Nuclear phenomenology at the intersection of nuclear structure and high-energy nuclear collisions

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January 11th 2023

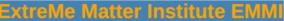






Nuclear and Quark Matter Seminar 2023

Intersection of nuclear structure and high-energy nuclear collisions: a new research direction.



EMMI Rapid Reaction Task Force

Nuclear Physics Confronts Relativistic Collisions of Isobars

Heidelberg University, Germany, May 30 – June 3 & October 12-14 2022

Organizers:

Giuliano Giacalone Jiangyong Jia Vittorio Somà You Zhou



Intersection of nuclear structure and high-energy nuclear collisions

Organizers:

Jiangyong Jia (Stony Brook & BNL)
Giuliano Giacalone (ITP Heidelberg)
Jacquelyn Noronha-Hostler (Urbana-Champaign)
Dean Lee (Michigan State & FRIB)
Matt Luzum (São Paulo)
Fugiang Wang (Purdue)

Jan 23rd - Feb 24th 2023



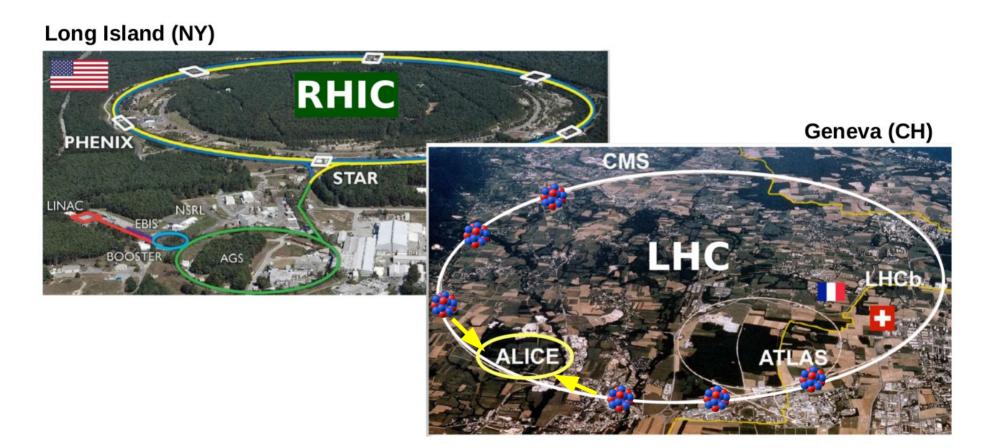
- Next Initial Stages conference (Copenhagen, 2023) will have a track related to nuclear structure.
- Input for Nuclear Physics LRP in the US, arXiv link
- Contributed input to NUPECC LRP 2024 [with Y. Zhou (NBI Copenhagen)]

OUTLINE

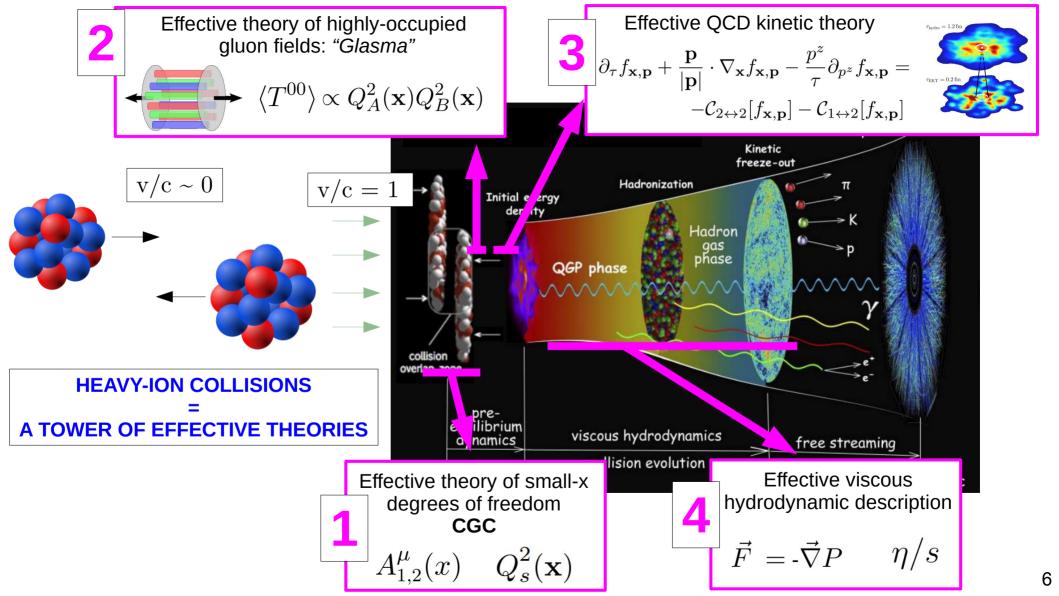
- 1 High-energy nuclear physics and anisotropic flow.
- 2 Nuclear structure input to high-energy nuclear collisions.
- 3 Nuclear shapes in high-energy nuclear experiments.
- 4 Prospects: theory and experiment.

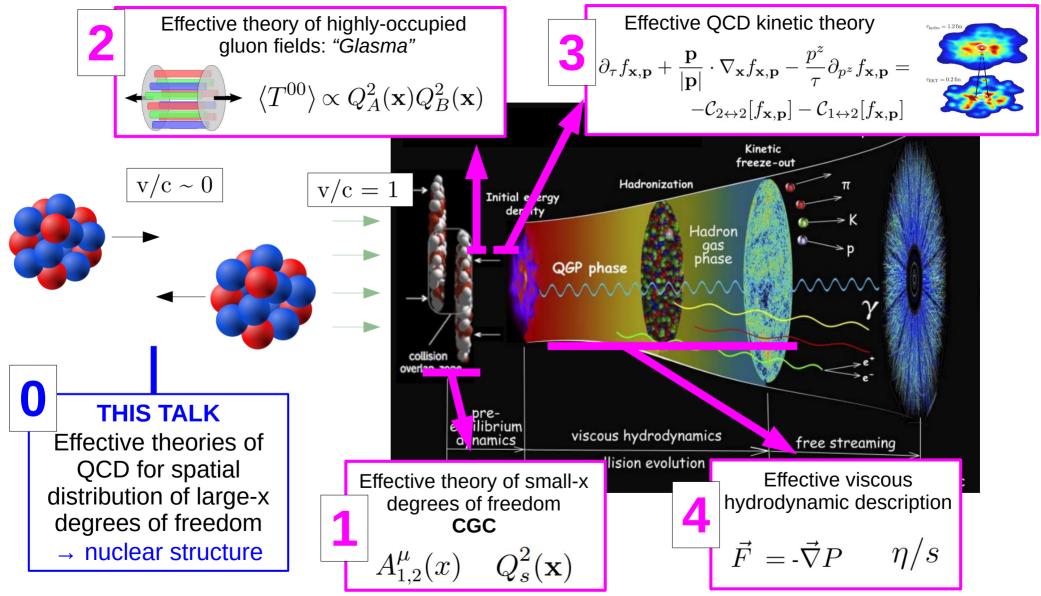
1 – High-energy nuclear physics and anisotropic flow.

HIGH ENERGY NUCLEAR PHYSICS

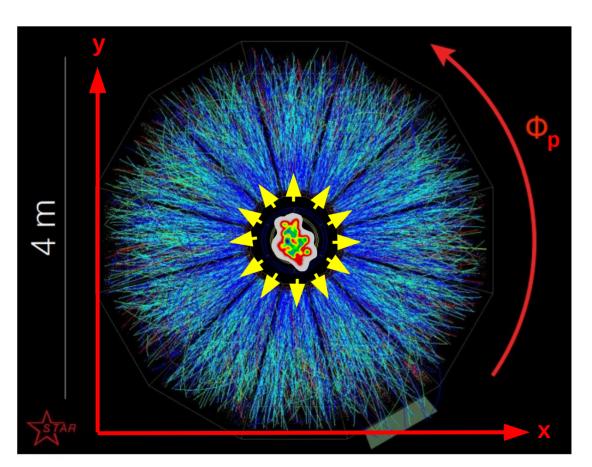


GOAL: studying emergent properties and phase diagram of strong-interaction matter.





How do we reconstruct the initial condition of the QGP?

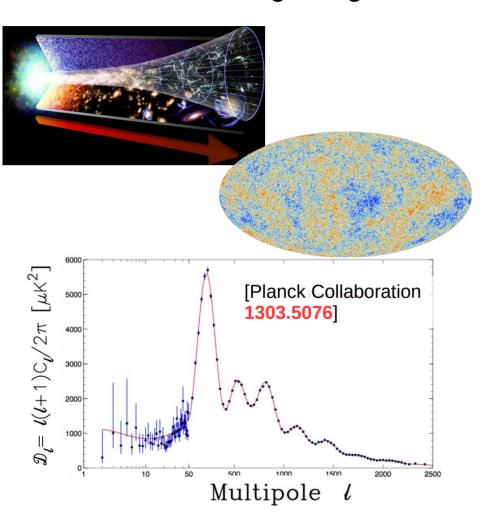


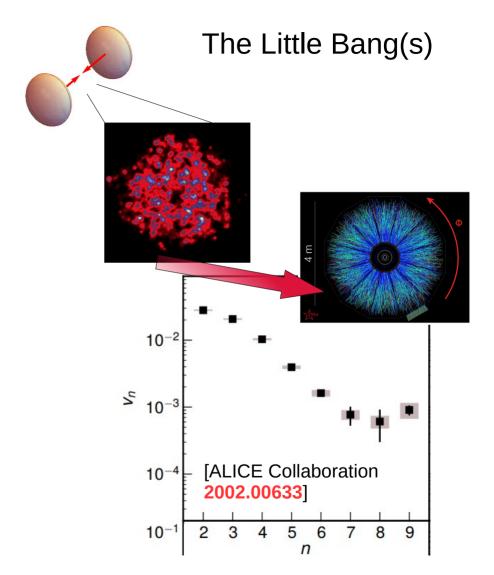
Hydrodynamics describes the motion of the bulk of the produced particles.

They sit at low momenta and follow the collective expansion of the system.

$$\frac{d^2N}{dp_{\rm T}d\phi} = \frac{dN}{2\pi dp_{\rm T}} \left(1 + 2\sum_{n=1}^{\infty} v_n \cos n(\phi - \Phi_n)\right)$$
 Explosiveness of the expansion Anisotropy of Azimuthal distribution

The Big Bang

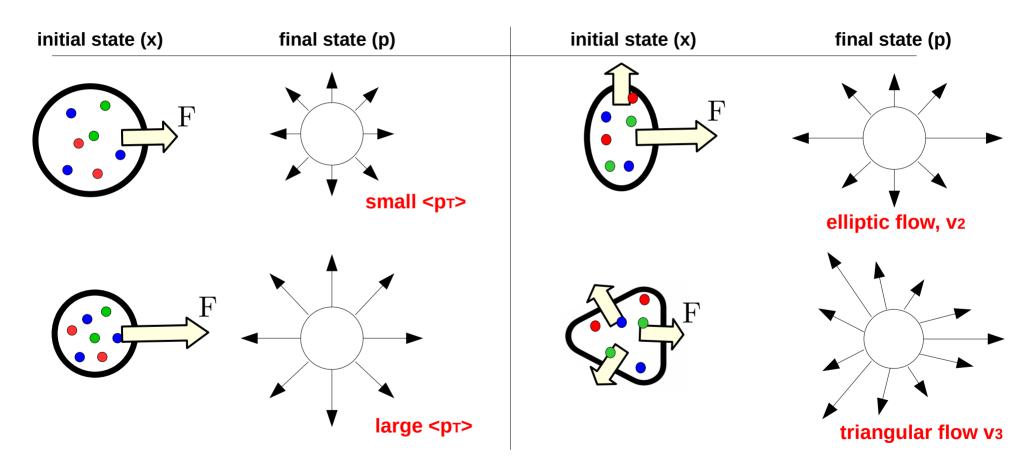




Mapping initial-state geometry to final-state observables via pressure-gradient force.

$$F = -\nabla P$$

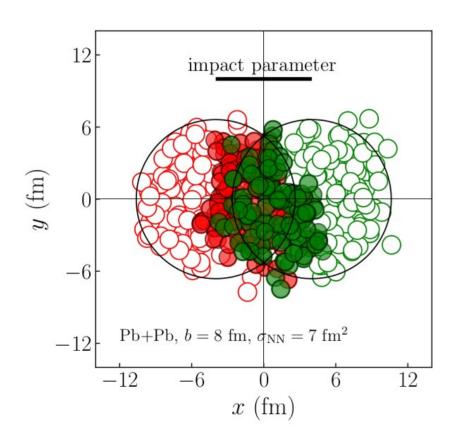
[Ollitrault, PRD 46 (1992) 229-245]



Shape and size of the QGP can be reconstructed from data!

2 – Nuclear structure input to high-energy nuclear collisions.

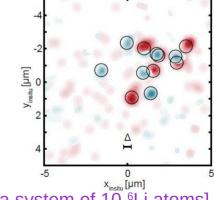
Formation of QGP starts with an input from nuclear structure.



High-energy model

Scattering occurs mainly within nucleons.

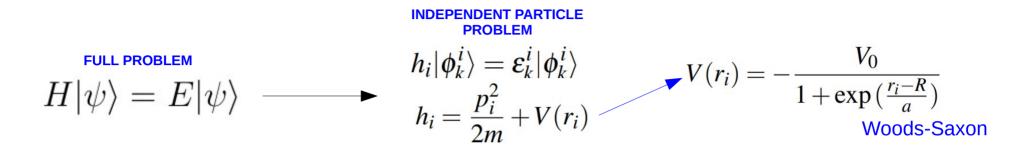
"quantum measurement" of the nucleon positions.



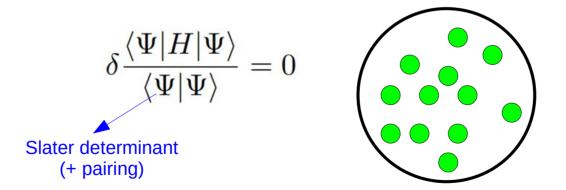
[from Sandra Brandstetter, $^{-5}$ $^{\circ}$ $^{\circ}$ $^{\circ}$ $^{\circ}$ Collapsed wave function of a system of 10 $^{\circ}$ Li atoms]

Origin of nucleon positions for "spherical" systems like ²⁰⁸Pb.

Effective description: independent sampling in common potential (mean field) is appropriate.



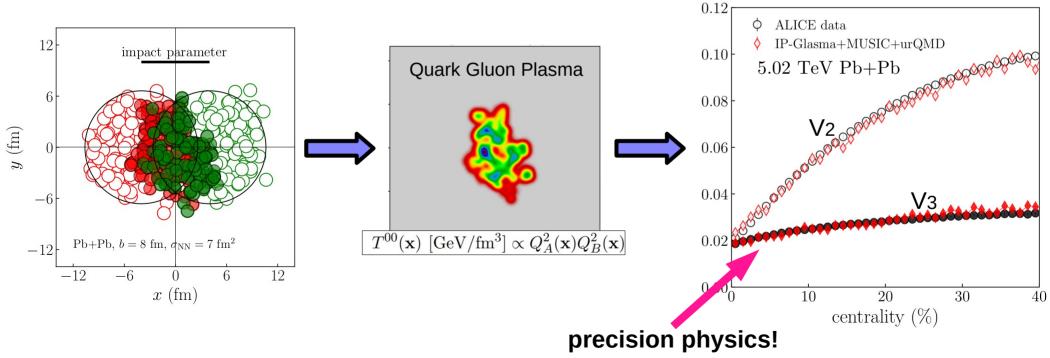
Ground state from variational equation with Ansatz of independent Fermions.



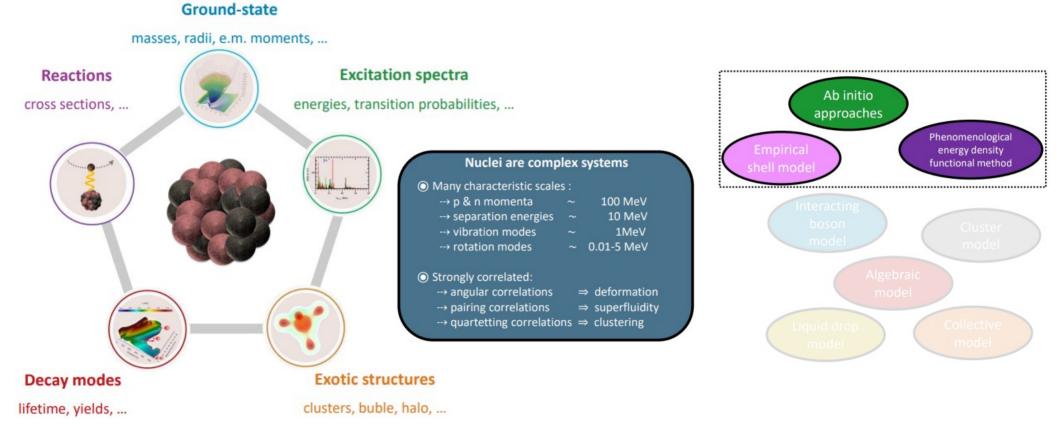
More realistic: Potential generated from effective nucleon-nucleon interaction (Gogny force, Skyrme force, etc.), in "Energy Density Functional" theory.

Mean-field-based approach works at high energy (justifies the MC Glauber approach).

Nucleus-nucleus interaction does not modify the shape of the interaction region on large scales.



Reminder: ²⁰⁸Pb is particular case of doubly-magic system. Atomic nuclei have rich phenomenology rooted in the strong nuclear force.

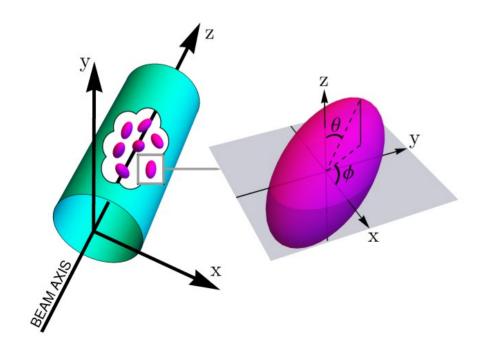


Describing heavy-ion collisions requires a priori knowledge of A-body correlation functions, e.g.,

$$\rho_k^{\rm JMNZ}(\vec{r}_1,\vec{r}_2,\vec{r}_3,\vec{r}_4) \equiv \langle \Psi_k^{\rm JMNZ} | c^\dagger(\vec{r}_1)c^\dagger(\vec{r}_2)c(\vec{r}_3)c(\vec{r}_4) | \Psi_k^{\rm JMNZ} \rangle \quad \text{2-body correlation function}$$

Help from low-energy nuclear physics:

Spatial correlations encapsulated in "intrinsic shapes". Instead of A-body correlation functions, use 1-body density with a deformed shape.



Keep a mean field approach.

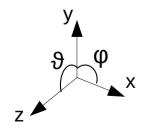
The bag of nucleons is now deformed and with a random orientation.

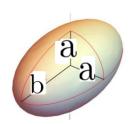
The interaction selects one such orientation.

Generalize the Woods-Saxon profile to include intrinsic deformations:

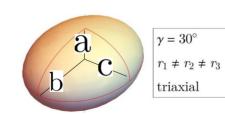
$$\rho(r,\Theta,\Phi) \propto \frac{1}{1+\exp\left(\left[r-R(\Theta,\Phi)\right]/a\right)} \ , \ R(\Theta,\Phi) = R_0 \bigg[1+\underline{\beta_2}\bigg(\cos\gamma Y_{20}(\Theta)+\sin\gamma Y_{22}(\Theta,\Phi)\bigg) +\underline{\beta_3}Y_{30}(\Theta) +\underline{\beta_4}Y_{40}(\Theta)\bigg]$$

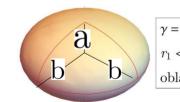
For $\beta_2 > 0$, the nucleus is prolate ($\gamma = 0$), triaxial ($\gamma = 30^0$), or oblate ($\gamma = 60^0$).











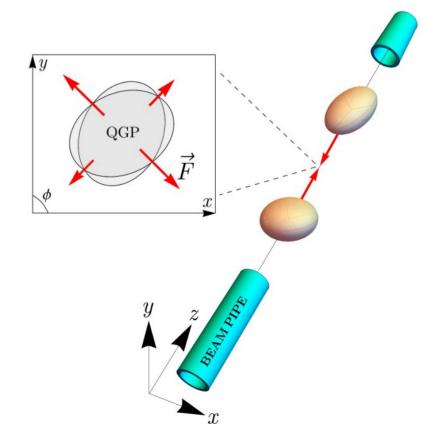


Intrinsic shapes are non-observable for direct measurements, but they leave their fingerprint on virtually all nuclear observables and phenomena

Michael Bender - RBRC Workshop Jan 2022

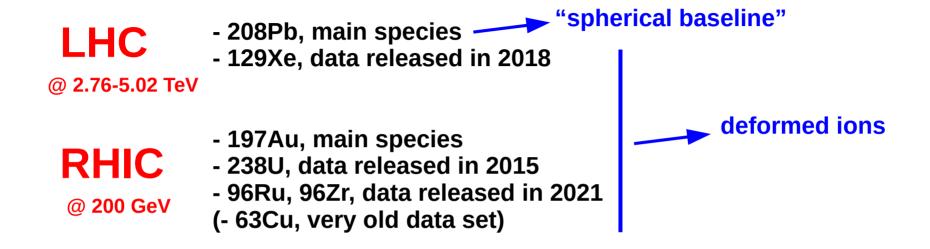
They will show up as well at high energy.





2 – Nuclear shapes in high-energy nuclear experiments.

Species that have been collided so far (excludes p-A, d-A, He-A):



New questions to address:

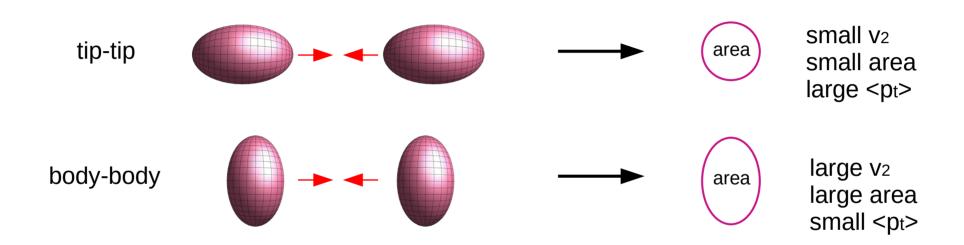
Testing high-energy model via crosscheck of nuclear deformation effects.

Are low-energy expectations compatible with high-energy observations?

HOW TO DO THAT? SHAPE-SIZE CORRELATION.

A new "classical phenomenon".

[Giacalone, PRL **124** (2020) 20, 202301 PRC **102** (2020) 2, 024901]



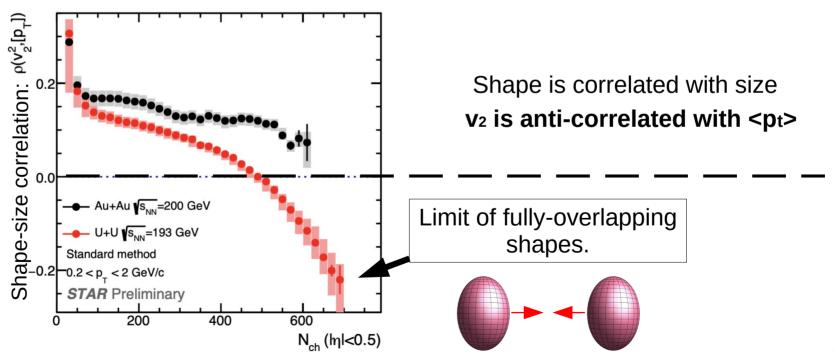
CENTRAL COLLISIONS OF (PROLATE) DEFORMED IONS

The ellipticity of the quark-gluon plasma is positively correlated with its area.

Deformation yields a negative correlation between v_2 and the $< p_t >$.

Signature of the strong prolate deformation of uranium-238.

$$R(\Theta, \Phi) = R_0 \left[1 + \beta_2 \left(\cos \gamma Y_{20}(\Theta) + \sin \gamma Y_{22}(\Theta, \Phi) \right) + \beta_3 Y_{30}(\Theta) + \beta_4 Y_{40}(\Theta) \right]$$



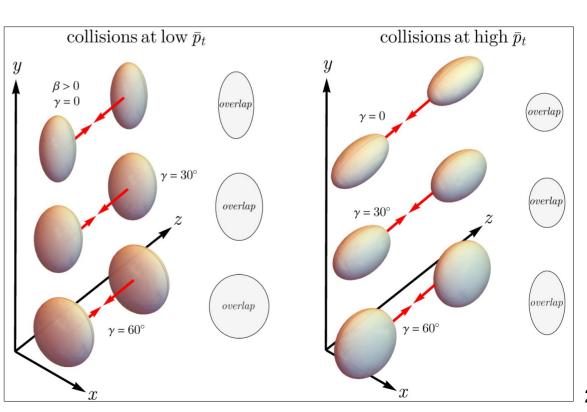
Signature of the triaxial deformation of xenon-129.

$$R(\Theta, \Phi) = R_0 \left[1 + \underline{\beta_2} \left(\cos \gamma Y_{20}(\Theta) + \sin \gamma Y_{22}(\Theta, \Phi) \right) + \underline{\beta_3} Y_{30}(\Theta) + \beta_4 Y_{40}(\Theta) \right]$$

Shape-size correlation is sensitive to the triaxiality, γ .

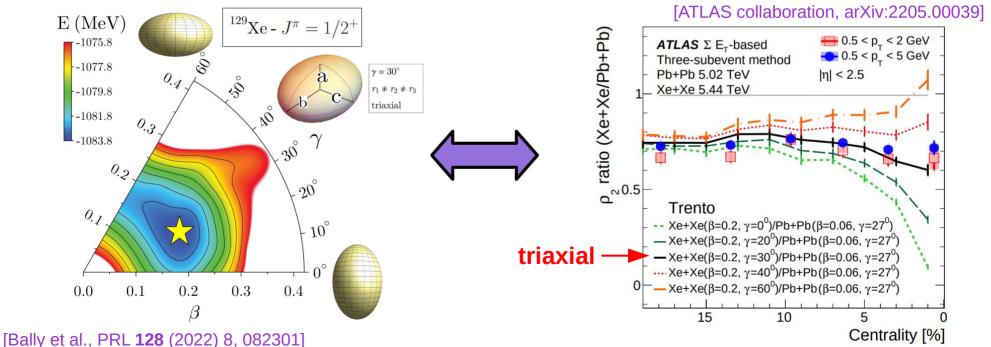
$$ho_2^{} \propto -\cos(3\gamma) eta_2^3$$

[see e.g. Jia, PRC 105 (2022) 4, 044905]

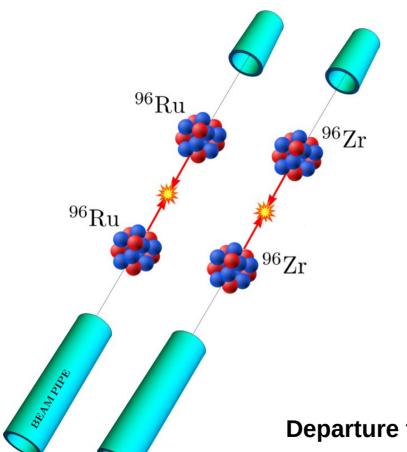


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Breakthrough of 2021: data from "isobar collisions" is released.



X and Y are isobars.

X+X collisions produce QGP with same properties as Y+Y collisions.

Ratios of observables (O) should be unity...

$$\frac{\mathcal{O}_{X+X}}{\mathcal{O}_{Y+Y}} \stackrel{?}{=} 1$$

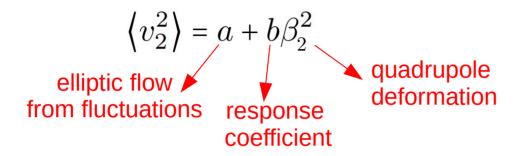
[STAR collaboration, PRC **105** (2022) 1, 014901] [Giacalone, Jia, Somà, PRC **104** (2021) 4, L041903]

Departure from unity is mainly due to nuclear structure.

Extremely precise measurements.

Signature of the quadrupole deformation of ruthenium-96.

In full generality, for quadrupole-deformed nuclei, at fixed multiplicity one has:



[Giacalone, PRC **99** (2019) 2, 024910] [Giacalone, Jia, Somà, PRC **104** (2021) 4, L041903] [Giacalone, Jia, Zhang, PRL **127** (2021) 24, 242301] [Jia, PRC **105** (2022) 1, 014905]

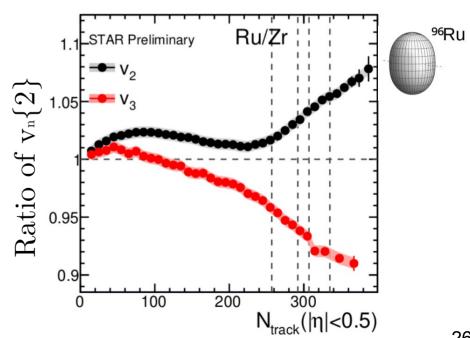
Isobar ratio and expand around the fluctuations:

$$\frac{\langle v_2^2\rangle_{\rm Ru+Ru}}{\langle v_2^2\rangle_{\rm Zr+Zr}} = 1 + c\left(\beta_{2,\rm Ru}^2 - \beta_{2,\rm Zr}^2\right)$$
 positive coeff

Low-energy nuclear physics tells us:

$$\beta_{2,Ru}^2 \gg \beta_{2,Zr}^2$$

Ratio should be above unity.



Signature of the octupole deformation of zirconium-96.

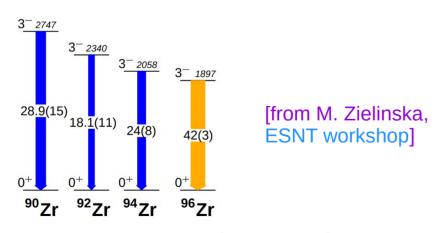
Same logic follows for octupole-deformed nuclei:

$$\frac{\langle v_3^2 \rangle_{\mathrm{Ru+Ru}}}{\langle v_3^2 \rangle_{\mathrm{Zr+Zr}}} = 1 + c \left(\beta_{3,\mathrm{Ru}}^2 - \beta_{3,\mathrm{Zr}}^2 \right) \qquad \text{[Jia, Zl]}$$

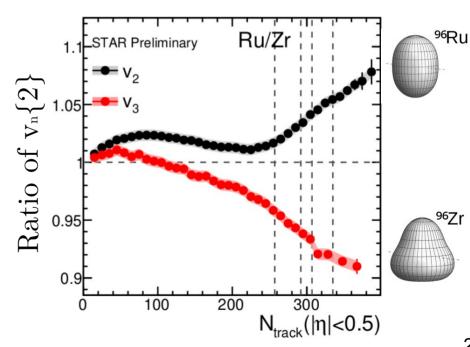
[Jia, Zhang, PRL **128** (2022) 2, 022301]

Significant octupole deformation from low-lying first 3⁻ state in ⁹⁶Zr.

No experimental information about ⁹⁶Ru.



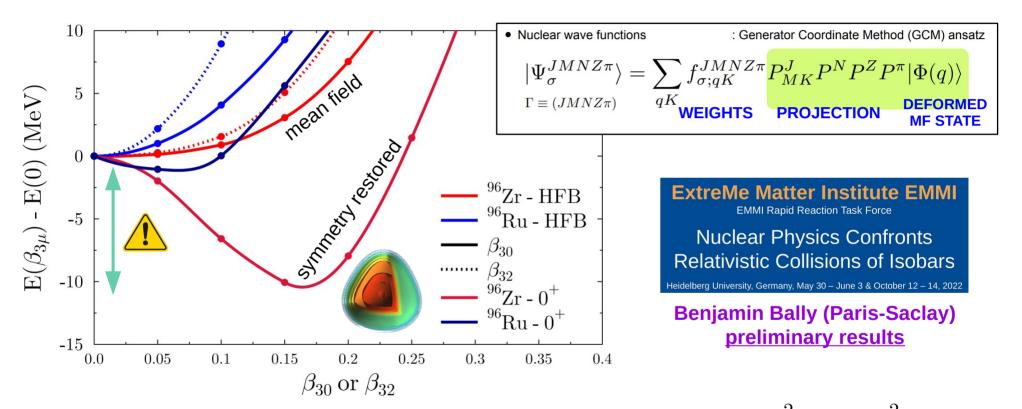
RHIC data implies $\beta_{3,\mathrm{Zr}}^2 \gg \beta_{3,\mathrm{Ru}}^2$



Explanation from nuclear structure theory?

Octupole deformation is a "beyond-mean-field" effect. Emerges from symmetry restoration.

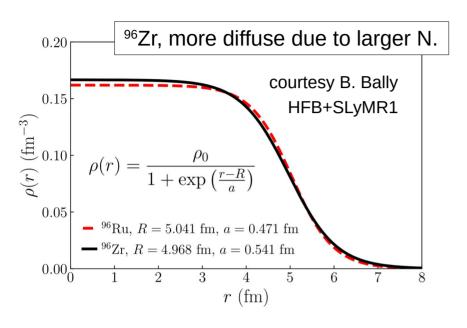
[Robledo, J.Phys.G 42 (2015) 5, 055109]



Preliminary work confirms large octupole deformation in zirconium. $eta_{3,{
m Zr}}^2\ggeta_{3,{
m Ru}}^2$

Large energy gain from symmetry restoration. New challenges in nuclear structure theory.

BONUS: Signature of skin thickness in (ratio of) fourth-order cumulant of v₂.

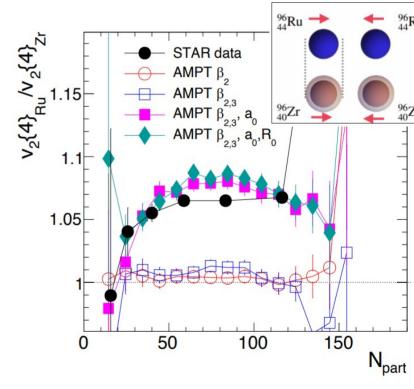


Gaussian model of $V_2=(v_x,v_y)$ fluctuations. Reaction plane is along x:

$$p(v_{2x}, v_{2y}) = \frac{1}{\pi \delta^2} \exp \left[-\frac{(v_{2x} - v_2^{\text{rp}})^2 + v_{2y}^2}{\delta^2} \right]$$
$$v_2\{4\} = v_2\{6\} = \dots = v_2\{\infty\} = v_2^{\text{rp}}$$

 $v_2(\infty) = v_2$ probes the skin

[Voloshin *et al.*, PLB **659** (2008) 537-541] [Jia, Giacalone, Zhang, arXiv:2206.10449]



see also [Nijs, van der Schee, arXiv:2112.13771] [Xu et al., arXiv:2111.14812] [Xu et al., PLB **819**, 136453 (2021)]

Answers to the initial questions:

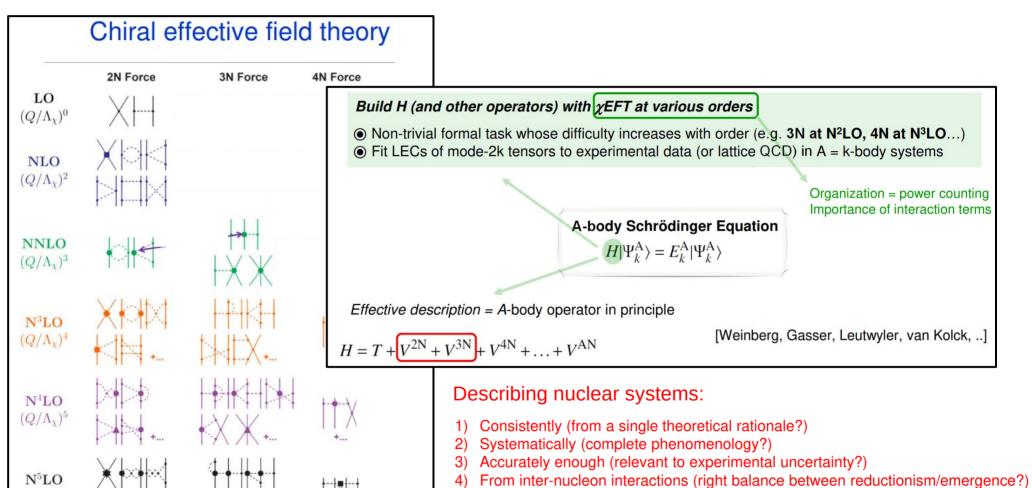
• Expectations from low-energy nuclear physics confirmed in high-energy data.

• Quadrupole, triaxiality, octupole (?), hexadecapole, radial profile differences between isobars.

- Great confidence that high-energy model is appropriate.
- No clear indication of modifications of nuclear geometry from enhanced gluon fluctuations (Lorentz boost).

3 – Prospects: theory and experiment

Going beyond shapes: connection with ab initio approaches.



 $(Q/\Lambda_{\chi})^6$

[from Thomas Duguet, ESNT workshop]

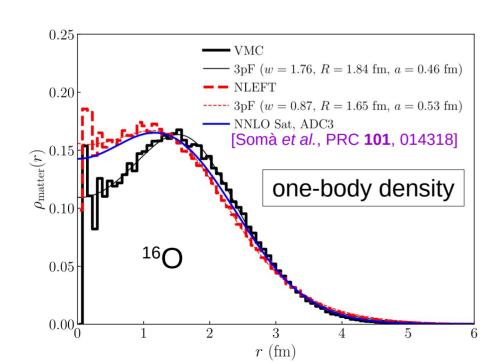
Rooted in QCD (sound connection to underlying EFT?)

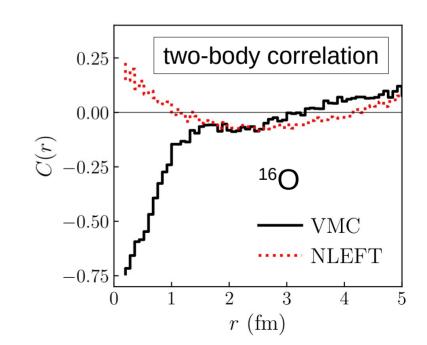
Going beyond shapes: connection with *ab initio* approaches.

Oxygen-oxygen collisions are ideal for the purpose.

- 6000 configurations from **cluster Variational Monte Carlo (VMC)** simulations. Interaction: AV18+UIX (not an EFT) with a repulsive core. [Lonardoni et al., PRC **96** (2017) 2, 024326]
- 15359 configurations from **Nuclear Lattice Effective Field Theory (NLEFT)**. Interaction: pionless chiral EFT. Pin-hole algorithm to determine nucleon positions.

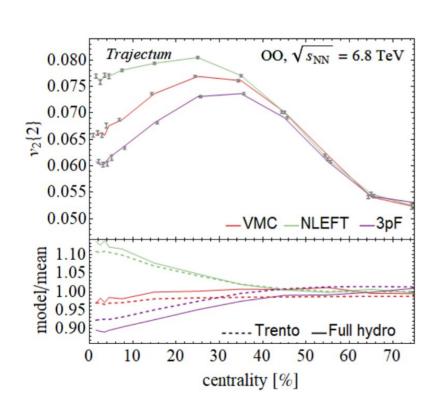
[Summerfield et al., PRC **104** (2021) 4, L041901]



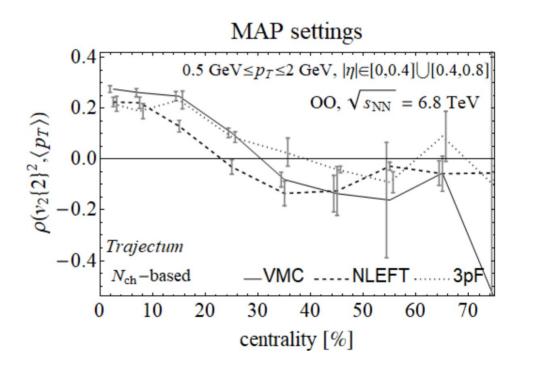


Study of shape-size correlations in oxygen collisions.

Different predictions from different frameworks... why? Different interaction or many-body solution? Role of short-range physics?

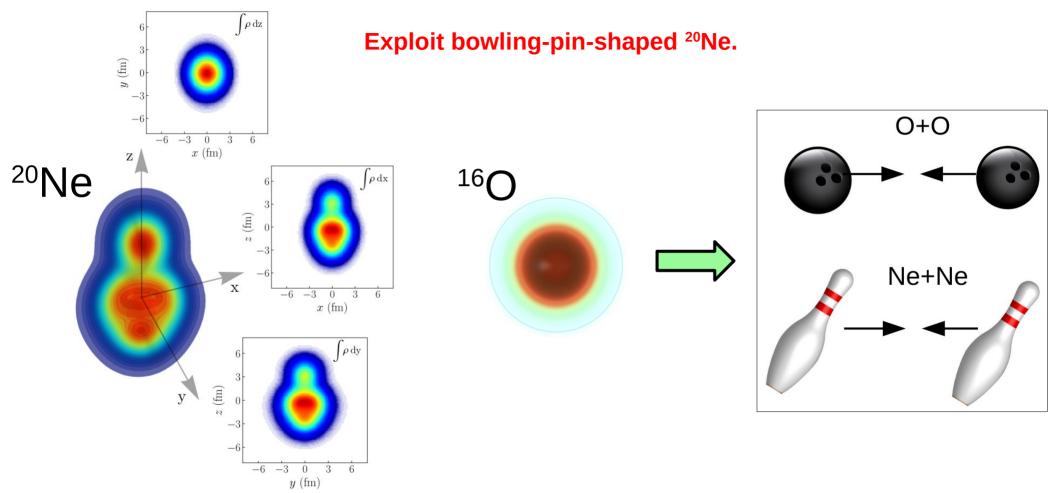


[Giacalone, Lee, Nijs, van der Schee, in preparation]



A new tool to test effective theories of QCD for nuclei.

Transparent evidence of a "geometric" origin of flow in a small system?



[Oxygen structure: VMC, Lonardoni *et al.*, PRC **96** (2017) 2, 024326] [Neon structure: variational calculation + XEFT, Frosini *et al.*, EPJA **58** (2022) 4, 63]

Bands are systematical uncertainties, large variations in parameter space (η /s, ζ /s, ICs, ...)

Large 20% effect on rms v₂.

Systematical uncertainty on ratio at % level!

("isobar criterion")

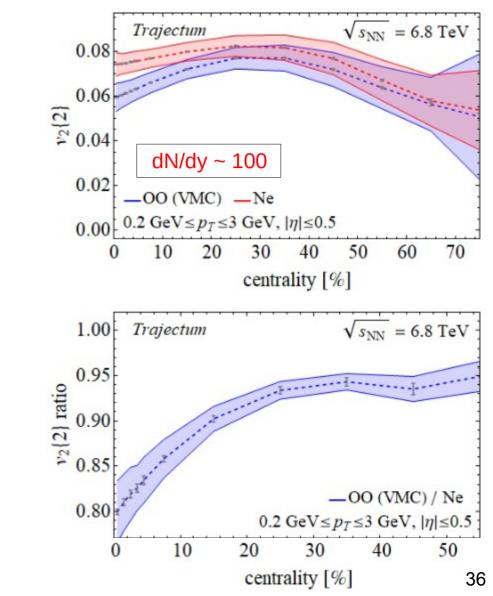


Unambiguous "geometric" interpretation.

OUR POINT

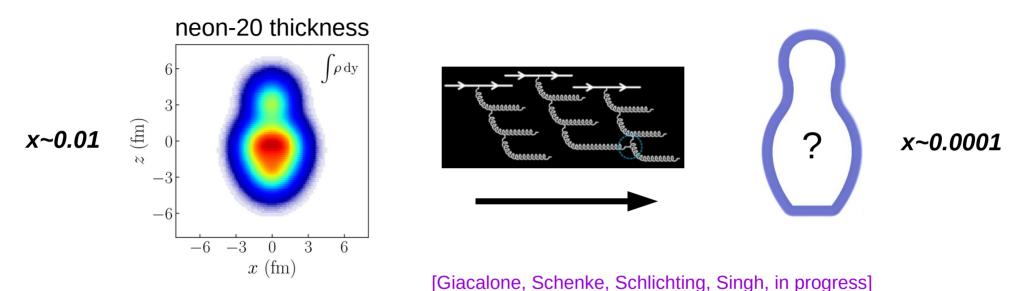
Brings more robust information than: p+Au vs. d+Au central O+O vs. peripheral Pb+Pb

[Trajectum (G Nijs, W van der Schee) + ab initio PGCM (Saclay + TU Darmstadt) + G Giacalone, to appear]



Case study: Impact of neon-neon collisions on small system program at LHC?

Role of small-x evolution?



- 1 ²⁰Ne in SMOG system of LHCb. Collider + fixed-target at the same time. Collisions at sqrt(s)=7000 GeV and sqrt(s)=70 GeV.
- **2** FOCAL upgrade of ALICE. "Dilute-dense" Ne+Ne, one small-x, one large-x.

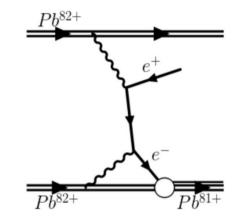
Role of quarks and gluons (QCD) for nuclear structure?

LHC – Run5 and Run6 (beyond 2032)

Possibility of collisions of additional species @ LHC Run 5 and Run 6?

Maximizing impact for both low- and high-energy communities?

Collide them in pairs (isobar strategy)?



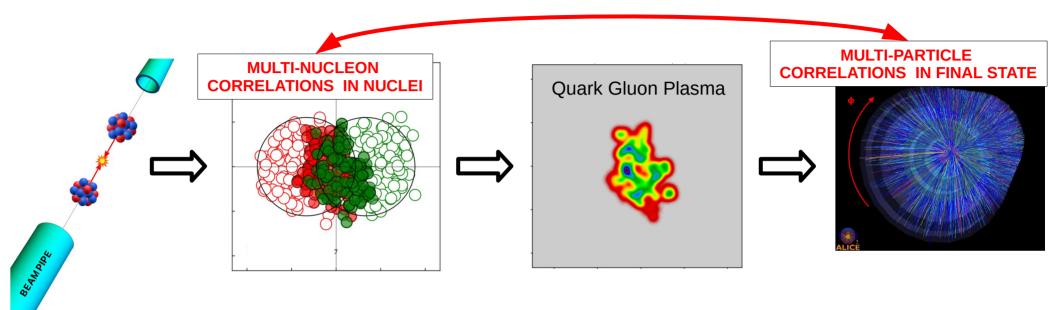
[from Alexander Kalweit, ESNT workshop]

[https://indico.cern.ch/event/1078695/]

Nucleon-nucleon
luminosity:
$\mathcal{L}_{\text{NN}} = A^2 \cdot \mathcal{L}_{AA}$

optimistic scenario	0-0	Ar-Ar	Ca-Ca	Kr-Kr	In-In	Xe-Xe	Pb-Pb
(LAA) (cm ⁻² s ⁻¹)	9.5·10 ²⁹	2.0·10 ²⁹	1.9·10 ²⁹	5.0.1028	2.3.1028	1.6·10 ²⁸	3.3.1027
(Lnn) (cm ⁻² s ⁻¹)	2.4·10 ³²	3.3.1032	3.0.1032	3.0.1032	3.0.1032	2.6.1032	1.4.1032
LAA (nb-1 / month)	1.6·10 ³	3.4·10 ²	3.1.102	8.4·10¹	3.9·10 ¹	2.6·10 ¹	5.6.100
LNN (pb-1 / month)	409	550	500	510	512	434	242

SUMMARY



- High-energy model coupled with mean-field description of nuclei provides excellent description of heavy-ion data.
- Collective spatial correlations (shapes) in nuclei show up clearly at high energy.
- Prospect theory: improved initial conditions and synergy with *ab-initio* nuclear theory.
- Prospect experiments: many opportunities to be discussed/investigated.

THANK YOU!

Intersection of nuclear structure and high-energy nuclear collisions

https://www.int.washington.edu/programs-and-workshops/23-1a

Jan 23rd - Feb 24th 2023



Organizers:

Jiangyong Jia (Stony Brook & BNL)
Giuliano Giacalone (ITP Heidelberg)
Jaki Noronha-Hostler (Urbana-Champaign)
Dean Lee (Michigan State & FRIB)
Matt Luzum (São Paulo)
Fuqiang Wang (Purdue)

BONUS: Neutron skin estimates from high-energy collisions? Two methods.

Difference in diffuseness gives access to neutron skin difference. Use isobars.

²⁰⁸Pb, ⁴⁸Ca ... can high-energy nuclear physics contribute to these efforts?

[Jia & Zhang, arXiv:2111.15559]

Nice results from STAR in an individual system: $\Delta r_{np}[{}^{197}\text{Au}{}] = 0.17 \pm 0.03 \; (\text{stat.}) \pm 0.08 \; (\text{syst.}) \; \text{fm}$ Consistent with low-energy nuclear theory.

[STAR Collaboration, arXiv:2204.01625]

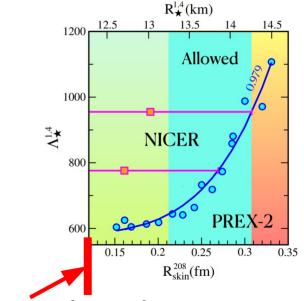
Recent measurements for ²⁰⁸Pb from weak form factor:

$$\Delta r_{np} = 0.283 \pm 0.071 \text{ fm}$$

$$L = (106 \pm 37) \text{ MeV}$$

Stiffer EoS than expected.

[PREX-II experiment, PRL **126** (2021) 17, 172502]



From NS merger observations.

[Reed et al., PRL **126** (2021) 17, 172503] [Fattoyev et al., PRL **120** (2018) 17, 172702]