

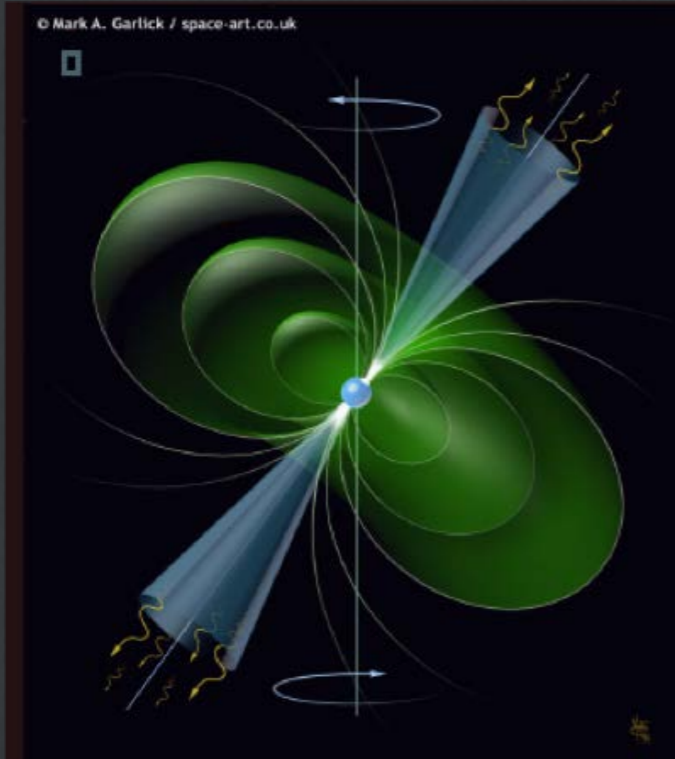
Terrestrial experiments to understand what is inside neutron stars

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<http://www.denseandstrange.ph.tum.de>

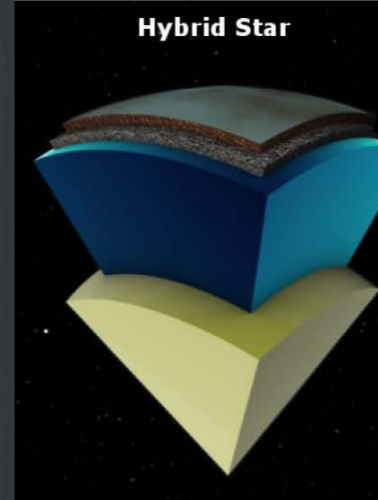
EMMI Colloquium, 24 May 2017

Facts about Neutron Stars



$R \sim 10-15 \text{ km}$
 $M \sim 1.5 M_{\odot}$

density ↓

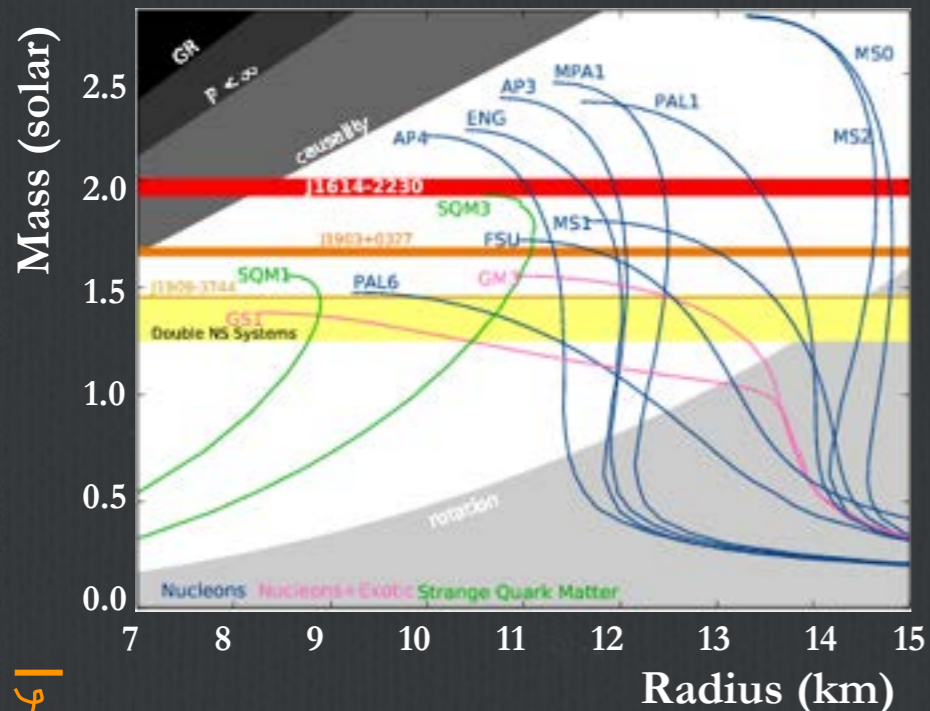


additionally the study of strangeness has some impact on the modelling of neutron stars.

Scenarios with antikaon condensate is disfavoured but actually this strongly depends on the real antikaon-nucleon interaction but there are other possibilities

- Very high density in the interior
- Strong magnetic fields
- Rotating object emitting Synchrotron radiation in Radio-Frequency (Pulsar character)
- Mass measured in binary systems with White Dwarfs (Shapiro Delay, WD Spectroscopy)
- Radius Measurement very difficult
- Masses ranging from $1.4 M_{\odot}$ to $2 M_{\odot}$

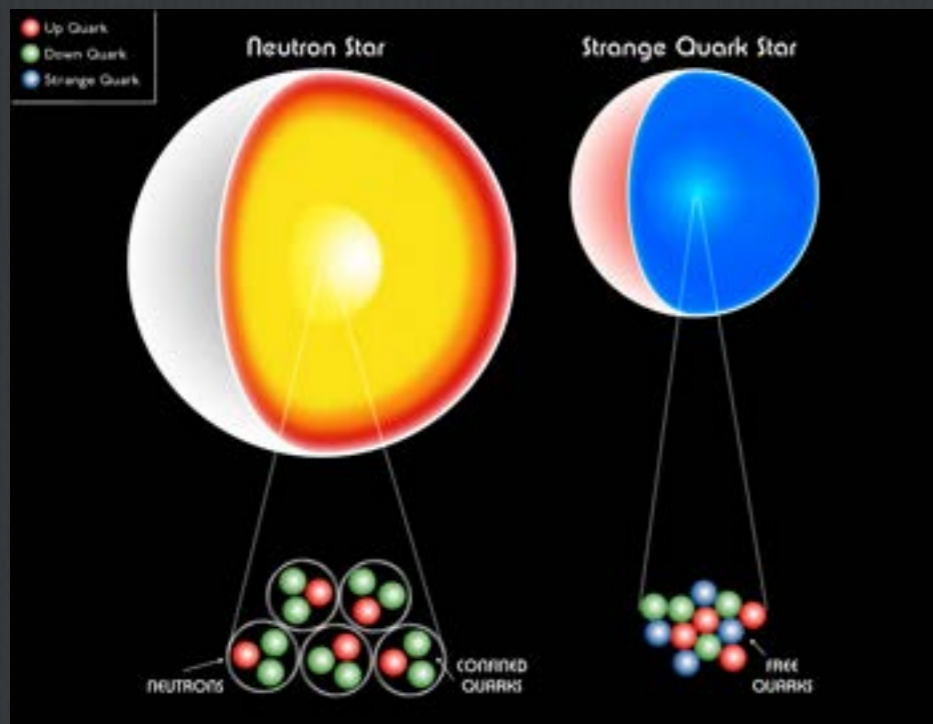
P. Demorest et al. Nature (467) (2010) 1081



What is inside Neutron Stars??

Speculations about Neutron Stars

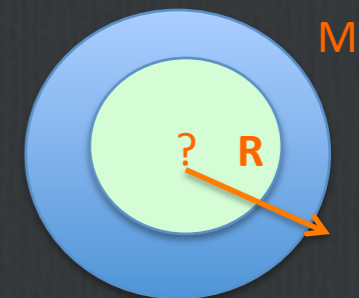
NSF, universetoday.com



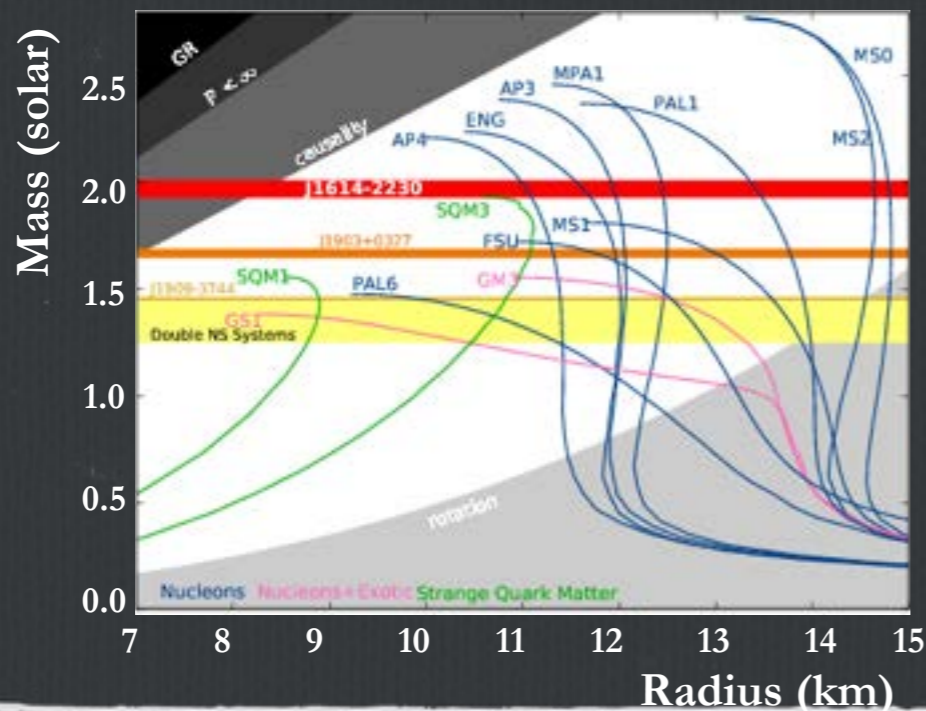
- Hadron composition
 - Only Nucleons
 - Antikaons-Nucleons condensate
 - Nucleons and Hyperons
- Nuclear Pasta
 - lasagne
 - spaghetti
- Quark star (Color super-conducting strange quark matter)

How to test different Hypotheses

- 1) Equation of State (EoS): Dependency of the pressure upon the density
- 2) Given an object with a certain density the internal pressure must be compensated by gravity
- 3) From $P(R)=0 \rightarrow$ the relation $M(R)$ can be determined for each EOS as a function of the assumed density



P. Demorest et al. Nature (467) (2010) 1081



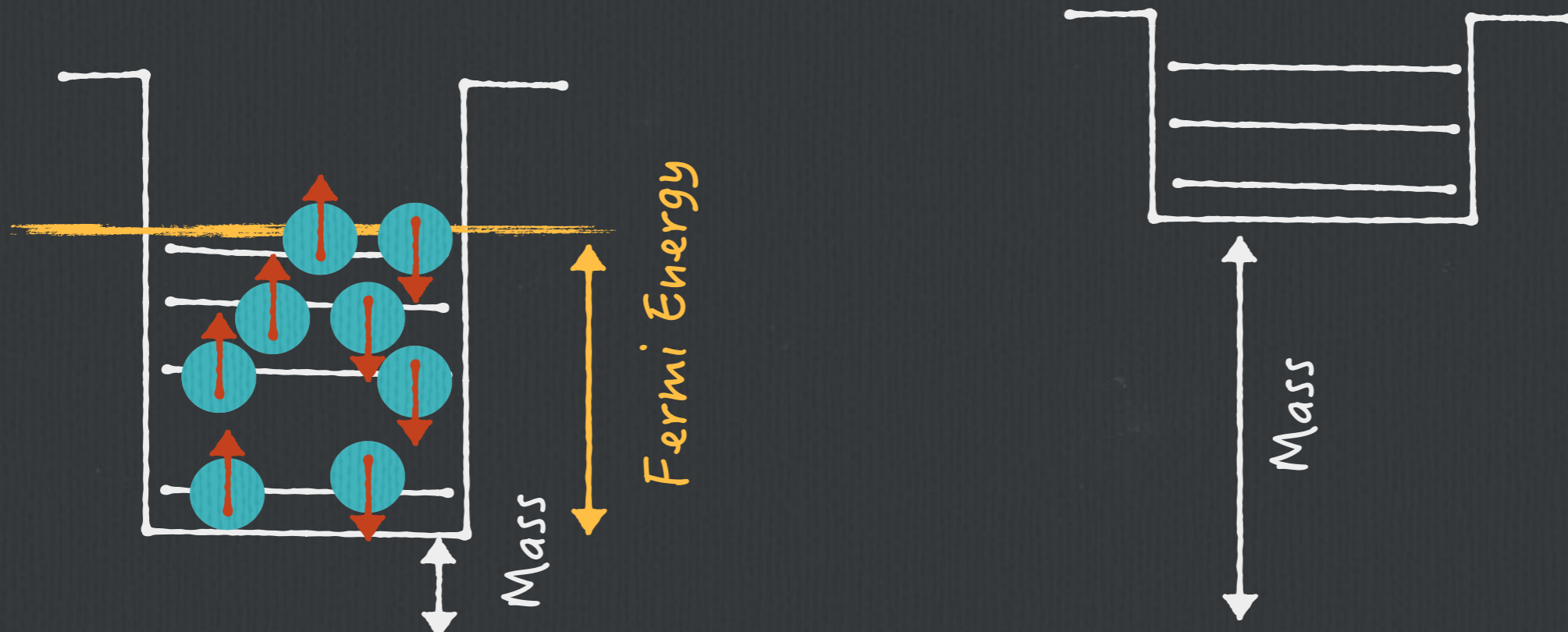
$$\rho = 2^{-8} \rho_0 ??$$

It is not so easy to fix the density but the EOS must cross the measured values of the masses!

Strange Hadron Production in NS

Neutrons (uud, $m = 938 \text{ MeV}$)

Λ Hyperons (uds, $m = 1115 \text{ MeV}$)



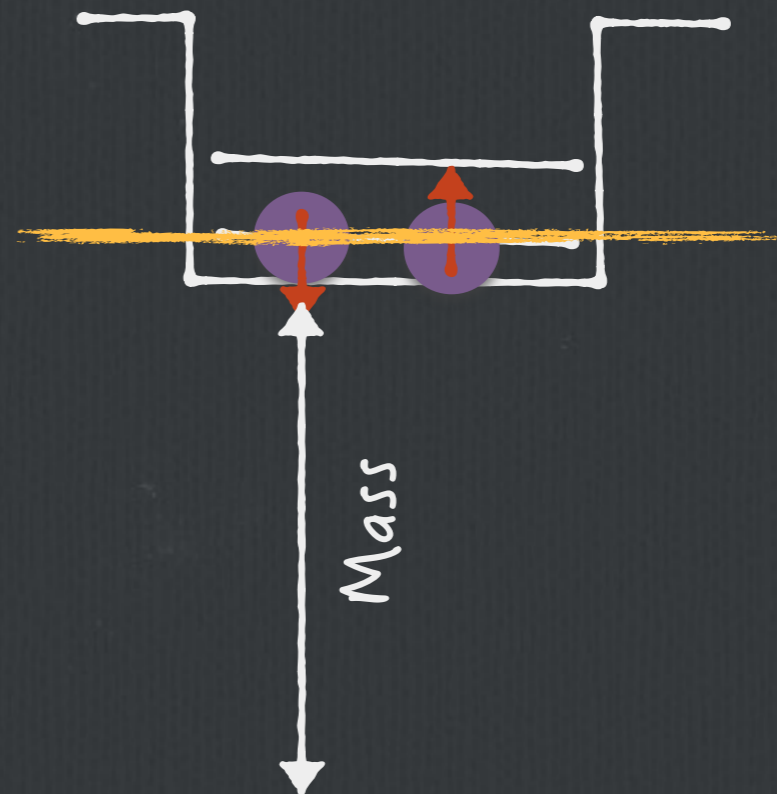
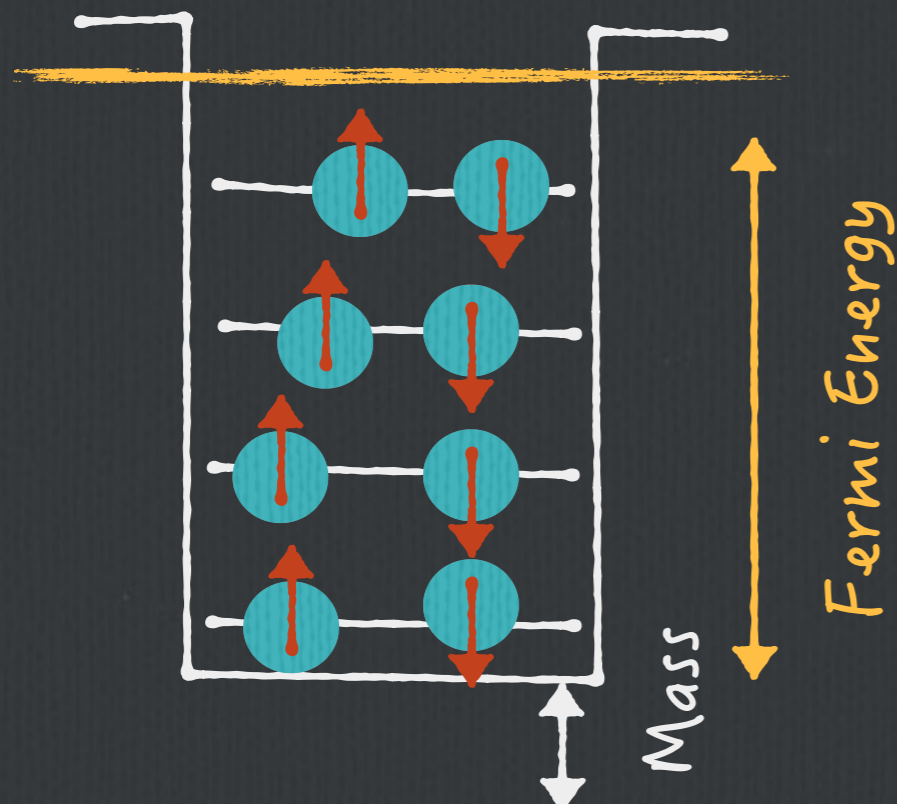
Chemical Potential $\mu = E_F + mass$

If the density increases also the Fermi Energy increases and hence the chemical potential

Strange Hadron Production in NS

Neutrons (uud, $m = 938$ MeV)

Λ Hyperons (uds, $m = 1115$ MeV)



In order to have chemical equilibrium $\mu_{neutron} = \mu_{\Lambda}$

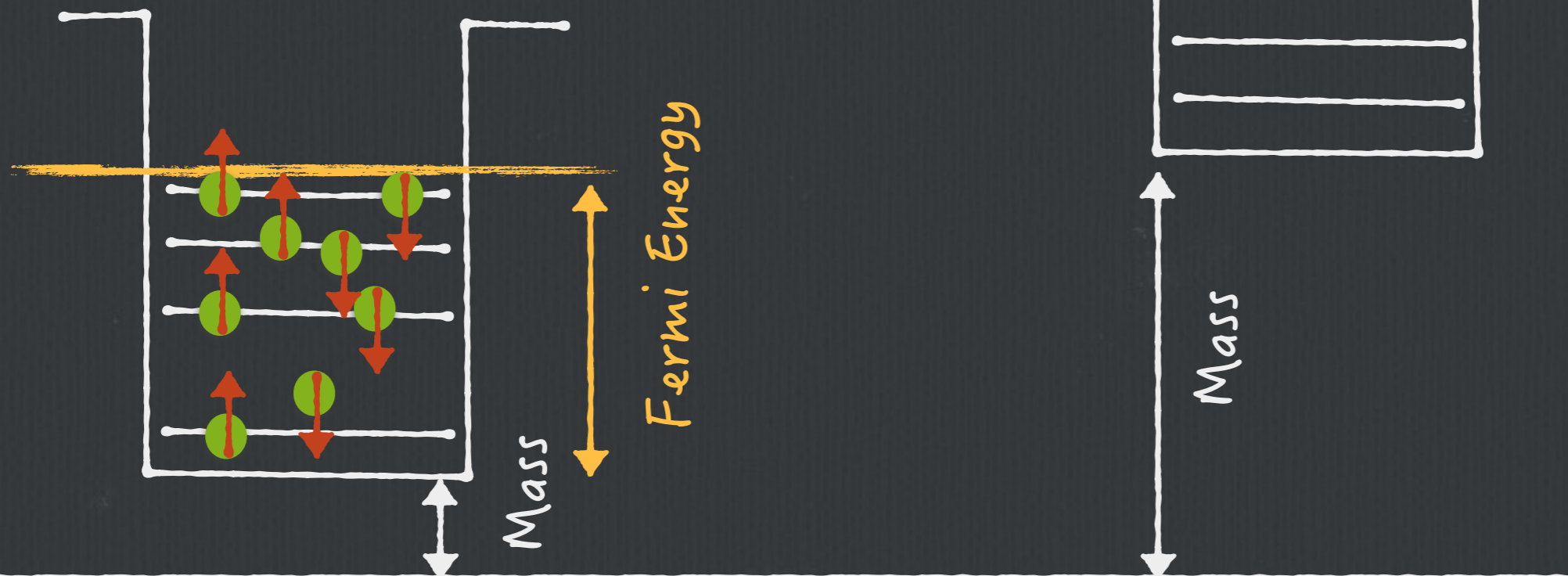
In this case it is energetically favourable to convert neutrons into hyperons

Strange Hadron Production in NS

$$n \rightarrow p + e^{-} + \bar{\nu}_e$$

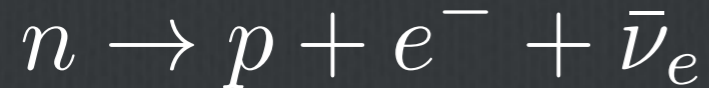
AntiKaons ($\bar{u}s, m= 490 \text{ MeV}$)

Electrons ($m= 511 \text{ KeV}$)



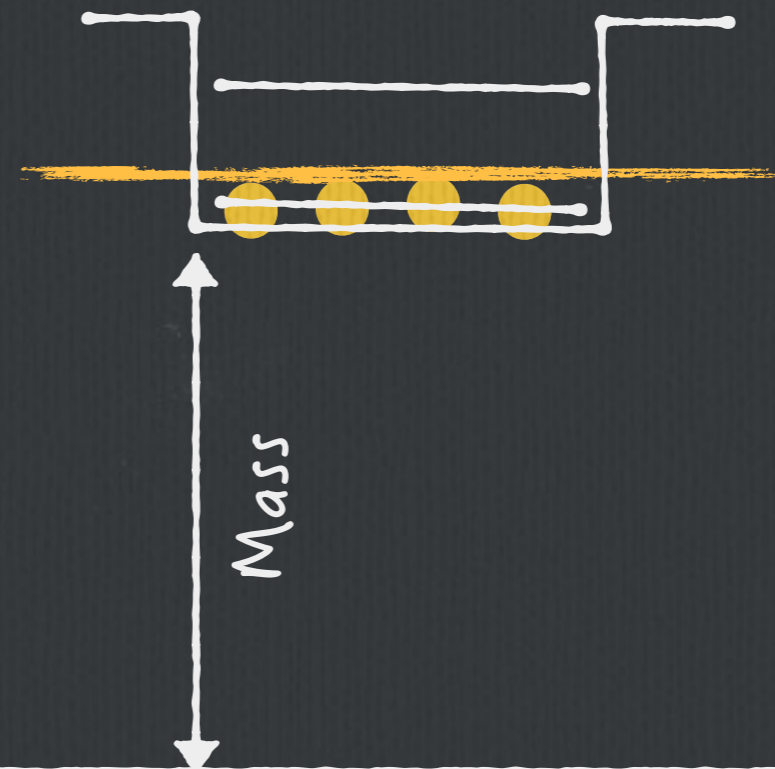
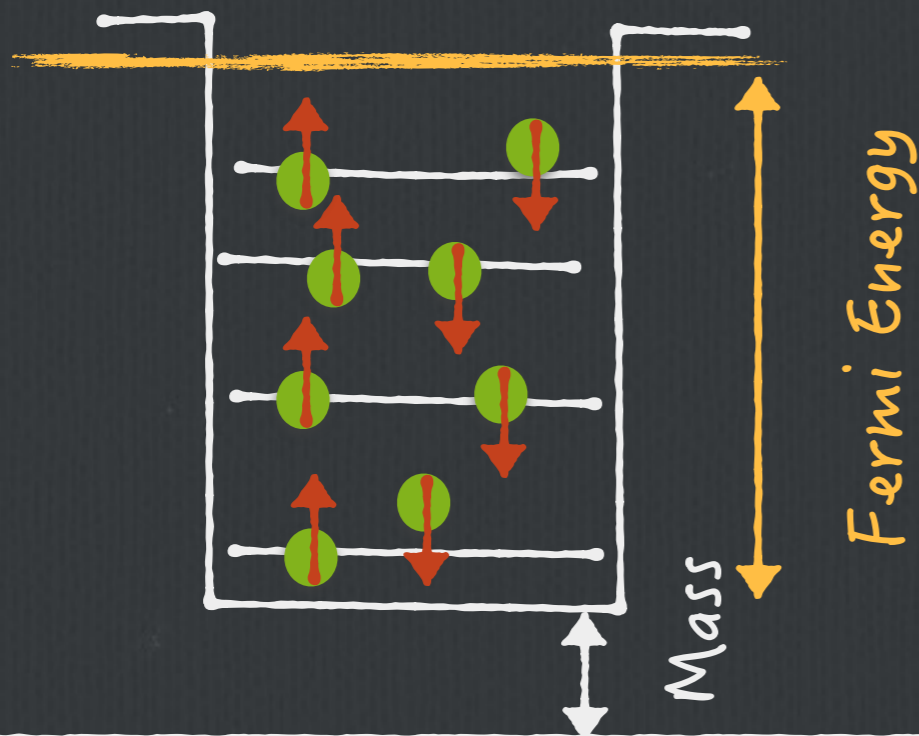
Chemical Potential $\mu = E_F + mass$

Strange Hadron Production in NS



AntiKaons ($\bar{u}s, m= 490 \text{ MeV}$)

Electrons ($m= 511 \text{ KeV}$)



Also in this case it can be energetically favourable to convert electrons into AntiKaons.

Furthermore: AntiKaons are bosons and hence they don't undergo Pauli blocking

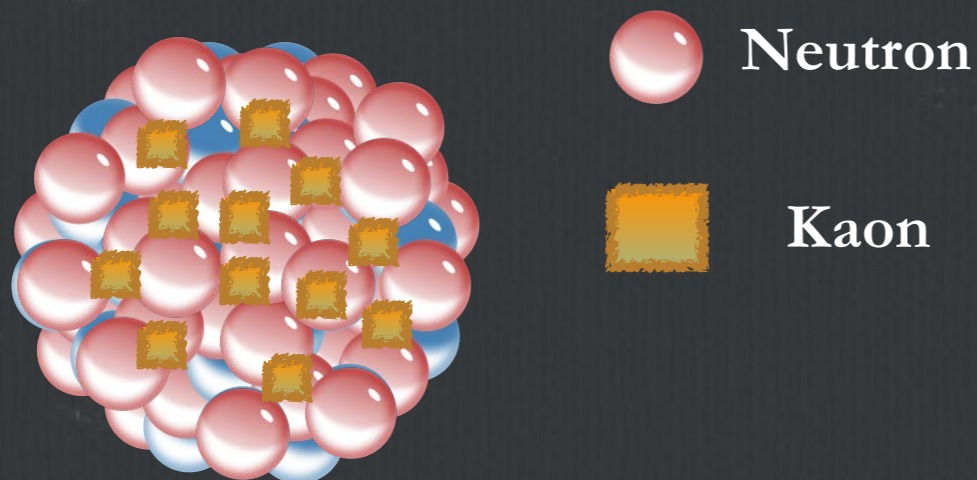
Scenario Nr. 1: Kaon Condensate

Since hadrons interact with each others
if the 'in-medium' mass of K^- drop within
dense nuclear matter it is even more
favorable to produce strangeness

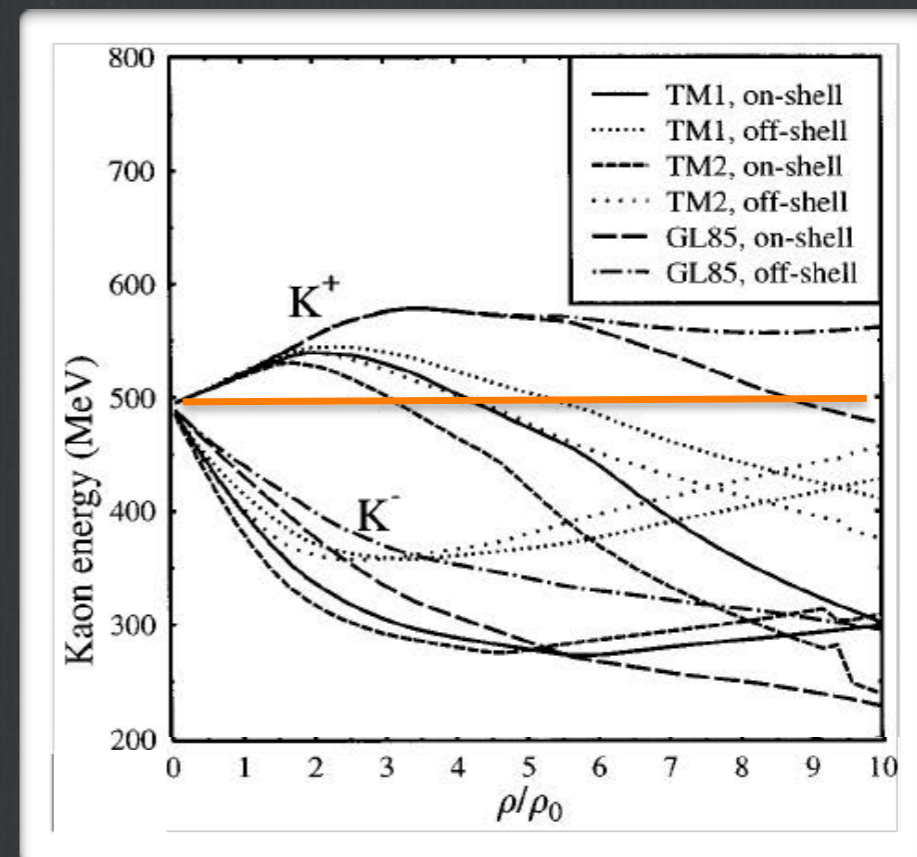
if $m_{K^*} < \mu_{e^-}$



No Pauli Blocking!

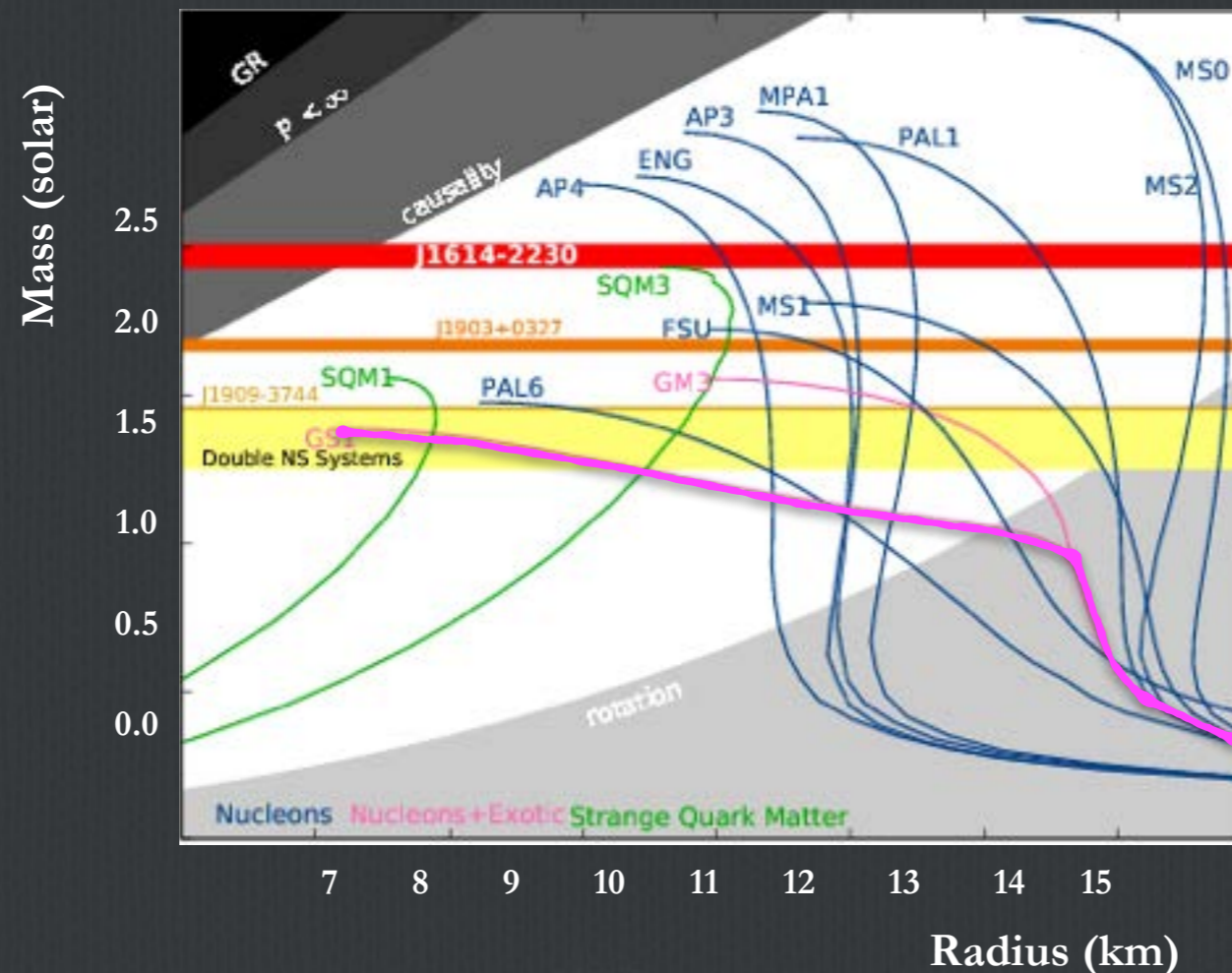


J. Schaffner and I. N. Mishustin
Phys. Rev. C **53**, 3 (1996)



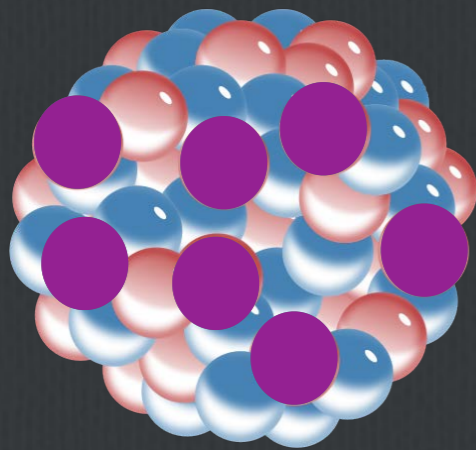
Large Masses Issue and Strangeness in NS

P. Demorest et al. Nature (467) (2010) 1081

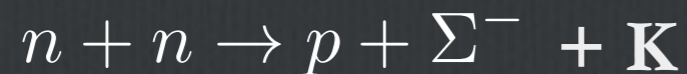


- Production of strangeness is energetically favourable
- It relieves the Fermi pressure of neutrons and protons
- But... a decrease of the pressure softens the EOS
- Decrease of the maximum mass of neutron stars
- $2 M_{\odot}$ neutron star measured
- EOS cannot be too soft
- Some EOS are disfavoured, for example Antikaon condensate

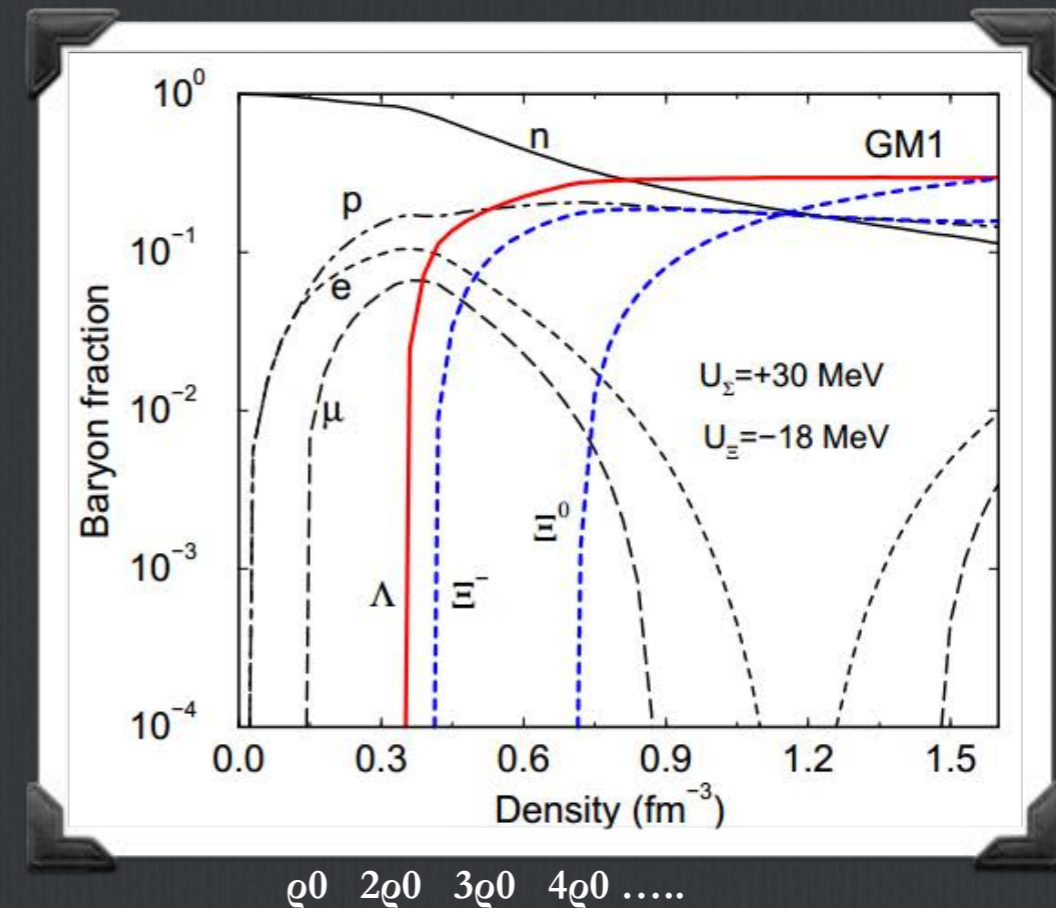
Scenario Nr. 2: Hyperon Star



Possible Processes:

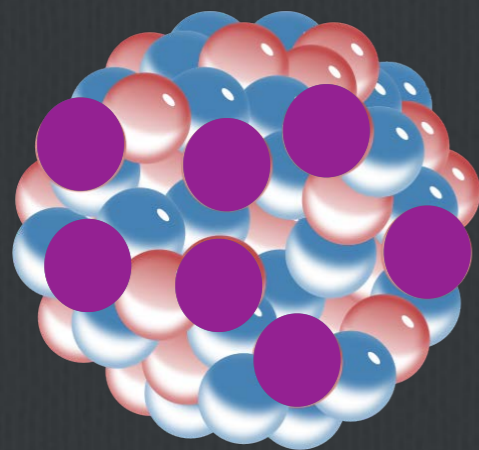


J. Schaffner-Bielich, NPA 804 (2008)



This scenario might also be problematic since the hyperon appearance implies new degree of freedom and hence a softening of the EOS

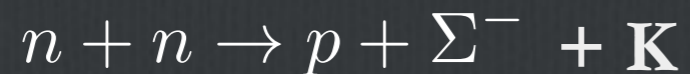
Scenario Nr. 2: Hyperon Star



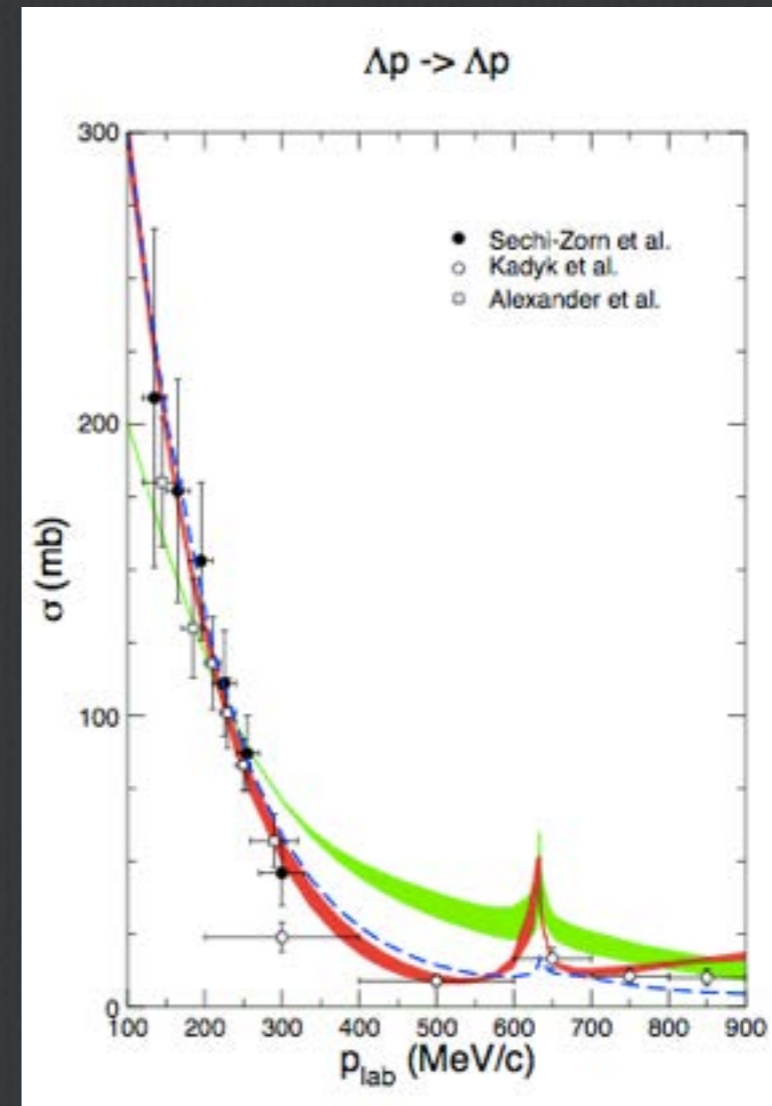
 Neutron

 Λ

Possible Processes:

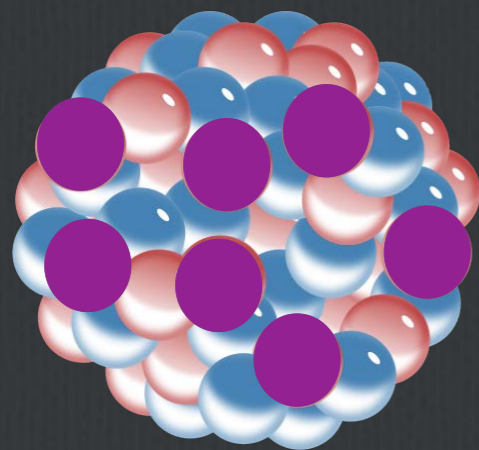


J. Haidenbauer, S. Petschauer et al.,
Nucl. Phys. A 915 (2013) 24



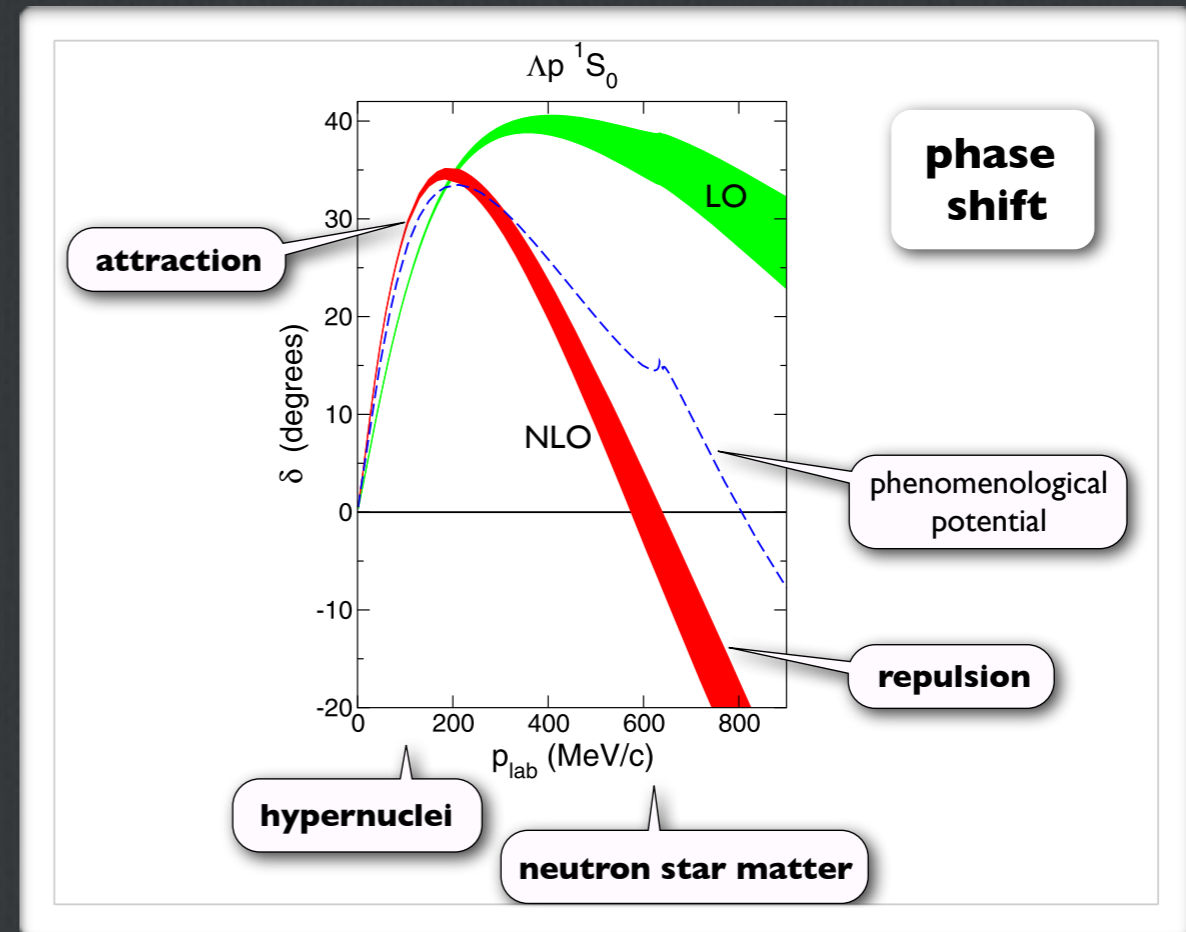
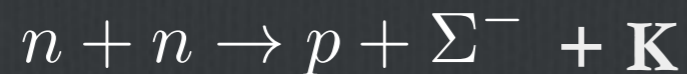
Λp scattering length extracted from scattering data and hypernuclei data for average Λp potential

Scenario Nr. 2: Hyperon Star



J. Haidenbauer, S. Petschauer et al.,
Nucl. Phys. A 915 (2013) 24

Possible Processes:

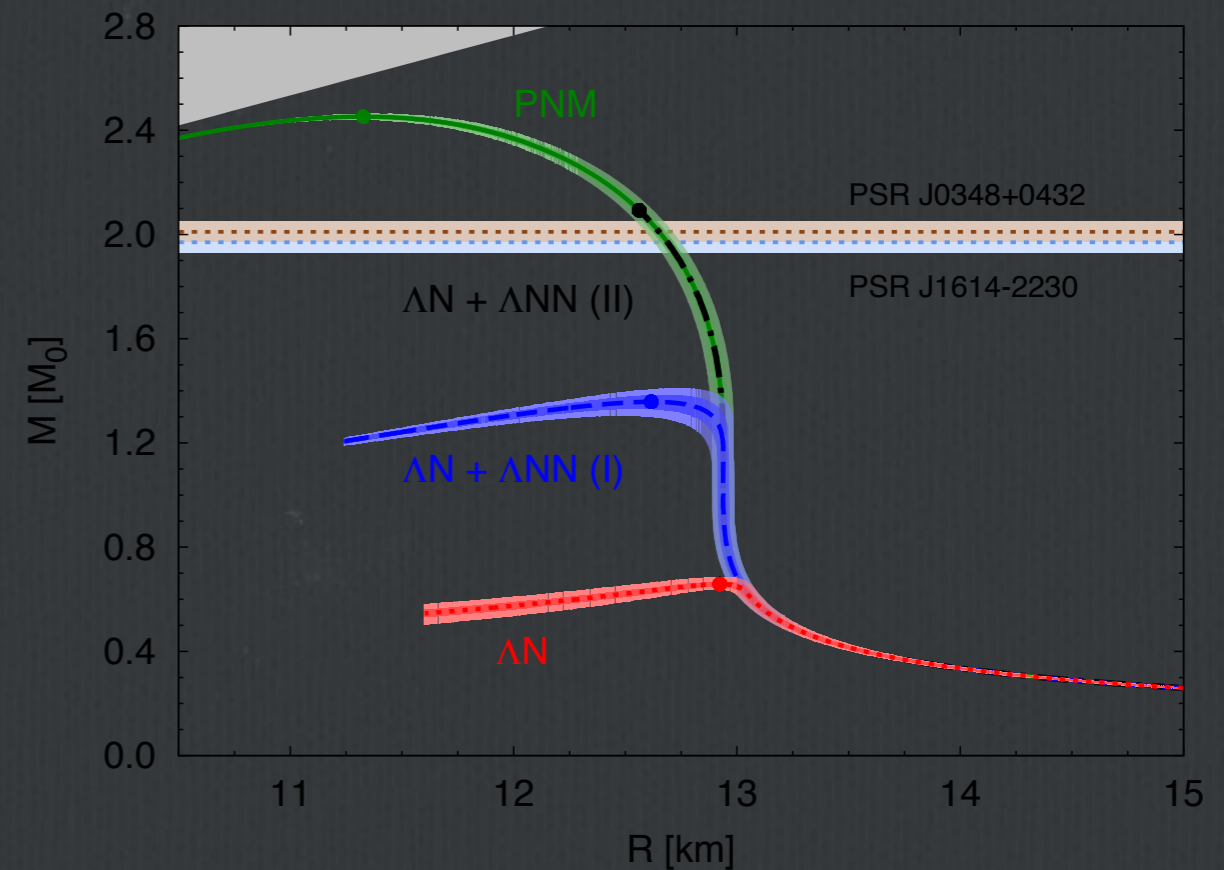
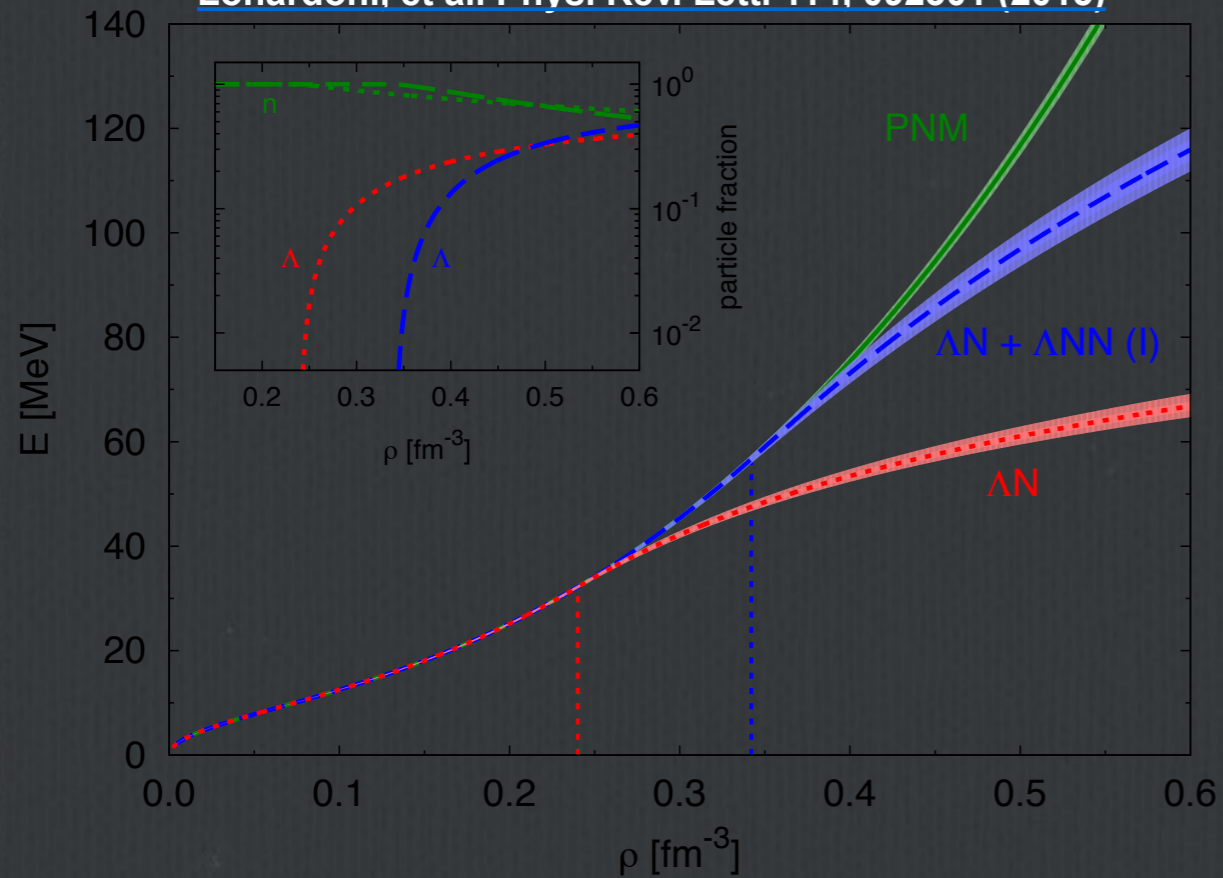


It all depends upon the Λ -N and Λ -NN interaction and whether or not it has a repulsive core

This repulsive core could stiffen again the EOS allowing for heavy neutron stars

EOS with Hyperons

Lonardonì, et al. Phys. Rev. Lett. 114, 092301 (2015)



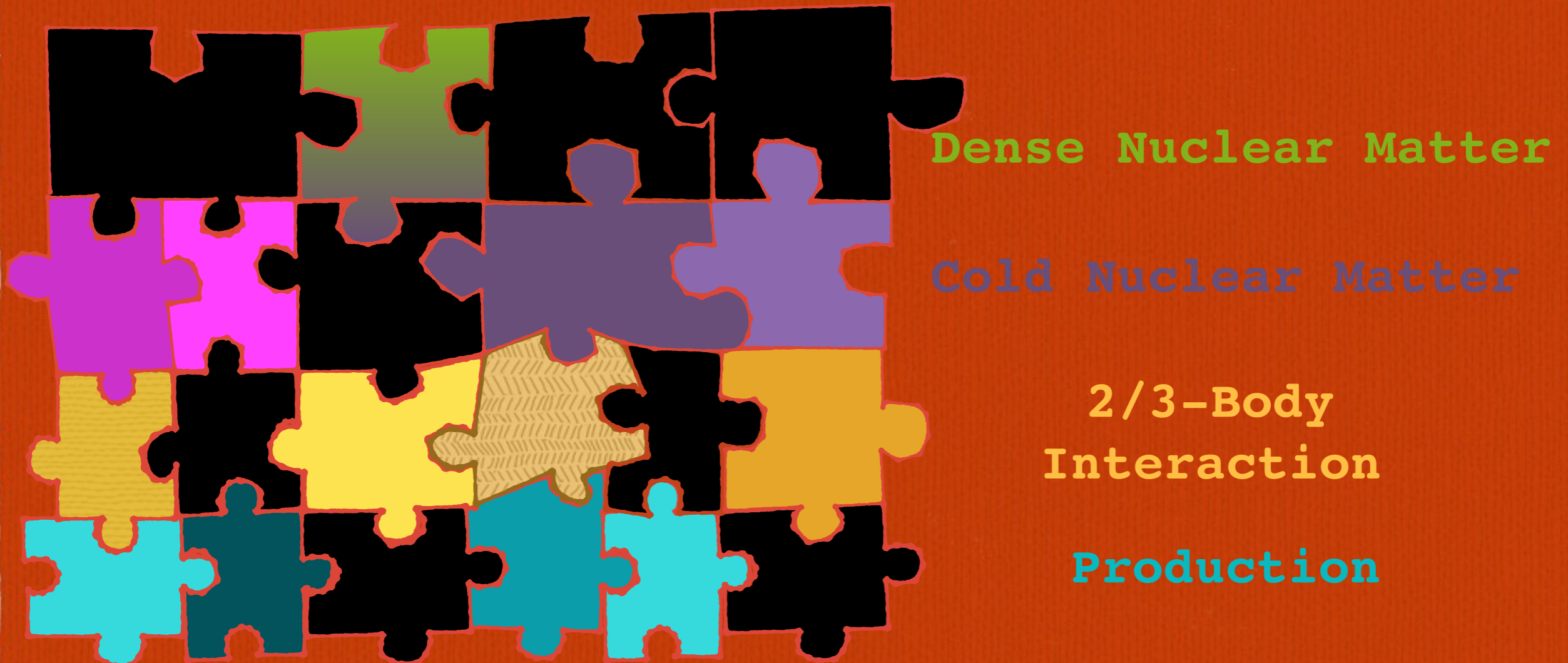
Λ -N, Λ -NN Interaction, in particular
the short range repulsive part
determines the fate of heavy hyperon
stars.

Equation of state of dense hadron matter

Study of the strange-hadron properties within nuclear matter

Still a puzzle with many missing pieces

Knowledge of the interaction is needed to extract an EOS with neutrons and strange hadrons.

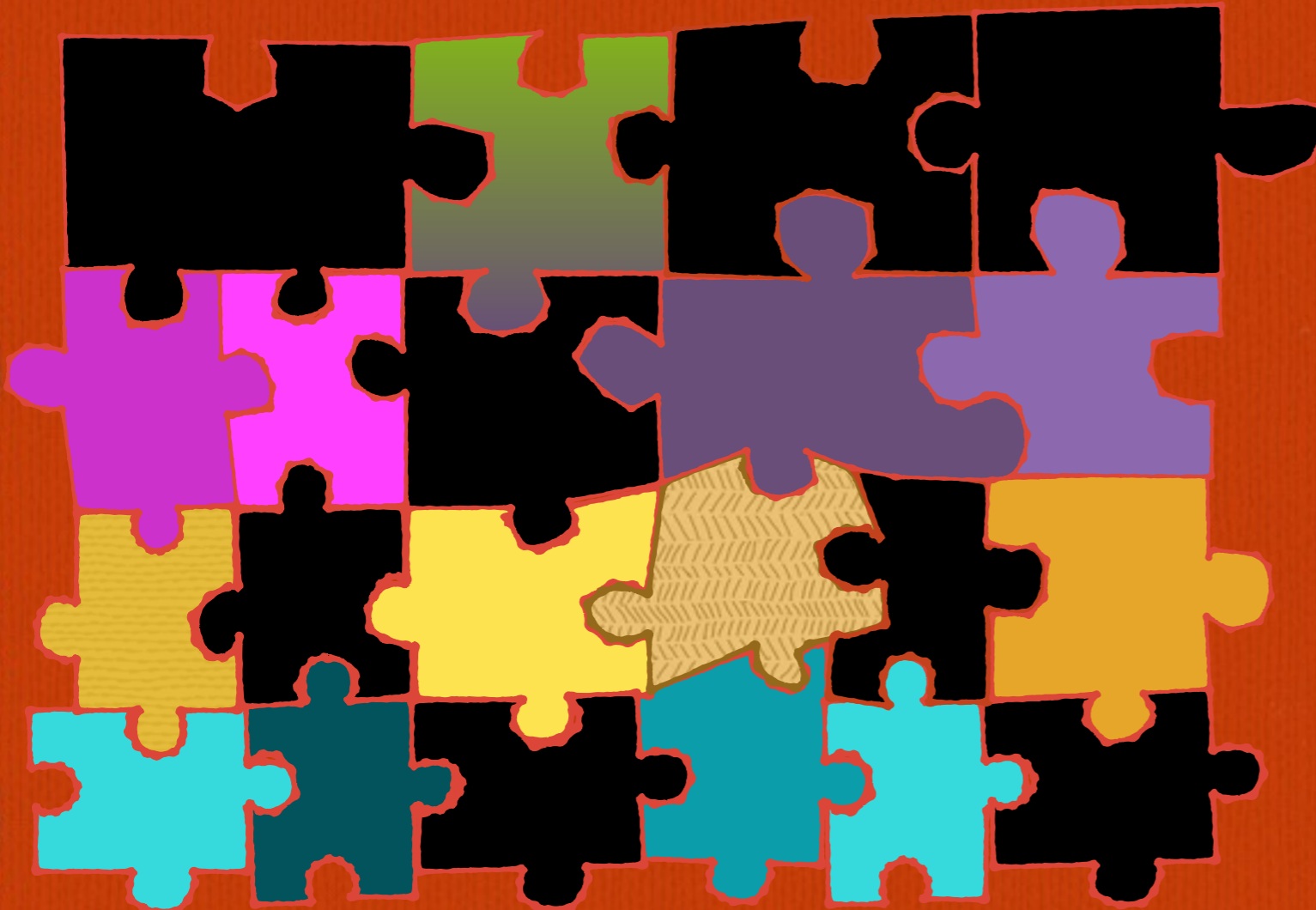


Equation of state of dense hadron matter

Study of the strange-hadron properties within nuclear matter

Still a puzzle with many missing pieces

Knowledge of the interaction is needed to extract an EOS with neutrons and strange hadrons.



- Λ -Nucleon
- Λ -Nucleon-Nucleon

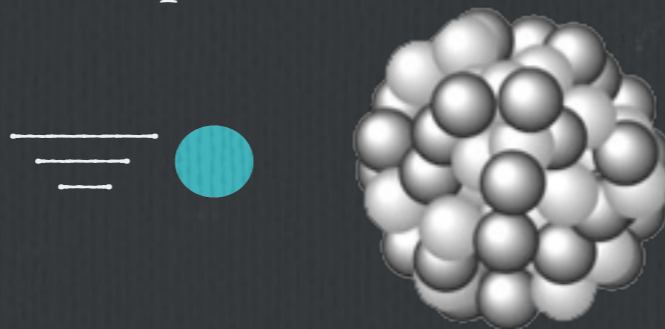
HADES at GSI

Fixed Target experiments, $E_{kin} \sim A \text{ GeV}$

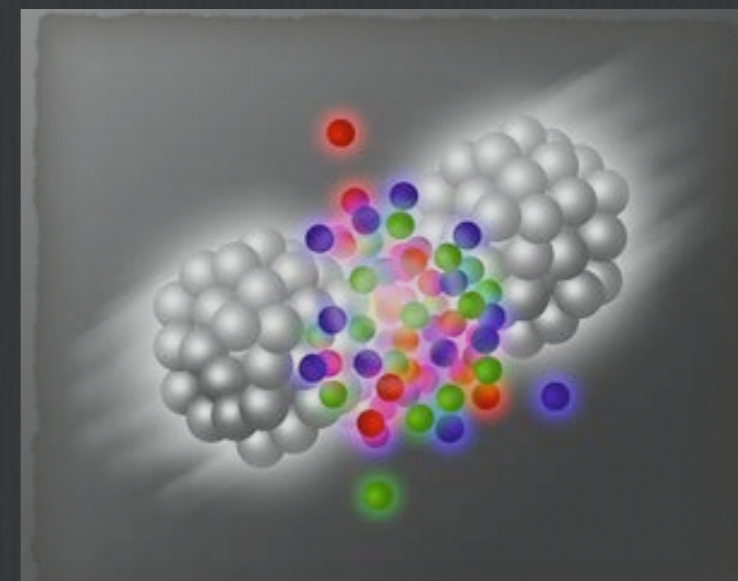
proton-proton



proton-nucleus

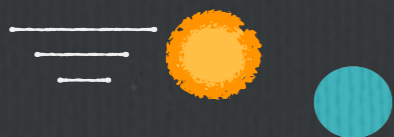


Heavy-ion Collisions $\rho_B < 2-3 \rho_0$

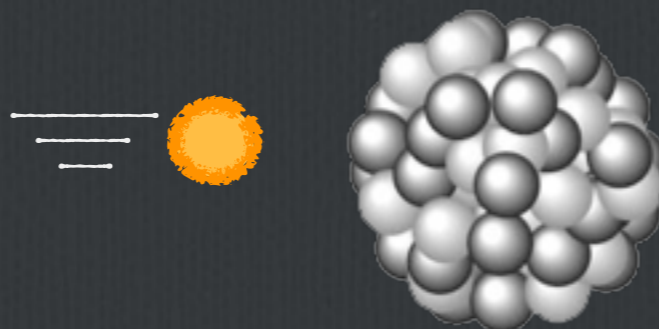


Vienna University of Technology

π -proton



π -nucleus



$T \sim 80-100 \text{ MeV}$

Vacuum

$\rho_B \sim \rho_0$

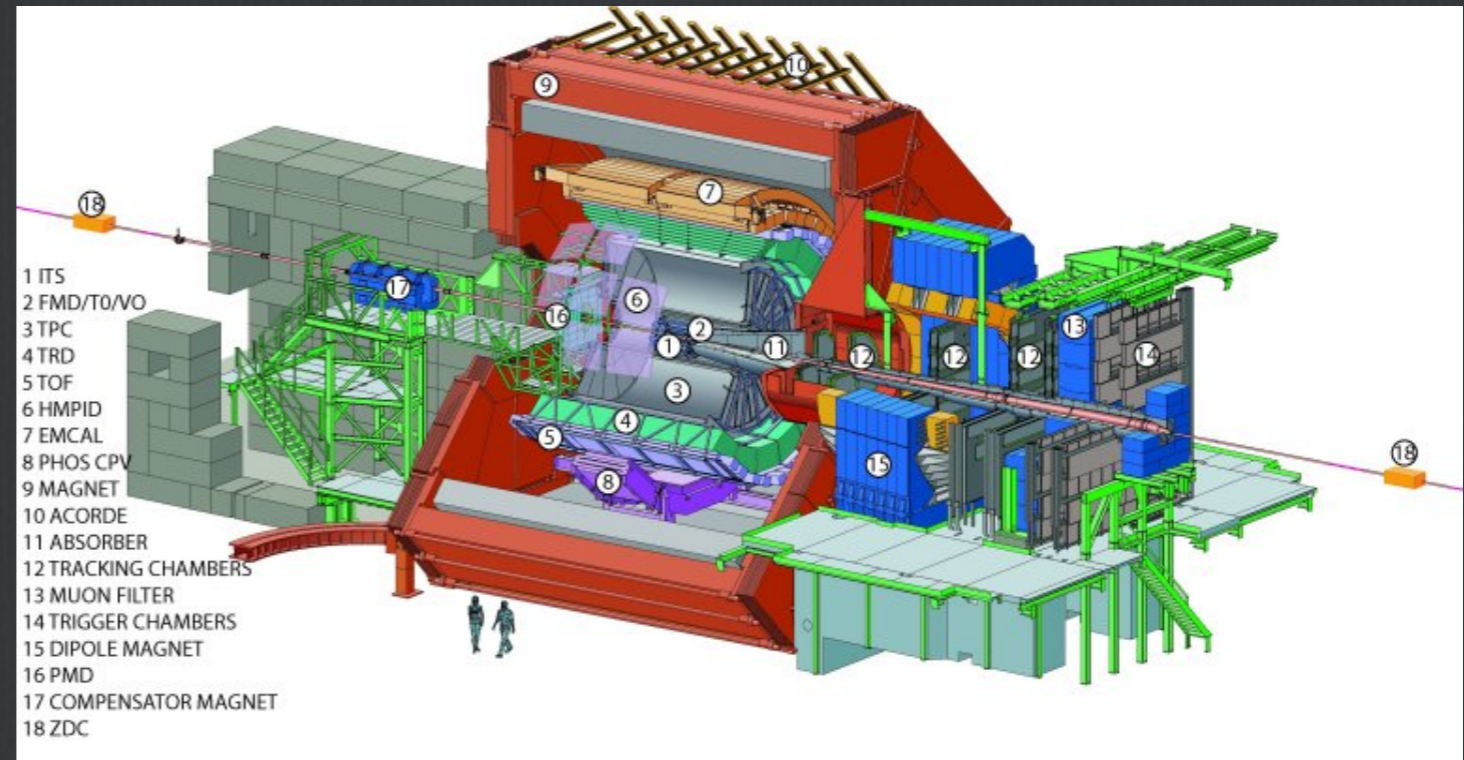
mention that elementary collisions have been always considered mainly as reference for the hic, where densities beyond nuclear matter can be formed. This is one of the role they play but there is more.

The reactions we are referring here to happen at GeV, fixed target and in particular the collisions I'm going to show refer to ...

The ALICE Experiment

Experiment at the LHC Collider

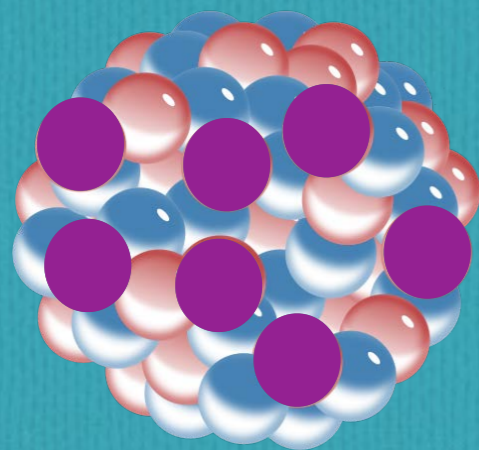
p+p at $\sqrt{s} = 7, 13 \text{ TeV}$



Very good Particle Identification
Energy Loss measurement in the large Volume
Time Projection Chamber

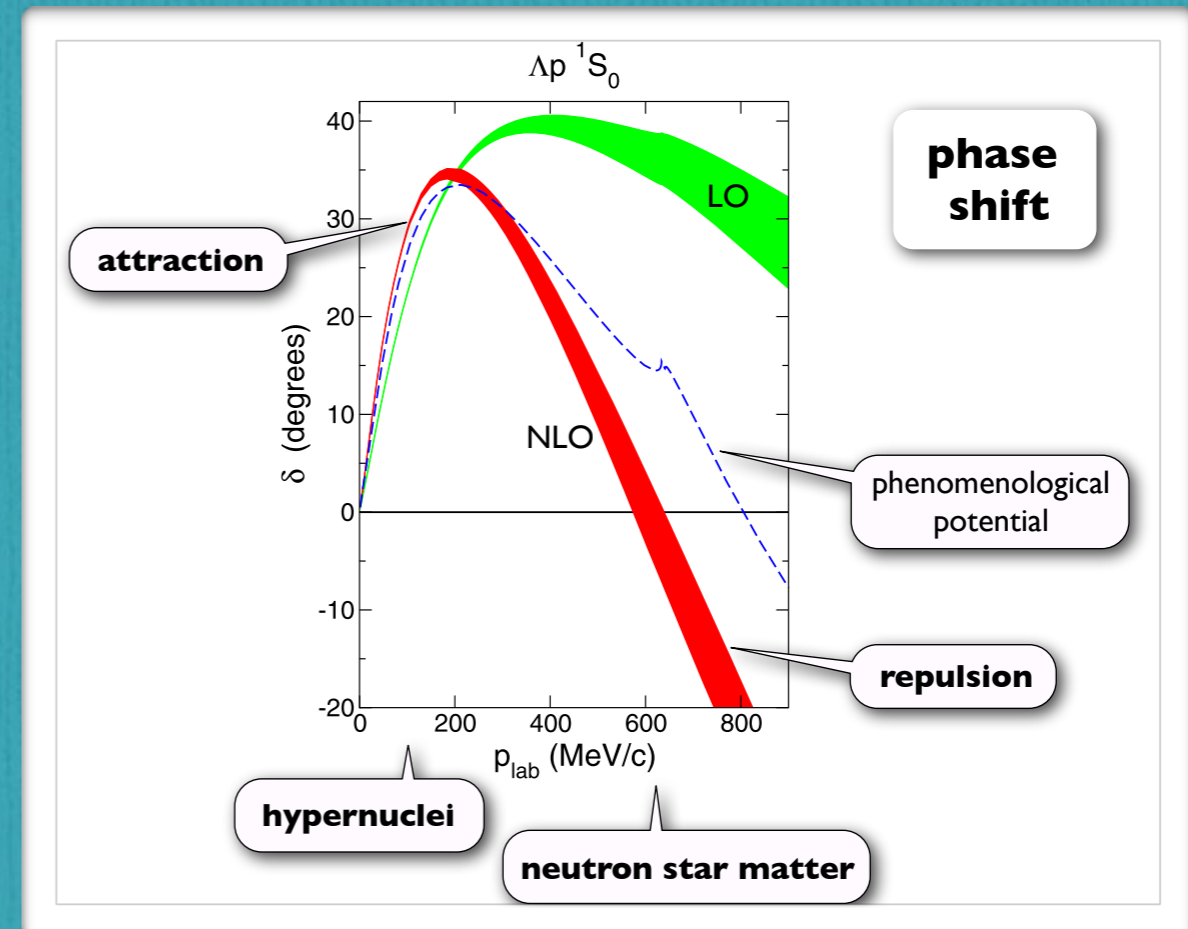
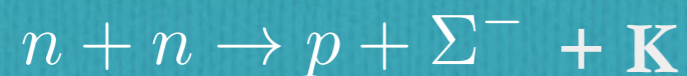
- + Measurement of the time of flight
- + + Excellent secondary vertex reconstruction capability

Scenario Nr. 2: Hyperon Star



J. Haidenbauer, S. Petschauer et al.,
Nucl. Phys. A 915 (2013) 24

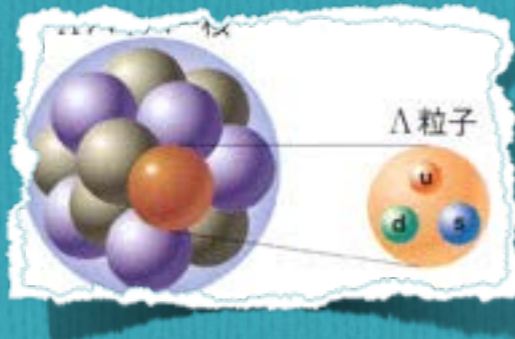
Possible Processes:



It all depends upon the Λ -N and Λ -NN interaction and whether or not it has a repulsive core

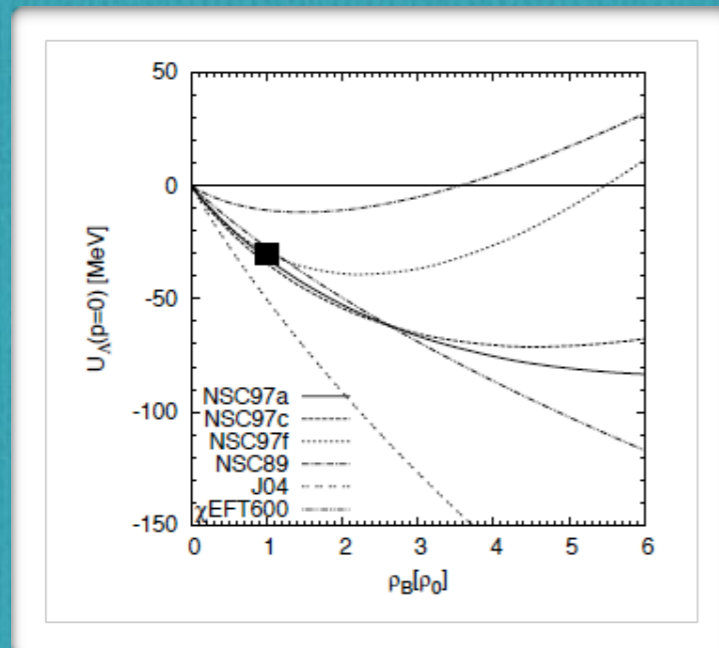
This repulsive core could stiffen again the EOS allowing for heavy neutron stars

Experimental Evidences



Λ Hypernuclei and Λ-p scattering

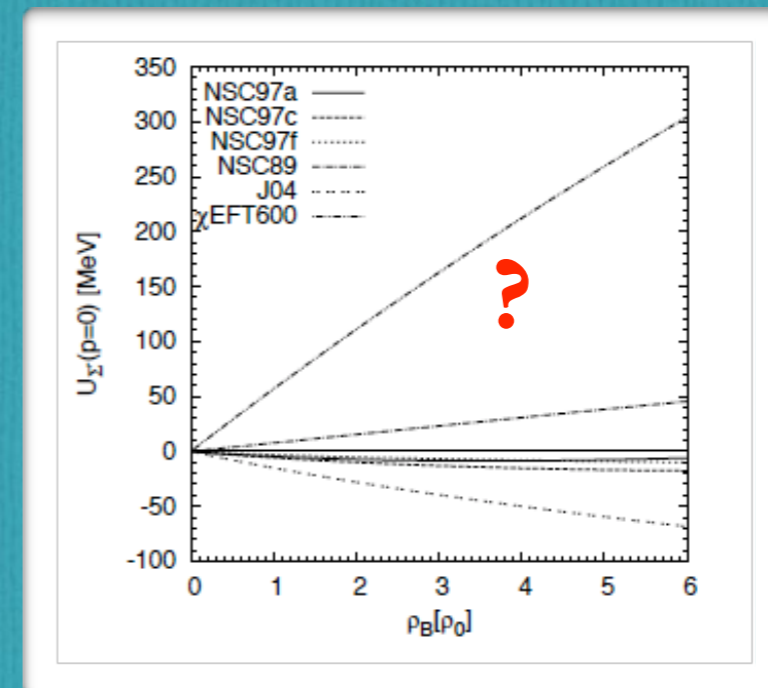
Λ-Nucleon Potential



$U \sim -30$ MeV (attractive)
from Hypernuclei

No idea yet about the momentum and
density dependence

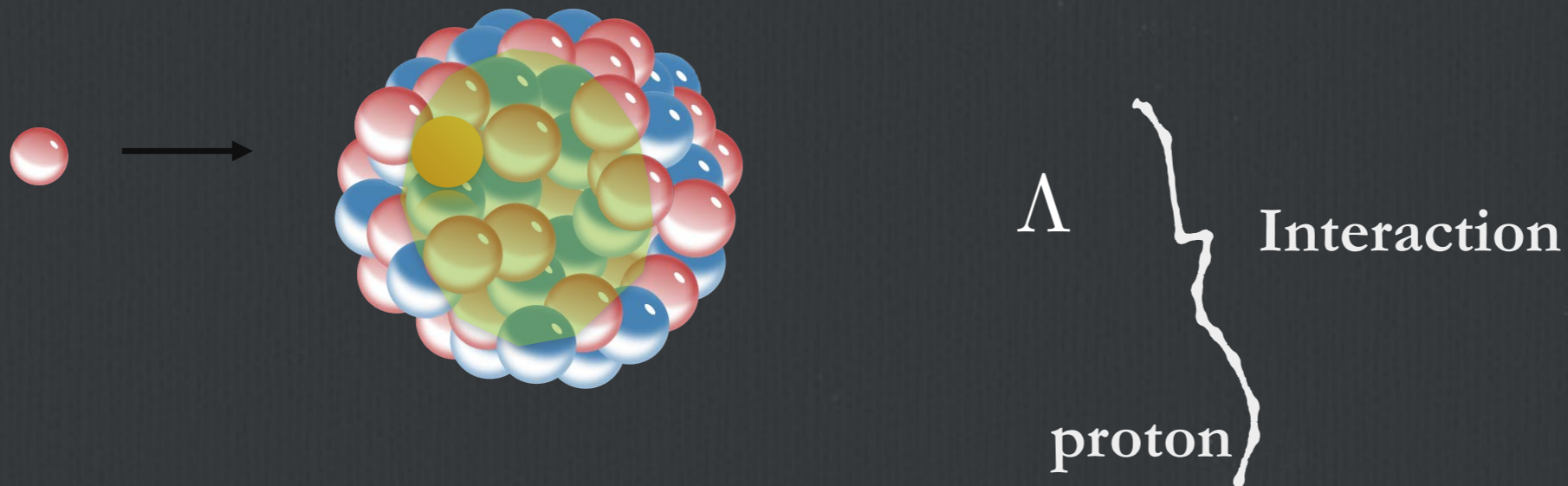
Σ-Nucleon Potential



No Idea at all

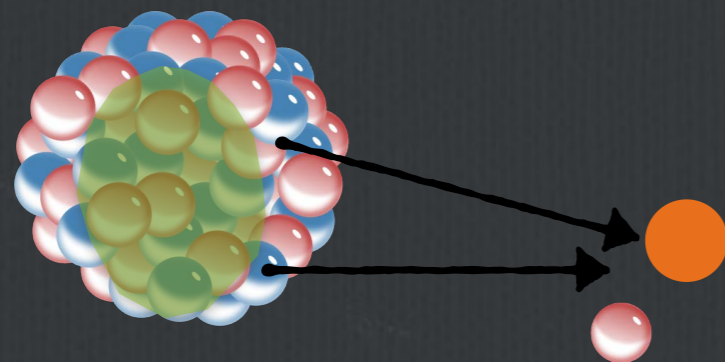
Femtoscscopy in $p+\Lambda/p+p$ reactions

$p+\text{Nb}$, 3.5 GeV

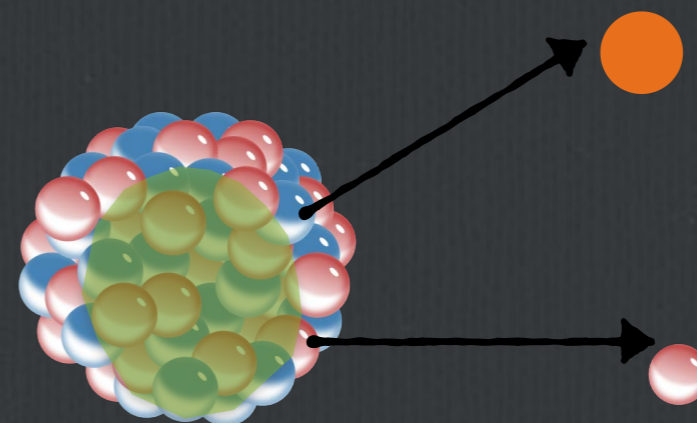


Surface where particles are emitted from
Kinematic Freeze-out surface

Attractive Λp Interaction

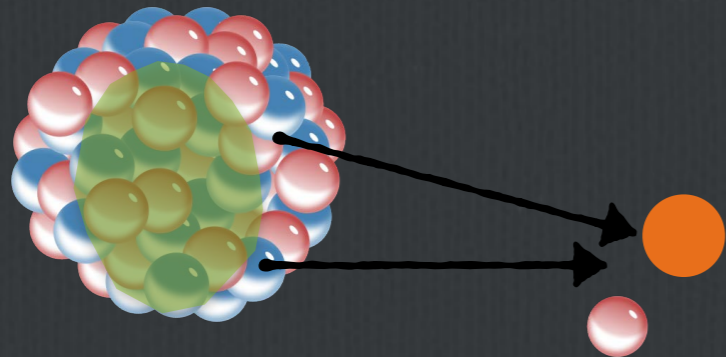


Repulsive Λp Interaction

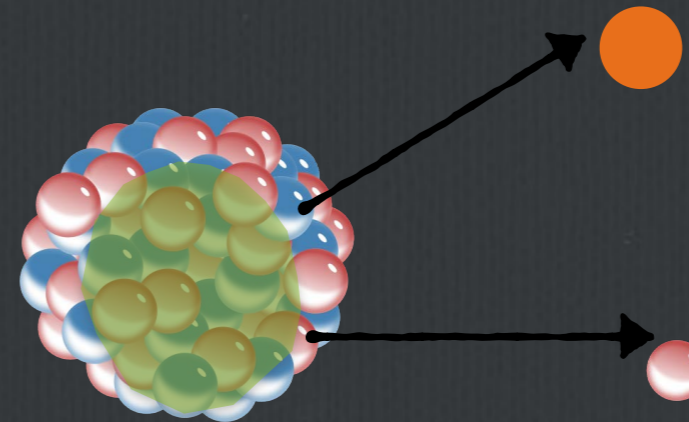


Femtoscscopy in $p+\Lambda/p+p$ reactions

Attractive Λp Interaction



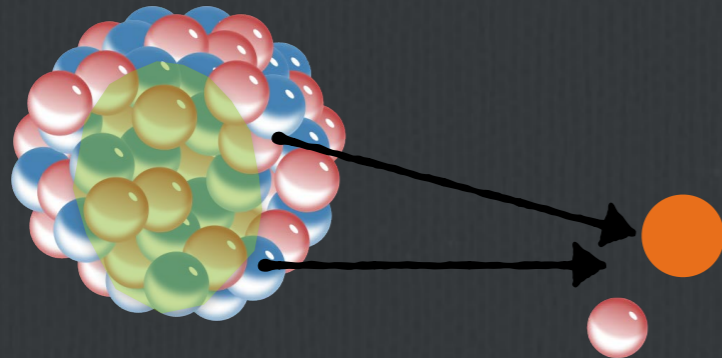
Repulsive Λp Interaction



- We can measure Λp pairs, their momentum and hence the distribution of the momentum difference.
- The source properties are taken from simulations.
- -> By looking at the distribution of the relative momentum we can infer on the final state interaction among the two particles

Correlation Function

Experimental Measurement



$$C(k^*) = \mathcal{N} \frac{N_{\text{same}}(k^*)}{N_{\text{mixed}}(k^*)}$$

$$k^* = \frac{1}{2} |\mathbf{p}_1^* - \mathbf{p}_2^*|$$

$$\mathbf{p}_1^* + \mathbf{p}_2^* = 0$$

Theoretical Function

F. Wang, and S. Pratt, Phys. Rev. Lett. 83 (1999) 3138

$$C(\vec{p}_a, \vec{p}_b) = \frac{\mathcal{P}(\vec{p}_a, \vec{p}_b)}{\mathcal{P}(\vec{p}_a)\mathcal{P}(\vec{p}_b)} \approx \frac{\int d^4 x_a d^4 x_b S(p_a, x_a) S(p_b, x_b) |\phi_{rel}(\vec{p}_b - \vec{p}_a)|^2}{\int d^4 x_a d^4 x_b S_a(\vec{p}_a, x_a) S_b(\vec{p}_b, x_b)}$$

The theoretical function can be expressed in terms of the scattering parameters assuming that the source can be parametrised by f.e. a Gaussian function and that the correlation function does not provide information about the short-range part of the interaction.

The Experimental Data

p+p/A at 3.2 GeV

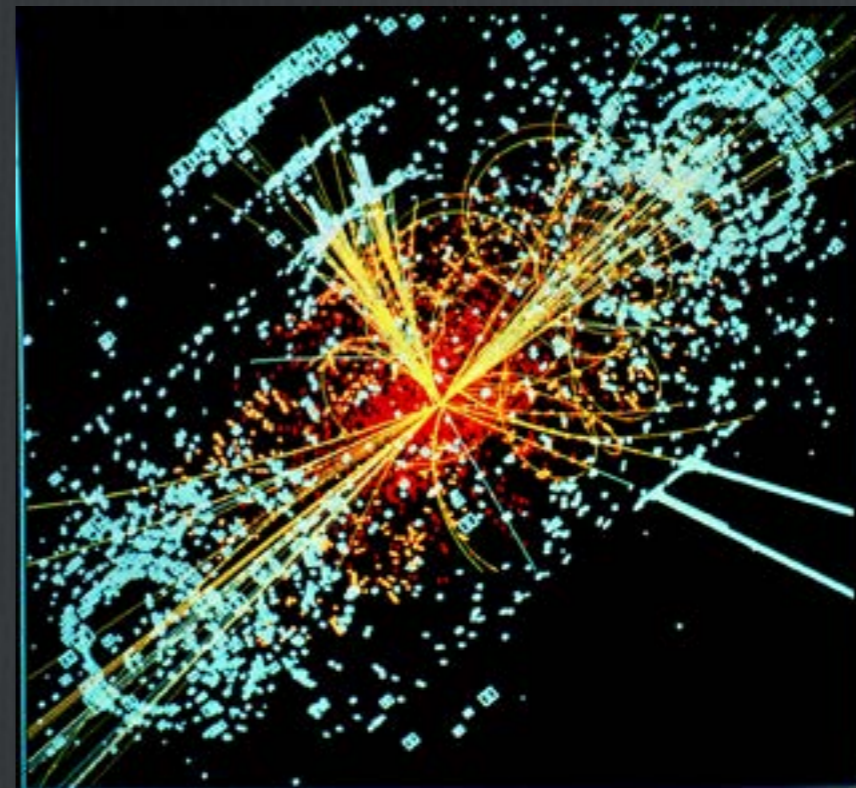


6 Particles/Evt

only 200.000 Λ/Σ but “clean” environment
better knowledge of the emitting source



p+p/A at 7 TeV RUN1



2000 Particles/Evt

large Λ and Σ statistics (~ 3 Mevt) but
more complicated source to be described

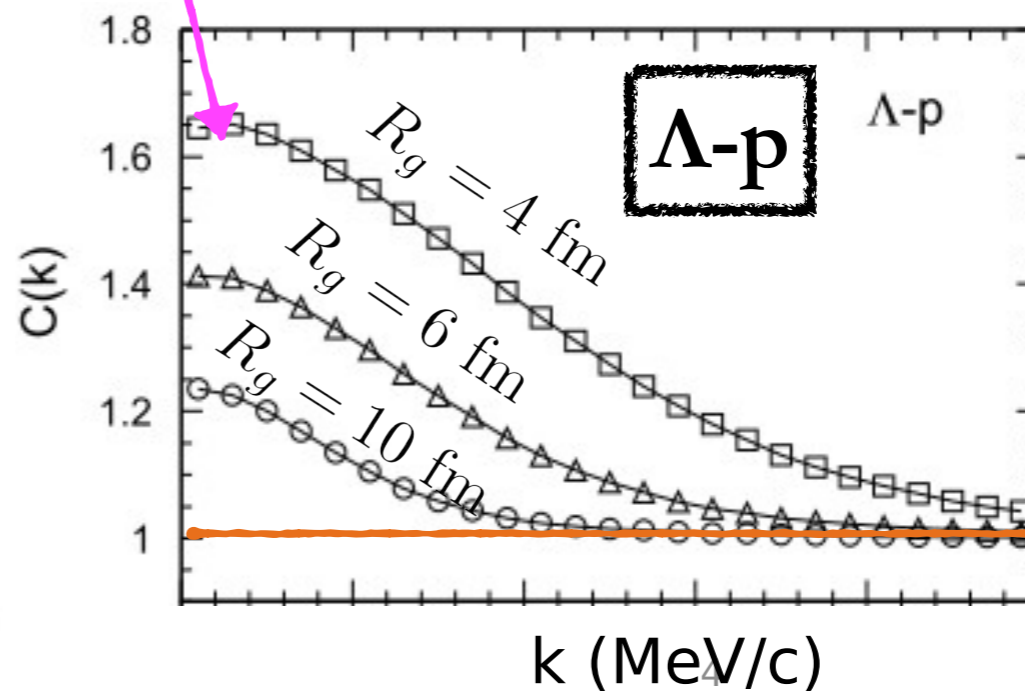
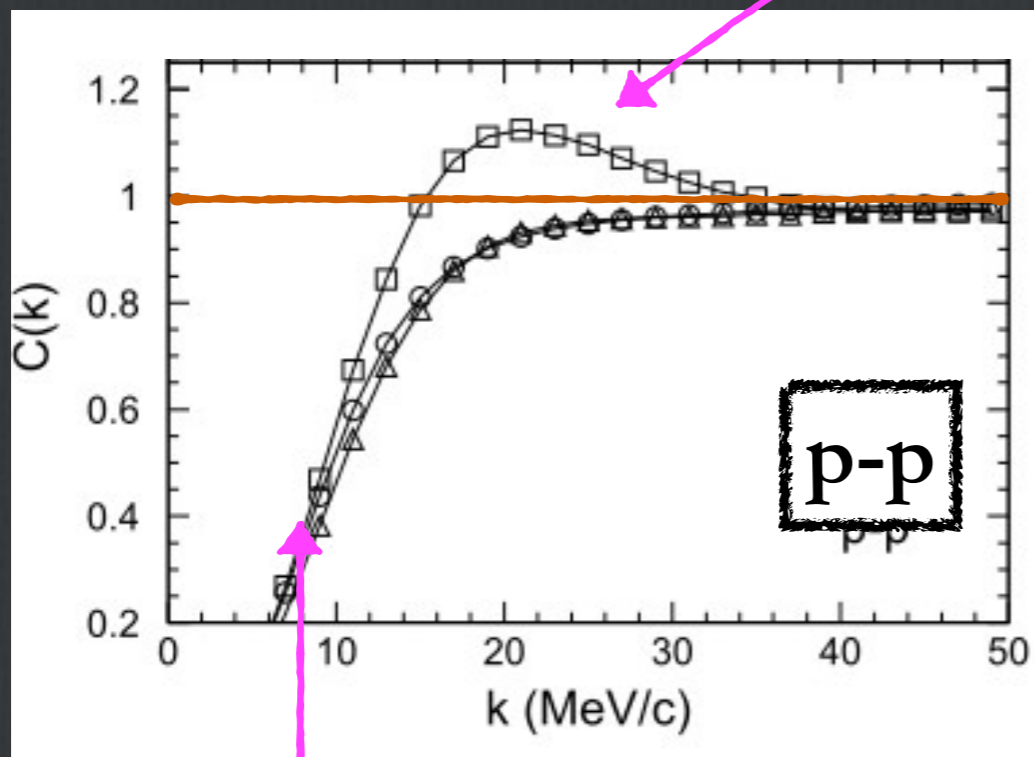


The Experimental Data

Examples of Correlations from Calculations

F. Wang and S. Pratt, Phys. Rev. Lett. 83, 3138 (1999).

Strong Attraction $C(k) > 1$



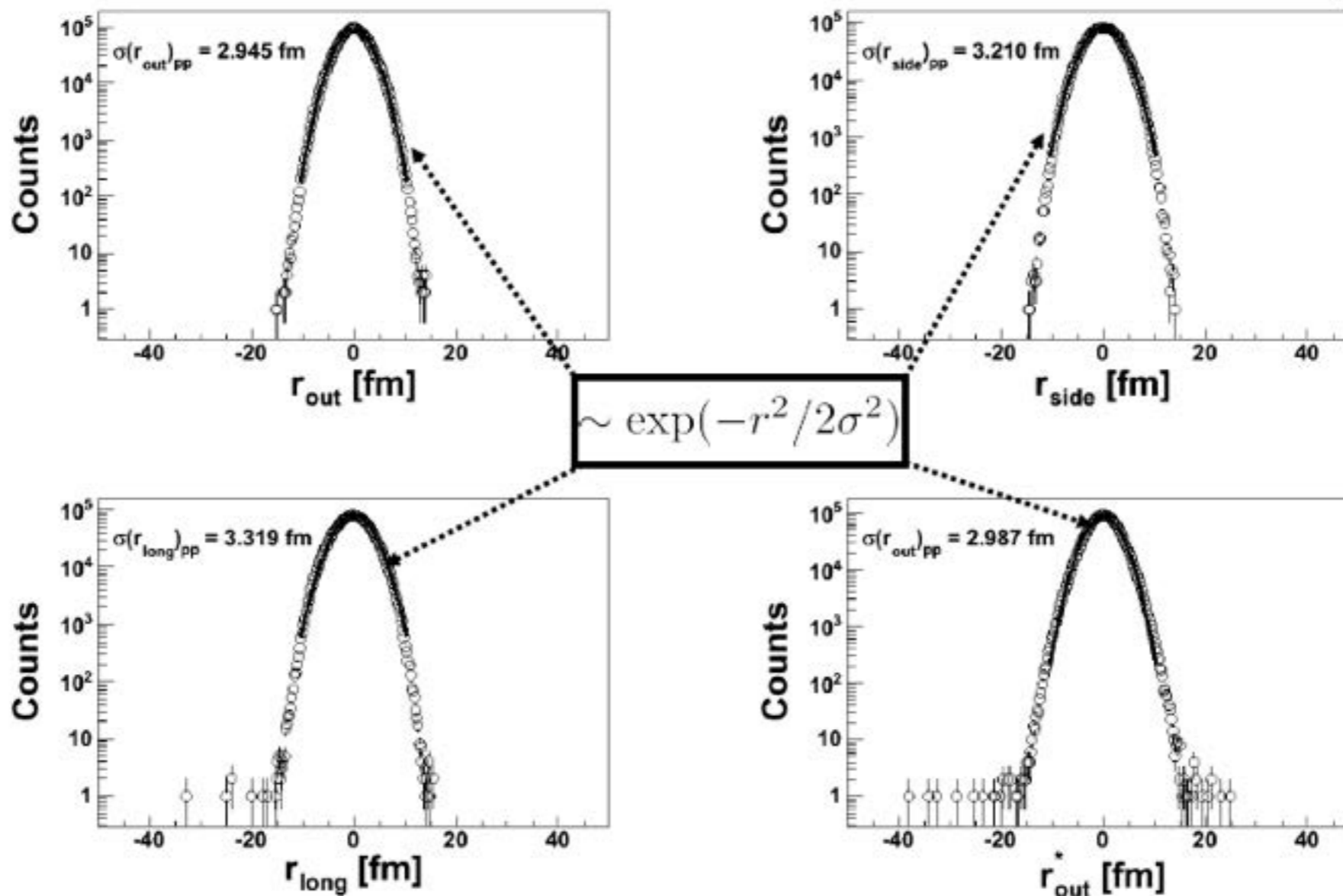
Coulomb Repulsion $C(k) < 1$

Sources from UrQMD

Source extraction from transport theory (UrQMD) - LCMS:

$$C^{ab}(k) = \int d^3r' S_P(r') |\phi(k, r')|^2 \quad k < 30 \text{ MeV}/c$$

Proton-Proton

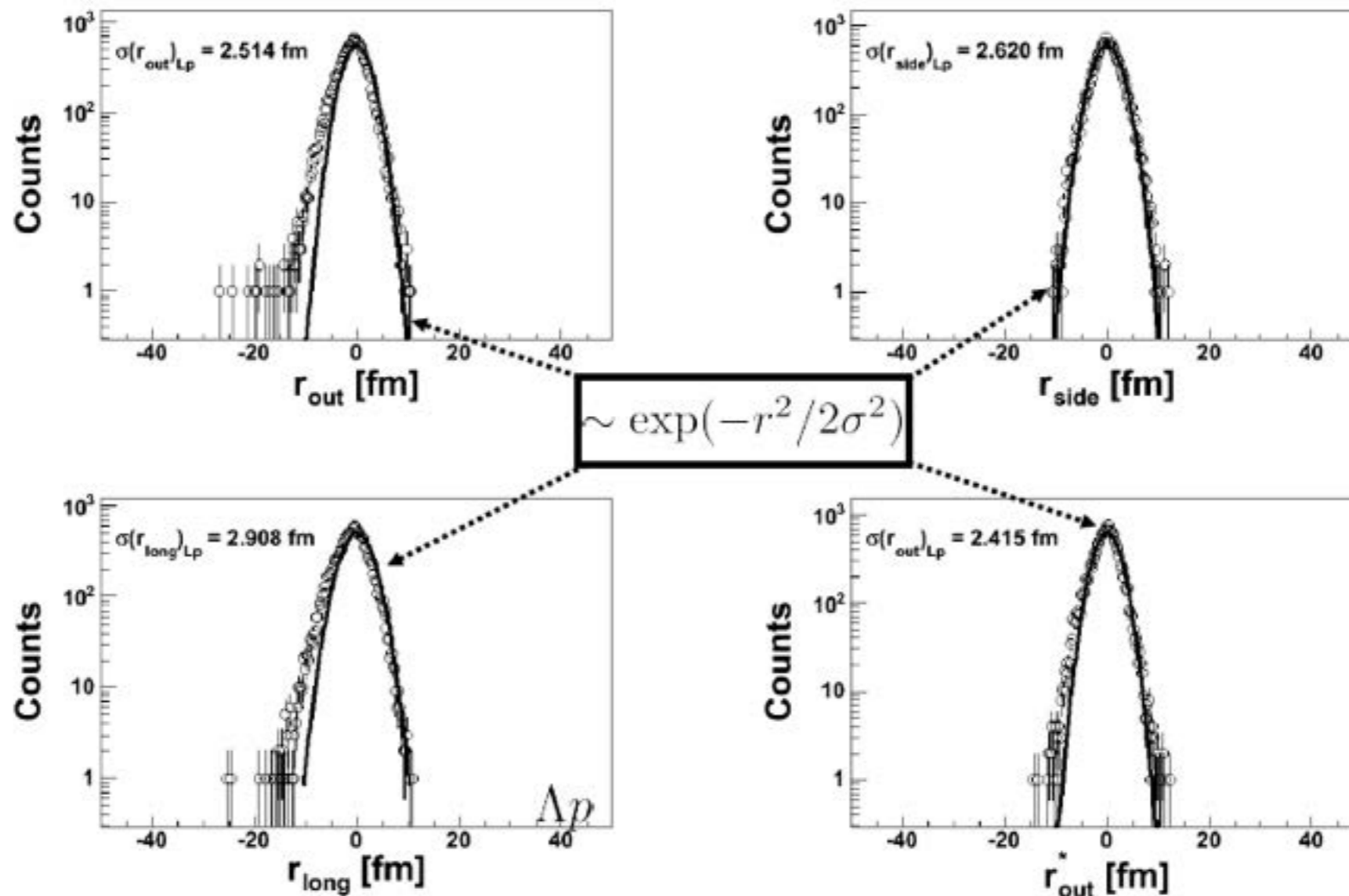


Sources from UrQMD

Source extraction from transport theory (UrQMD) - LCMS:

$$C^{ab}(k) = \int d^3r' S_P(\mathbf{r}') |\phi(\mathbf{k}, \mathbf{r}')|^2 \quad k < 30 \text{ MeV}/c$$

Λp

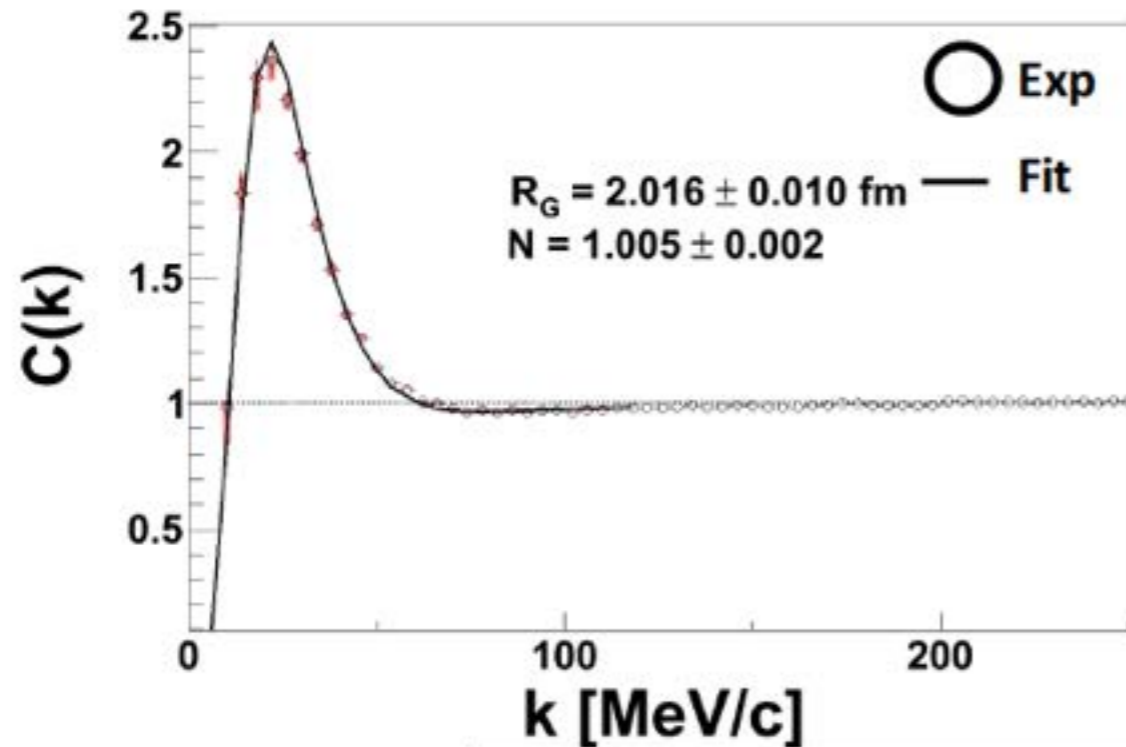


p-p correlation in p+Nb collisions at 3.5 GeV

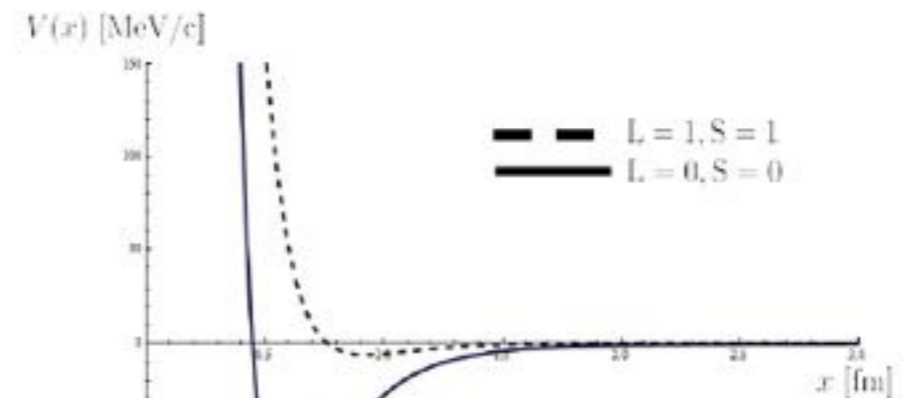
1.2 Billions evts

Information about the source – proton proton correlation function:

Extract source size: $C^{ab}(k) = N \int d^3r' S_P(r') |\phi(\mathbf{k}, \mathbf{r}')|^2$



Potential used for strong interaction:



B. D. Day, Phys. Rev. C 24, (1981), 1203

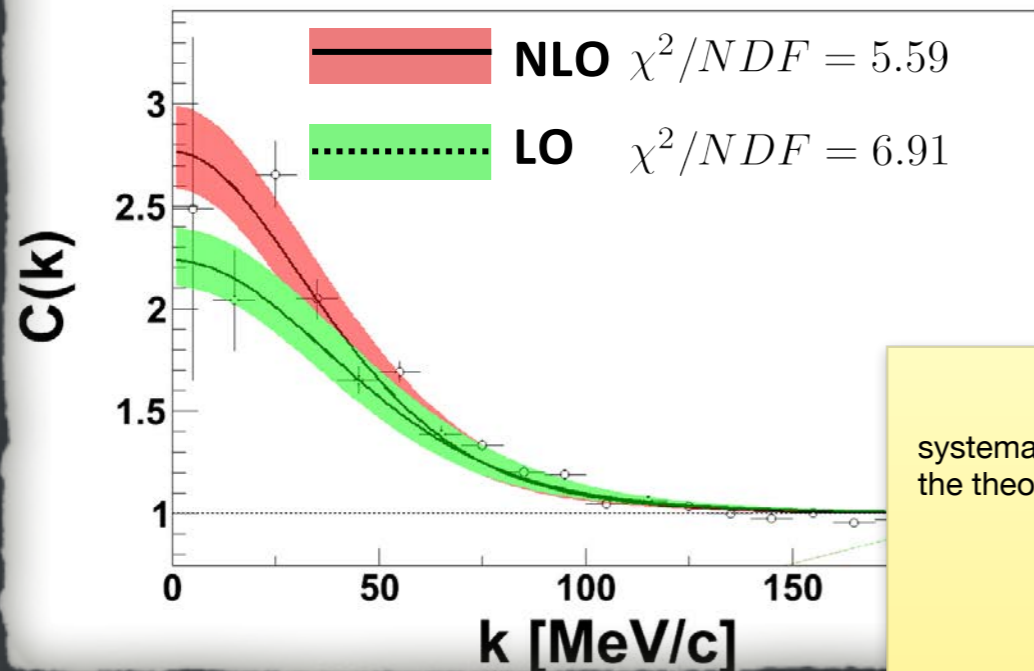
$$\frac{d^2 w}{d\rho^2} + \left[1 - \frac{2\eta}{\rho} - \frac{l(l+1)}{\rho^2} - \frac{2\mu}{k^2} V(\rho) \right] = 0 \quad S(r) \sim \exp(-r^2/4R_G^2)$$



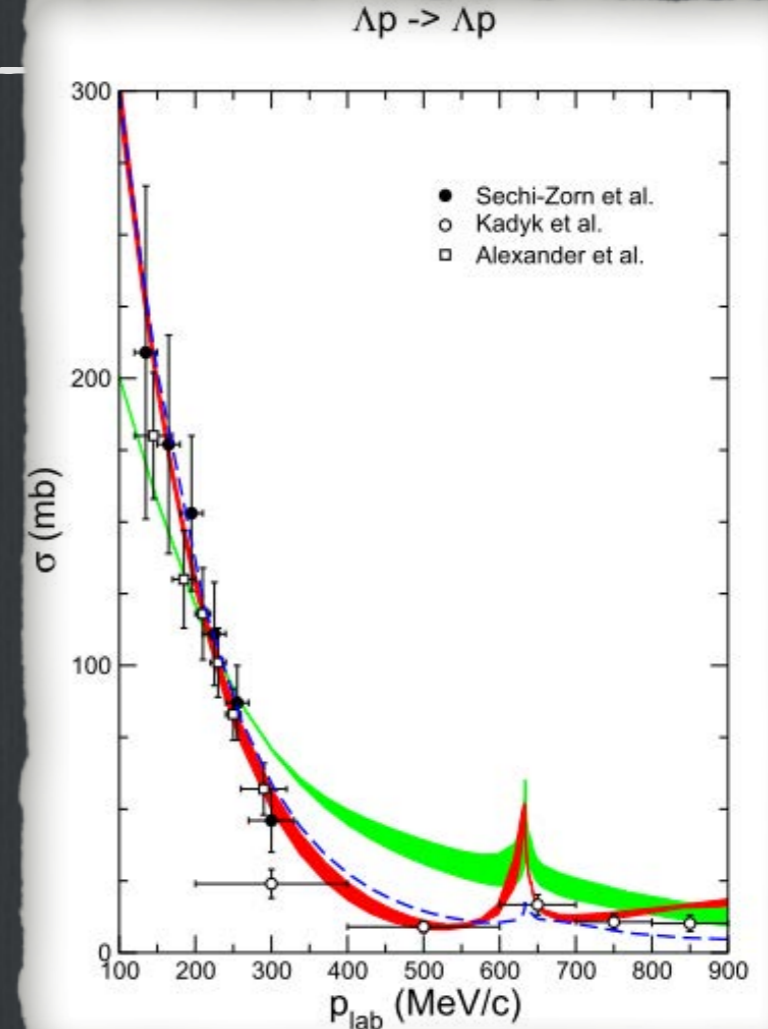
$$R_G = 2.016 \pm 0.010^{+0.039}_{-0.027} \text{ fm}$$

Λ -p Correlation in p+Nb collisions at 3.5 GeV

J. Adamczewski-Musch et al., [HADES coll.] Phys. Rev. C. 94 (2016).



systematic of the error on the radius on the theory



$$C(k) = 1 + \sum_S \rho_S \left[\frac{1}{2} \left| \frac{f^S(k)}{R_G^{\Lambda p}} \right|^2 \left(1 - \frac{d_0^S}{2\sqrt{\pi} R_G^{\Lambda p}} \right) + 2 \frac{\mathcal{R} f^S(k)}{\sqrt{\pi} R_G^{\Lambda p}} F_1(Q R_G^{\Lambda p}) - \frac{\mathcal{I} f^S(k)}{R_G^{\Lambda p}} F_2(Q R_G^{\Lambda p}) \right]$$

Λ -p correlation function obtained by substituting the NLO and the LO scattering length values in the Lednicky's model.

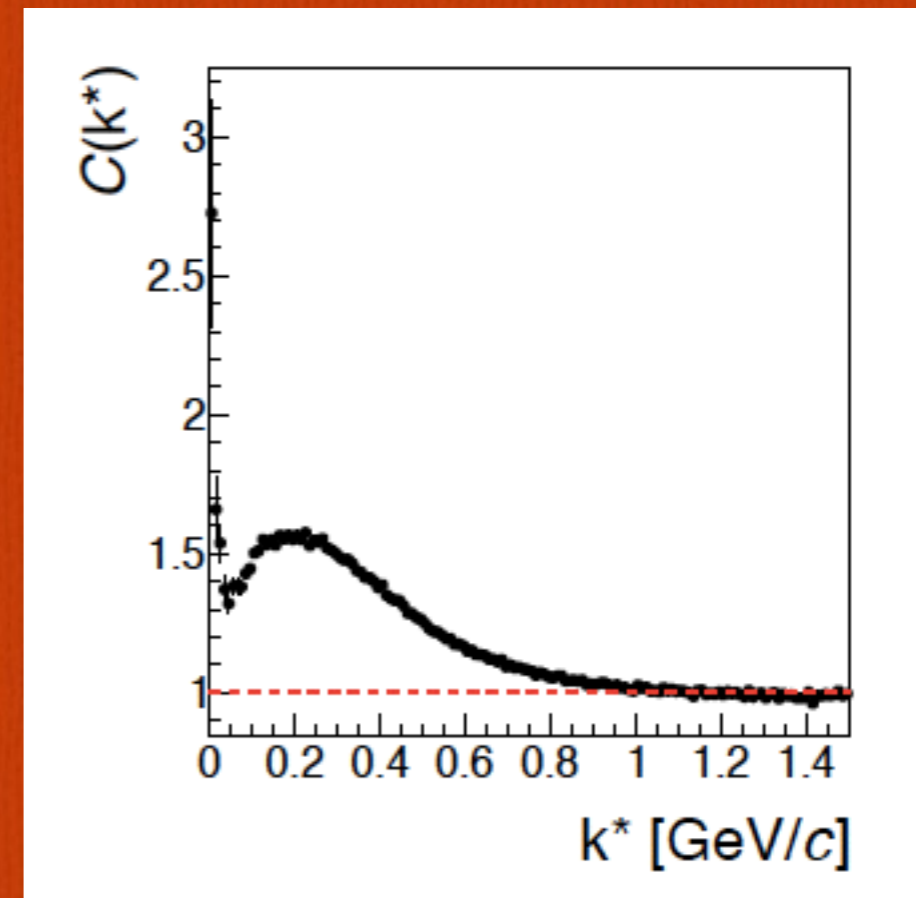
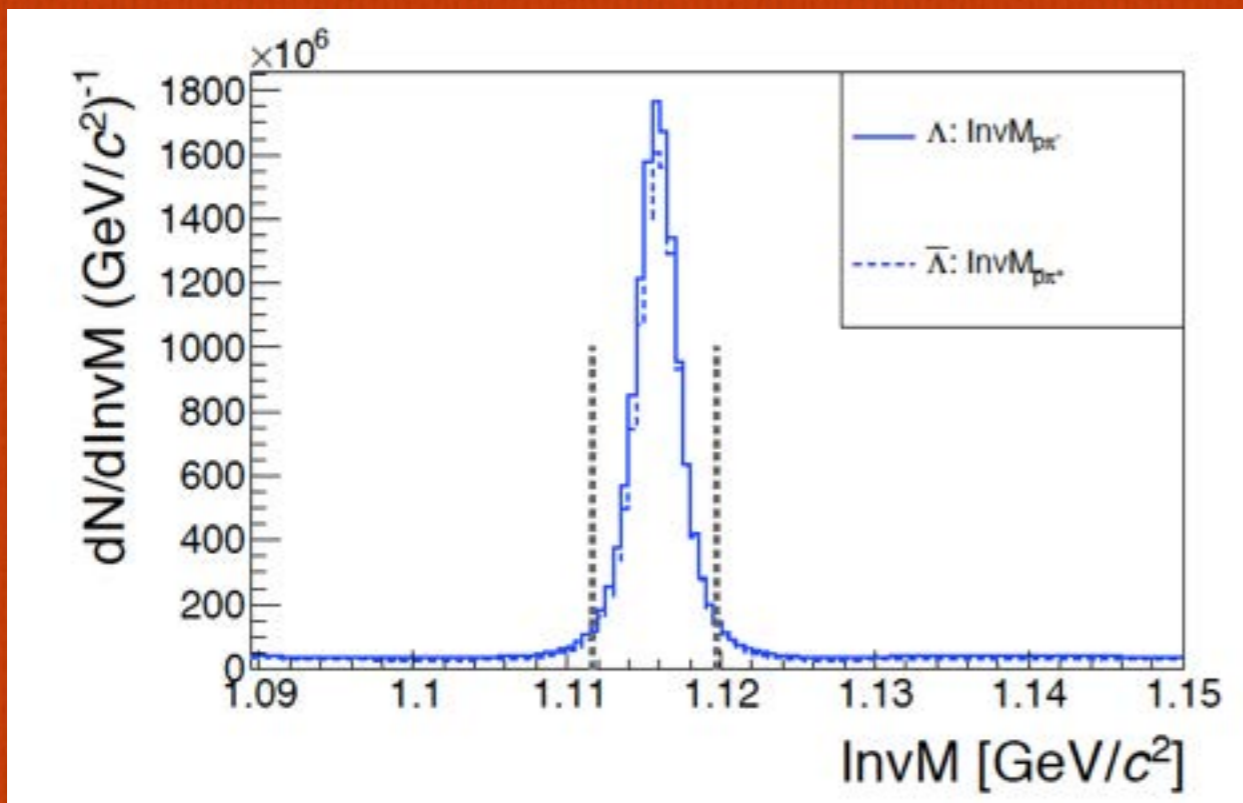
Substitute scattering data!!

ALICE data

p+p 7 TeV, RUN 1 ~250 Millions Events

Excellent Purity for Λ

$p - \bar{p}$ Correlation



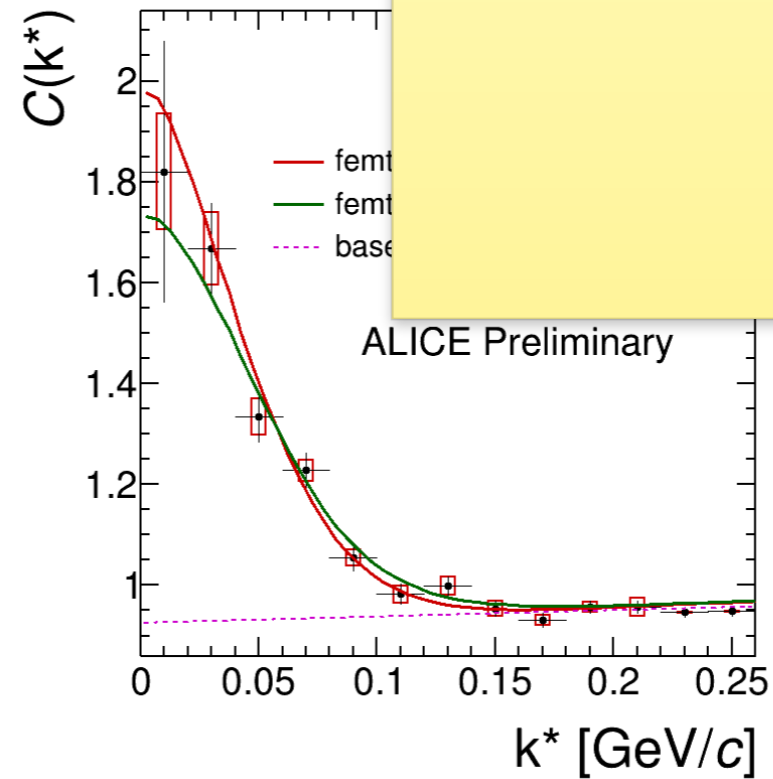
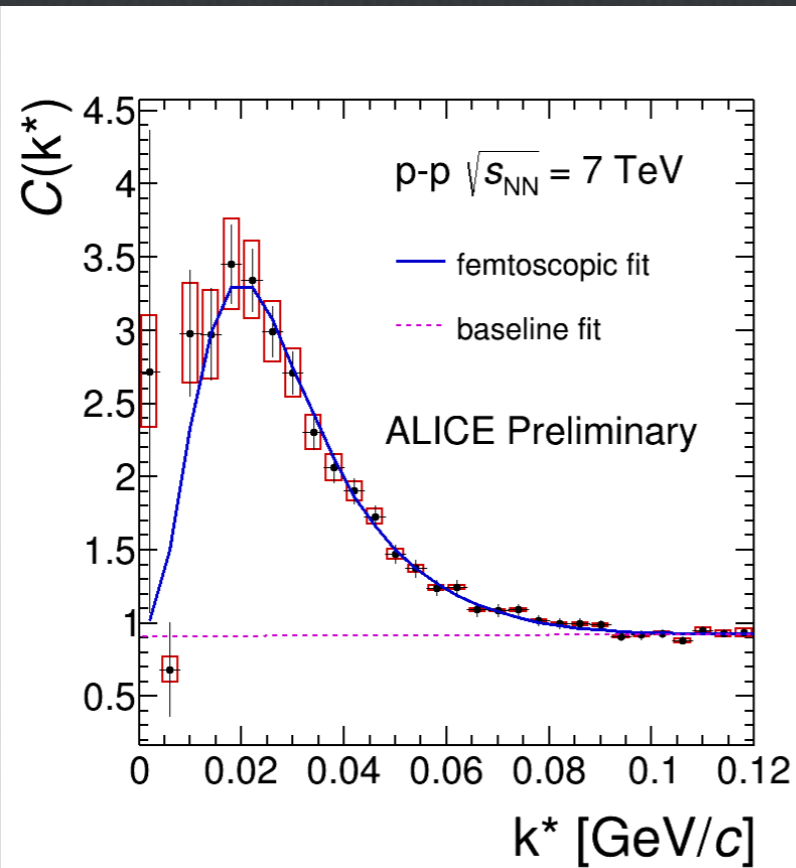
Minijets background present for Baryon-Antivaryon correlation
Not there for Baryon-Baryon correlation

p+p at much larger energy

p-p Correlation

Λp C

systematic error only on the experimental data and extracted parameters, radius in this case
Lines represent the fit for the standard case

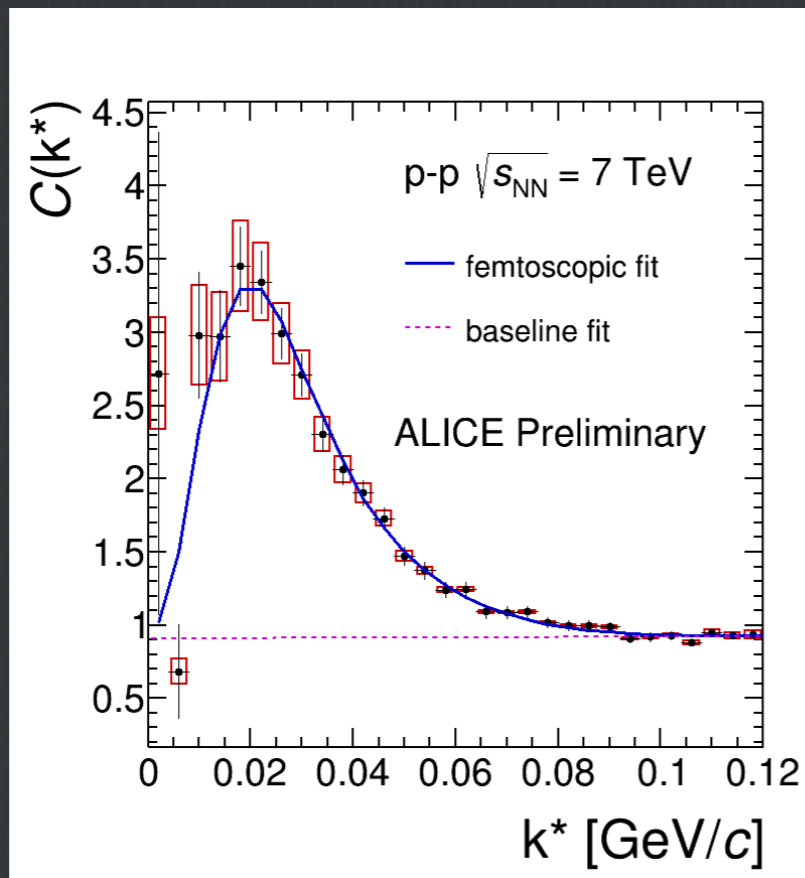


$$C(k^*)_{pp,tot} = \mathcal{N}_{pp} \left(1 + \underbrace{\lambda_{pp}}_{0.76} (C(k^*)_{pp} - 1) + \underbrace{\lambda_{p\Lambda}}_{0.16} (C(k^*)_{p\Lambda} - 1) \right) C(k^*)_{baseline}$$

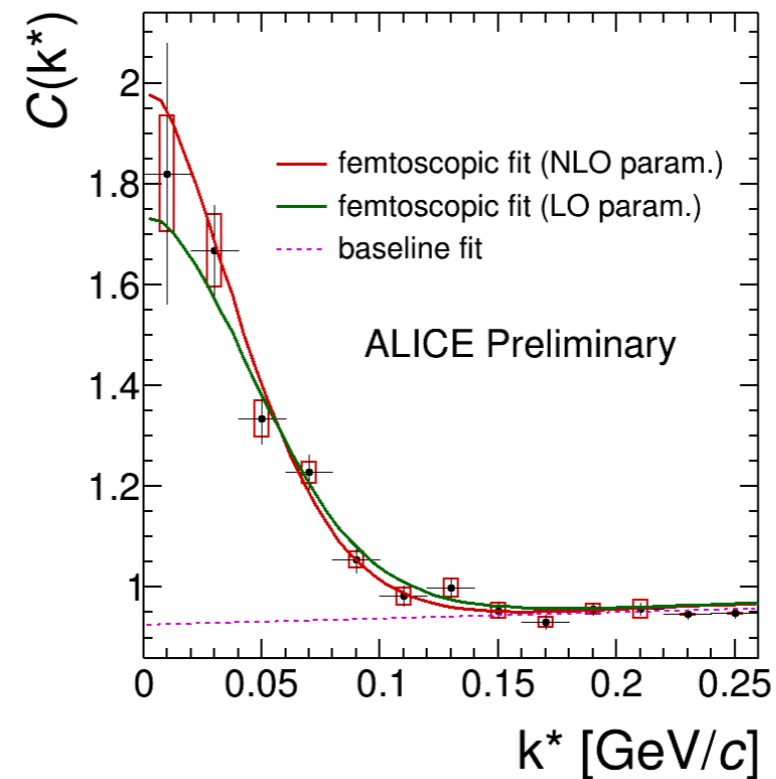
$$C(k^*)_{p\Lambda,tot} = \mathcal{N}_{p\Lambda} \left(1 + \underbrace{\lambda_{p\Lambda}}_{0.53} (C(k^*)_{p\Lambda} - 1) + \underbrace{\lambda_{p\Sigma^0}}_{0.17} (C(k^*)_{p\Sigma^0} - 1) + \underbrace{\lambda_{p\Xi^-}}_{0.10} (C(k^*)_{p\Xi^-} - 1) \right) C(k^*)_{baseline}$$

p+p at much larger energies (7 TeV)

p-p Correlation



Δp Correlation



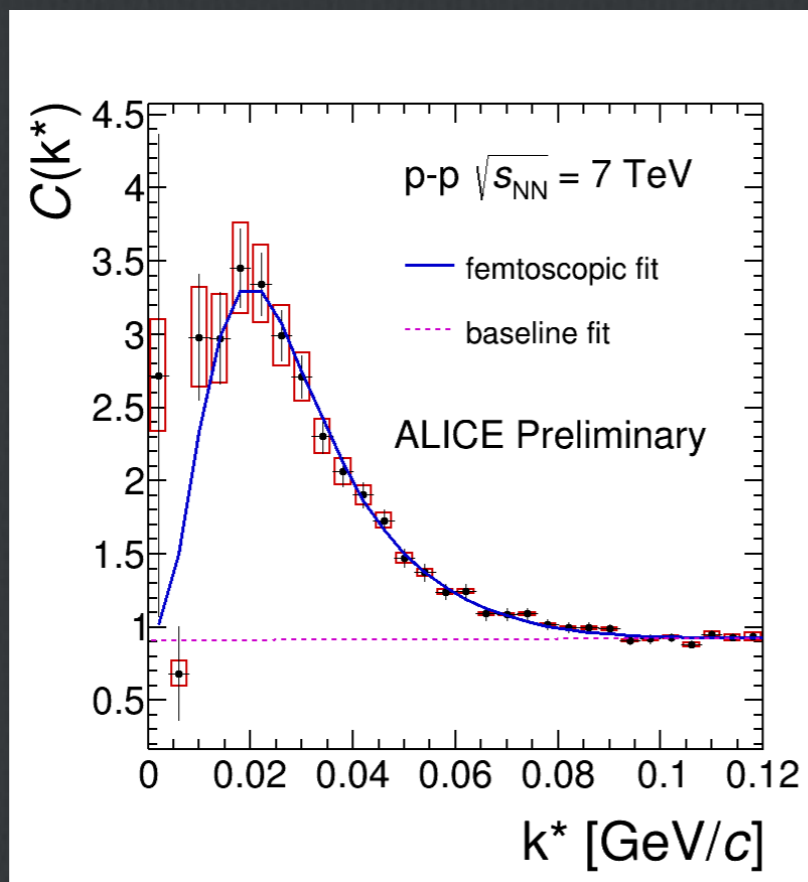
RUN1 Statistics

Factor 5 more available from RUN2 Statistics (middle of 2017)

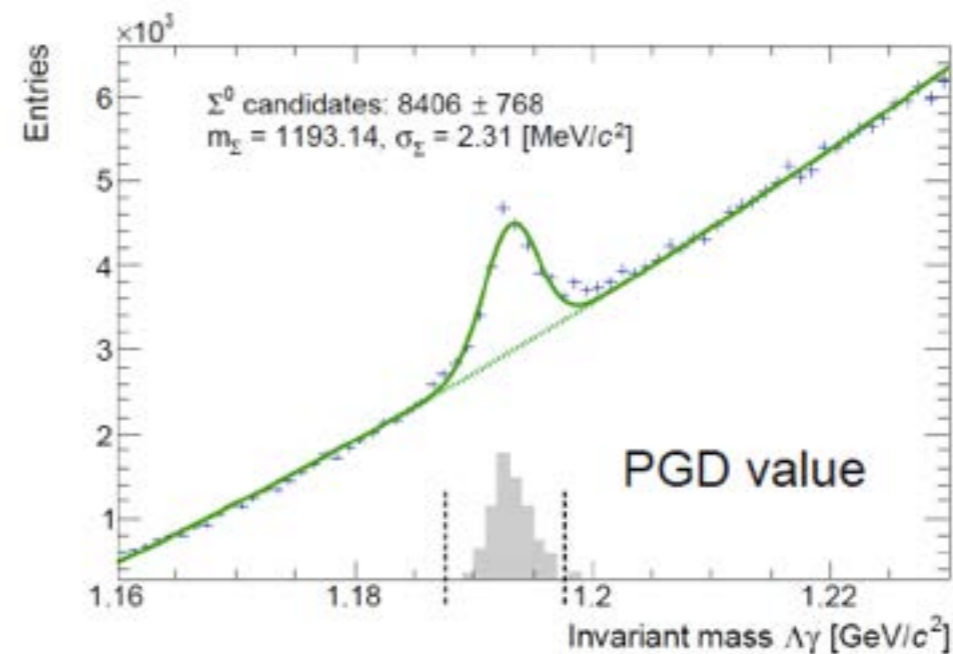
Extension to $\Sigma^0/\Sigma^+/\Xi - p$ correlations

p+p at much larger energies (7 TeV)

p-p Correlation



Λp Correlation



RUN2 - LHC16I (326M events, pass1)

RUN1 Statistics

Factor 5 more available from RUN2 Statistics (middle of 2017)

Extension to $\Sigma^0 / \Sigma^+ / \Xi - p$ correlations

Test-Bed for Lattice Calculations

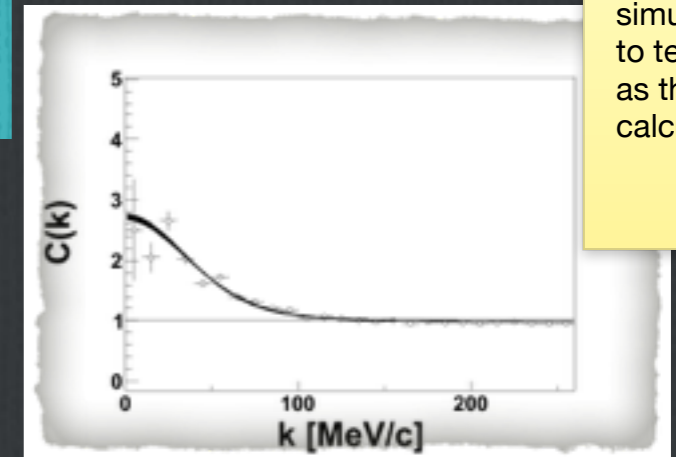
Simulation of the particle
Production and Freeze-
Out coordinates

After-Burner which
includes the relevant
Interactions

Comparison with
the measured
correlations

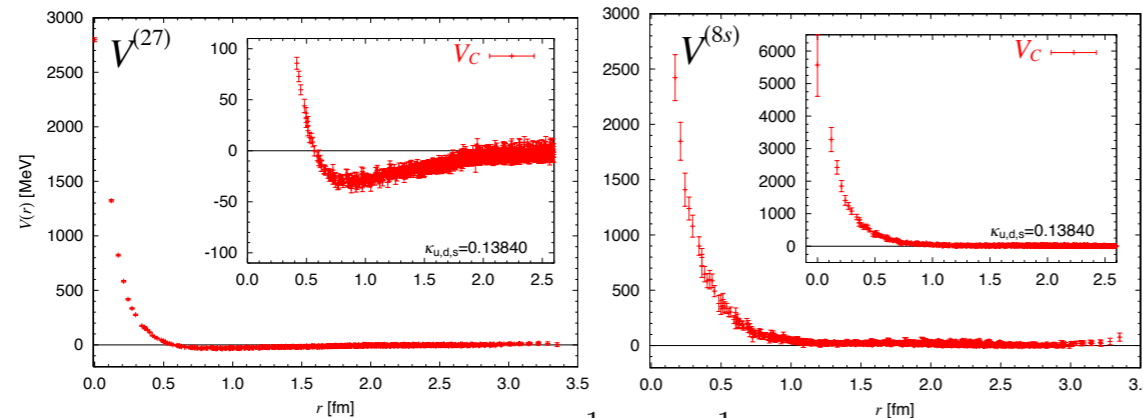
Tuning of
the strong
interaction

instead of full
simulations
to test full s
as those res
calculations

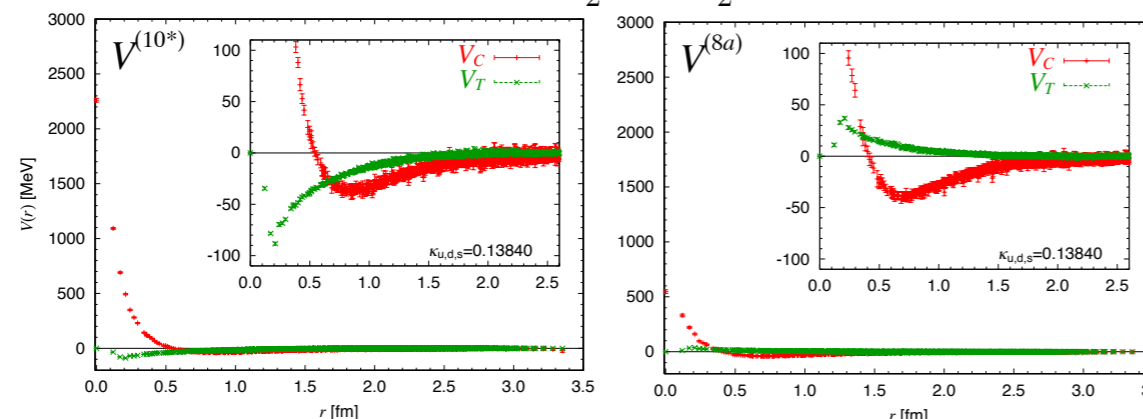


$m_\pi = 470 \text{ MeV}$

$$\Lambda N(^1S_0) = \frac{9}{10}[27] + \frac{1}{10}[8_s]$$



$$\Lambda N(^3S_1) = \frac{1}{2}[10^*] + \frac{1}{2}[8_a]$$



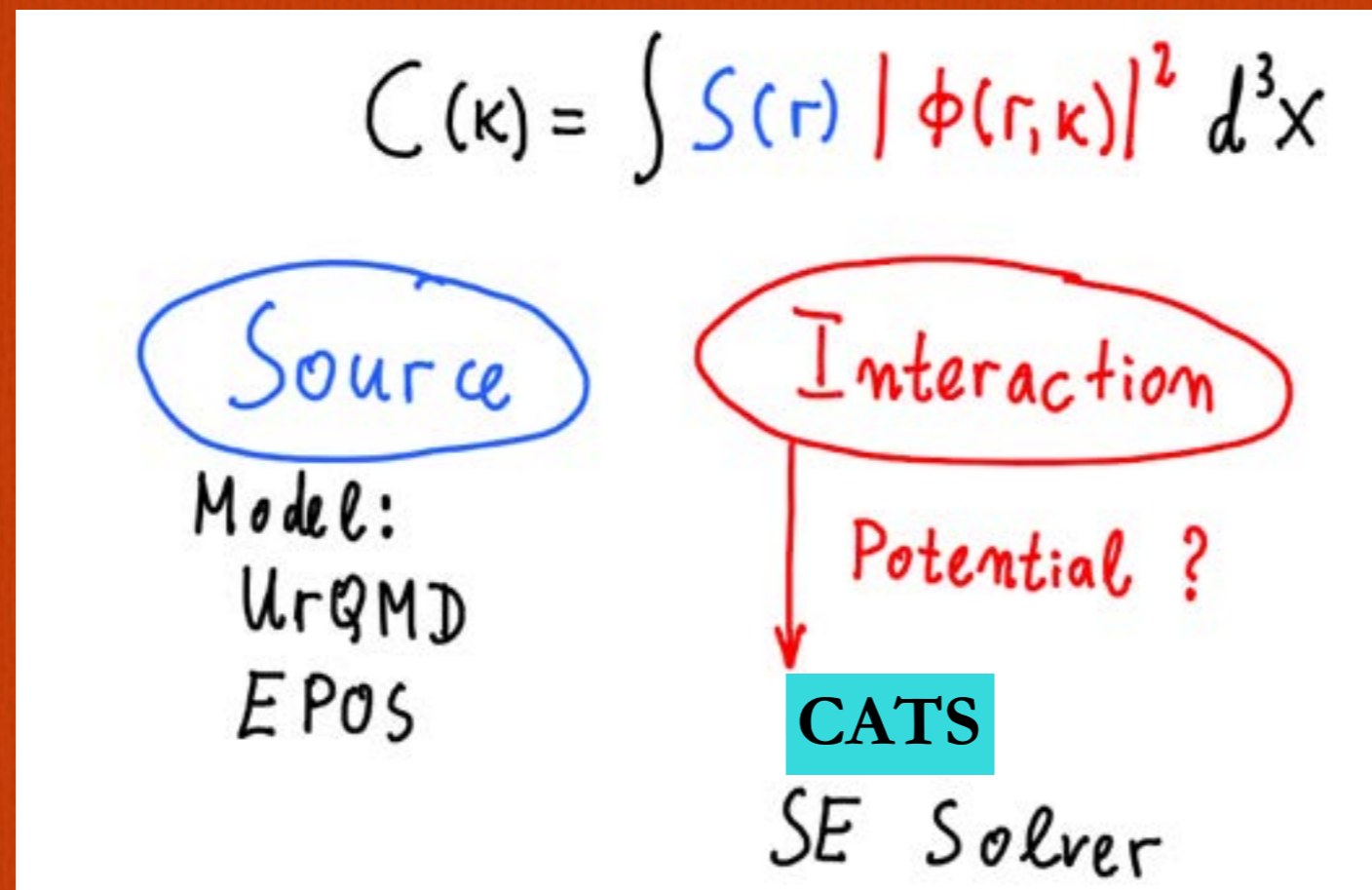
Hyperon-Nucleon Correlation
Hyperon-Nucleon-Nucleon
Correlation??

Mainly a matter of statistics

Our Afterburner

Idea:

- Event generator (UrQMD or EPOS) or Gaussian distribution for the source sampling
- Schrödinger equation solver



Output:

Theoretical correlation function to be compared with the experimental data

Correlation Analysis Tool using the Schrödinger equation

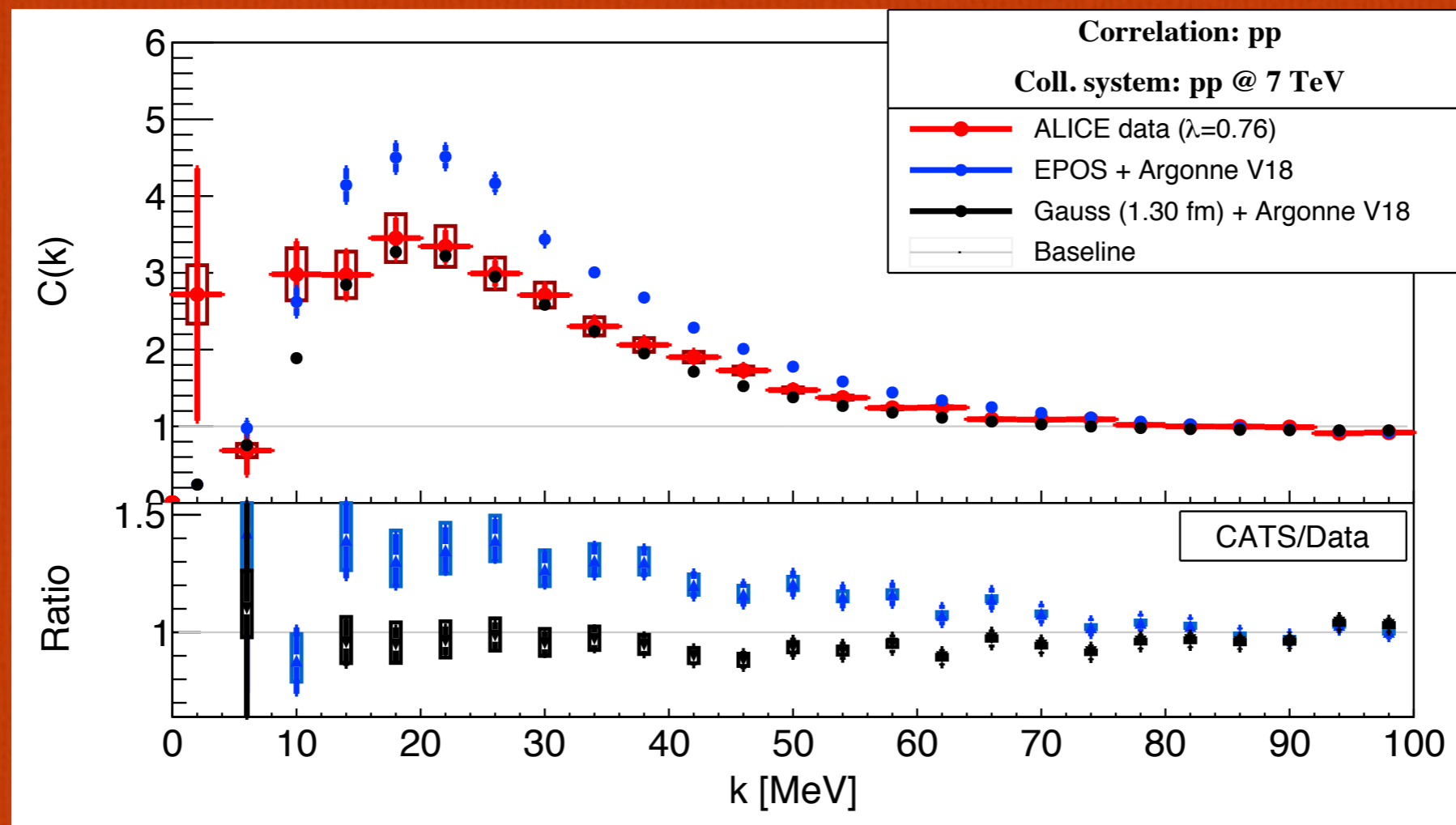


CATS

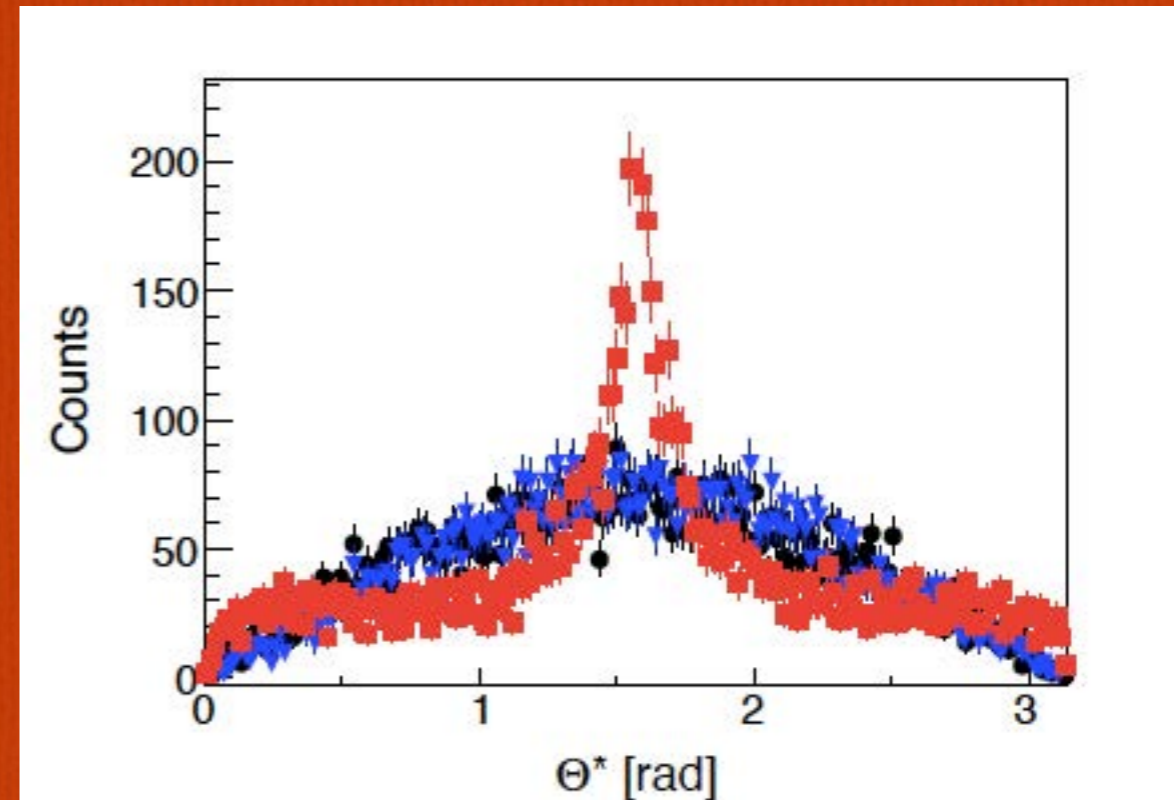
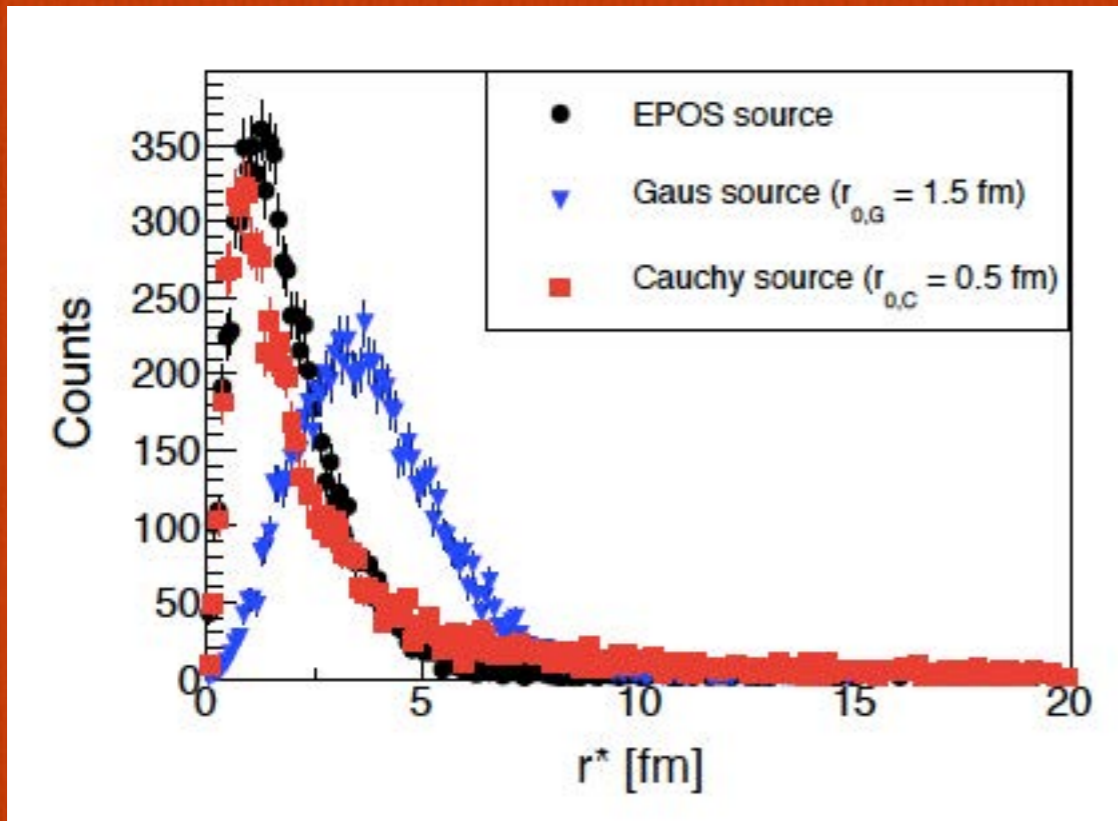


Exact solution, no asymptotic solution (large distances) as in CRAB*

* <http://www.pa.msu.edu/~pratts/freecodes/crab/home.html>



Source in EPOS



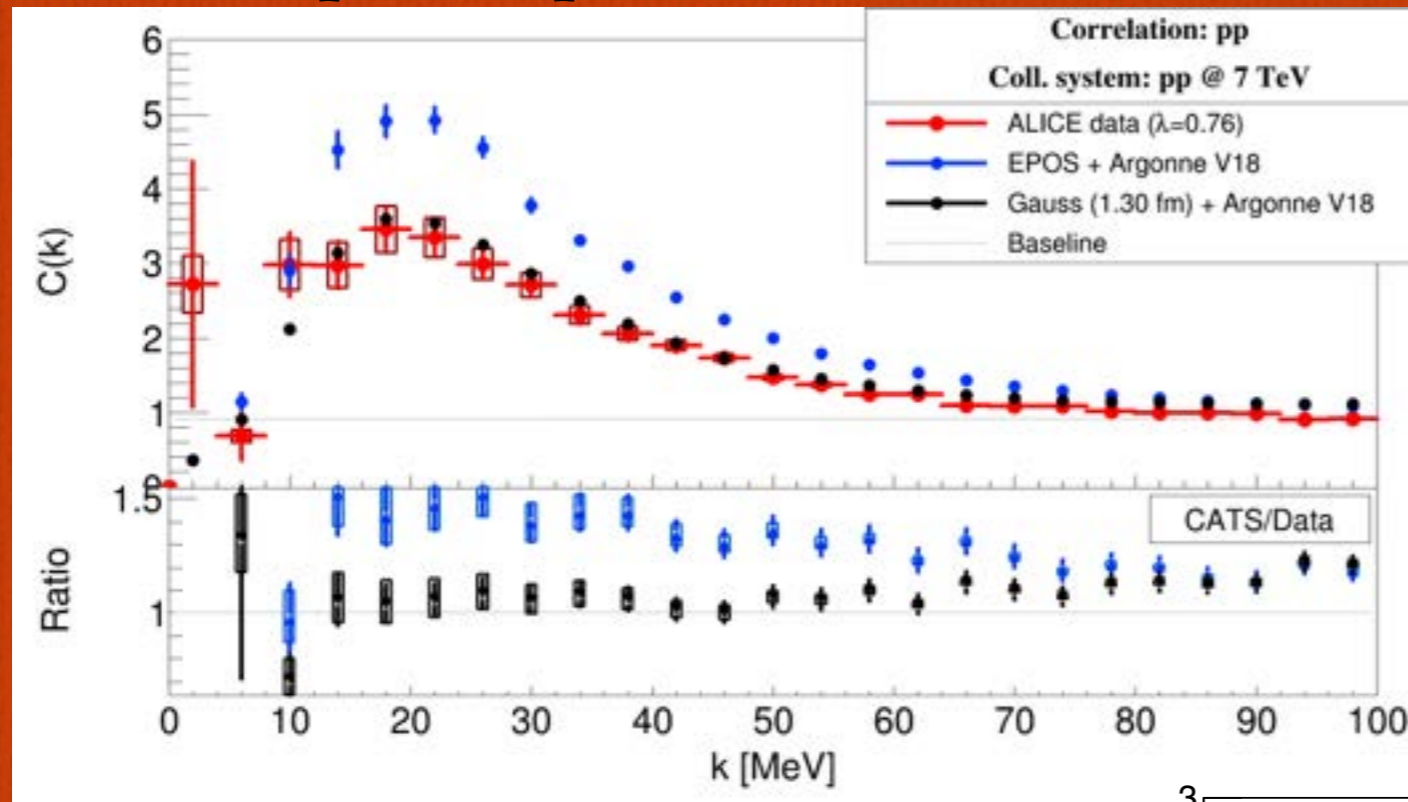
Cauchy Function:

$$f(x) = \frac{1}{\pi(1+x^2)}$$

The EPOS generator does not deliver a Gaussian source!

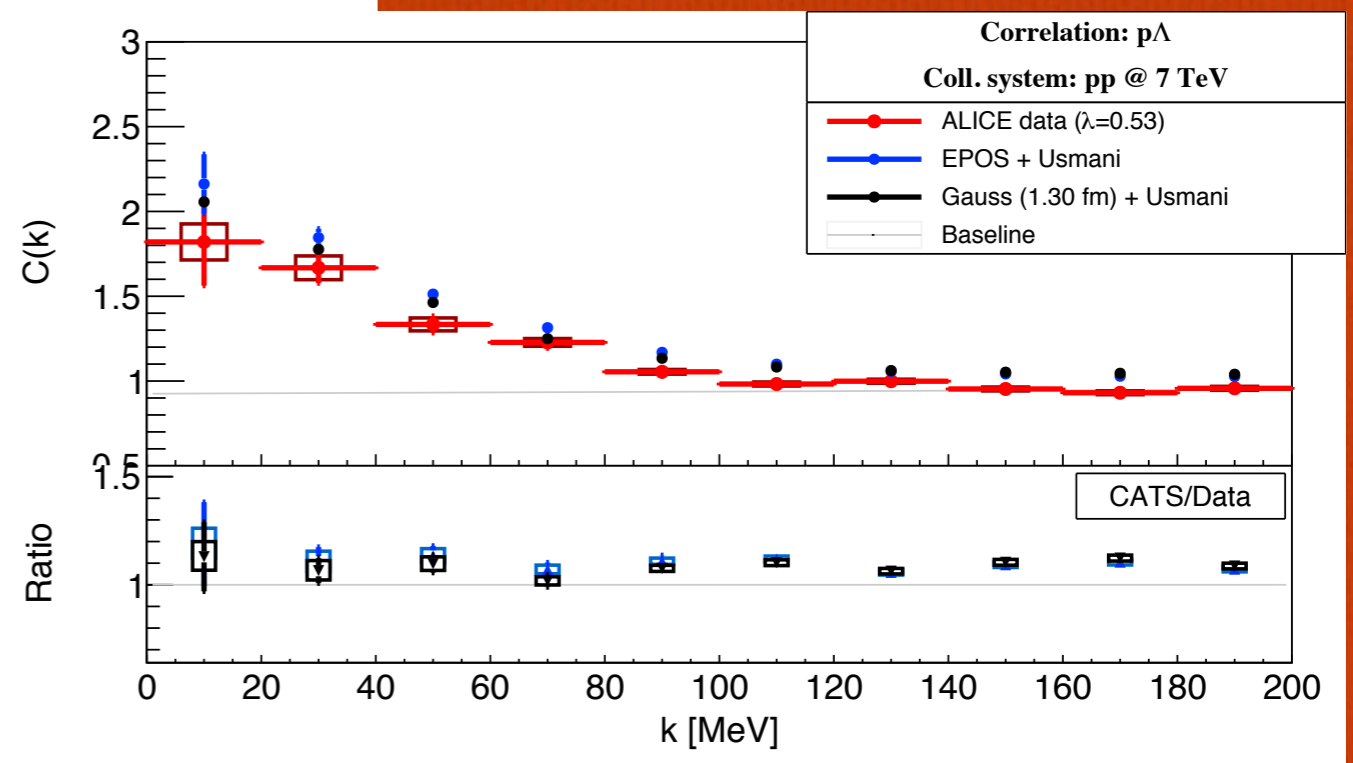
CATS and ALICE data

proton-proton correlation



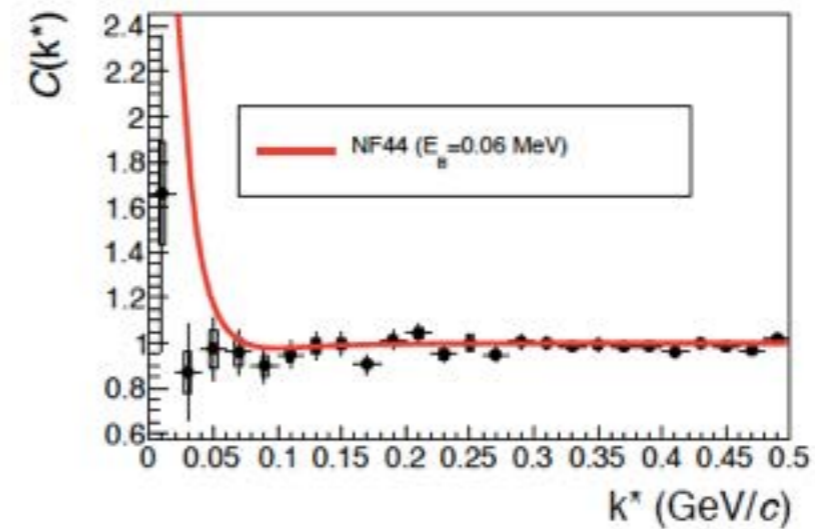
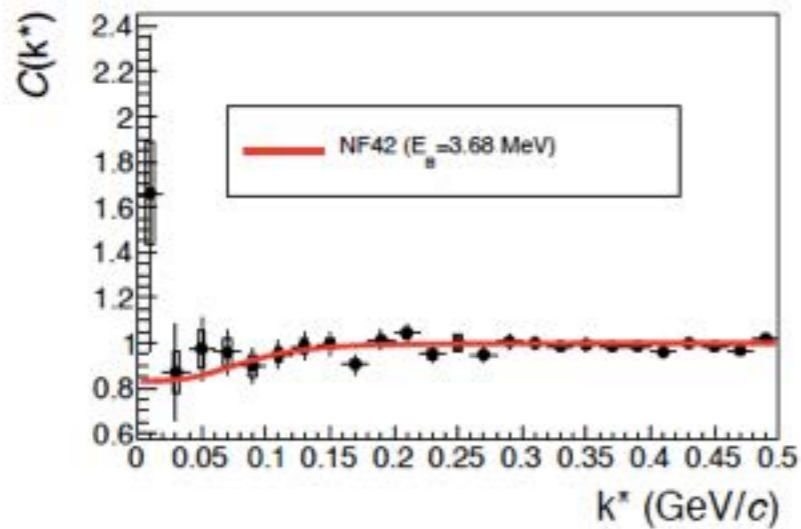
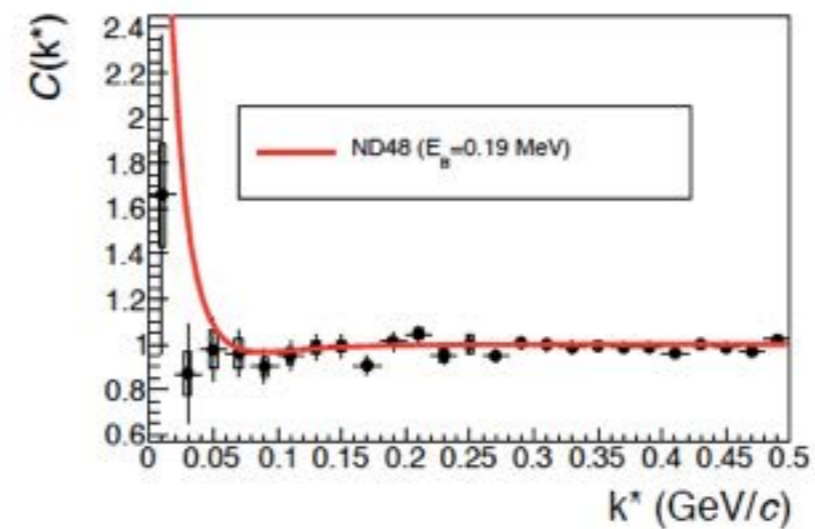
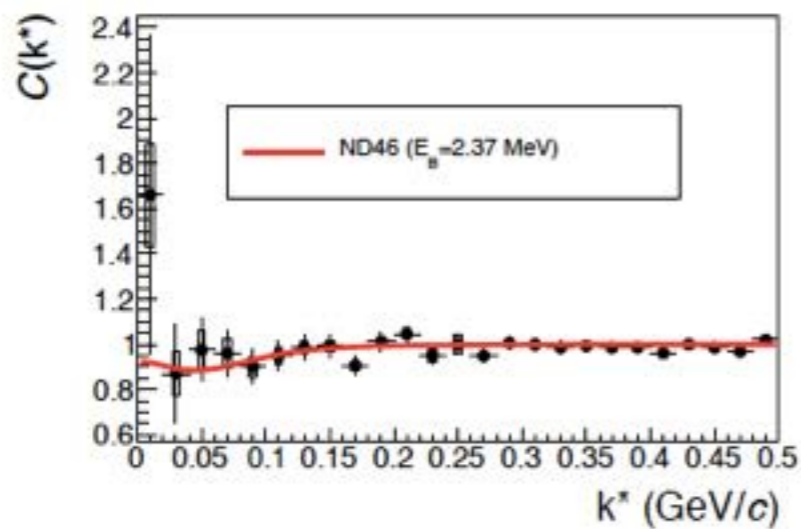
pp correlation are obtained with EPOS+CATS do not match the experimental data.
But a Gaussian source + CATS does it.

Λ -proton correlation

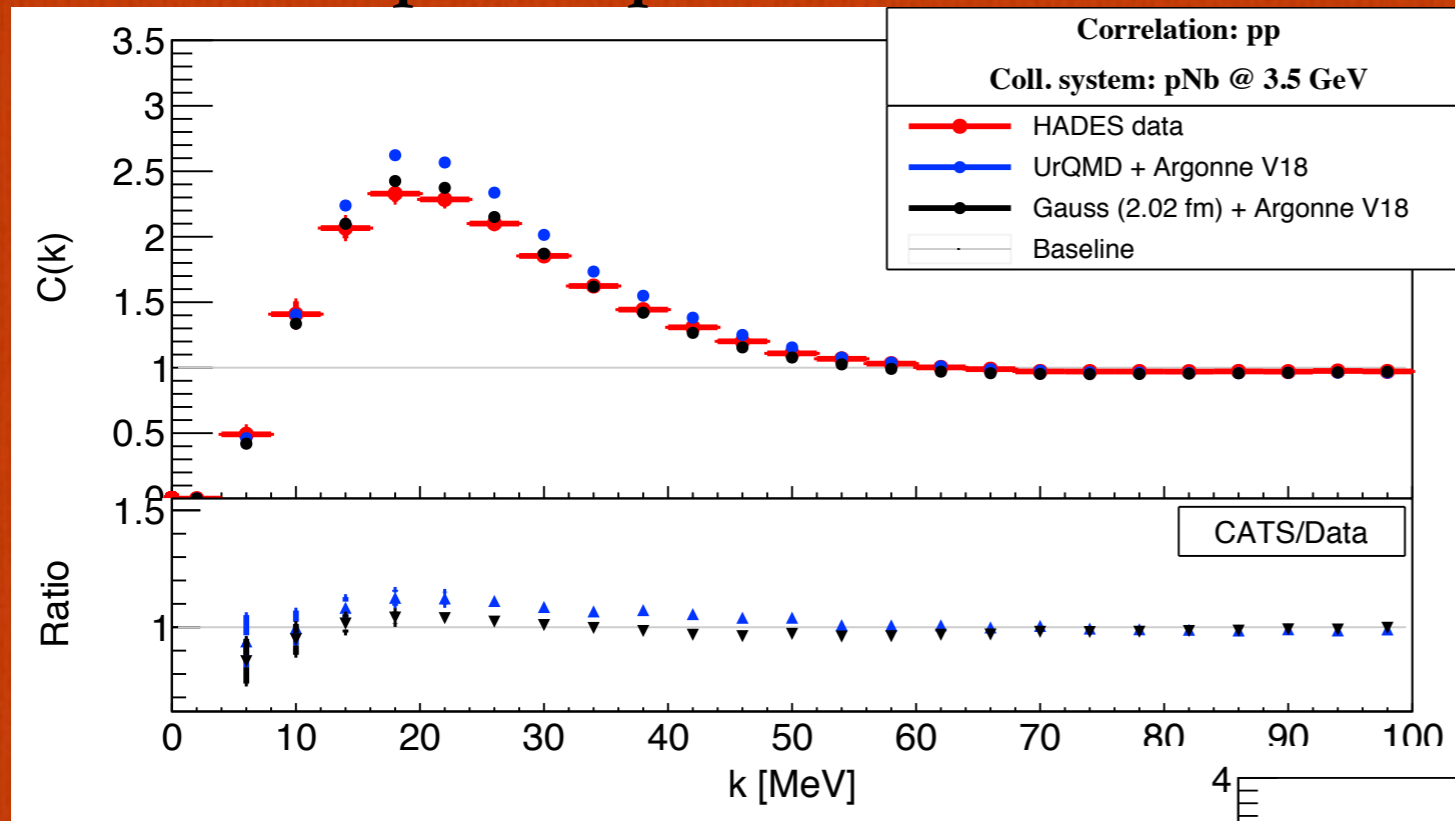


$\Lambda - \Lambda$ Correlation

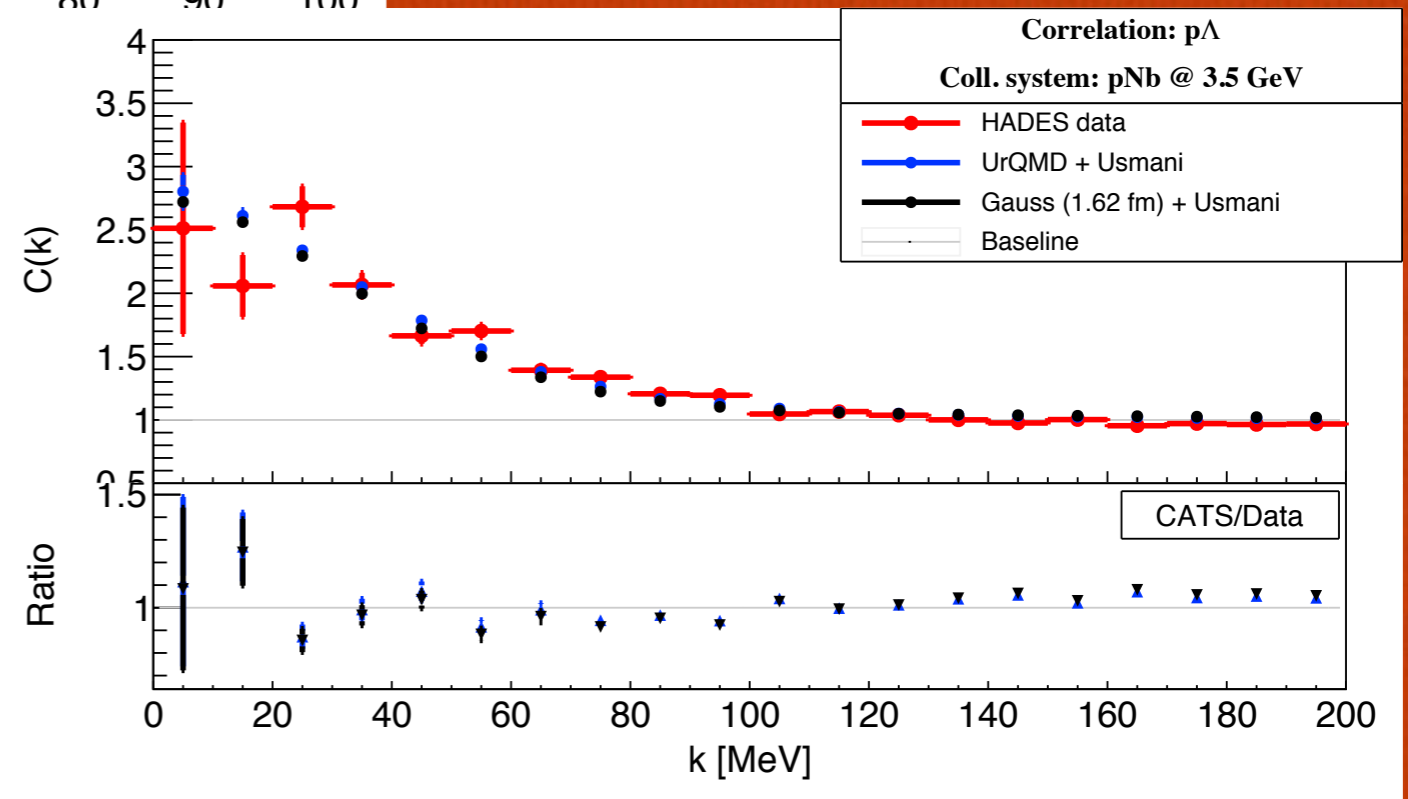
$$E_B = \frac{(\hbar c)^2 \kappa^2}{m_\Lambda}, \kappa = \frac{1}{d_0} \left(1 - \sqrt{1 - \frac{2d_0}{a}} \right)$$



proton-proton correlation



Λ -proton correlation



The agreement is more reasonable for UrQMD+ CATS

Summary and Outlook

- Hadron-Hadron interactions have to be understood in detail to compute a realistic EOS for neutron stars
- New tools to study Hyperon-Nucleon interaction: Femtoscopy in elementary reactions
- pp and Lambda-p correlations studied with the HADES and ALICE data.



The Group

<http://www.denseandstrange.ph.tum.de>

