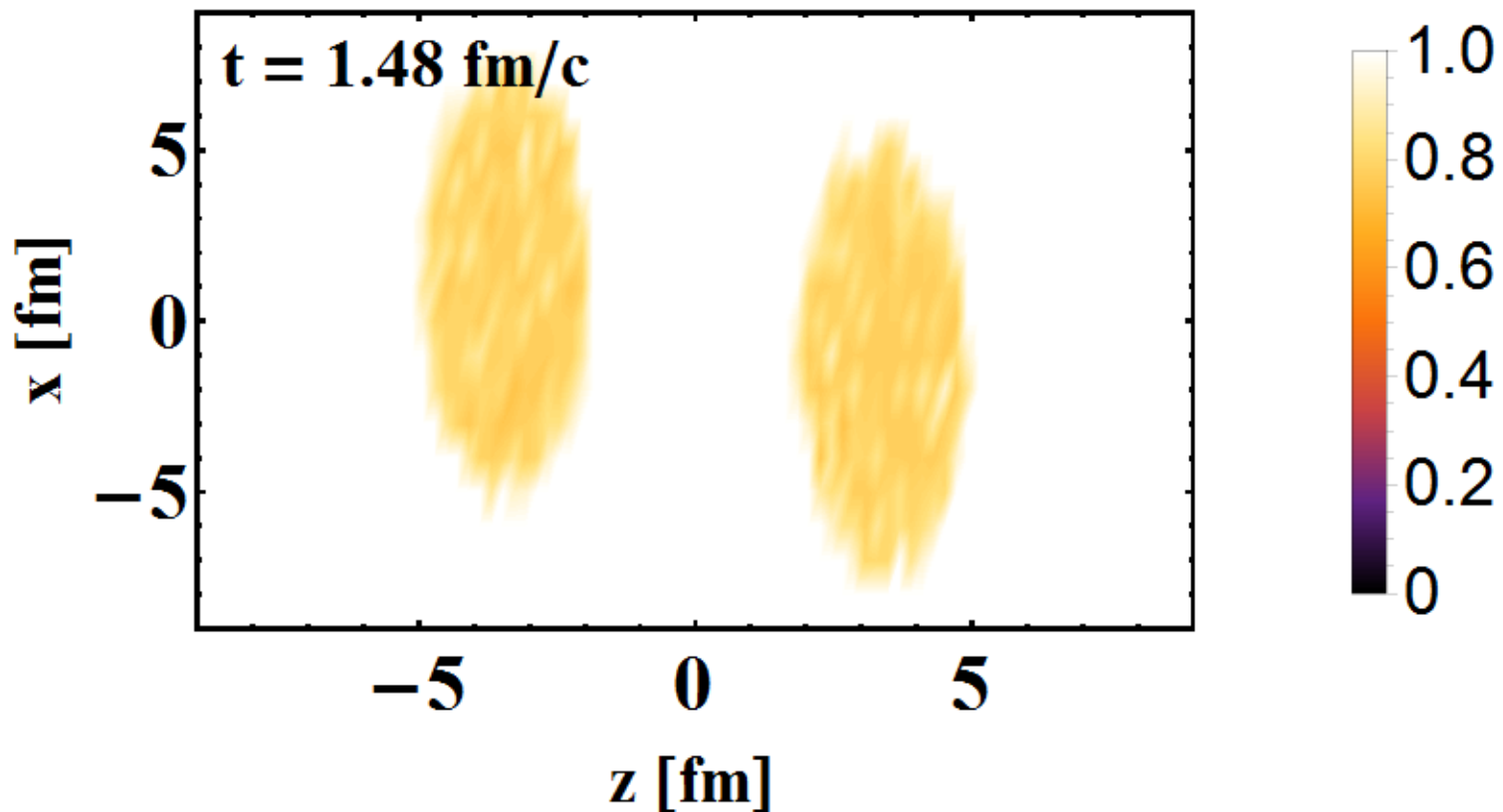
2) Scenario 'PHSD' – CSR+QGP:



Pb+Pb @ 30 AGeV – 0-5% central

Ratio of the quark scalar condensate compared to vacuum as a function of time:

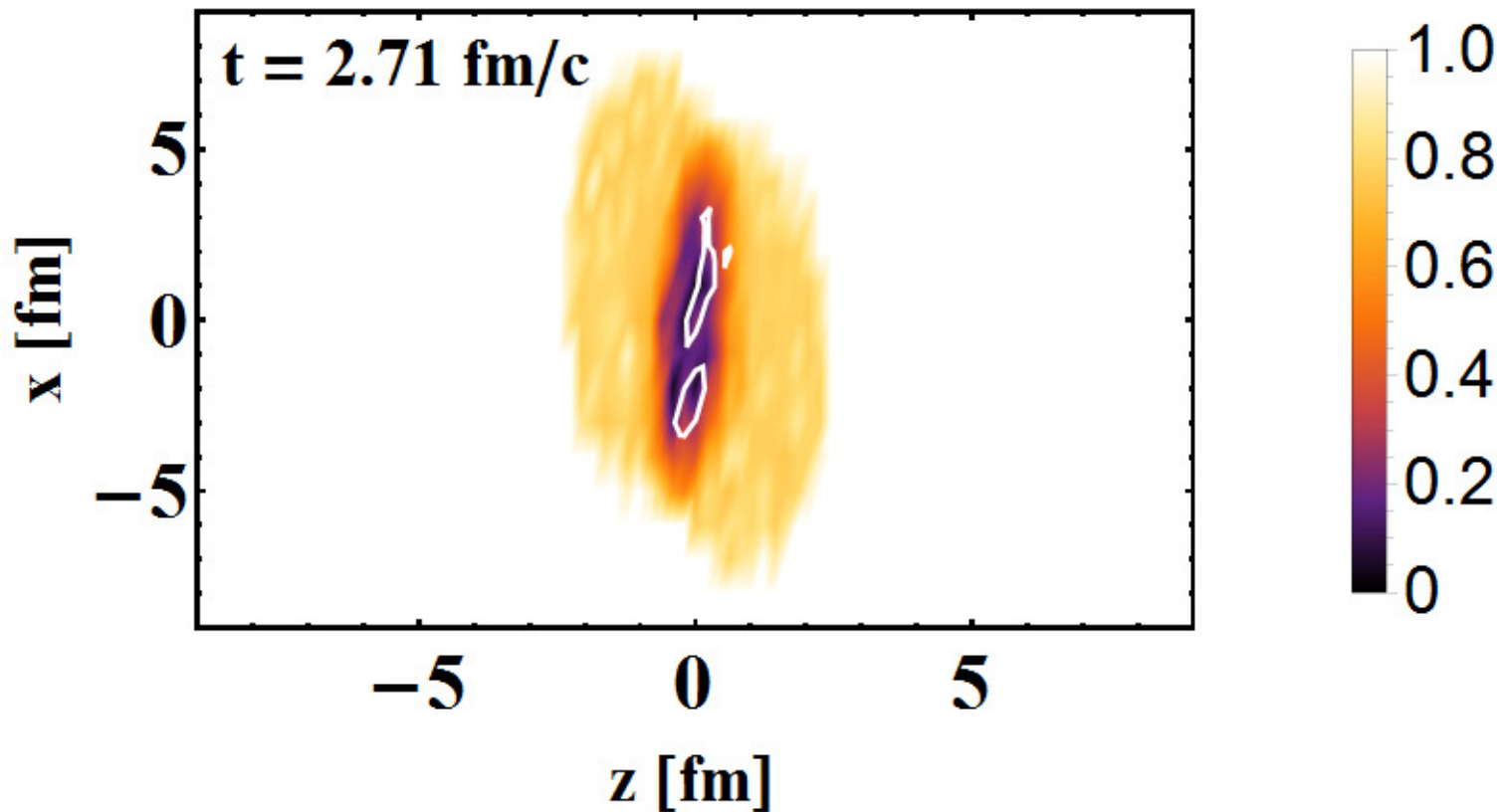
$$\frac{\langle q \bar{q} \rangle}{\langle q \bar{q} \rangle_v}$$



Pb+Pb @ 30 AGeV – 0-5% central

Ratio of the quark scalar condensate compared to vacuum as a function of time:

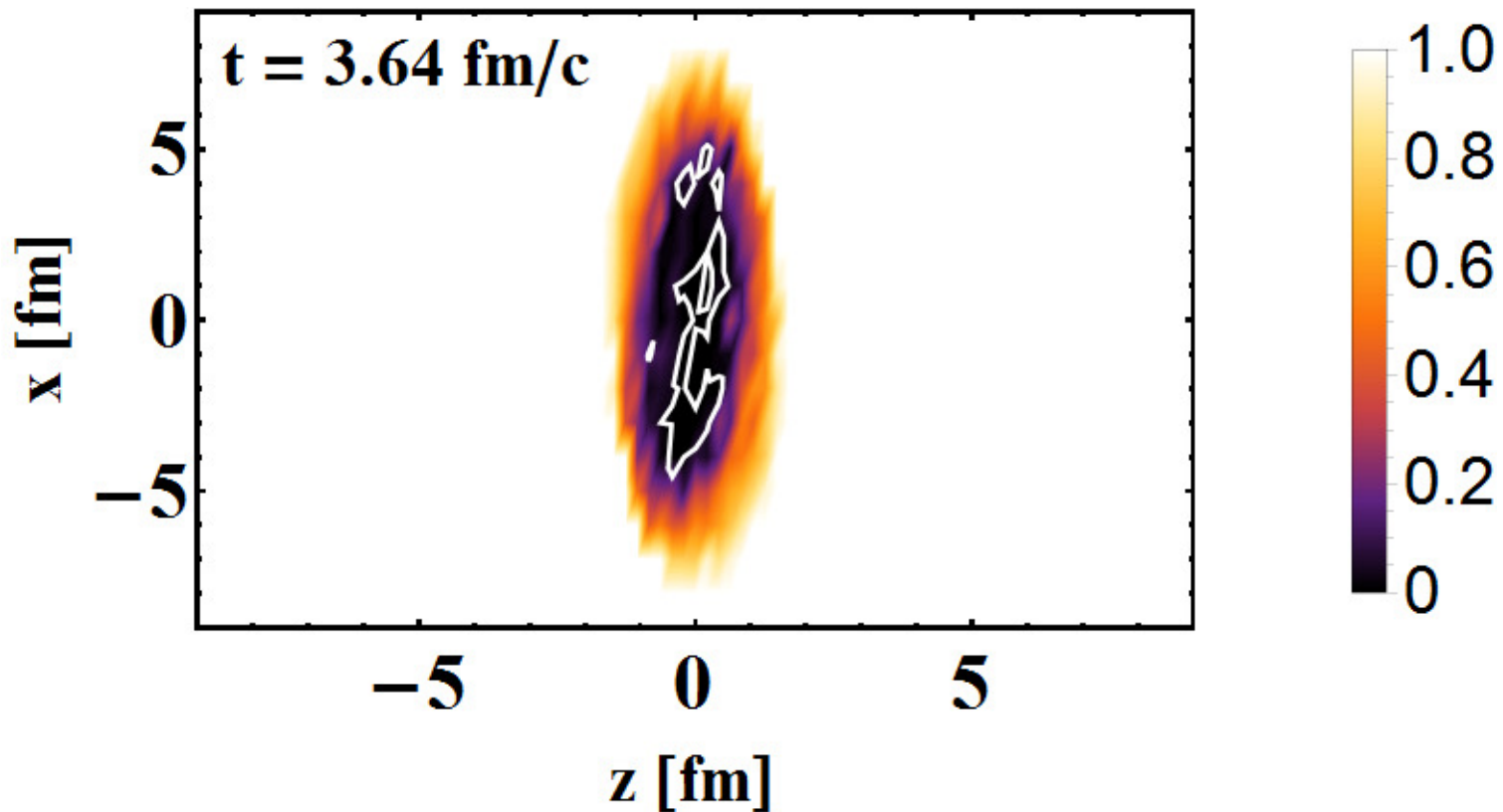
$$\frac{\langle q \bar{q} \rangle}{\langle q \bar{q} \rangle_v}$$



Pb+Pb @ 30 AGeV – 0-5% central

Ratio of the quark scalar condensate compared to vacuum as a function of time:

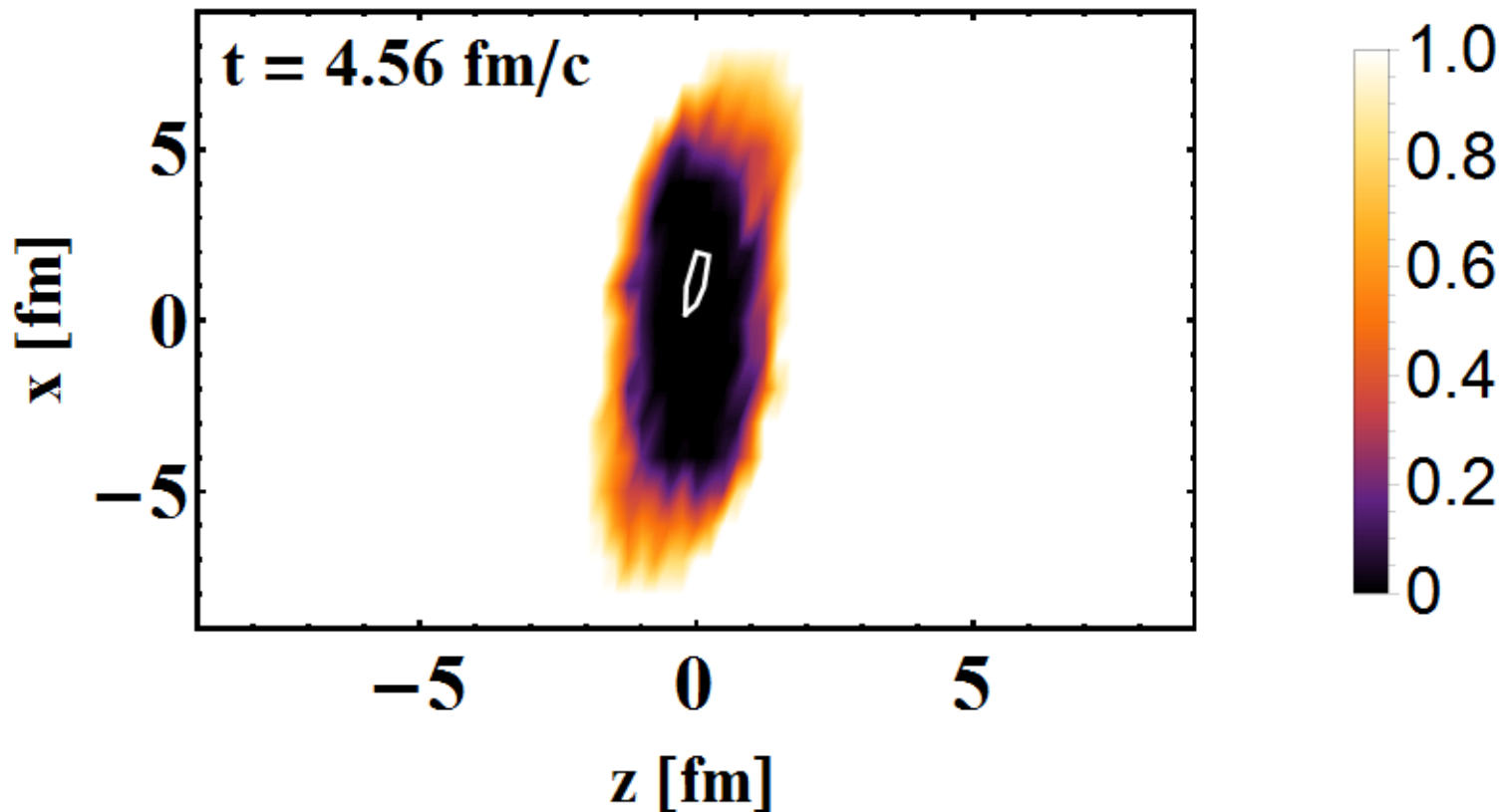
$$\frac{\langle q \bar{q} \rangle}{\langle q \bar{q} \rangle_v}$$



Pb+Pb @ 30 AGeV – 0-5% central

Ratio of the quark scalar condensate compared to vacuum as a function of time:

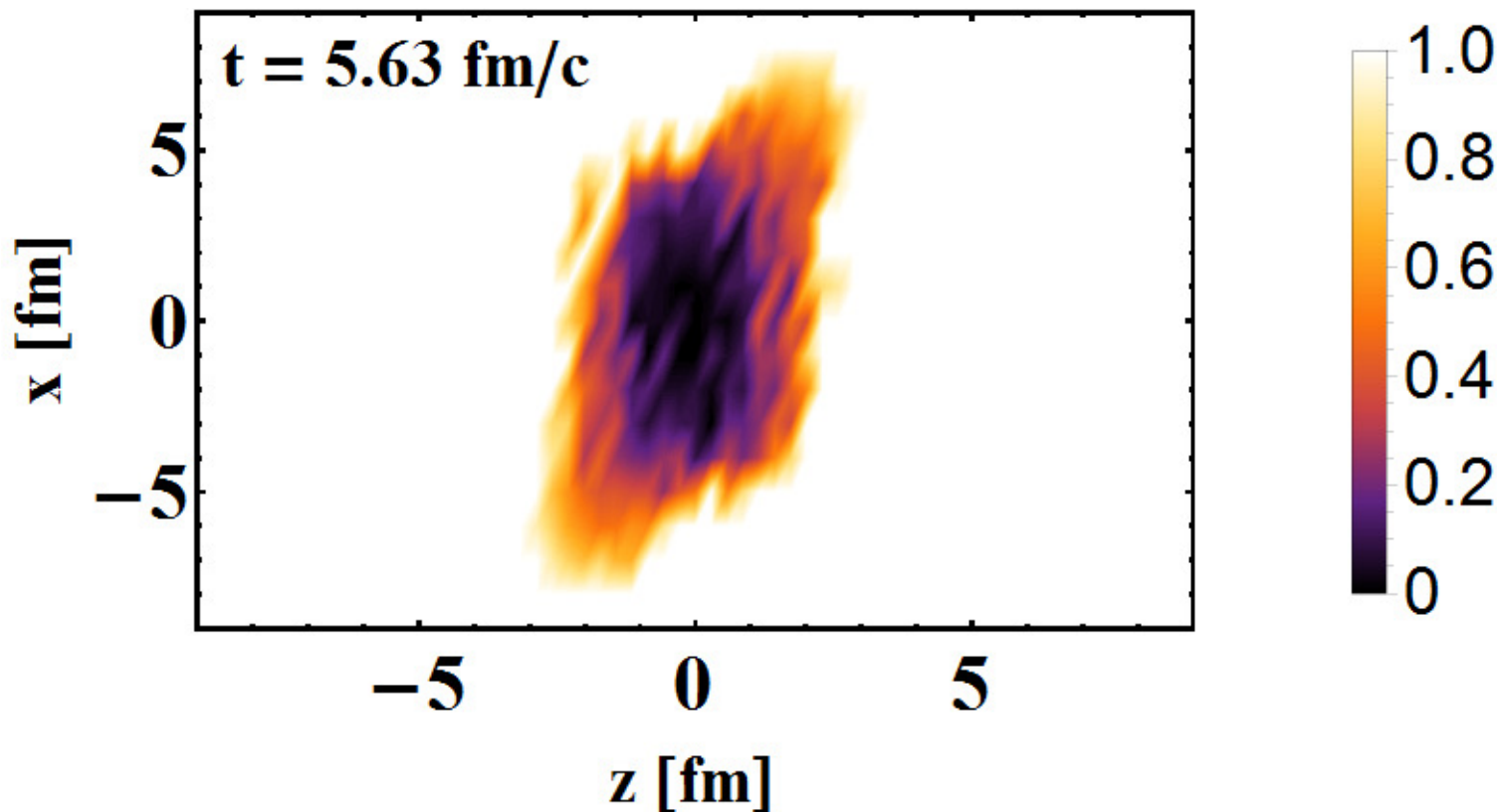
$$\frac{\langle q \bar{q} \rangle}{\langle q \bar{q} \rangle_v}$$



Pb+Pb @ 30 AGeV – 0-5% central

Ratio of the quark scalar condensate compared to vacuum as a function of time:

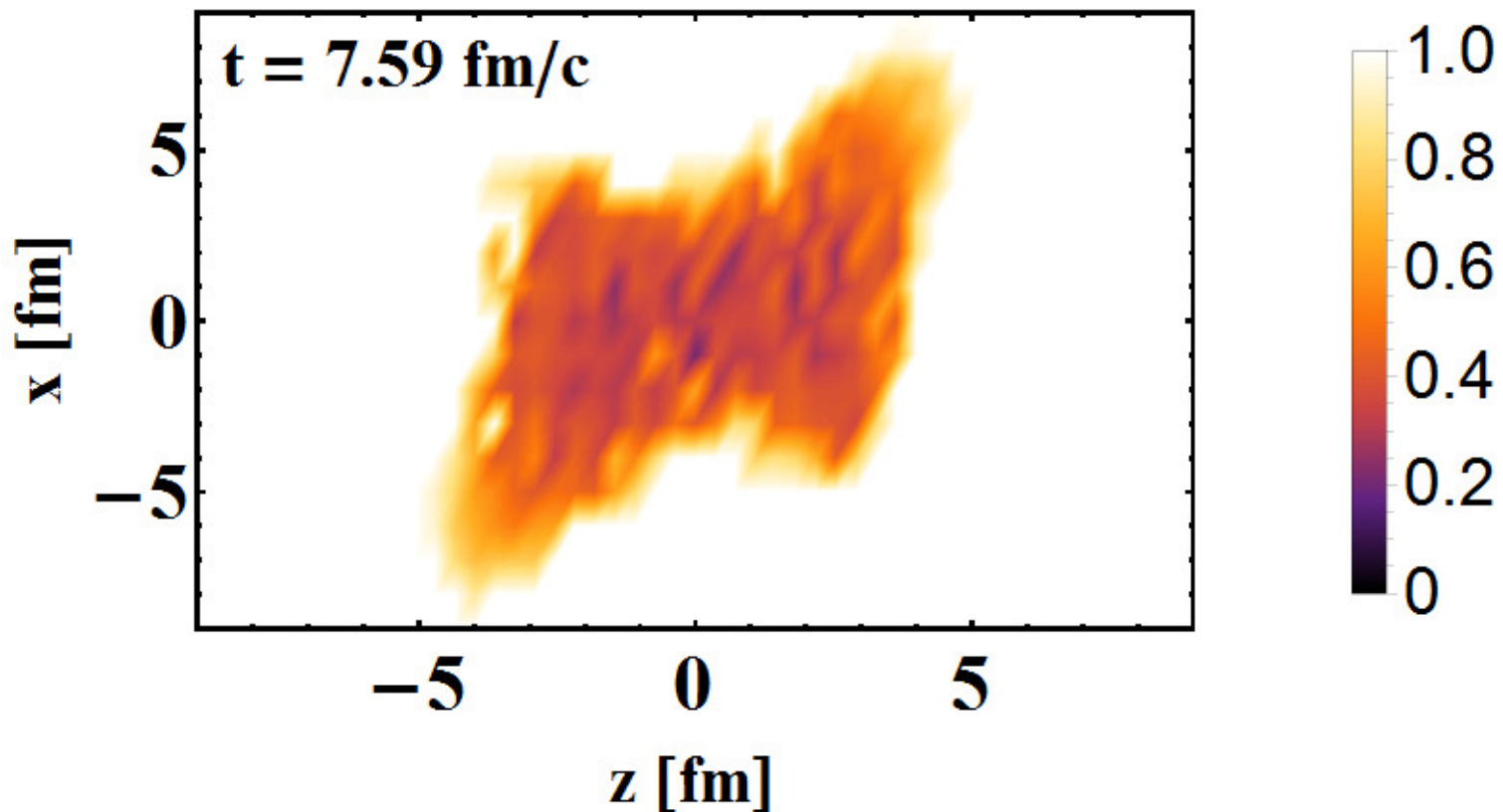
$$\frac{\langle q \bar{q} \rangle}{\langle q \bar{q} \rangle_v}$$



Pb+Pb @ 30 AGeV – 0-5% central

Ratio of the quark scalar condensate compared to vacuum as a function of time:

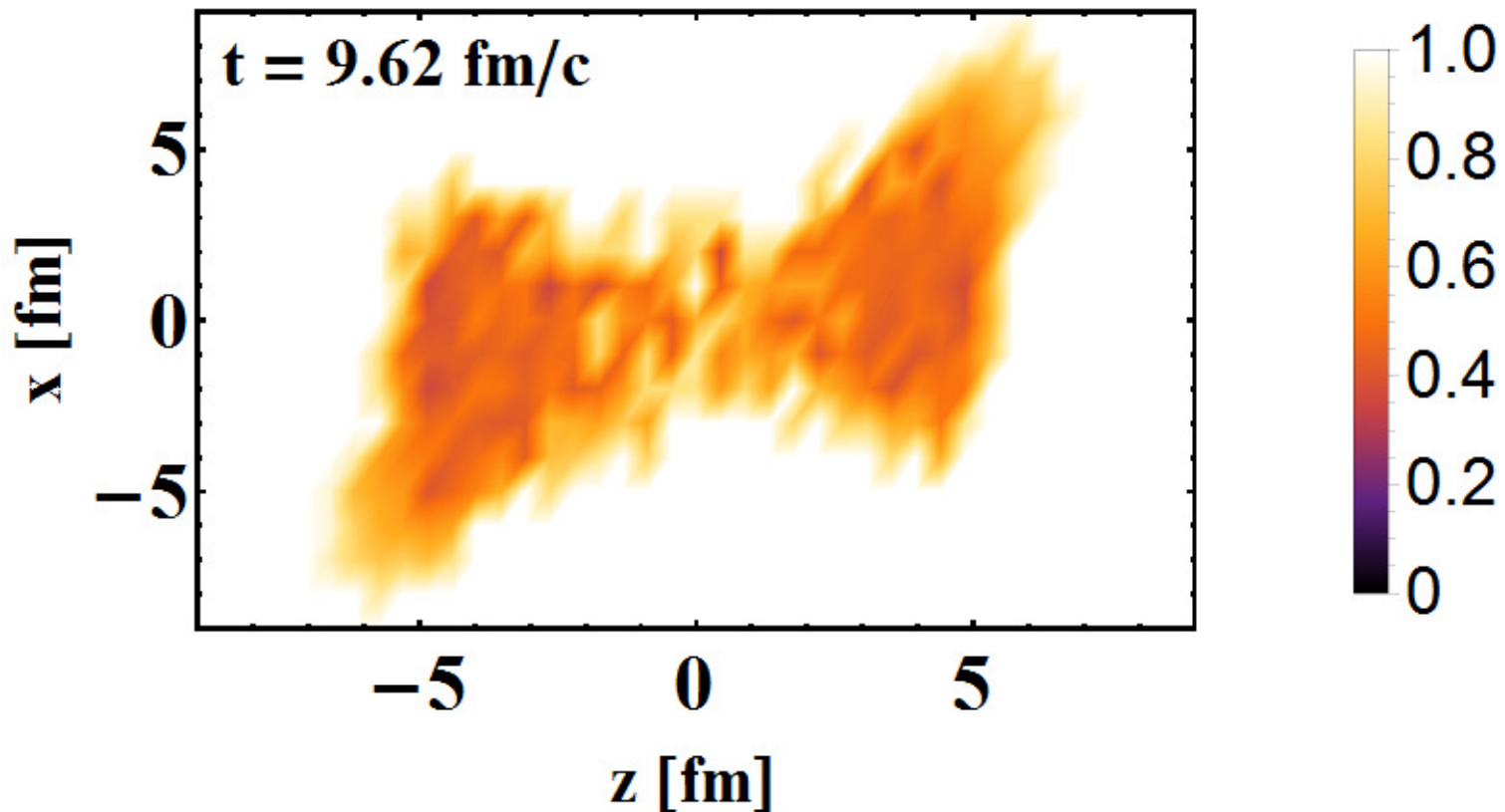
$$\frac{\langle q \bar{q} \rangle}{\langle q \bar{q} \rangle_v}$$



Pb+Pb @ 30 AGeV – 0-5% central

Ratio of the quark scalar condensate compared to vacuum as a function of time:

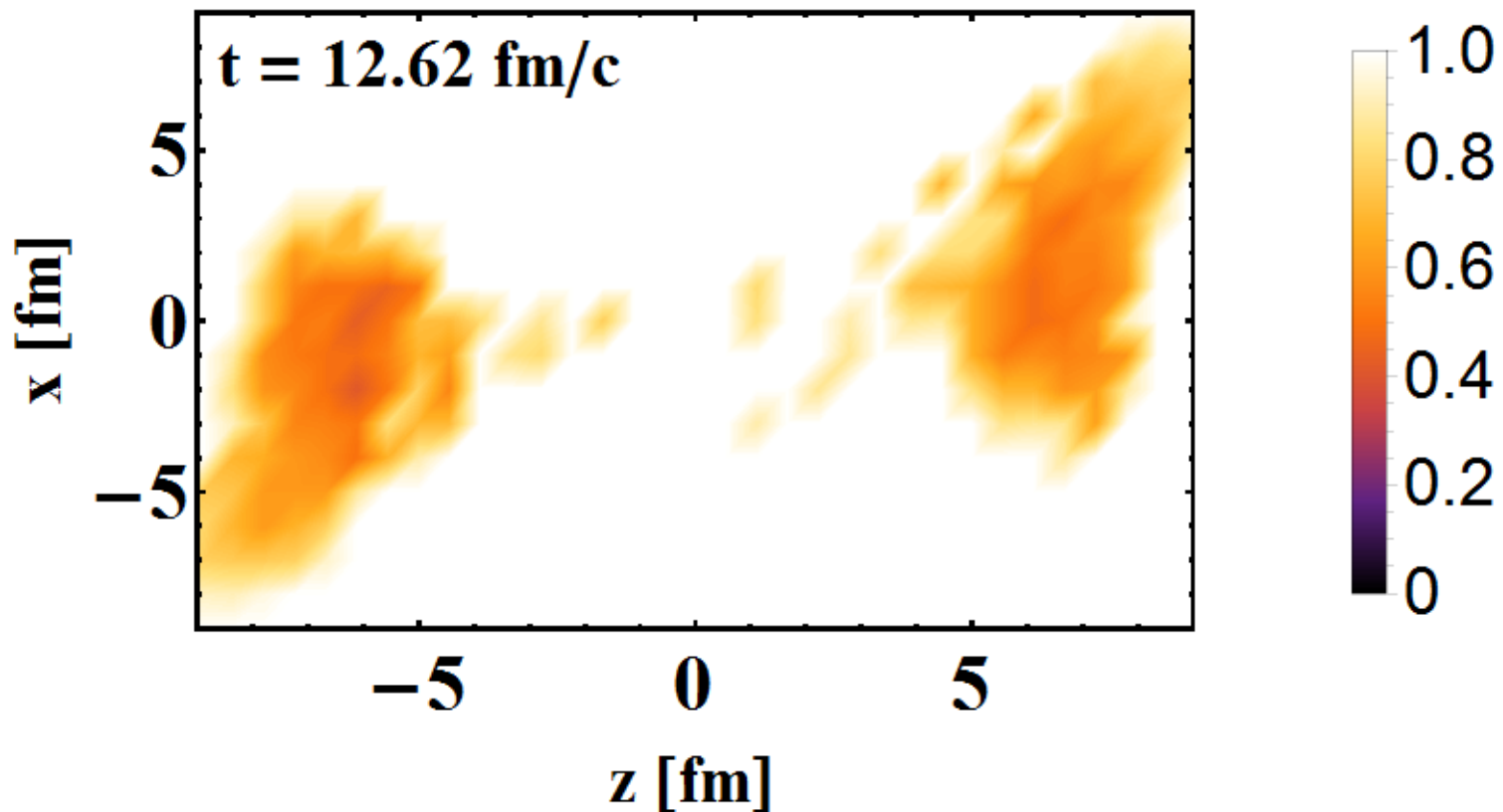
$$\frac{\langle q \bar{q} \rangle}{\langle q \bar{q} \rangle_v}$$



Pb+Pb @ 30 AGeV – 0-5% central

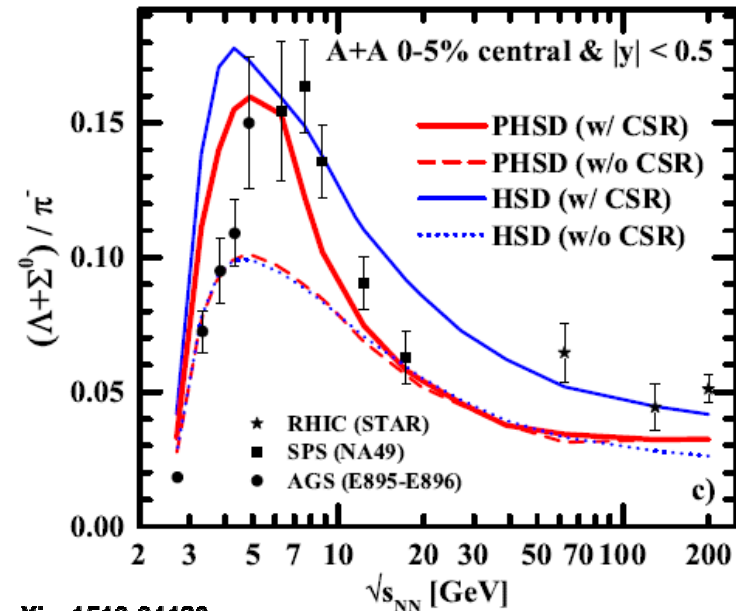
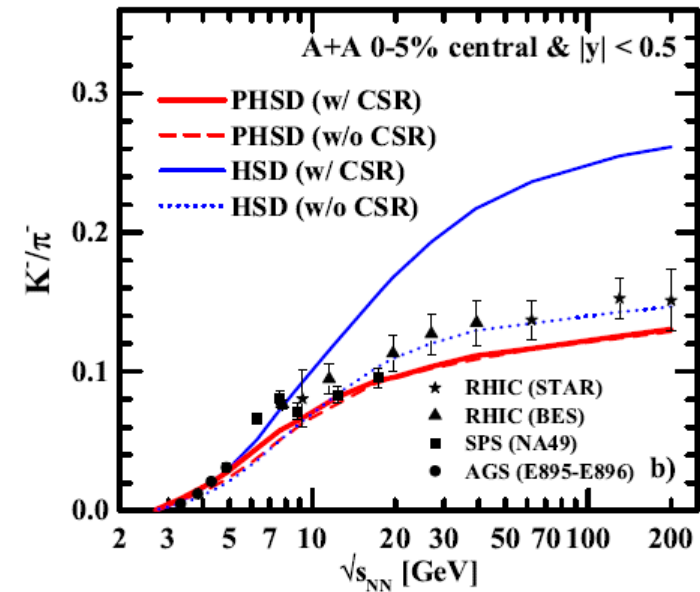
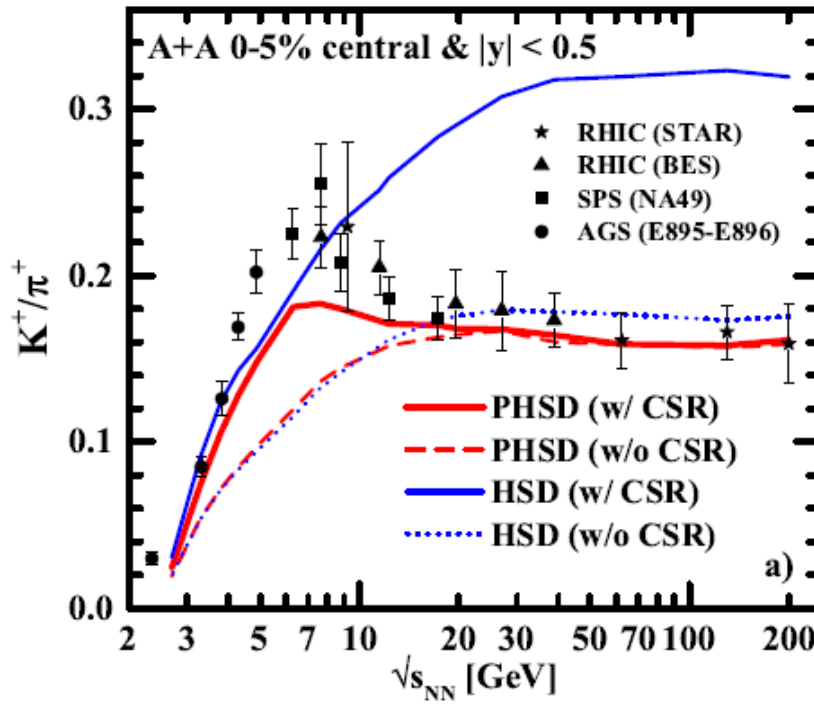
Ratio of the quark scalar condensate compared to vacuum as a function of time:

$$\frac{\langle q \bar{q} \rangle}{\langle q \bar{q} \rangle_v}$$





PHSD results with chiral symmetry restoration

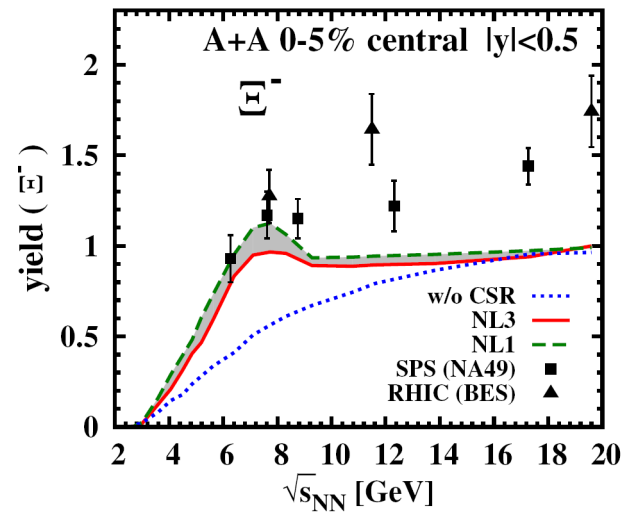
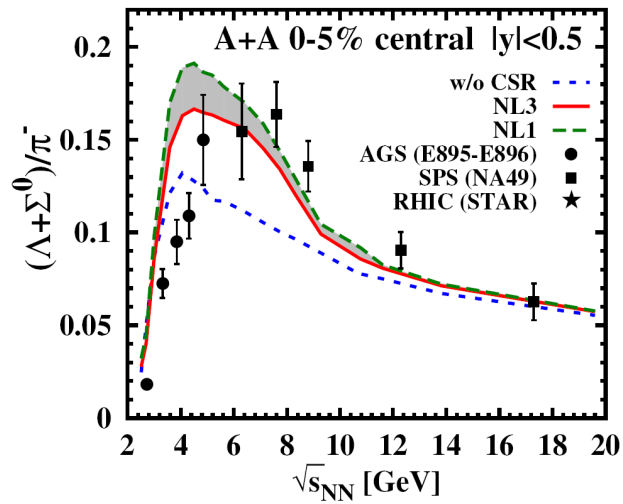
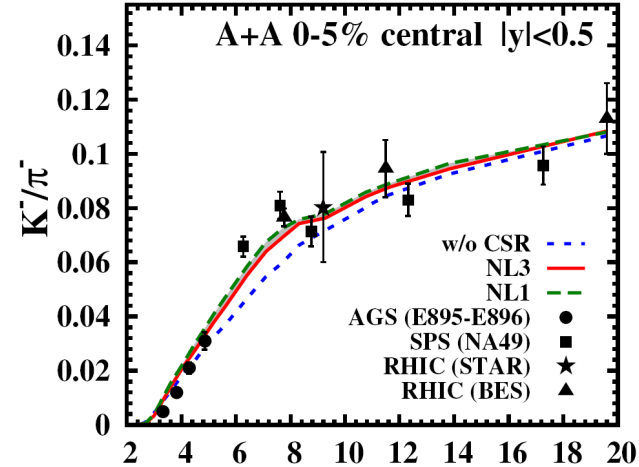
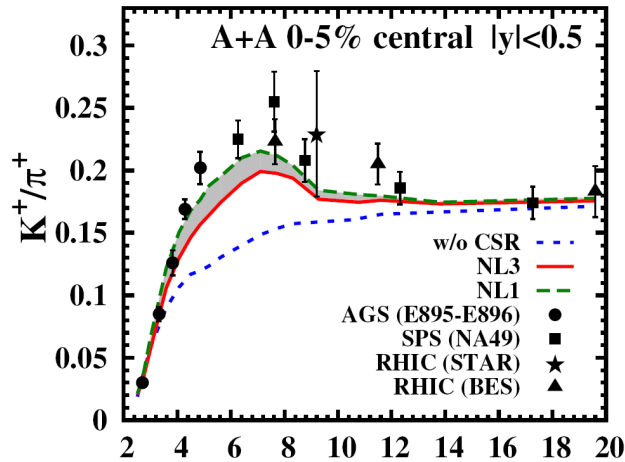


→ The **strangeness enhancement** seen experimentally at FAIR/NICA energies probably involves the approximate **restoration of chiral symmetry in the hadronic phase**



Excitation function of hadron ratios

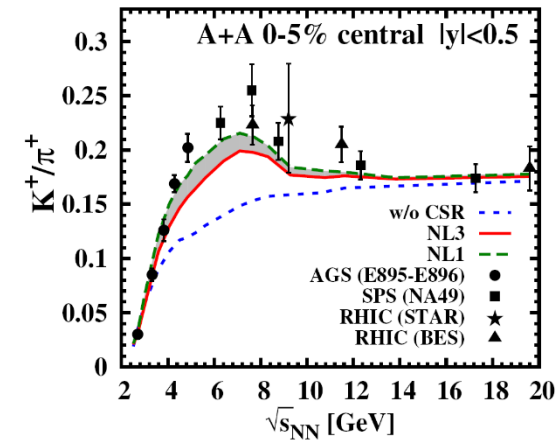
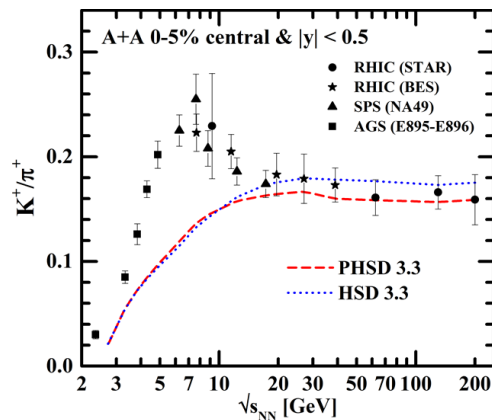
Alessia Palmese, Pierre Moreau:



→ low sensitivity to the nuclear EoS

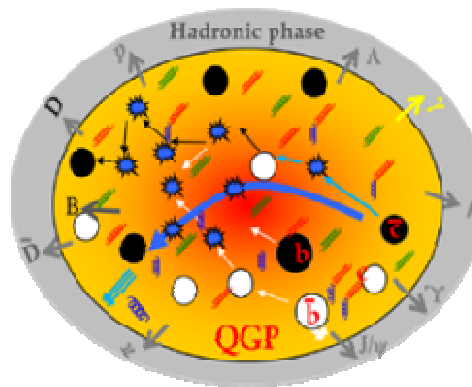


Summary I



- The **strangeness enhancement** seen experimentally by NA49 and STAR at a bombarding energy ~ 20 A GeV (FAIR/NICA energies!) cannot be attributed to deconfinement
- Including essential aspects of **chiral symmetry restoration** in the hadronic phase, we observe a **rise in the K^+/π^+ ratio** at low $\sqrt{s_{NN}}$ and then a **drop** due to the appearance of a deconfined partonic medium \rightarrow a **'horn'** emerges

Charm in A+A



Thanks to Taesoo Song, Hamza Berrehrah

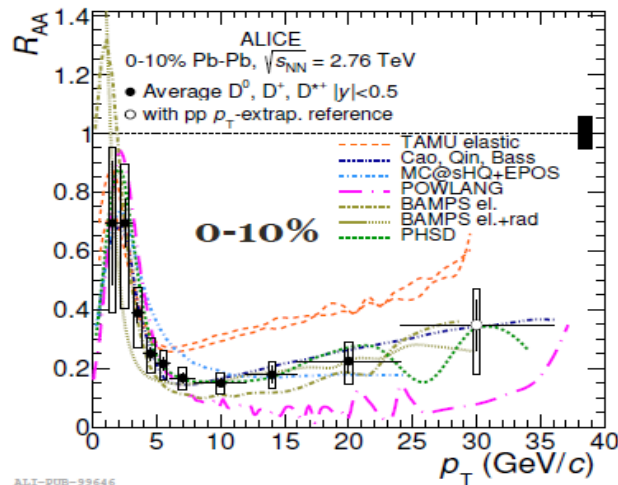
Tomography of QGP by heavy quarks

Hope to use 'heavy quark probes' for a tomography of the early stage of the QGP

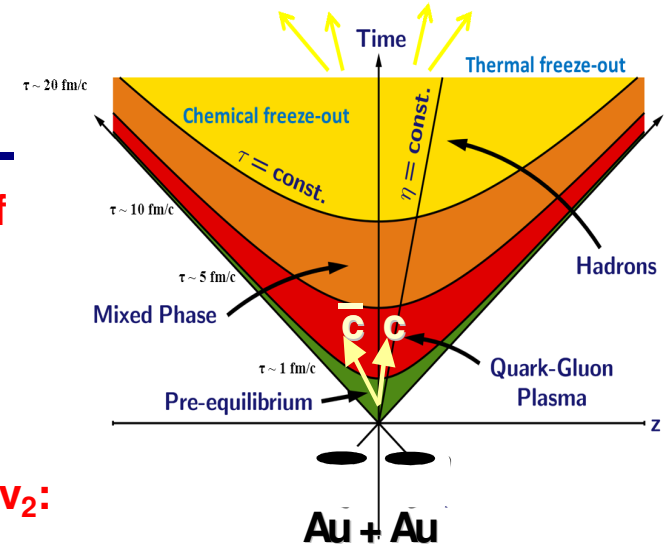
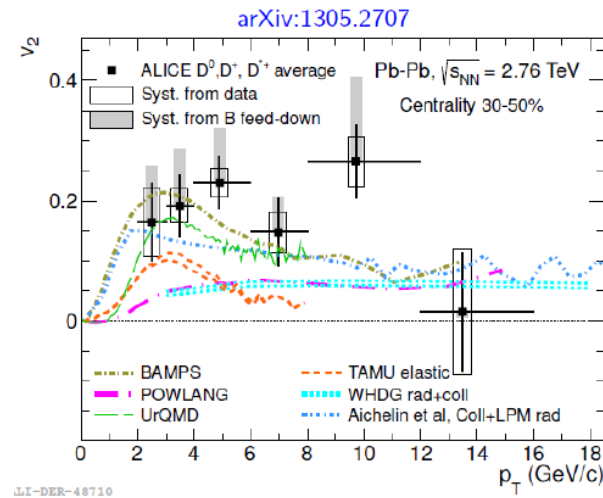
Experimental signals:

1. Nuclear modification factor:

$$R_{AA}(p_T) \equiv \frac{dN_D^{Au+Au}/dp_T}{N_{\text{binary}}^{Au+Au} \times dN_D^{p+p}/dp_T}$$



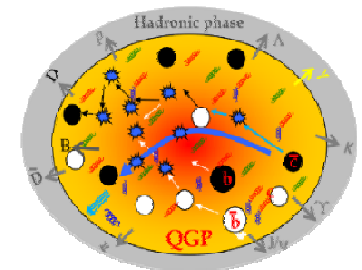
2. Elliptic flow v_2:



What is the origin for the “energy loss” of charm at large p_T?

Collisional energy loss (elastic scattering $Q+q \rightarrow Q+q$)
vs radiative (gluon bremsstrahlung $Q+q \rightarrow Q+q+g$) ?

→ Challenge for theory: simultaneous description of R_{AA} and v_2 !

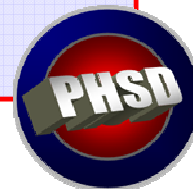
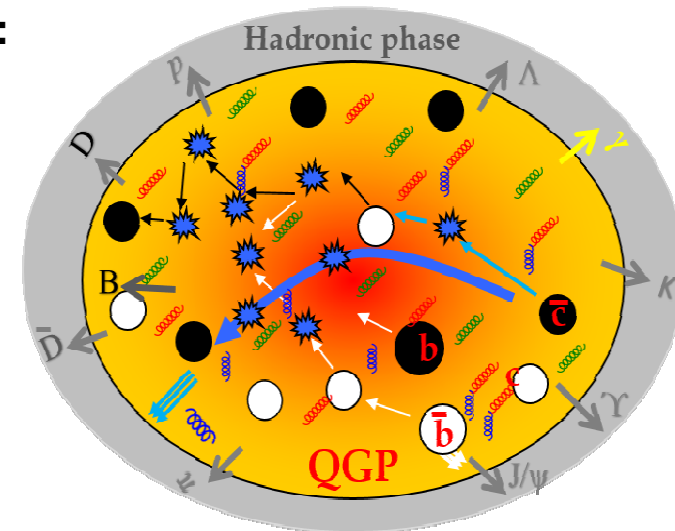


Dynamics of heavy quarks in A+A

1. **Production** of heavy (charm and bottom) quarks in initial binary collisions
2. **Interactions in the QGP:**
elastic scattering $Q+q \rightarrow Q+q$ → collisional energy loss
gluon bremsstrahlung $Q+q \rightarrow Q+q+g$ → radiative energy loss
3. **Hadronization:** c/cbar quarks → D(D*)-mesons:
coalescence vs fragmentation
4. **Hadronic interactions:**
D+baryons; D+mesons

The goal: to model the dynamics of charm quarks/mesons in all phases on a **microscopic basis**

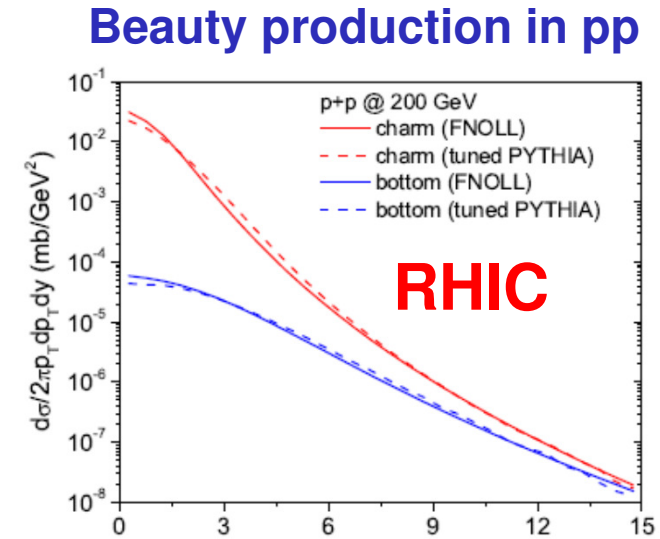
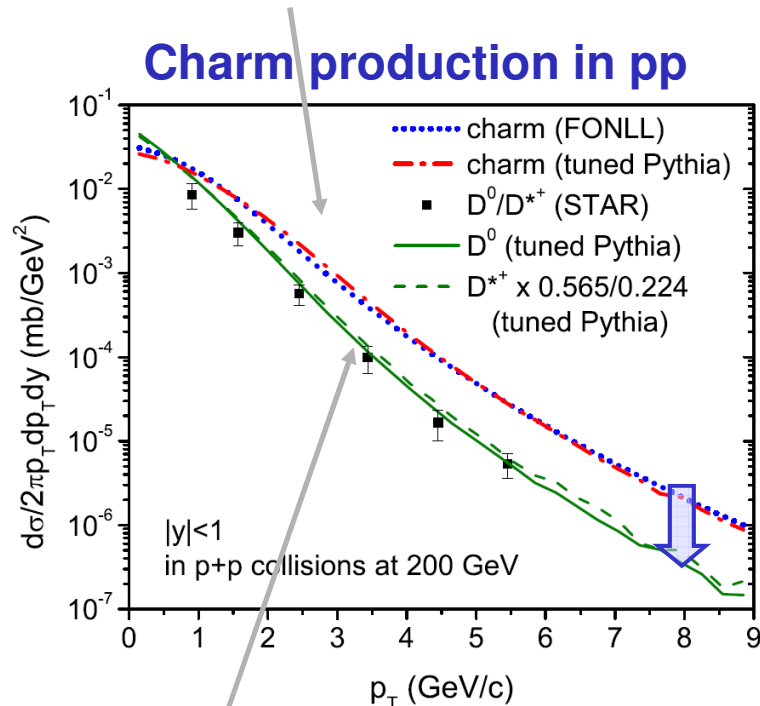
The tool: PHSD approach





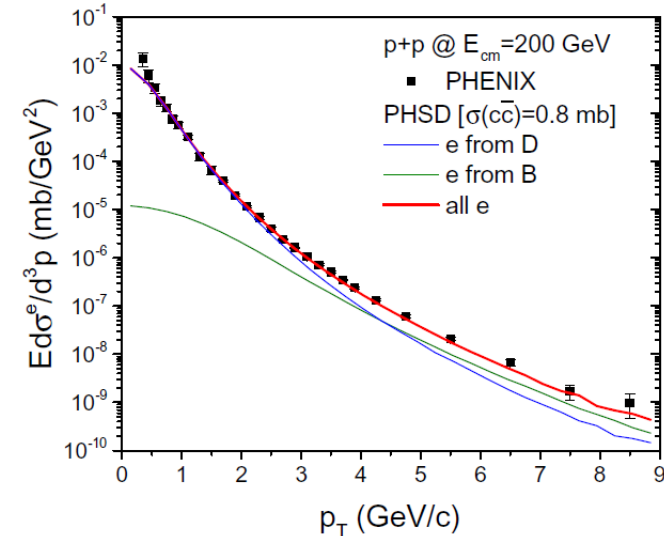
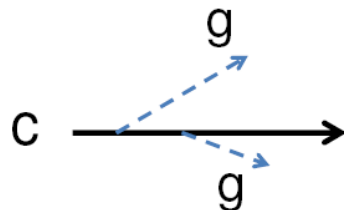
Heavy quark/hadrons production in p+p collisions

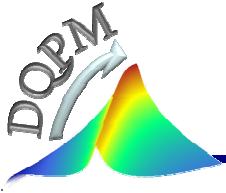
1) **Momentum distribution of heavy quarks:** use 'tuned' PYTHIA event generator to reproduce FONLL (fixed-order next-to-leading log) results (R. Vogt et al.)



2) **Charm/beauty hadron production in pp by heavy-quark fragmentation:**

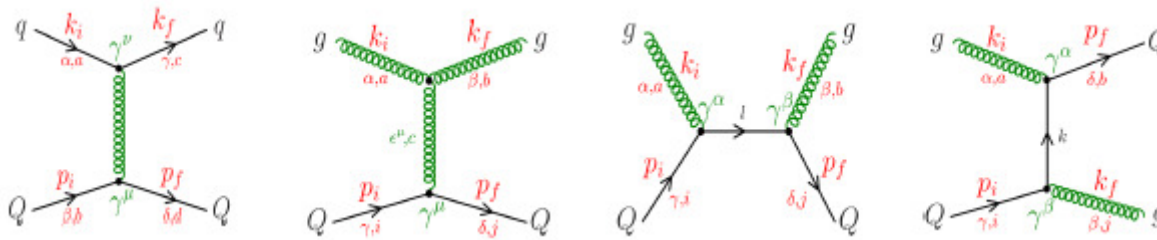
- D^0 20 %
- D^+ 17.4 %
- D^{*0} 21.3 %
- D^{*+} 22.4 %
- Ds^+ 8 %
- Λ_c 9.4 %



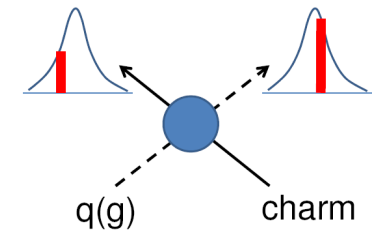


Heavy quark scattering in the QGP (DQPM)

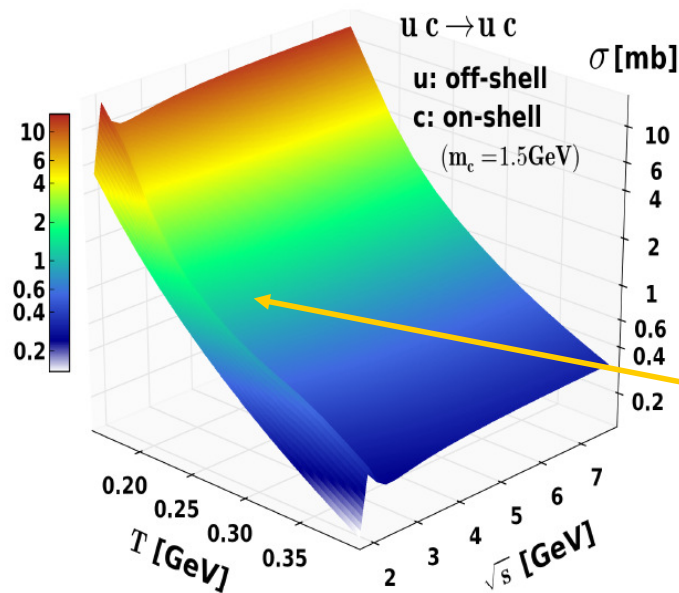
- Elastic scattering with off-shell massive partons $Q+q(g) \rightarrow Q+q(g)$



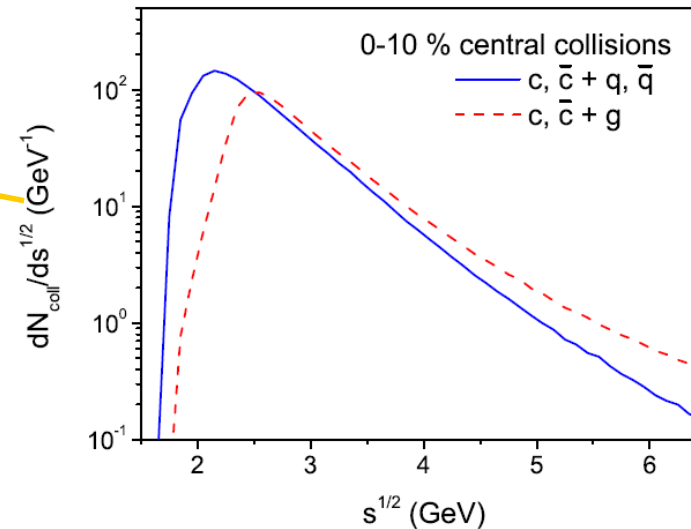
Non-perturbative QGP!

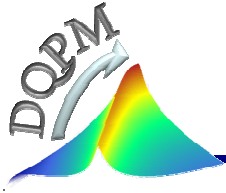


- Elastic cross section $uc \rightarrow uc$



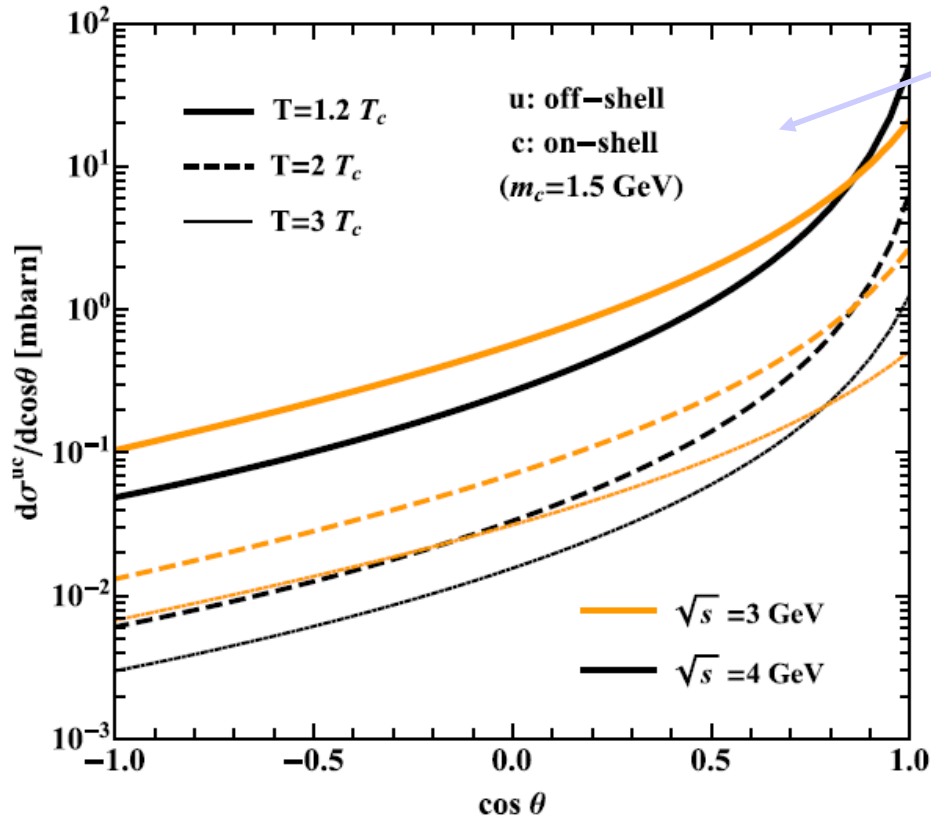
- Distributions of $Q+q$, $Q+g$ collisions vs $s^{1/2}$ in Au+Au, 10% central





Heavy quark scattering in the QGP

□ **Differential elastic cross section** for $uc \rightarrow uc$ for $s^{1/2} = 3$ and 4 GeV at $1.2T_c$, $2T_c$ and $3T_c$



□ **DQPM - anisotropic angular distribution**

Note: pQCD - strongly forward peaked
 → **Differences between DQPM and pQCD** :
 less forward peaked angular distribution
 leads to **more efficient momentum transfer**

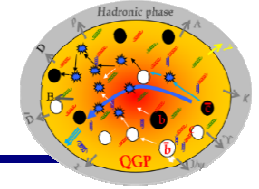
□ **Central Au+Au, 200 A GeV:**
 N(cc) ~ 19 pairs,
 N(Q+q) ~ 130, N(Q+g) ~ 85 collisions
 → each charm quark makes
 ~ **6 elastic collisions**

→ **Smaller number** (compared to pQCD)
 of elastic scatterings with **massive**
 partons leads to a **large energy loss**

! Note: **radiative energy loss** is **NOT included** yet in PHSD,
 it is expected to be **small** due to the large gluon mass in the DQPM



Hadronization of heavy quarks in A+A

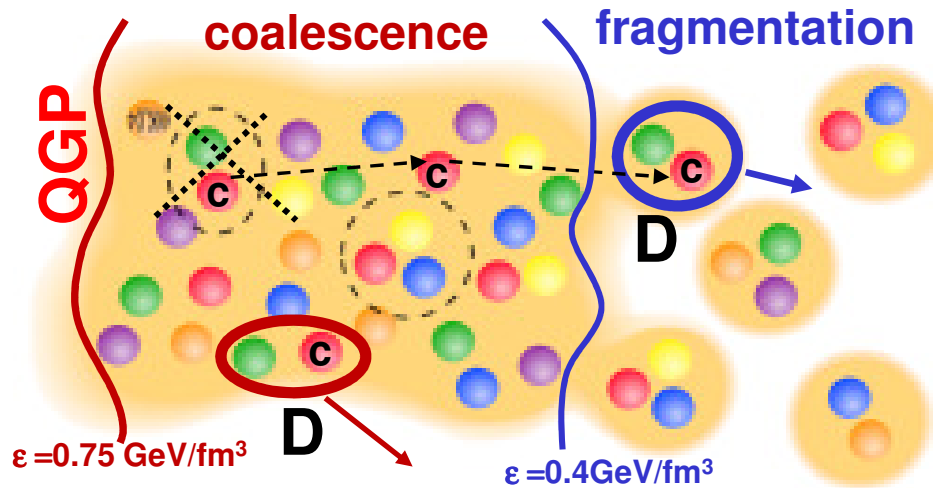


□ PHSD: if the local energy density $\epsilon \rightarrow \epsilon_C \rightarrow$ hadronization of heavy quarks to hadrons

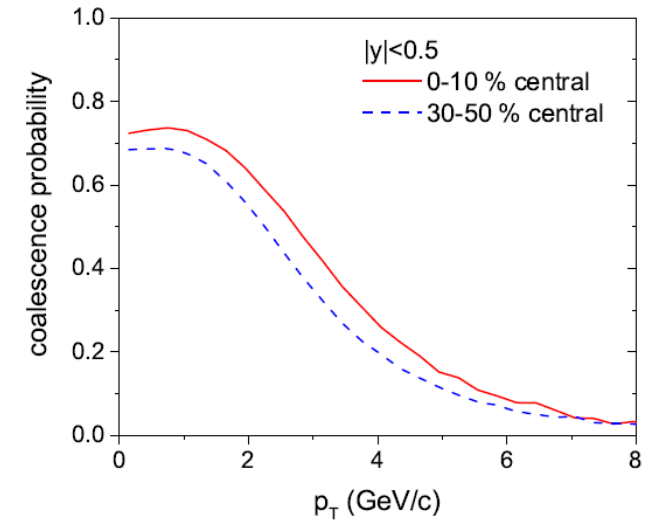
T. Song et al., PRC 93 (2016) 034906

Dynamical hadronization scenario for heavy quarks :

coalescence with $\langle r \rangle = 0.9$ fm & **fragmentation**
 $0.4 < \epsilon < 0.75$ GeV/fm³ $\epsilon < 0.4$ GeV/fm³



Coalescence probability in Au+Au at LHC



Coalescence probability for $c + \bar{q} \rightarrow D$

$$f(\rho, \mathbf{k}_\rho) = \frac{8g_M}{6^2} \exp \left[-\frac{\rho^2}{\delta^2} - \mathbf{k}_\rho^2 \delta^2 \right]$$

where $\rho = \frac{1}{\sqrt{2}}(\mathbf{r}_1 - \mathbf{r}_2)$, $\mathbf{k}_\rho = \sqrt{2} \frac{m_2 \mathbf{k}_1 - m_1 \mathbf{k}_2}{m_1 + m_2}$

← Width $\delta \leftarrow$ from root-mean-square radius of meson $\langle r \rangle$:

$$\langle r^2 \rangle = \frac{3}{2} \frac{m_1^2 + m_2^2}{(m_1 + m_2)^2} \delta^2$$

Degeneracy factor : $g_M = 1$ for D, = 3 for $D^* = D^*_0(2400)^0$, $D^*_1(2420)^0$, $D^*_2(2460)^{0\pm}$



Modelling of D-meson scattering in the hadronic gas

1. D-meson scattering with mesons

Model: effective chiral Lagrangian approach with heavy-quark spin symmetry

L. M. Abreu, D. Cabrera, F. J. Llanes-Estrada, J. M. Torres-Rincon, *Annals Phys.* 326, 2737 (2011)

Interaction of $D=(D^0, D^+, D^+_s)$ and $D^*=(D^{*0}, D^{*+}, D^{*+}_s)$ with octet $(\pi, K, Kbar, \eta)$:

$$\begin{aligned} \mathcal{L}_{LO} = & \langle \nabla^\mu D \nabla_\mu D^\dagger \rangle - m_D^2 \langle D D^\dagger \rangle - \langle \nabla^\mu D^{*\nu} \nabla_\mu D_\nu^{*\dagger} \rangle \\ & + m_D^2 \langle D^{*\mu} D_\mu^{*\dagger} \rangle + ig \langle D^{*\mu} u_\mu D^\dagger - D u^\mu D_\mu^{*\dagger} \rangle \\ & + \frac{g}{2m_D} \langle D^*_\mu u_\alpha \nabla_\beta D_\nu^{*\dagger} - \nabla_\beta D^*_\mu u_\alpha D_\nu^{*\dagger} \rangle \epsilon^{\mu\nu\alpha\beta} \end{aligned}$$

with

$$u_\mu = i (u^\dagger \partial_\mu u - u \partial_\mu u^\dagger)$$

$$U = u^2 = \exp\left(\frac{\sqrt{2}i\Phi}{f}\right) \quad \Phi = \begin{pmatrix} \frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{6}}\eta & \pi^+ & K^+ \\ \pi^- & -\frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{6}}\eta & K^0 \\ K^- & \bar{K}^0 & -\frac{2}{\sqrt{6}}\eta \end{pmatrix}$$

2. D-meson scattering with baryons

Model: G-matrix approach: interactions of $D=(D^0, D^+, D^+_s)$ and $D^*=(D^{*0}, D^{*+}, D^{*+}_s)$ with nucleon octet $J^P=1/2^+$ and Delta decuplet $J^P=3/2^+$

C. Garcia-Recio, J. Nieves, O. Romanets, L. L. Salcedo, L. Tolos, *Phys. Rev. D* 87, 074034 (2013)

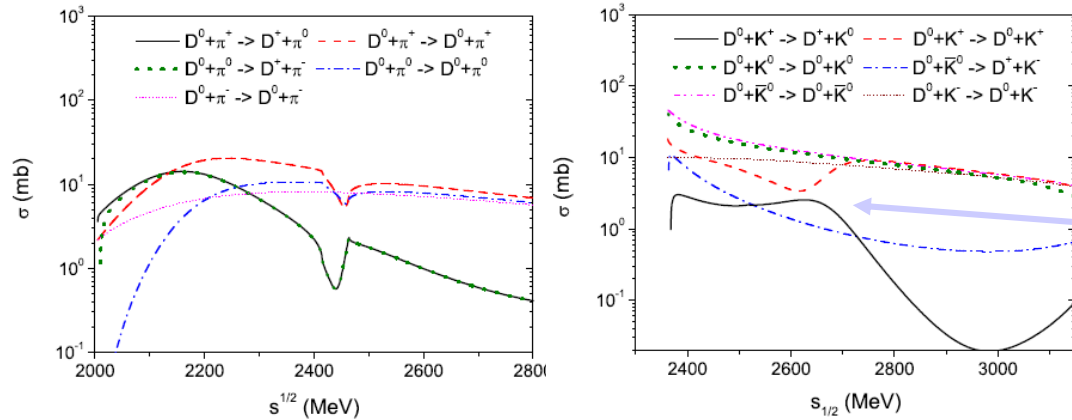
Unitarized scattering amplitude \rightarrow from solution of coupled-channel Bethe-Salpeter equations:

$$T = T + VGT$$



D-meson scattering in the hadron gas

1. D-meson scattering with mesons

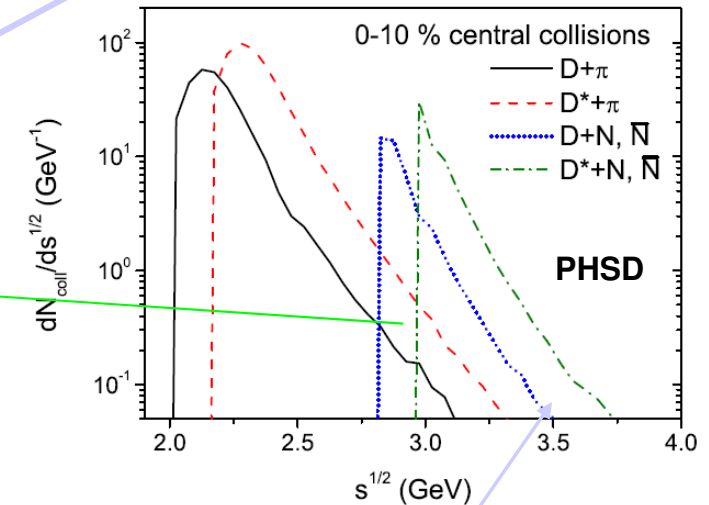
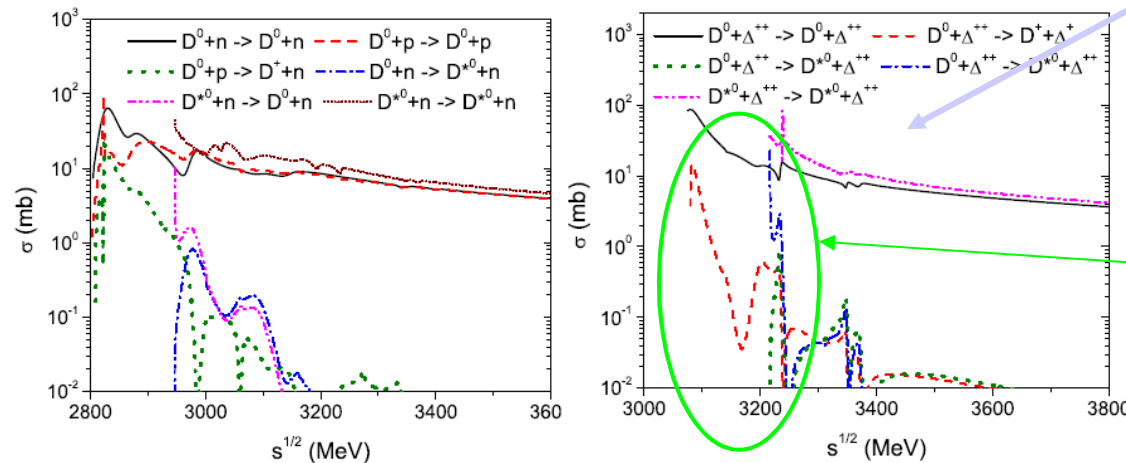


1a) cross sections with $m = \rho, \omega, \phi, K^*, \dots$ taken as

$$\sigma(D, D^* + m) = 10 \text{ mb}$$

→ Strong **isospin dependence** and complicated structure (due to the resonance coupling) of $D+m, D+B$ cross sections!

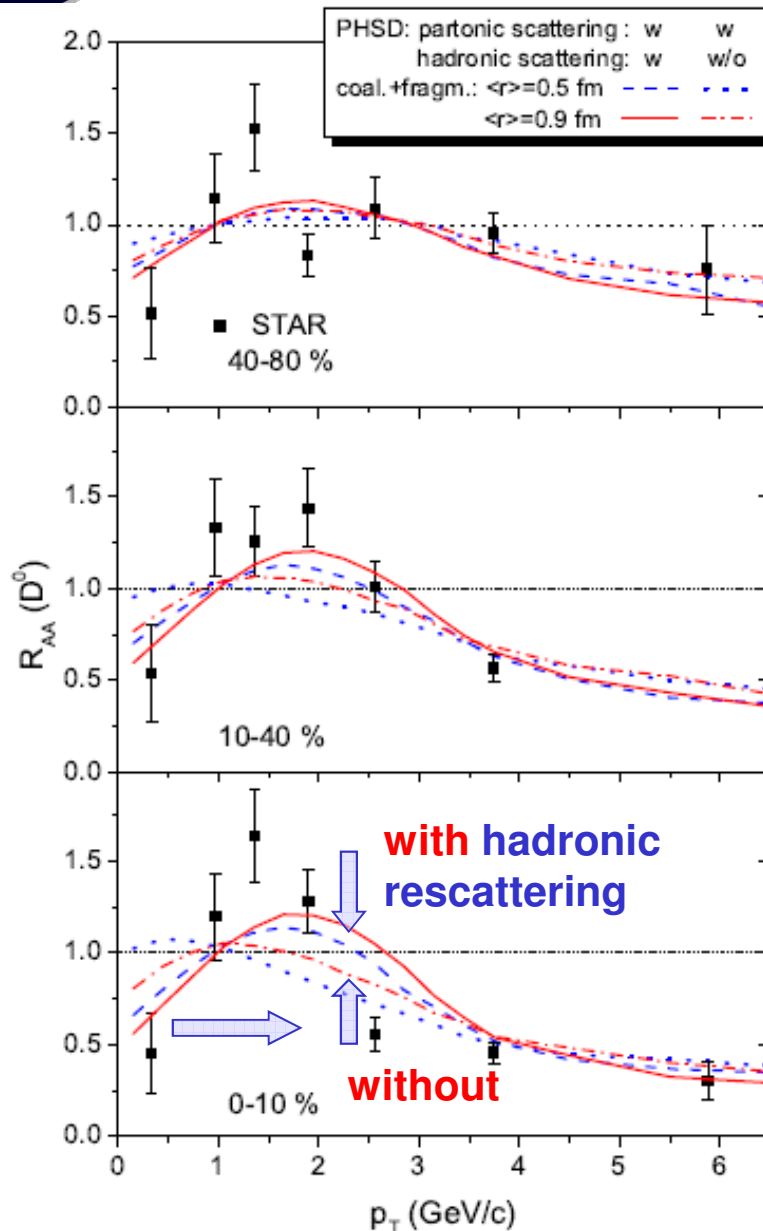
2. D-meson scattering with baryons



→ Hadronic interactions become ineffective for the energy loss of D, D^* mesons at high transverse momentum (i.e. large $s^{1/2}$)



R_{AA} at RHIC: hadronic rescattering



Influence of hadronic rescattering:

! Model study: (with partonic rescattering)
with / without hadronic rescattering

Central Au+Au at $s^{1/2} = 200$ GeV :

$N(D, D^*) \sim 30$

$N(D, D^* + m) \sim 56$ collisions

$N(D, D^* + B, Bbar) \sim 10$ collisions

→ each D, D^* makes

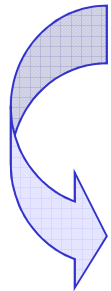
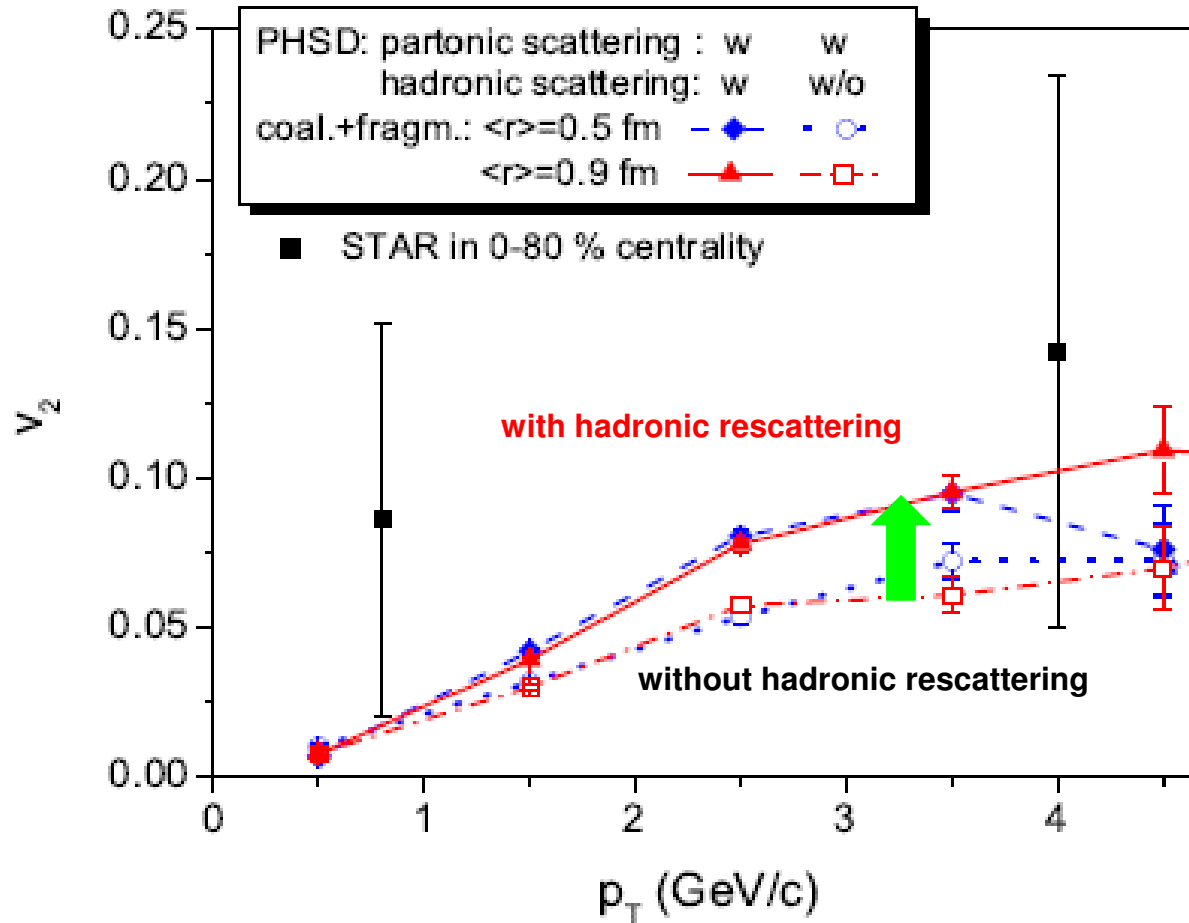
~ 2 scatterings with hadrons

□ Hadronic rescattering moves R_{AA} peak to higher p_T !

□ The height and position of the R_{AA} peak at low p_T depends on the hadronization scenario: coalescence/fragmentation!



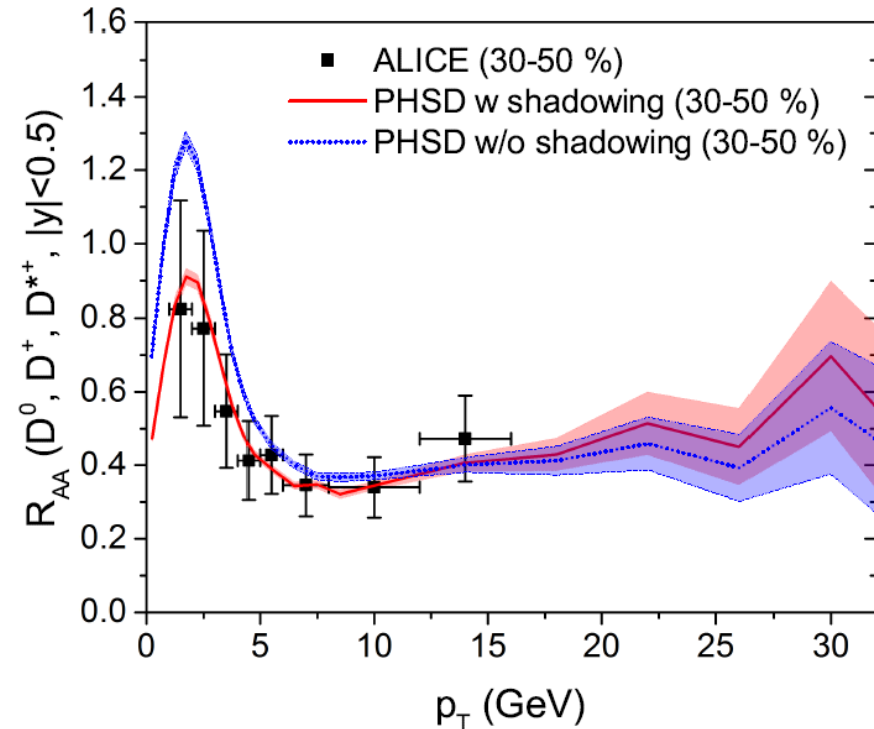
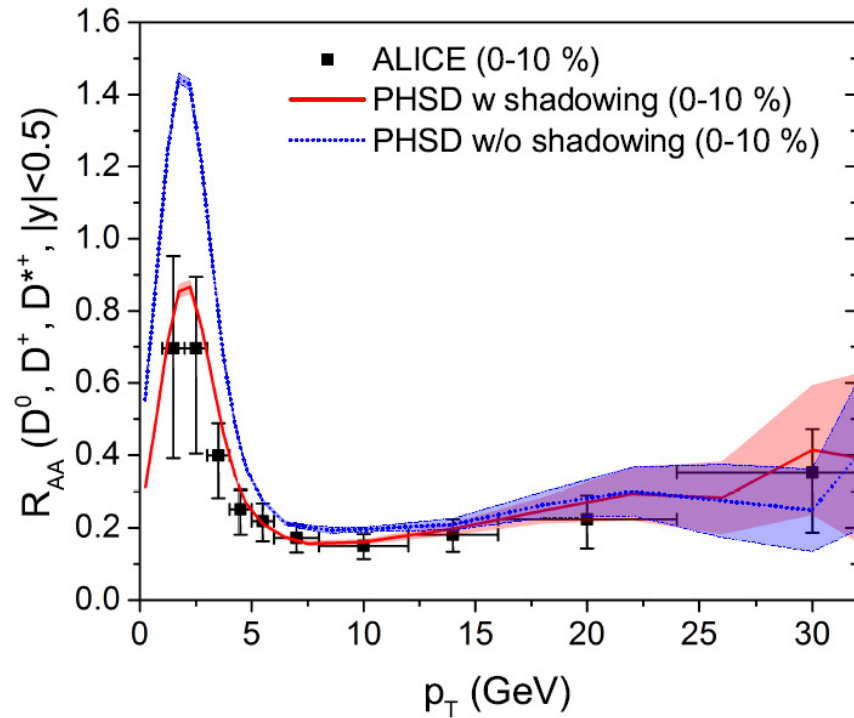
D-meson elliptic flow v_2 at RHIC



- Hadronic rescattering substantially increases v_2 at larger p_T
- v_2 is less sensitive to the hadronization scenarios than R_{AA}



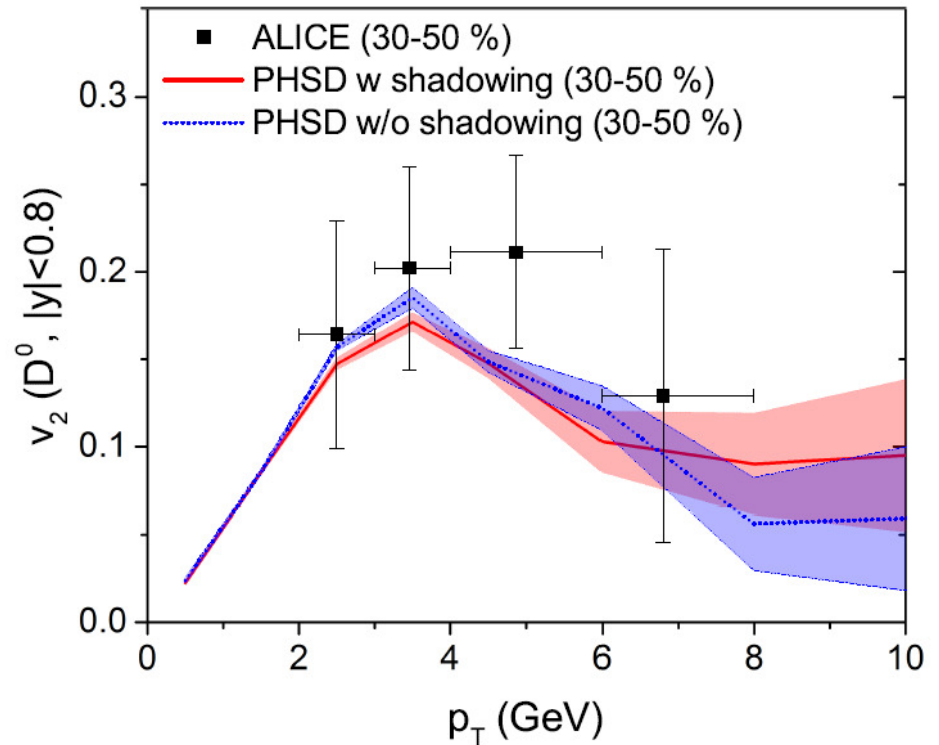
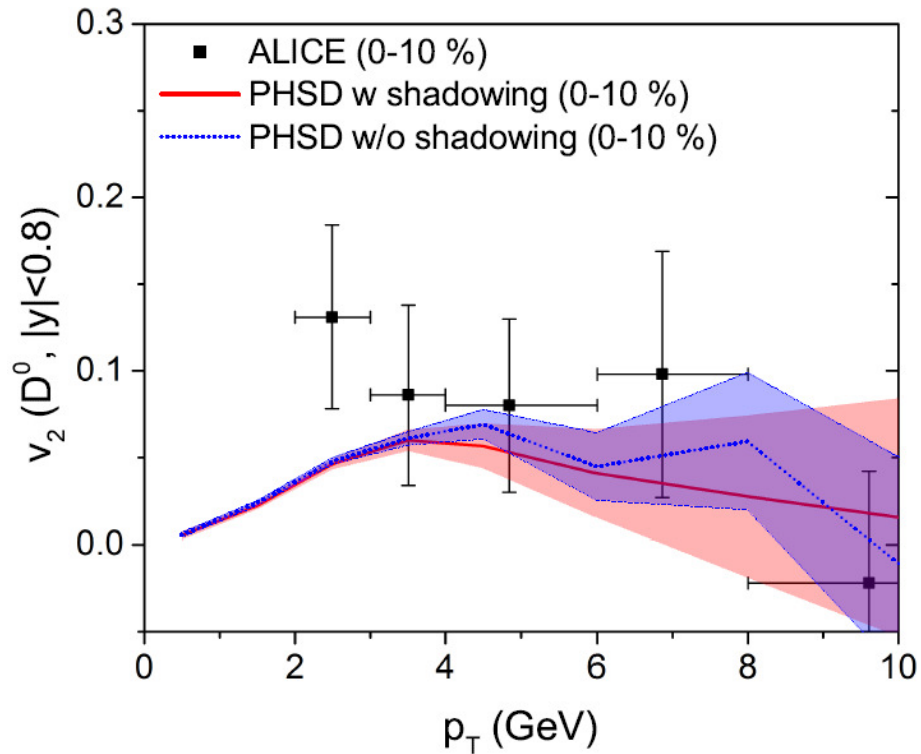
Charm R_{AA} at LHC



- in PHSD the energy loss of D-mesons at high p_T can be dominantly attributed to partonic scattering
- Shadowing effect suppresses the low p_T and slightly enhances the high p_T part of R_{AA}
- Hadronic rescattering moves R_{AA} peak to higher p_T



Charm v_2 at LHC

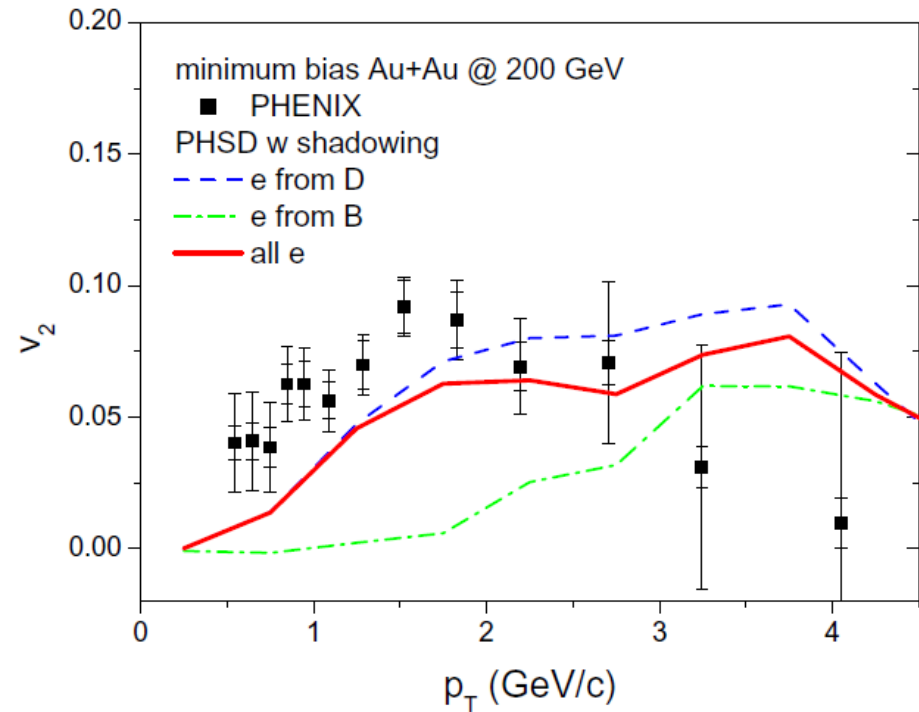
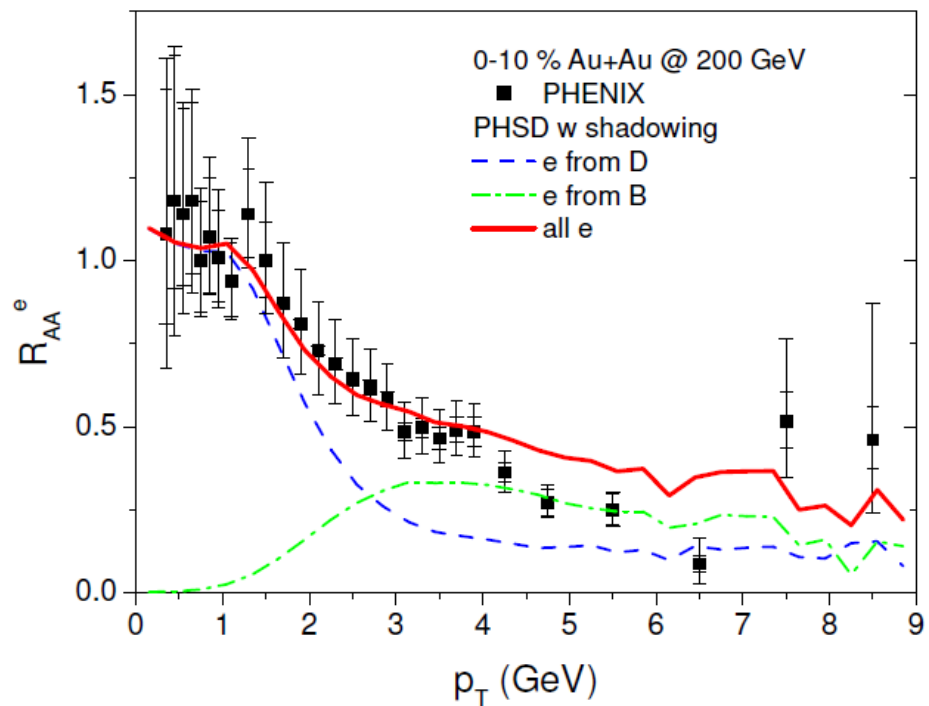


- Shadowing effect has small impact on v_2
- **Hadronic rescattering** increases v_2



R_{AA}^e and v_2^e from single electrons: beauty contribution

R_{AA} and v_2 vs p_T from single electrons in Au+Au @ 200 GeV

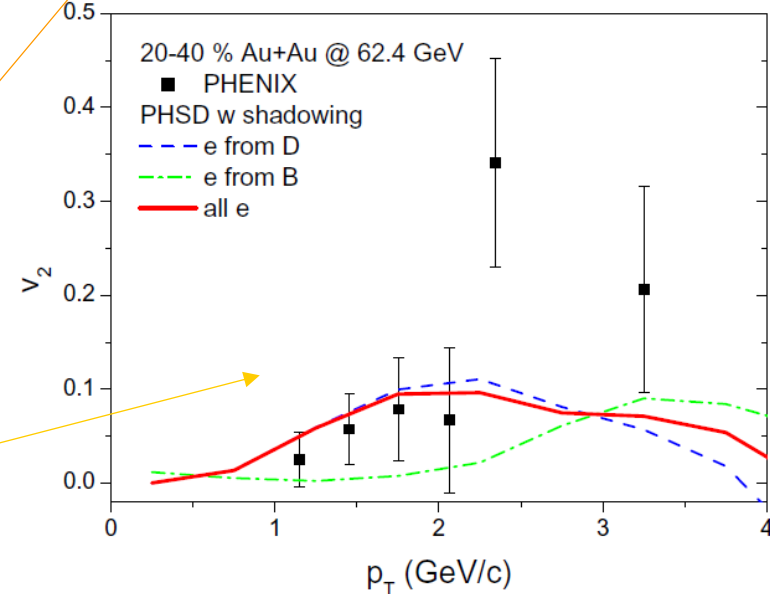
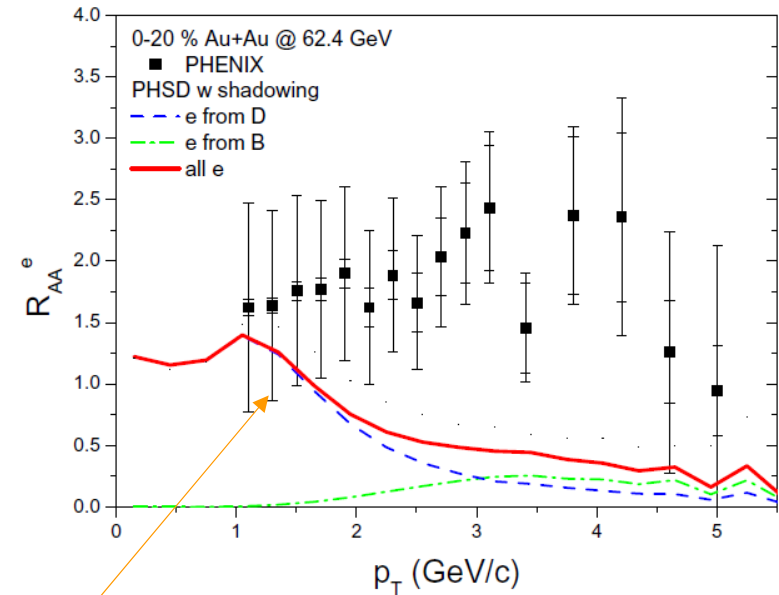
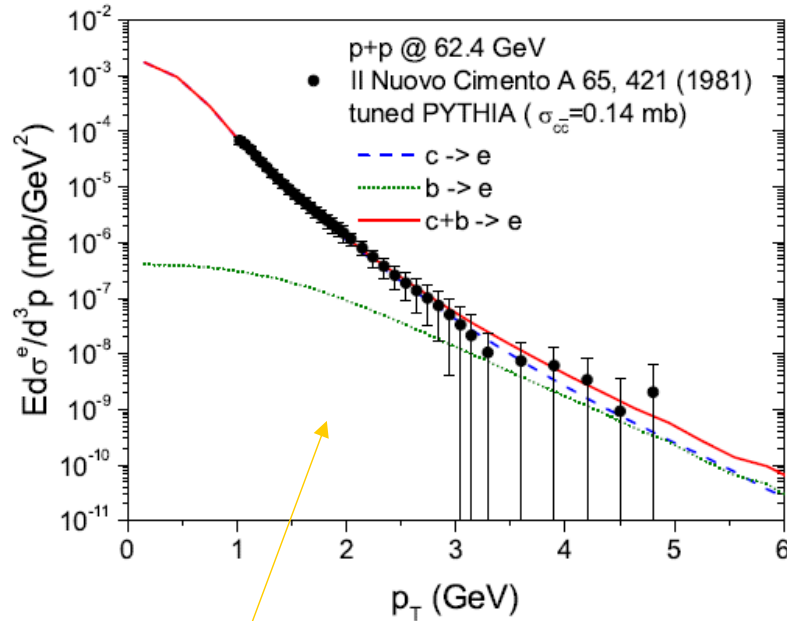


□ Feed back from beauty contribution becomes dominant at $p_T > 3$ GeV

T. Song et al., in progress



R_{AA}^e and v_2^e from single electrons from Au+Au at 62.4 GeV

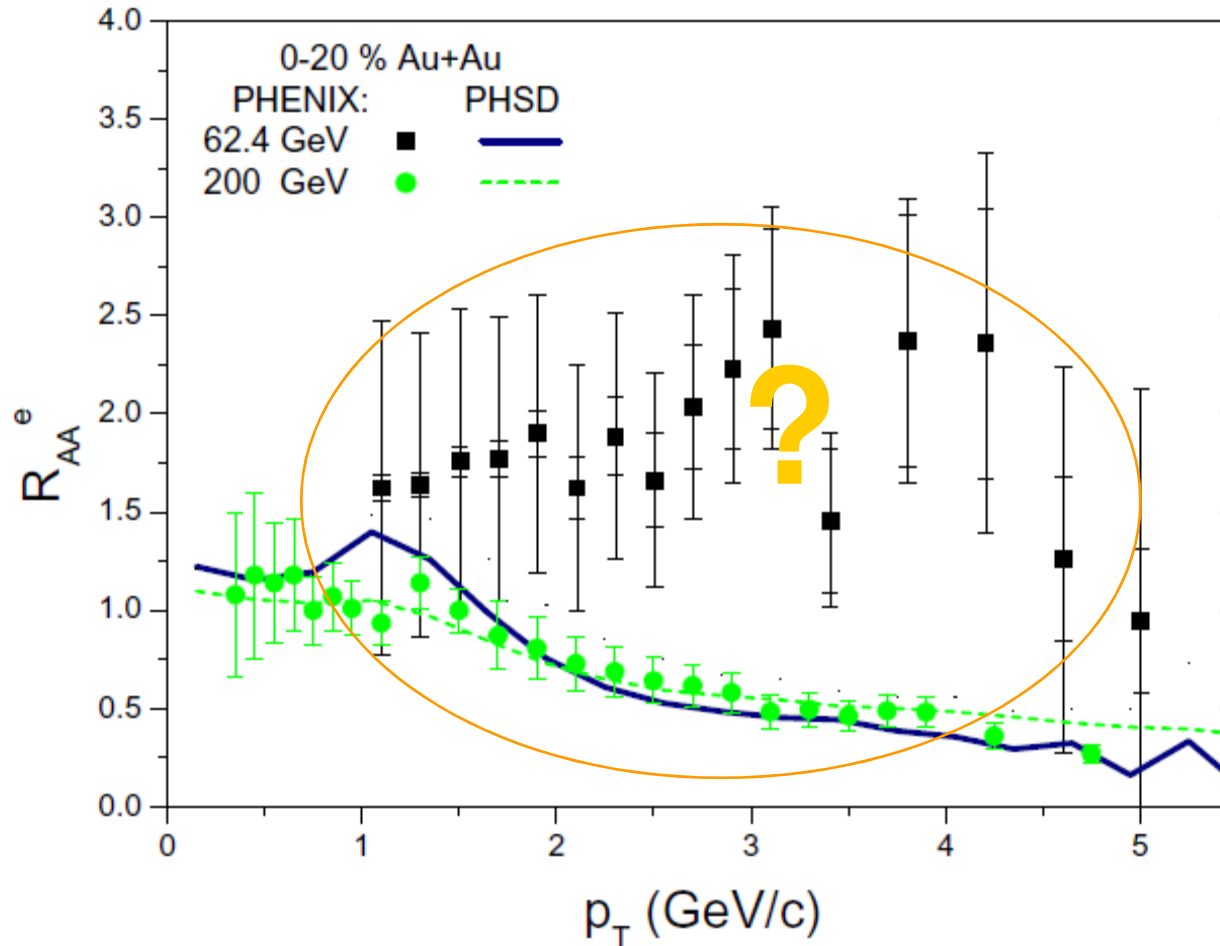


- ❑ PHSD: **pp data on electron p_T spectra** are well reproduced
- ❑ PHENIX data on **R_{AA}^e from single electrons from Au+Au at 62.4 GeV** are not reproduced
- ❑ **v_2^e from single electrons from Au+Au at 62.4 GeV** is in line with data

T. Song et al., in progress



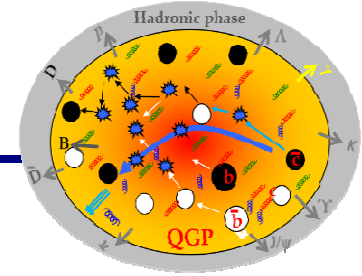
R_{AA}^e from single electrons: 62.4 vs. 200 GeV



□ PHENIX: R_{AA}^e from single electrons from Au+Au at 62.4 GeV are much larger than at 200 GeV !

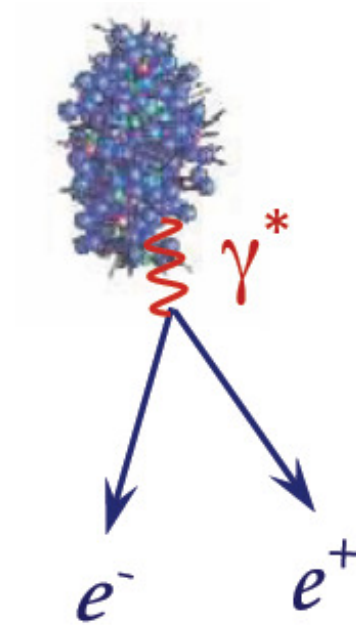


Summary II



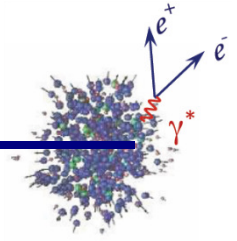
- **PHSD** provides a **microscopic description** of non-equilibrium charm dynamics in the partonic and hadronic phases
- **Partonic rescattering** suppresses the high p_T part of R_{AA} , generates v_2
- **Hadronic rescattering** moves R_{AA} peak to higher p_T , increases v_2
- The structure of R_{AA} at low p_T is sensitive to the **hadronization scenario**, i.e. to the balance between **coalescence and fragmentation**
- **Shadowing effects** suppress R_{AA} at LHC
- The **exp data** for the R_{AA} and v_2 at RHIC and LHC are described in the PHSD:
 - by **QGP collisional energy loss** due to the **elastic scattering** of charm quarks with massive quarks and gluons in the QGP phase
 - + by the **dynamical hadronization scenario** „coalescence & fragmentation“
 - + by **strong hadronic interactions** due to the elastic scattering of D, D^* mesons with mesons and baryons
- Feed back from **beauty contribution** for R_{AA}^e and v_2^e from single electrons from Au+Au at 200 GeV becomes dominant at $p_T > 3$ GeV

Dileptons



Thanks to Olena Linnyk

Dilepton sources



from the QGP via partonic (q,qbar, g) interactions:



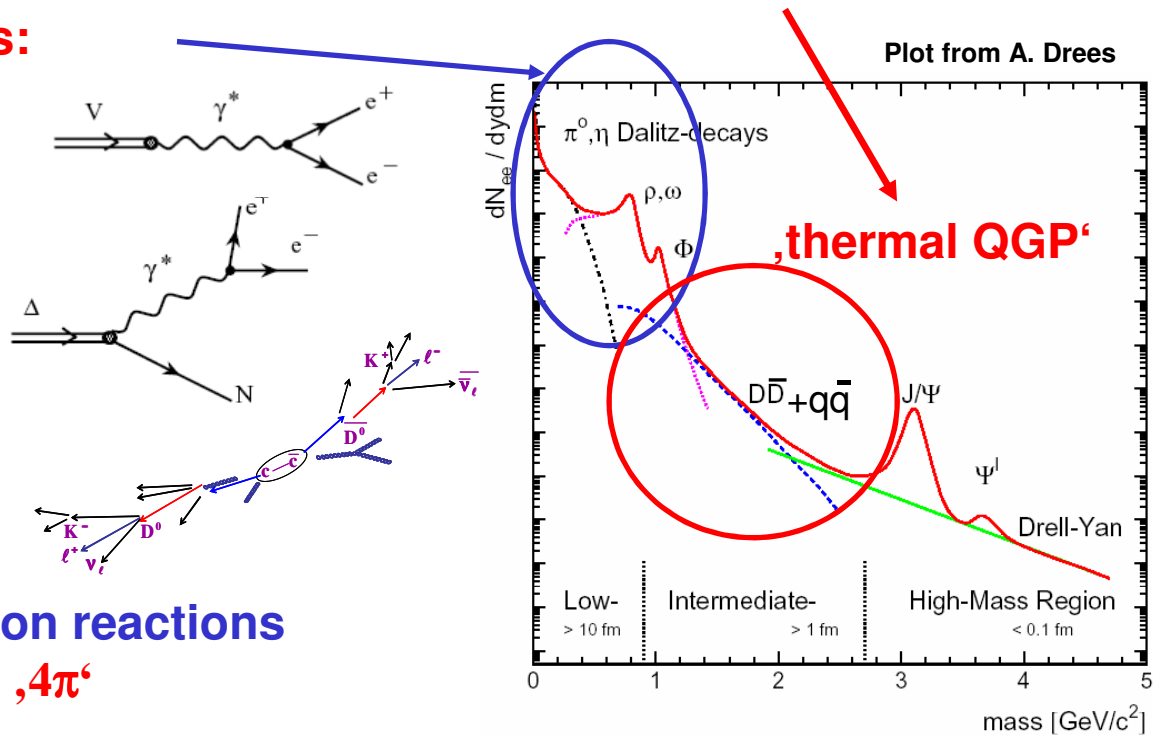
from hadronic sources:

- direct decay of vector mesons ($\rho, \omega, \phi, J/\Psi, \Psi'$)

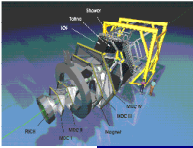
- Dalitz decay of mesons and baryons ($\pi^0, \eta, \Delta, \dots$)

- correlated D+Dbar pairs

- radiation from multi-meson reactions ($\pi+\pi, \pi+\rho, \pi+\omega, \rho+\rho, \pi+a_1$) - „ 4π “



! Advantage of dileptons:
 additional „degree of freedom“ (M) allows to disentangle various sources



Dileptons at SIS energies - HADES

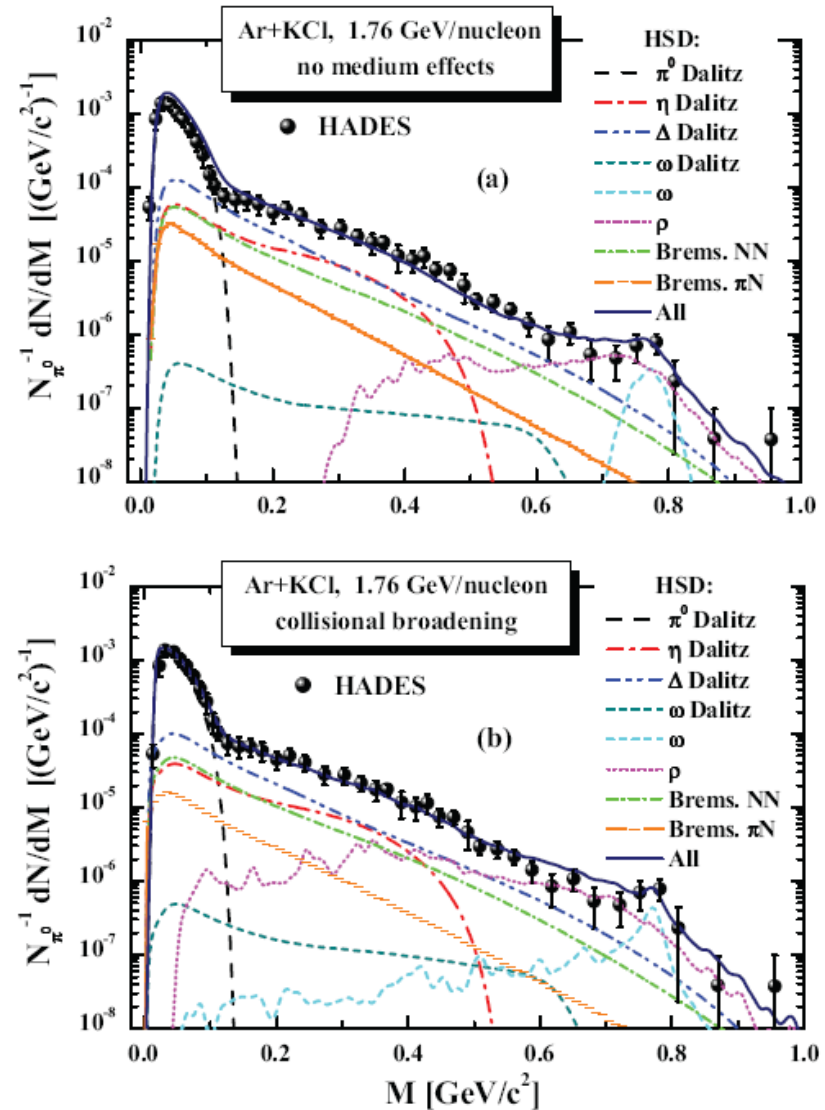
□ **HADES:** dilepton yield dN/dM scaled with the **number of pions N_{π^0}**

□ **Dominant hadronic sources at $M > m_{\pi}$:**

- η, Δ Dalitz decays
- NN bremsstrahlung
- direct ρ decay

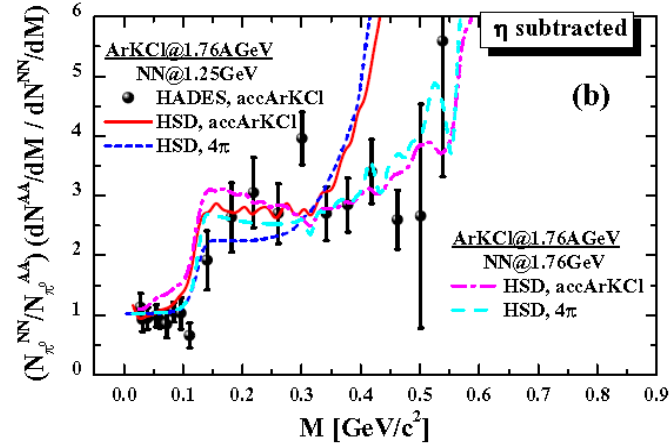
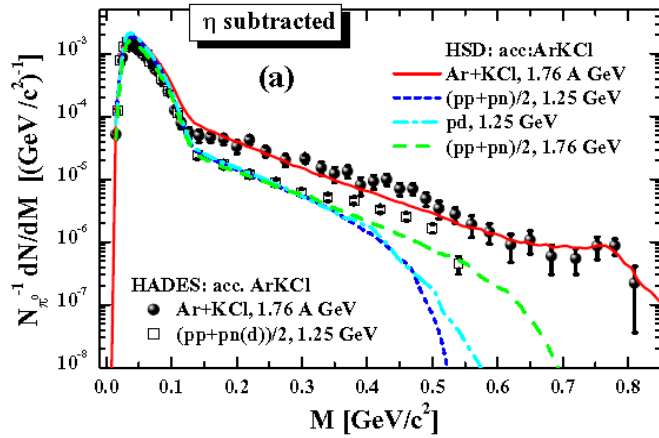
➤ ρ meson = strongly interacting resonance
strong collisional broadening of the ρ width

- In-medium effects are more pronounced for heavy systems such as Ar+KCl then C+C
- The peak at $M \sim 0.78$ GeV relates to ω/ρ mesons decaying in vacuum

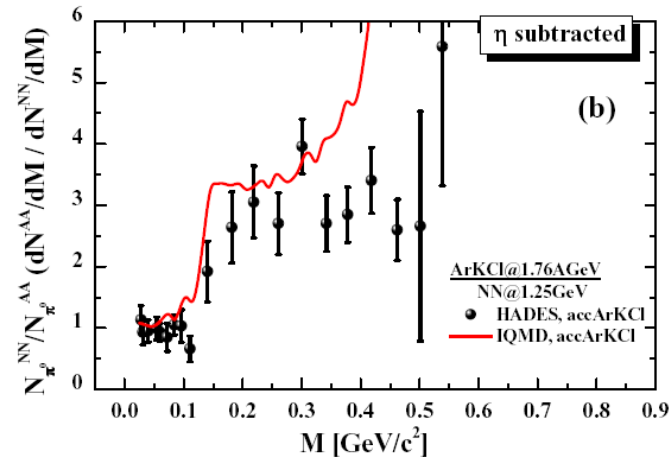
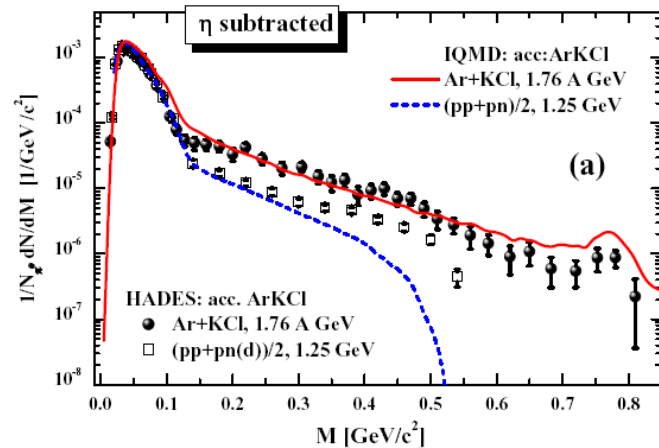


Dileptons at SIS energies: A+A vs. N+N

- ratio of AA/NN spectra (scaled by $N_{\pi 0}$) after subtracted η contribution



■ HSD



■ IQMD

➔ Strong enhancement of dilepton yield in A+A vs. NN is reproduced by HSD and IQMD for C+C at 1.0, 2.0 A Gev and Ar+KCl at 1.75 A GeV

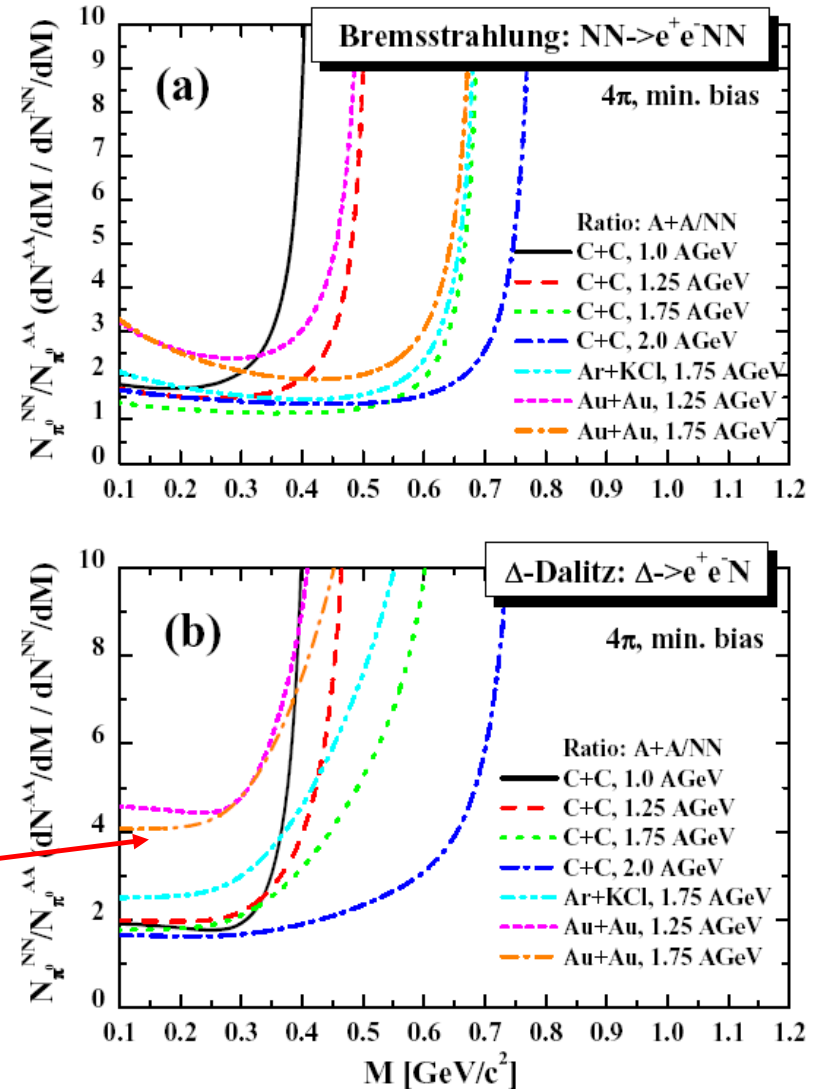
Dileptons at SIS (HADES): A+A vs NN

Two contributions to the enhancement of dilepton yield in A+A vs. NN

1) the **pN bremsstrahlung** which scales with the number of collisions and not with the number of participants, i.e. pions;

2) the **multiple Δ regeneration** – dilepton emission from intermediate Δ 's which are part of the reaction cycles $\Delta \rightarrow \pi N$; $\pi N \rightarrow \Delta$ and $NN \rightarrow N\Delta$; $N\Delta \rightarrow NN$

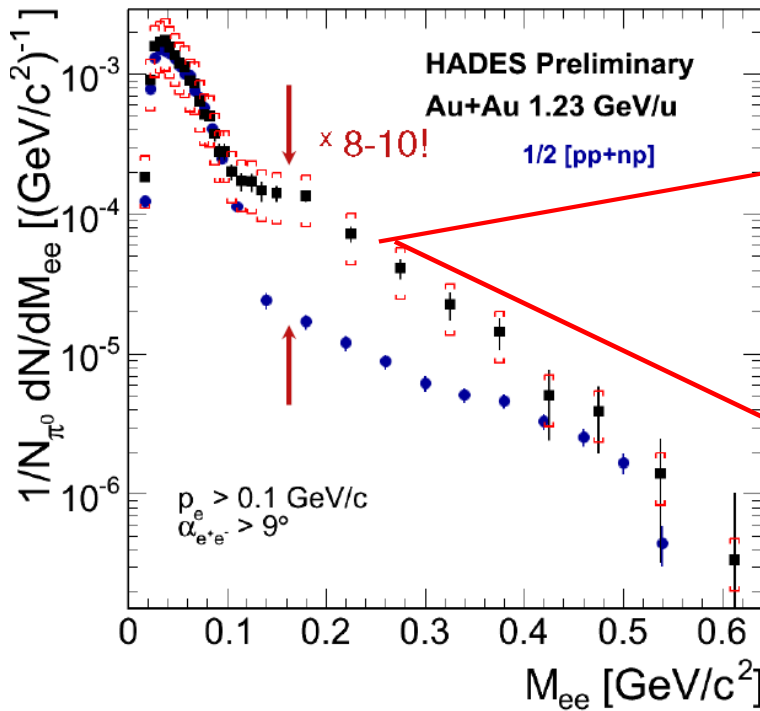
Enhancement of dilepton yield in A+A vs. NN increases with the system size!



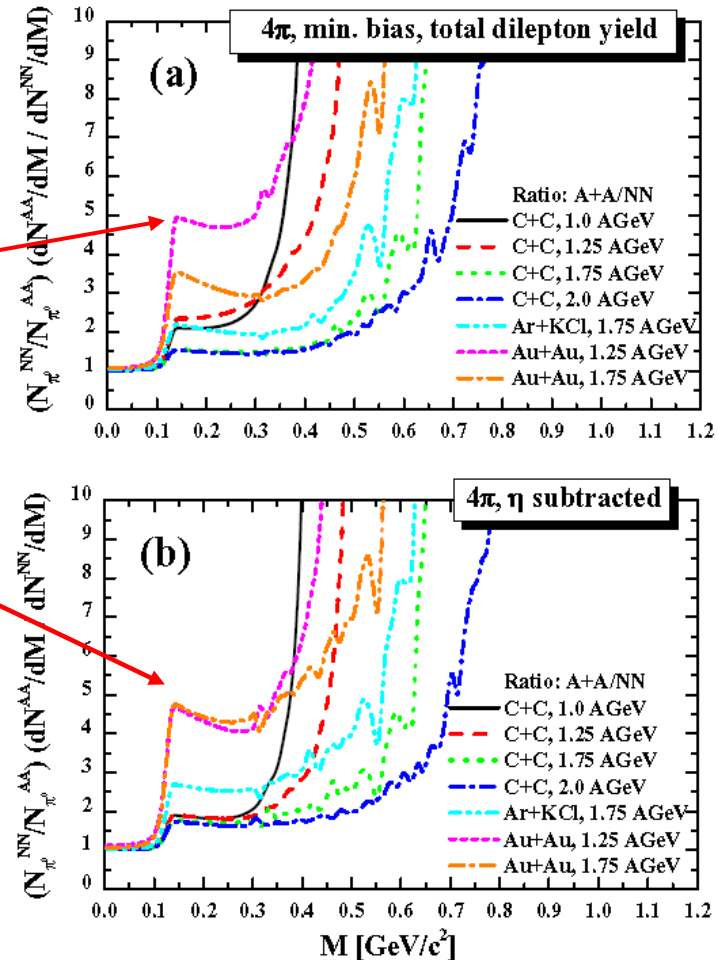
Dileptons at SIS (HADES): Au+Au

HADES preliminary: Au+Au, 1.23 A GeV

T. Galatyuk, QM'2014



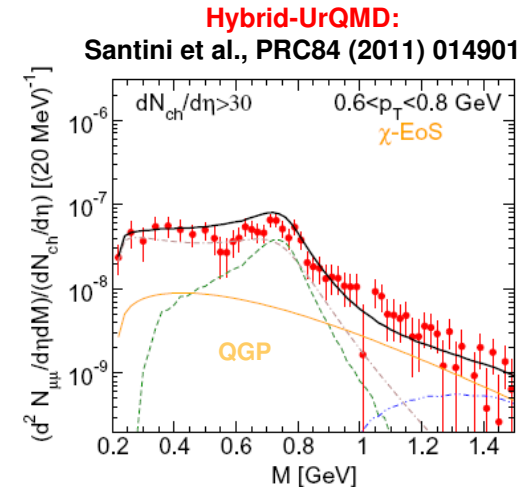
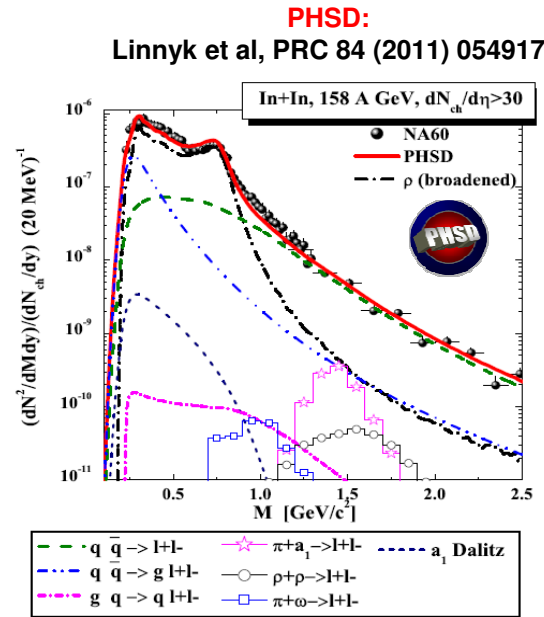
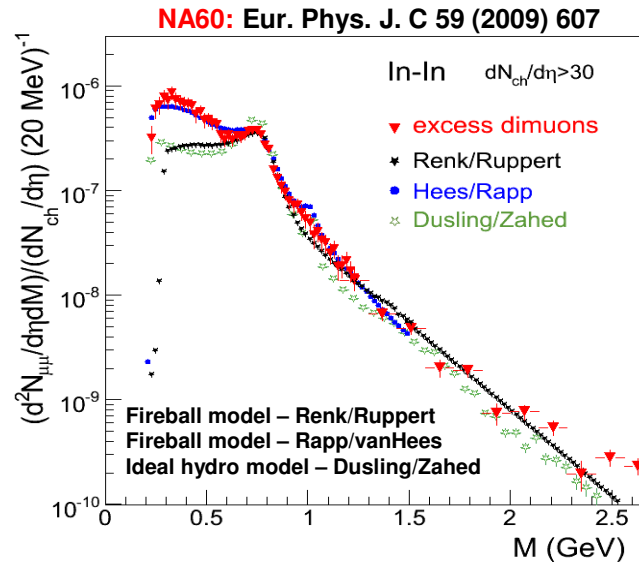
▪ HSD predictions (2013)



- Strong in-medium enhancement of dilepton yield in Au+Au vs. NN
- related to Δ regeneration

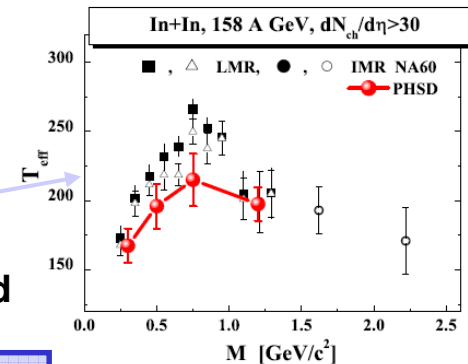
Lessons from SPS: NA60

Dilepton invariant mass spectra:



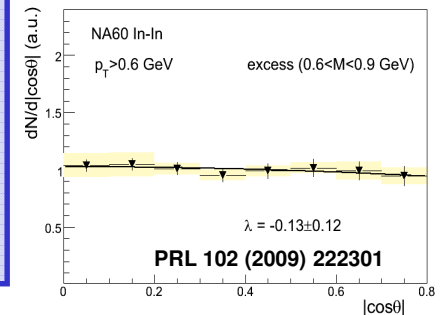
Inverse slope parameter T_{eff} :

spectrum from QGP is softer than from hadronic phase since the QGP emission occurs dominantly before the collective radial flow has developed



Message from SPS: (based on NA60 and CERES data)

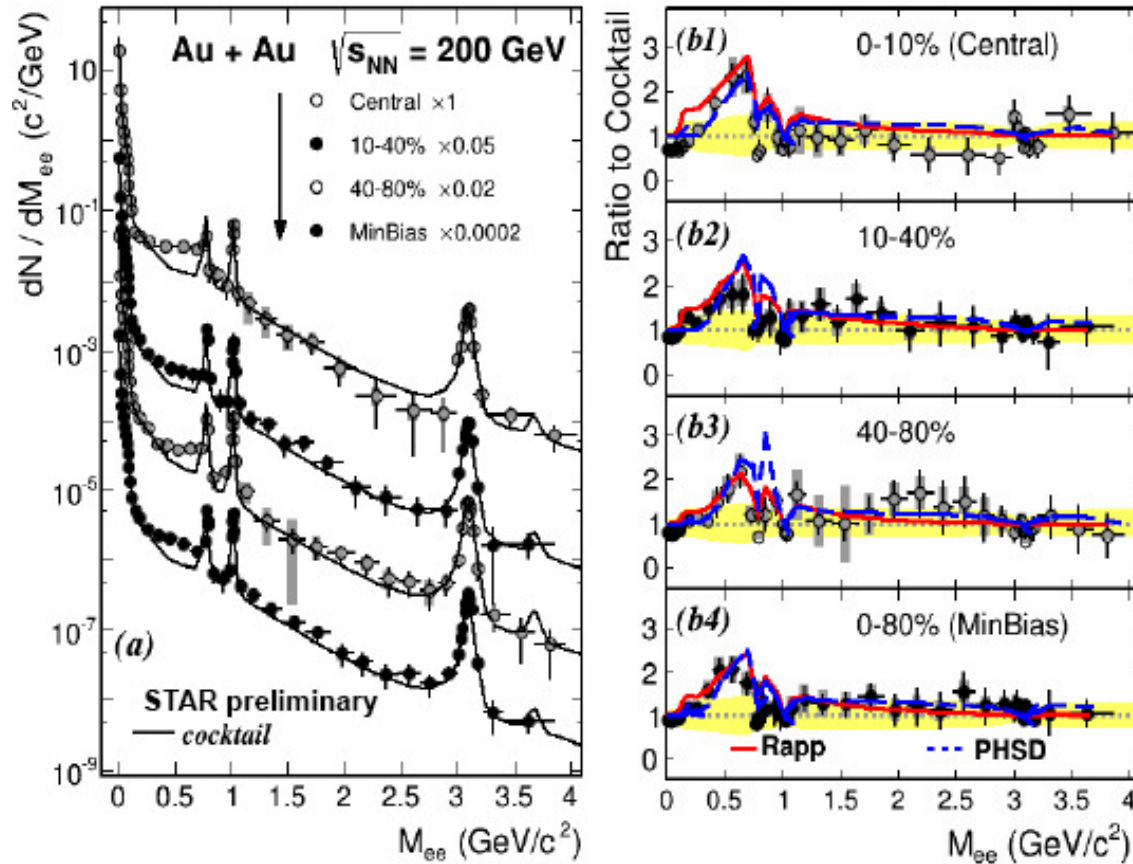
- 1) Low mass spectra - evidence for the **in-medium broadening of ρ -mesons**
- 2) Intermediate mass spectra above 1 GeV - dominated by **partonic radiation**
- 3) The rise and fall of T_{eff} – evidence for the thermal **QGP radiation**
- 4) **Isotropic angular distribution** – indication for a **thermal origin of dimuons**



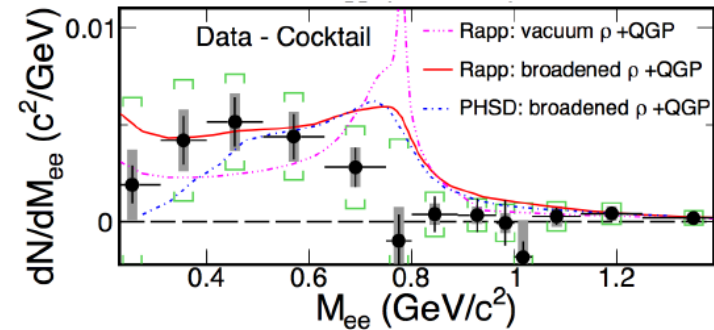
Dileptons at RHIC: STAR data vs model predictions

(STAR: arXiv:1407.6788)

Centrality dependence of dilepton yield



Excess in low mass region, min. bias



Models (predictions):

- Fireball model – R. Rapp
- PHSD

Low masses:

collisional broadening of ρ

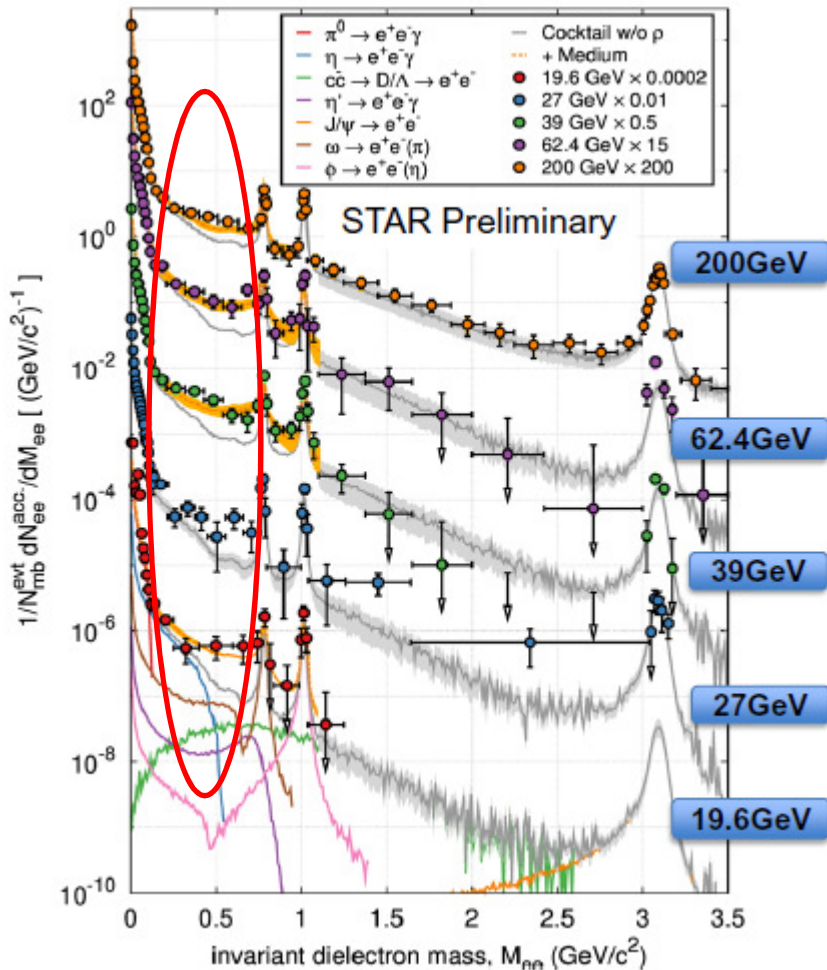
Intermediate masses:

QGP dominant

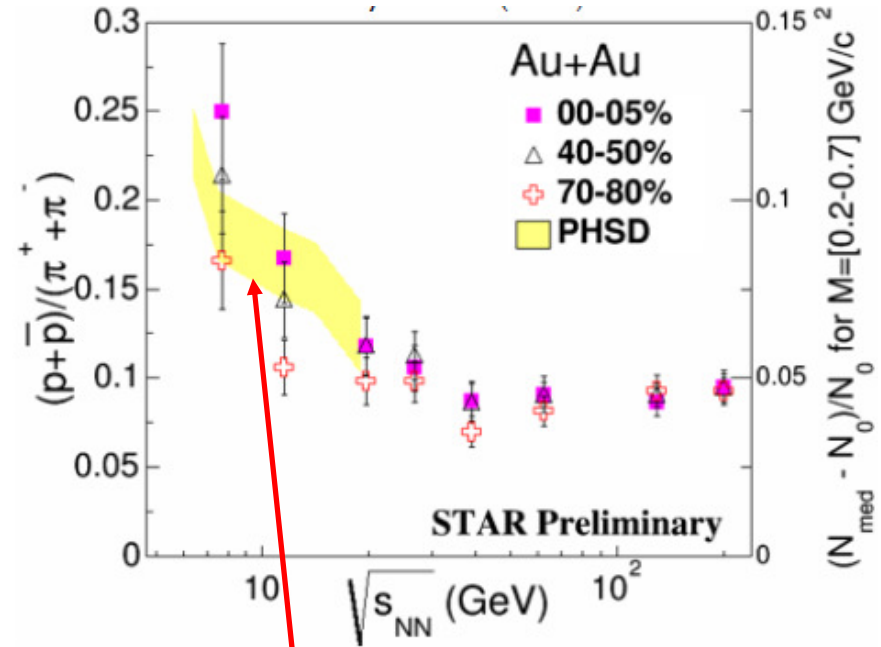
Message: STAR data are described by models within a collisional broadening scenario for the vector meson spectral function + QGP

Dileptons from RHIC BES: STAR

(Talk by Nu Xu at QM'2014)



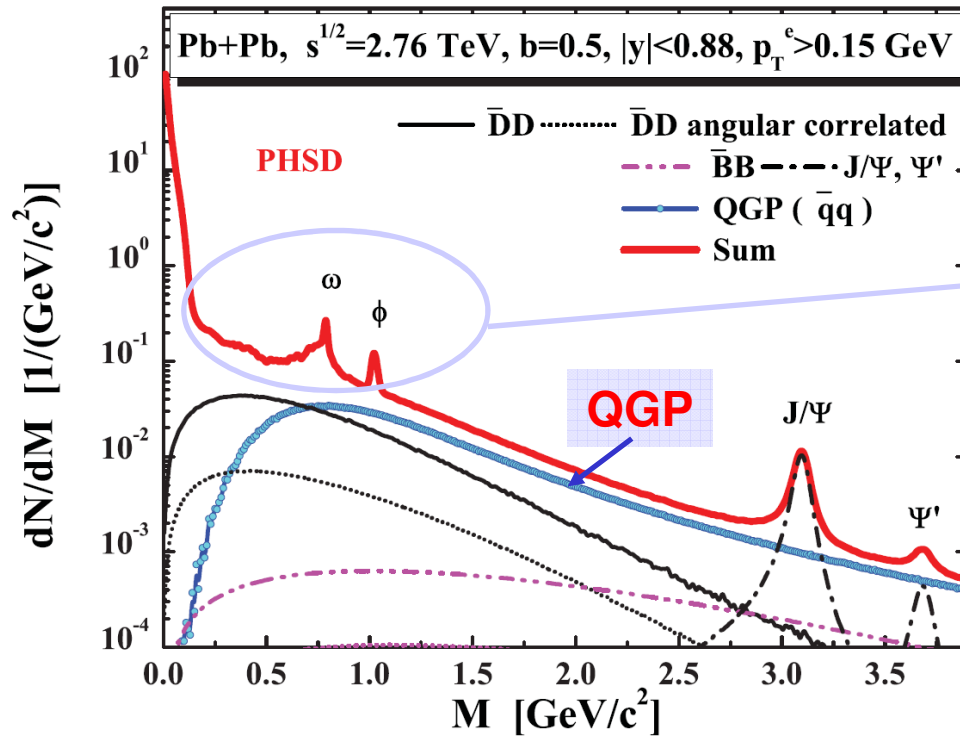
(Talk by Nu Xi at 23d CBM Meeting'14)



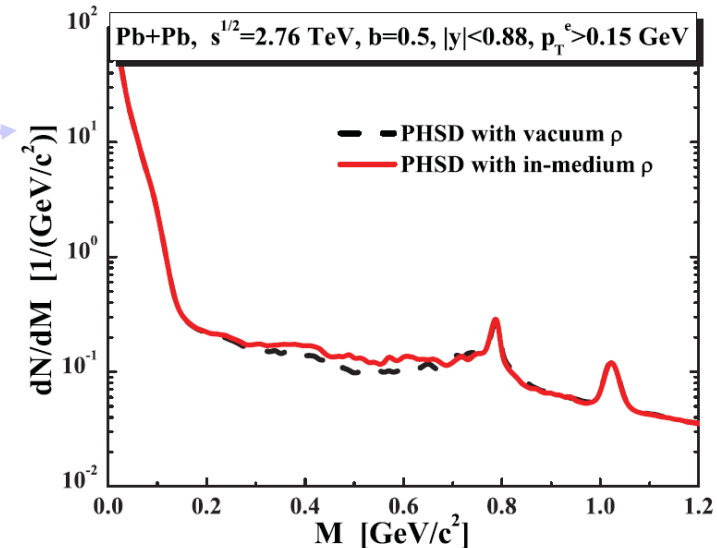
Message:

- BES-STAR data show a **constant low mass excess** (scaled with $N(\pi^0)$) within the measured energy range
 - PHSD model: **excess increasing with decreasing energy** due to a longer ρ -propagation in the high baryon density phase
- Good perspectives for future experiments –
CBM(FAIR) / MPD(NICA)

Dileptons at LHC



O. Linnyk, W. Cassing, J. Manninen, E.B., P.B. Gossiaux, J. Aichelin, T. Song, C.-M. Ko, Phys.Rev. C87 (2013) 014905; arXiv:1208.1279



Message:

- low masses - hadronic sources: **in-medium effects for ρ mesons are small**
- intermediate masses: **QGP + D/Dbar**
 - charm 'background' is smaller than thermal QGP yield
 - **QGP($\bar{q}q$) dominates at $M>1.2$ GeV \rightarrow clean signal of QGP at LHC!**



Summary III



Dilepton spectra - according to the PHSD predictions - show sizeable changes due to the different in-medium scenarios (as collisional broadening and dropping mass) which can be observed experimentally

- **In-medium effects** can be observed at all energies from SIS to LHC
- At SPS, RHIC and LHC the **QGP** ($q\bar{q}$) dominates at $M > 1.2$ GeV

Thanks to:

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Giessen University

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Alessia Palmese
Eduard Seifert

Volodya Konchakovski



**FIAS Frankfurt Institute
for Advanced Studies**



Bundesministerium
für Bildung
und Forschung



DAAD

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Universitat Autònoma
de Barcelona



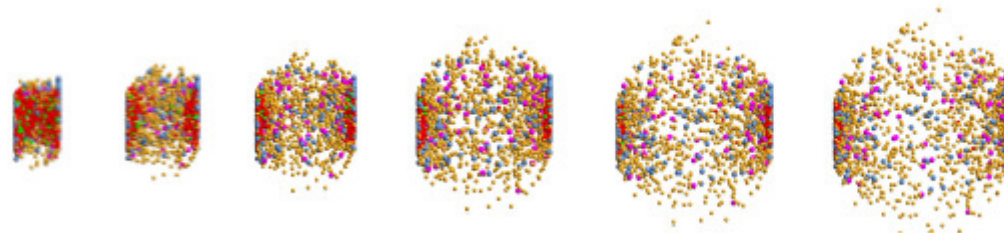
Thank you!

- Baryons
- Antibaryons
- Mesons
- Quarks
- Gluons

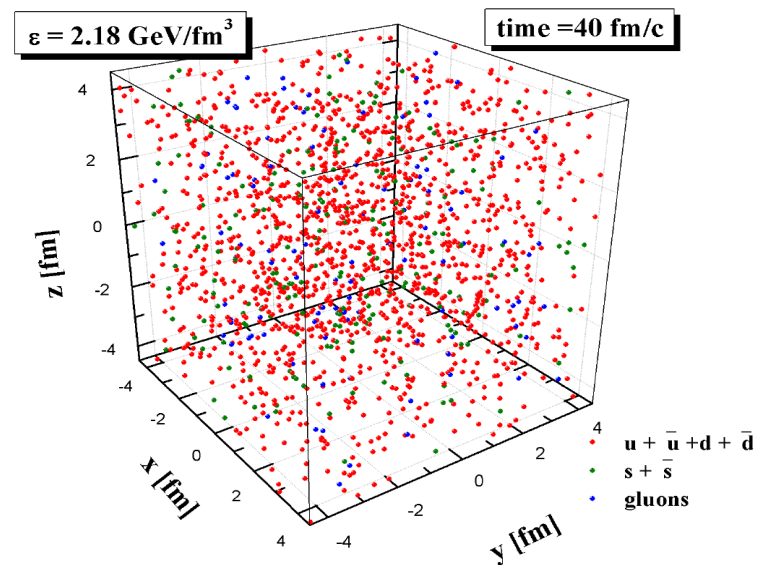
$\text{Au} + \text{Au} \sqrt{s_{\text{NN}}} = 200 \text{ GeV}$



$b = 2.2 \text{ fm}$ – Section view



Properties of the QGP in equilibrium using PHSD





Properties of parton-hadron matter: shear viscosity

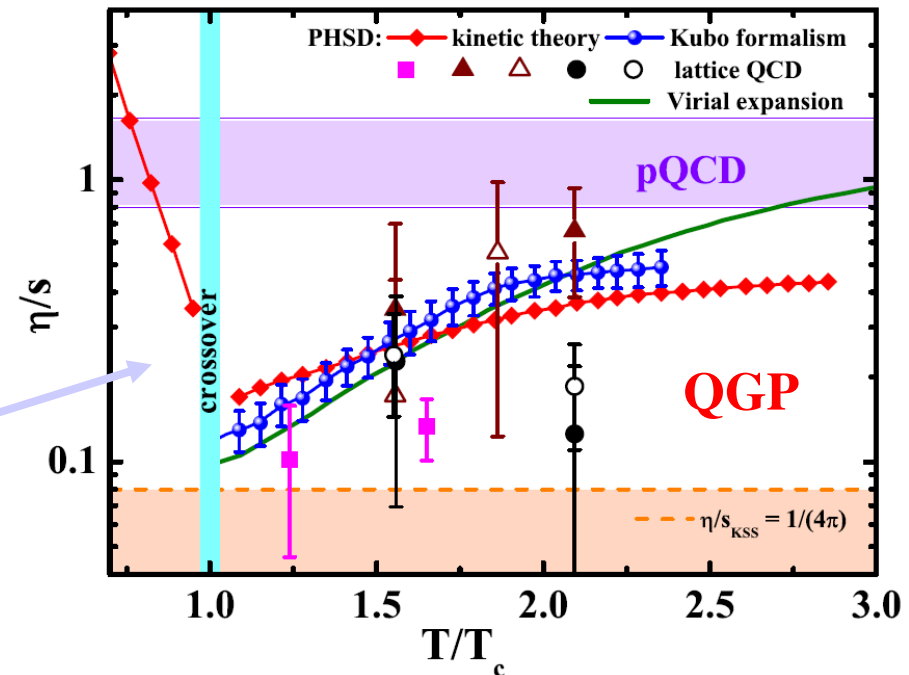
η/s using Kubo formalism and the relaxation time approximation (,kinetic theory‘)

□ $T=T_c$: η/s shows a minimum (~ 0.1) close to the critical temperature

□ $T>T_c$: QGP - pQCD limit at higher temperatures

□ $T<T_c$: fast increase of the ratio h/s for hadronic matter →

- lower interaction rate of hadronic system
- smaller number of degrees of freedom (or entropy density) for hadronic matter compared to the QGP



Virial expansion: S. Mattiello, W. Cassing, Eur. Phys. J. C 70, 243 (2010)

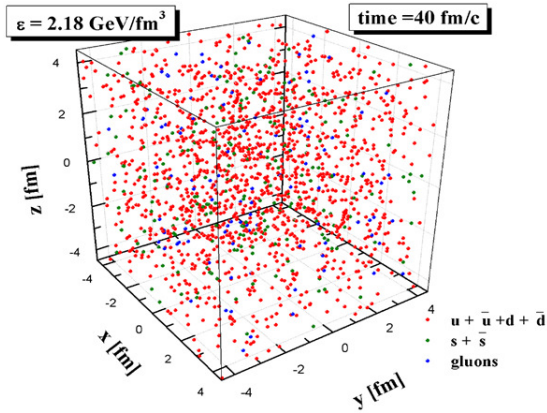
QGP in PHSD = strongly-interacting liquid



QGP in equilibrium: Transport properties at finite (T, μ_q) : η/s

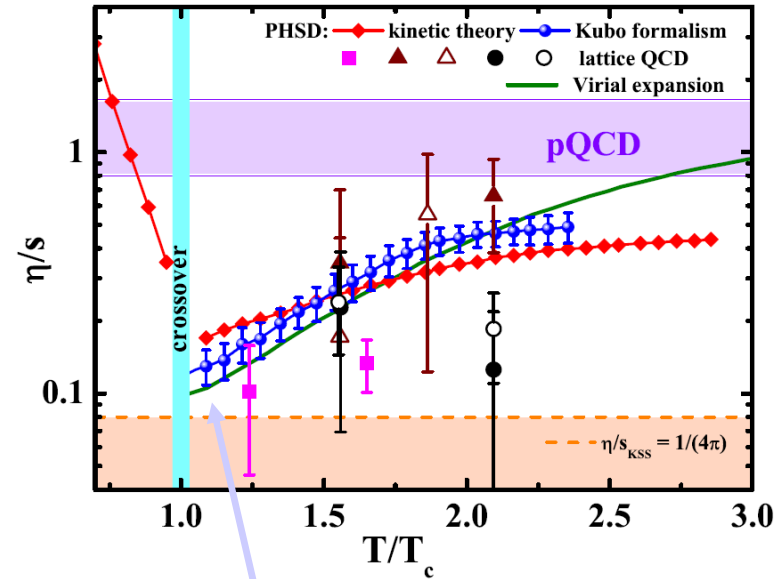
Infinite hot/dense matter =

PHSD in a box:



Shear viscosity η/s at finite T

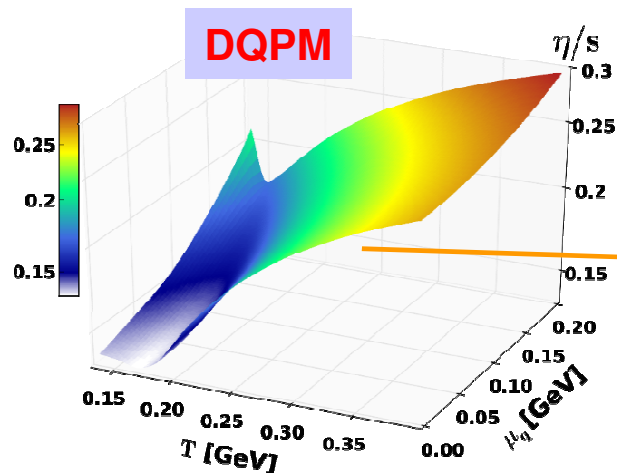
V. Ozvenchuk et al., PRC 87 (2013) 064903



Shear viscosity η/s at finite (T, μ_q)

IQCD:

$$\frac{T_c(\mu_q)}{T_c(\mu_q = 0)} = \sqrt{1 - \alpha \mu_q^2} \approx 1 - \alpha/2 \mu_q^2 + \dots$$



QGP in PHSD = strongly-interacting liquid

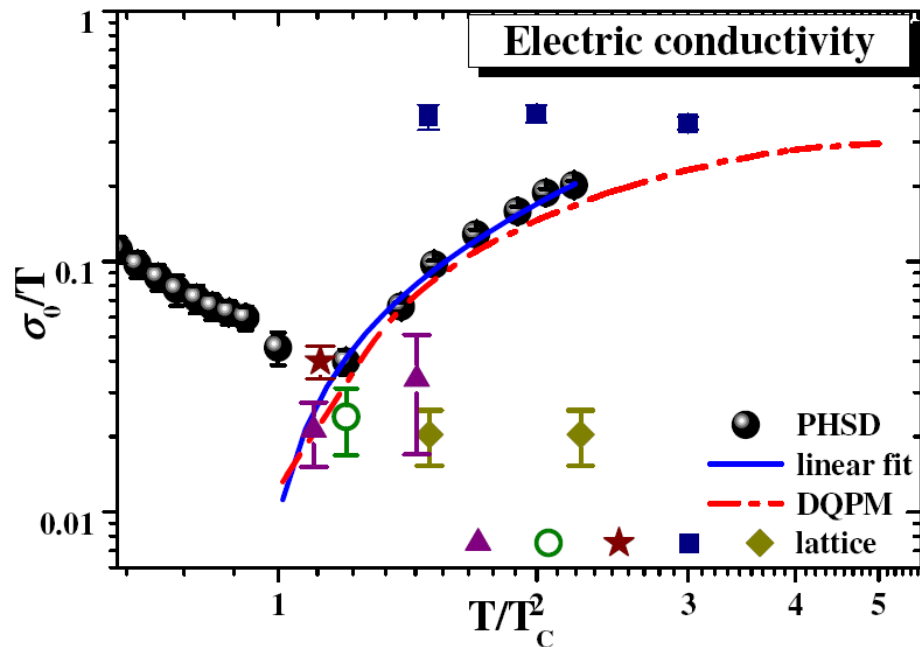
η/s : $\mu_q=0 \rightarrow$ finite μ_q : smooth increase as a function of (T, μ_q)

H. Berrehrh et al. arXiv:1412.1017



Properties of parton-hadron matter: electric conductivity

- The response of the strongly-interacting system in equilibrium to an external electric field eE_z defines the **electric conductivity** σ_0 :



$$\frac{\sigma_0}{T} = \frac{j_{eq}}{E_z T},$$

$$j_z(t) = \frac{1}{V} \sum_j eq_j \frac{p_z^j(t)}{M_j(t)},$$

→ the **QCD matter** even at $T \sim T_c$ is a **much better electric conductor than Cu or Ag** (at room temperature) by a factor of 500 !

- **Photon (dilepton) rates** at $q_0 \rightarrow 0$ are related to electric conductivity σ_0
- Probe of **electric properties of the QGP**

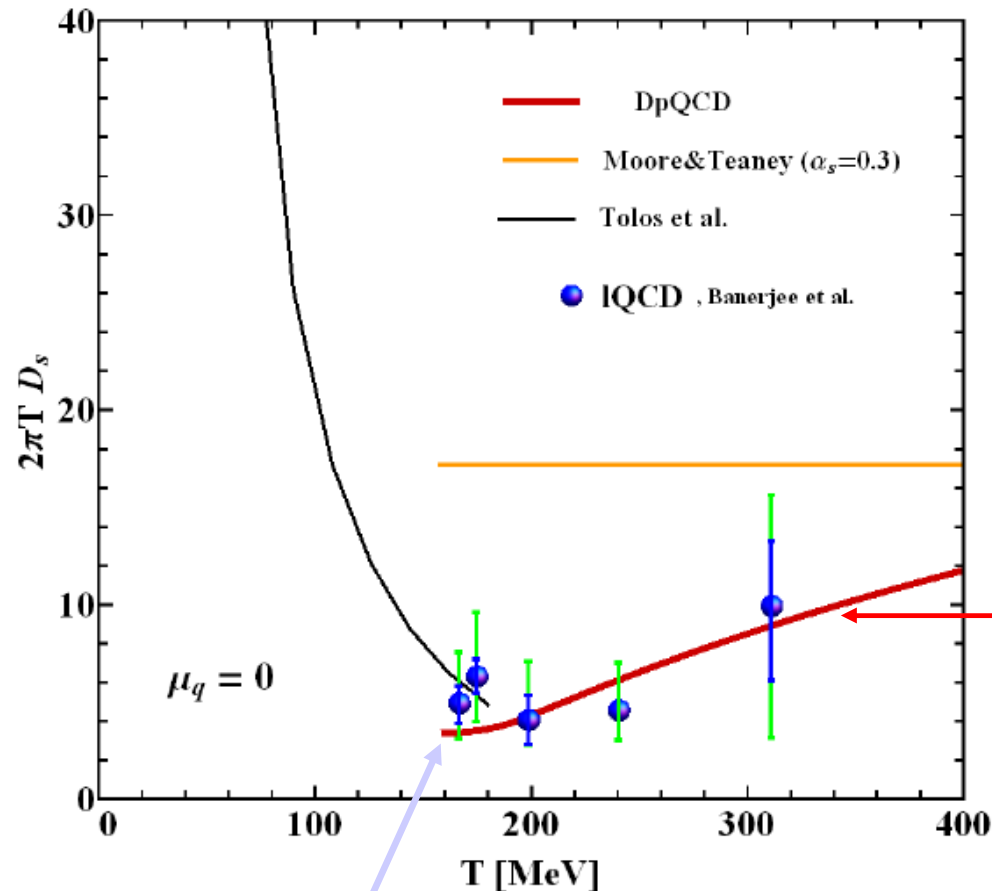
$$q_0 \left. \frac{dR}{d^4x d^3q} \right|_{q_0 \rightarrow 0} = \frac{T}{4\pi^3} \sigma_0$$

W. Cassing et al., PRL 110(2013)182301



Charm spatial diffusion coefficient D_s in the hot medium

- D_s for heavy quarks as a function of T for $q = 0, \mu_q = 0$



□ $T < T_c$: **hadronic D_s**
L. Tolos, J. M. Torres-Rincon,
Phys. Rev. D 88, 074019 (2013)

□ $T > T_c$: **QGP D_s**

● pQCD - G. D. Moore, D. Teaney,
Phys. Rev. C 71, 064904 (for $a_s=0.3$)

● **DQPM** - H. Berrehrach et al,
arXiv:1406.5322 [hep-ph]

● IQCD - Banerjee et al.,
Phys. Rev. D 85, 014510 (2012).

➔ **Continuous transition !**

H. Berrehrach et al, PRC (2014), arXiv:1406.5322 [hep-ph]