



Benchmarking of Trapping particles induced by space charge and nonlinear resonances

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HB2006, 1st June 2006, Tsukuba

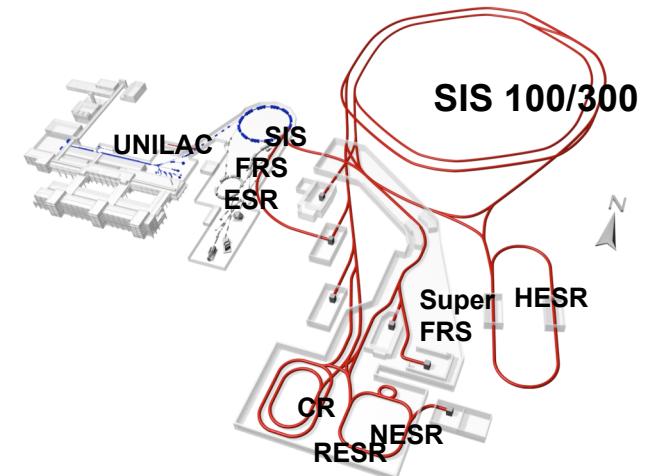
Motivation

The aim of the code benchmarking is to confirm the space charge induced trapping of particles in a bunch during long term storage. Numerical investigation and experiments at the CERN-PS have been performed in 2002-2003 but

no other code has been used to confirm the mechanism

and to reproduce the measurements.

In SIS100 of FAIR project long term beam loss prediction are mandatory



Participants

Person	CODE	Laboratory
G.Franchetti	MICROMAP	GSI
S. Machida	SIMPSONS	RAL

The benchmarking effort is open to other participants.

The actual results and all the steps of the benchmarking
are available on the web in

http://www-linux.gsi.de/~giuliano/research_activity/trapping_benchmarking/main.html

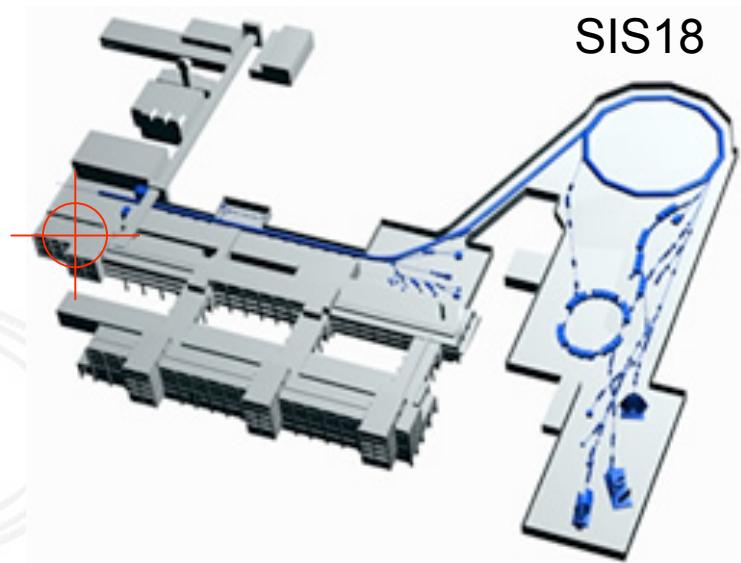
http://www-linux.gsi.de/~giuliano/research_activity/trapping_benchmarking/main.html

Framework of Benchmarking

The benchmarking framework has the parameters of SIS18

Experiment S317

- 4 Measurement campaign starting from December 2006.
- 24 shifts of beam



Controlled highly resolved measurement data will be available for benchmarking codes, on emittance growth and beam loss perdition

S317 Experiment @ GSI

Experimental studies of high-intensity effects and beam loss issues in the FAIR synchrotrons.

O. Boine-Frankenheim, P. Forck, G. Franchetti, B. Franczak,
T. Giacomini, I. Hofmann, M. Kirk, V. Kornilov, S.Y. Lee¹, A. Parfenova, P. Spiller

GSI Darmstadt, 64291 Darmstadt, Germany

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H. Hotchi², A. Molodojentsev³, M. Tomizawa³, S. Igarashi³, M. Ikegami³

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S. Machida

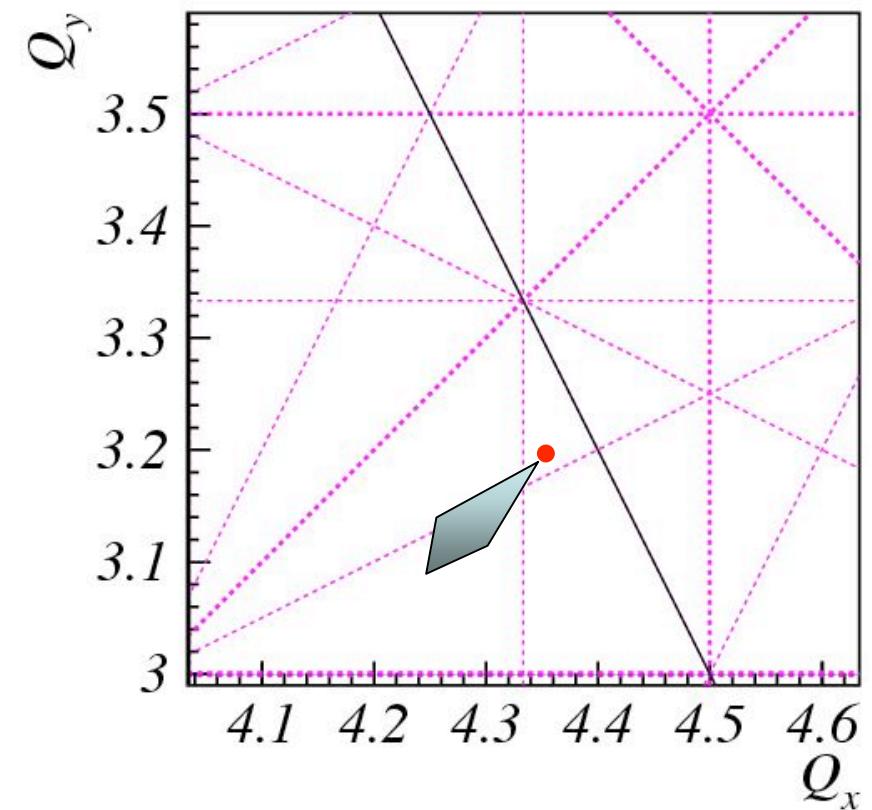
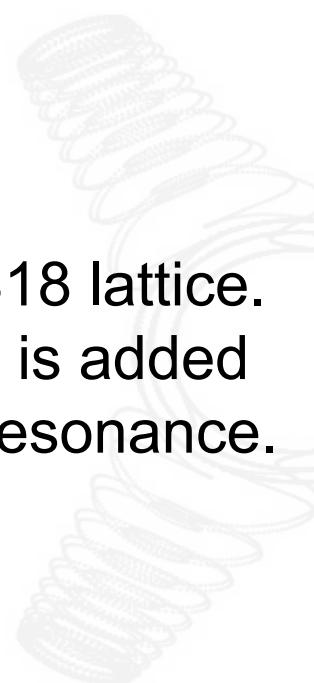
Rutherford Appleton Laboratory, Chilton, Didcot, Oxon, UK

S317 scheduling

http://www-linux.gsi.de/~giuliano/research_activity/trapping_benchmarking/main.html

Benchmarking conditions

We use the linear SIS18 lattice.
An external sextupole is added
to excite a 3rd order resonance.



Parameters (for benchmarking purpose)

PARAMETERS for sets 1-6

Lattice SIS18

Strength of the sextupole (when used) $K_2 = 0.2 \text{ m}^{-2}$

Maximum tuneshift $\Delta Q_x = 0.1$

Horizontal transverse size (rms) $X_{\text{rms}} = 5 \text{ mm}$

Vertical transverse size (rms) $Y_{\text{rms}} = 5 \text{ mm}$

Longitudinal size (rms) $Z_{\text{rms}} = 40.35 \text{ m}$

Horizontal emittance (2σ) $\epsilon_x = 12.57 \text{ mm mrad}$

Vertical emittance (2σ) $\epsilon_y = 9.30 \text{ mm mrad}$

Turns for 1 synchrotron oscillation $N_{\text{synch}} = 15000$

Bunch length ($4 \sigma_z$) $\tau = 3472.7 \text{ ns}$

Kinetic energy $E_k = 11.4 \text{ MeV/u}$

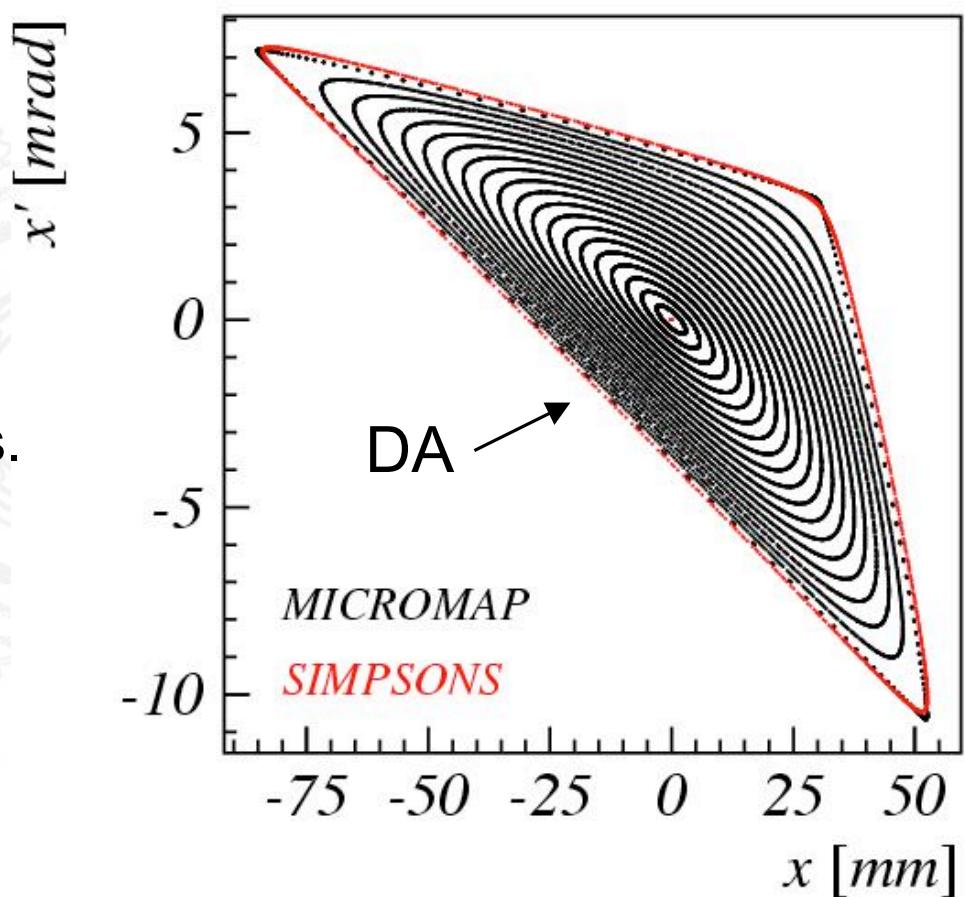
Gamma transition $\gamma_t = 5$

momentum spread at $3\sigma_z$ $\Delta p/p = 2.5 \times 10^{-4}$

Step 1: Phase Space topology

control that phase space near the 3rd order resonance has the same topology for all codes.

$Q_x = 4.338$, $Q_y = 3.2$,



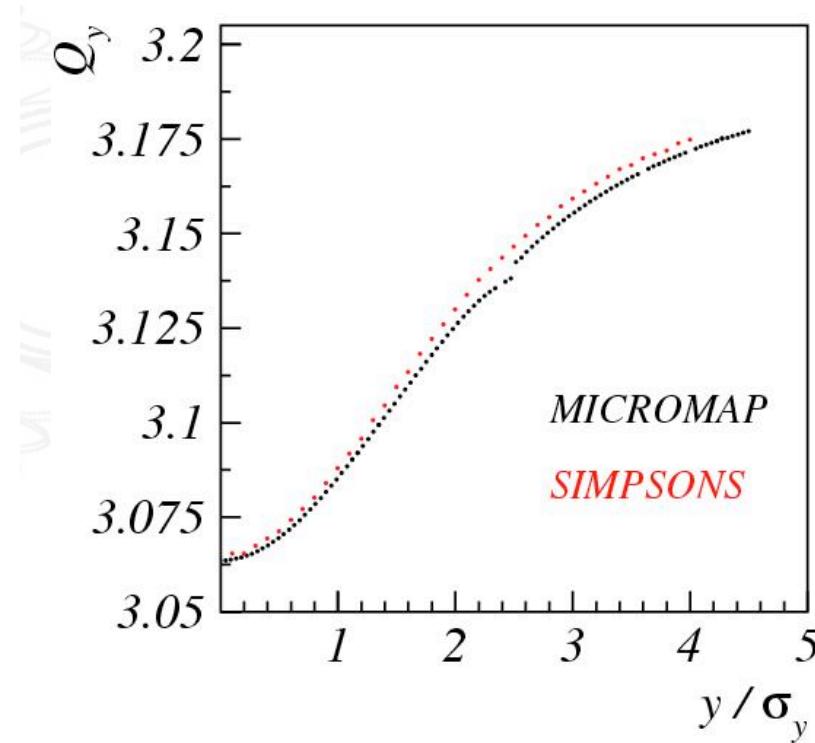
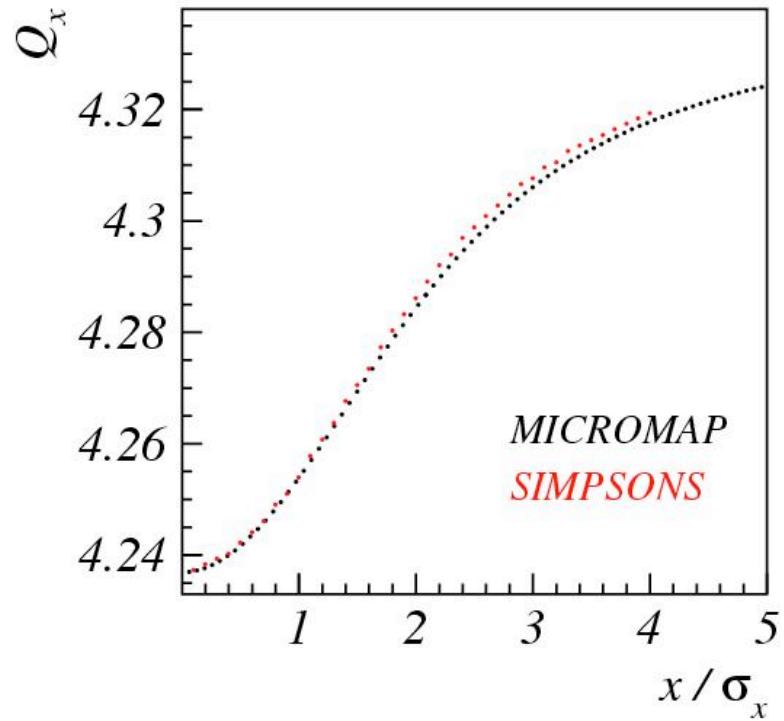
Step 2: Detuning + sextupole off

Sextupole off: the detuning is caused by space charge only

The tunes are computed at $z = 0$, and the synch. motion has been kept frozen.

$$Q_{x0} = 4.338$$

$$Q_{y0} = 3.2$$



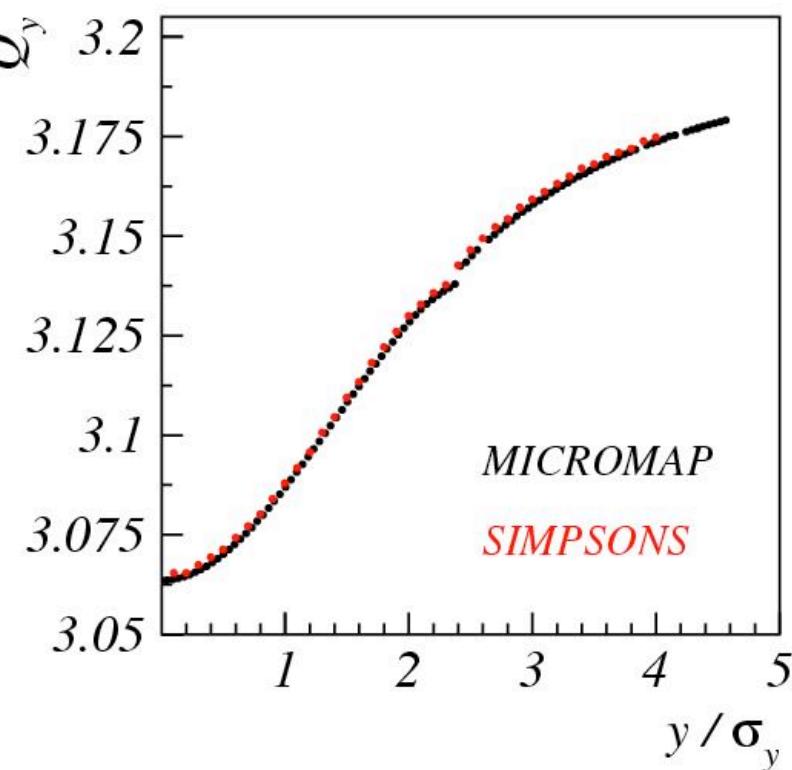
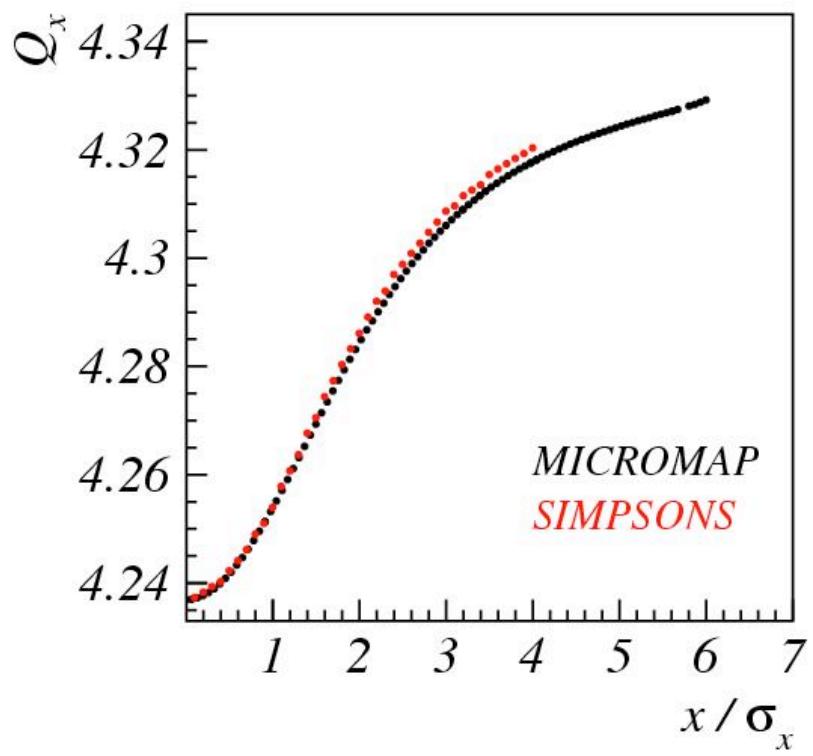
Step 3: Detuning + sextupole on

Sextupole on: nothing happen because the island are too far

$$Q_{x0} = 4.338$$

Synch. Frozen
 $Z = 0$

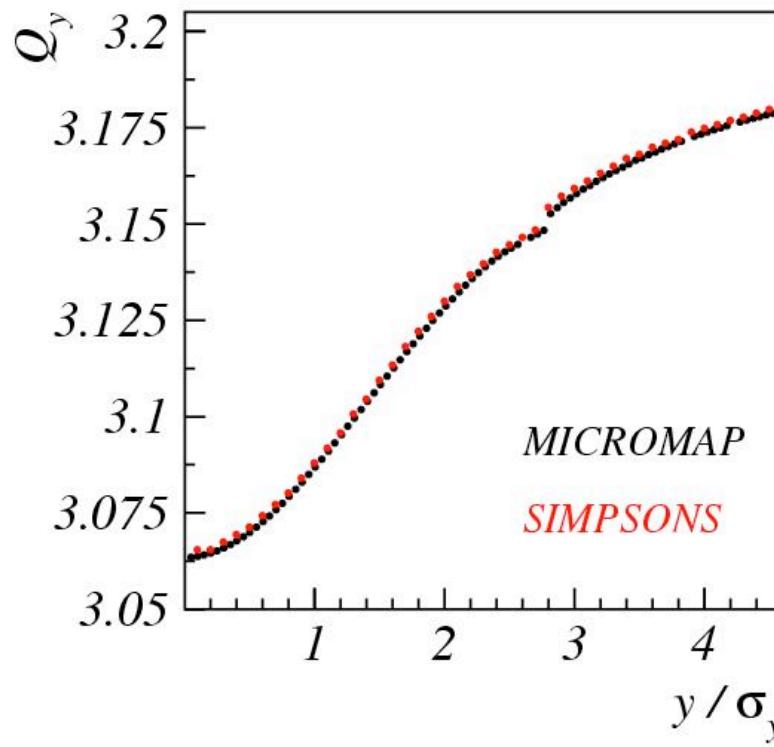
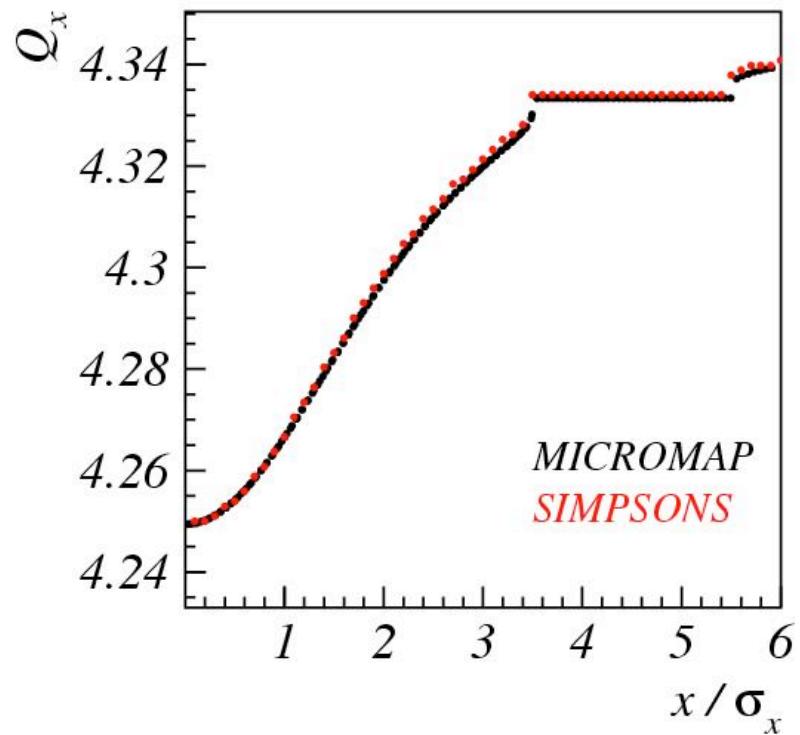
$$Q_{y0} = 3.2$$



Step 4: Near the 3rd order resonance

Taking a tune farer from the resonance
we see the 3rd order island

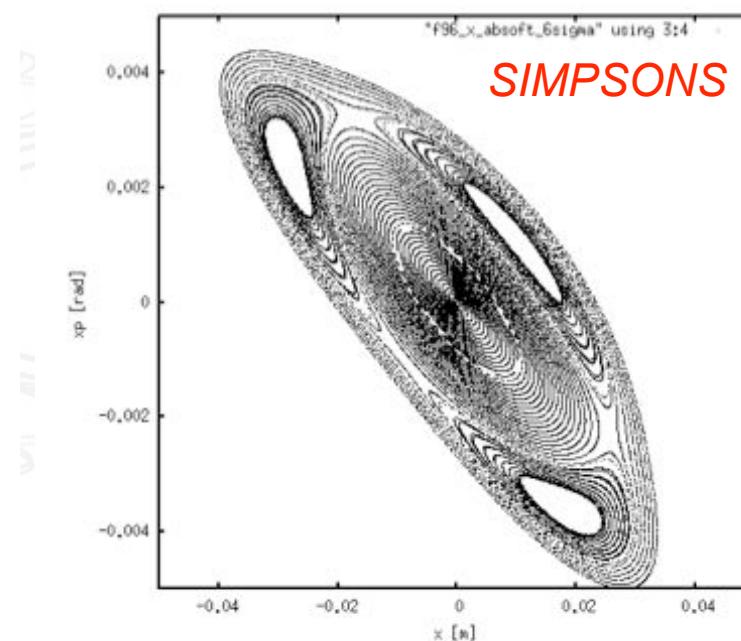
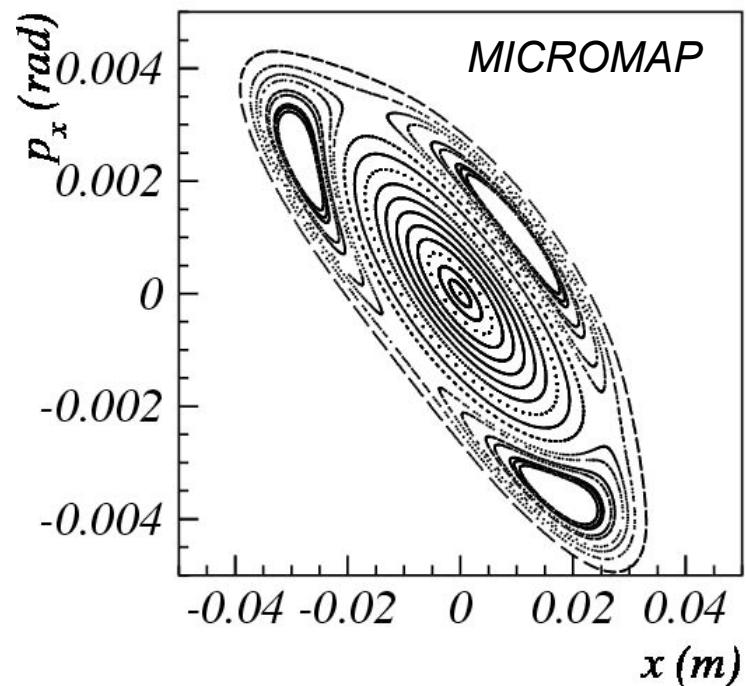
$$Q_x = 4.3504$$
$$Q_y = 3.2$$



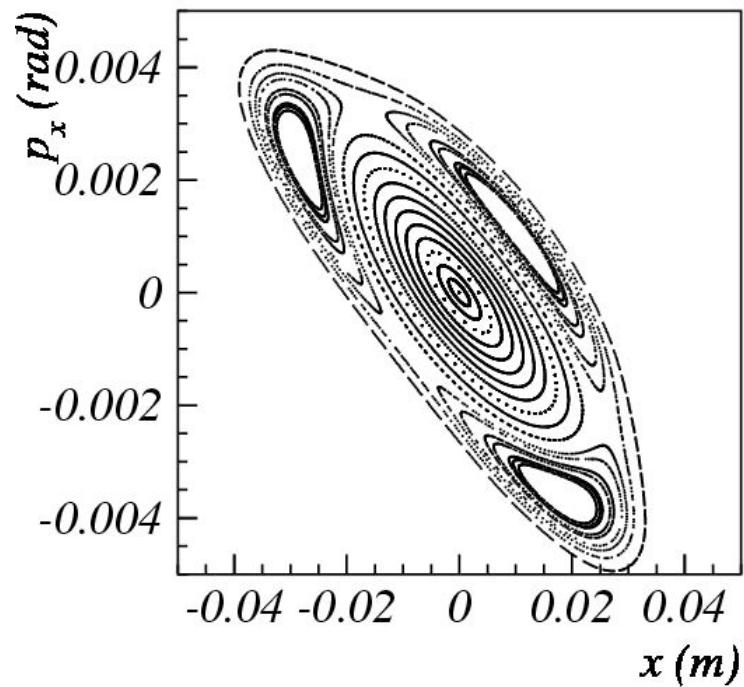


Step 5: phase space + SC

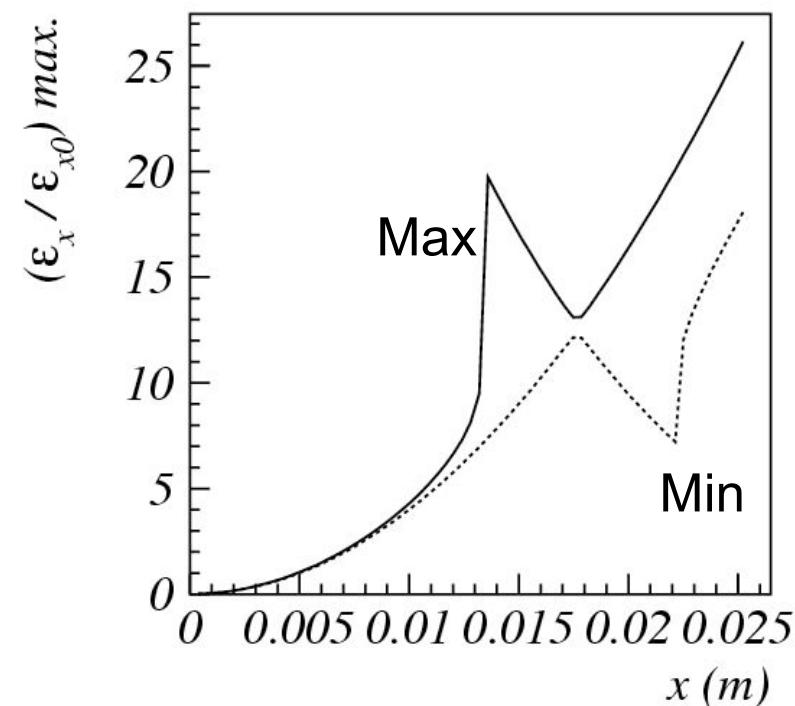
Phase space at $z = 0$, with frozen synch. motion
 $Q_x = 4.3504$ $Q_y = 3.2$



Step 5: single particle invariant vs. orbit



Max and Min value
Of single particle invariant



Step 6: Trapping for $N_{\text{synch}} = 1.5 \times 10^4$

Trapping regime

$$Q_x = 4.3504$$

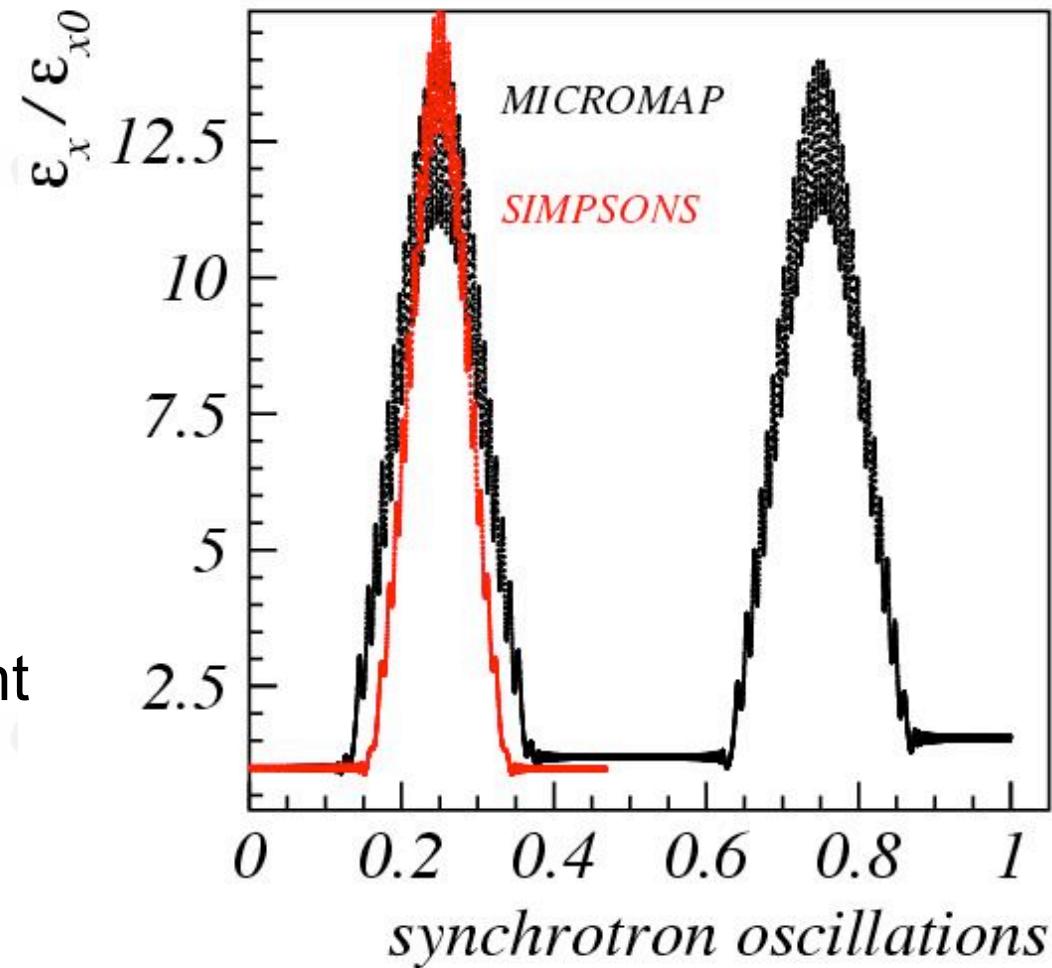
$$Q_y = 3.2$$

$$x = 5 \text{ mm}, p_x = 0$$

$$y = p_y = 0,$$

$$z = 2.5\sigma_z, p_z = 0$$

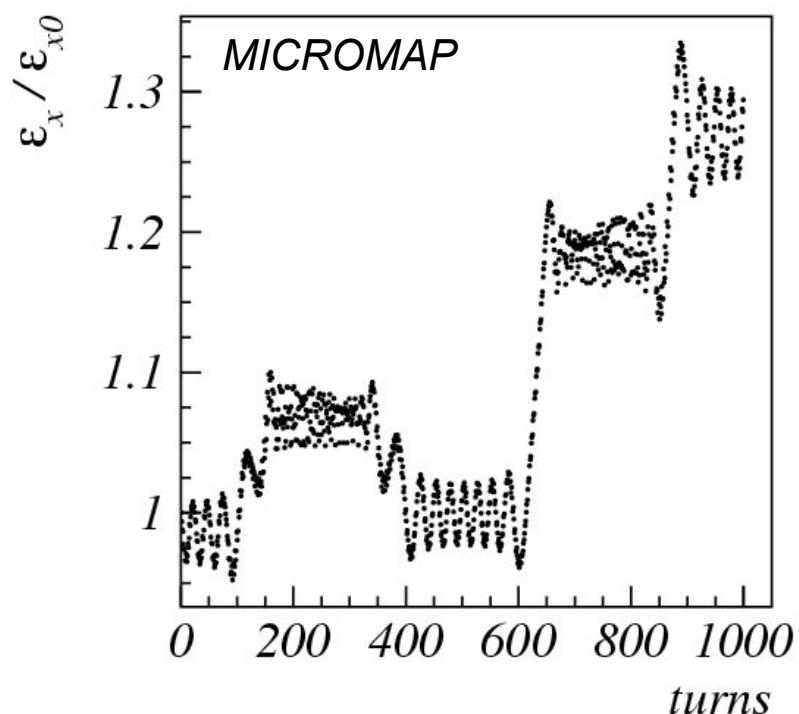
Excellent agreement



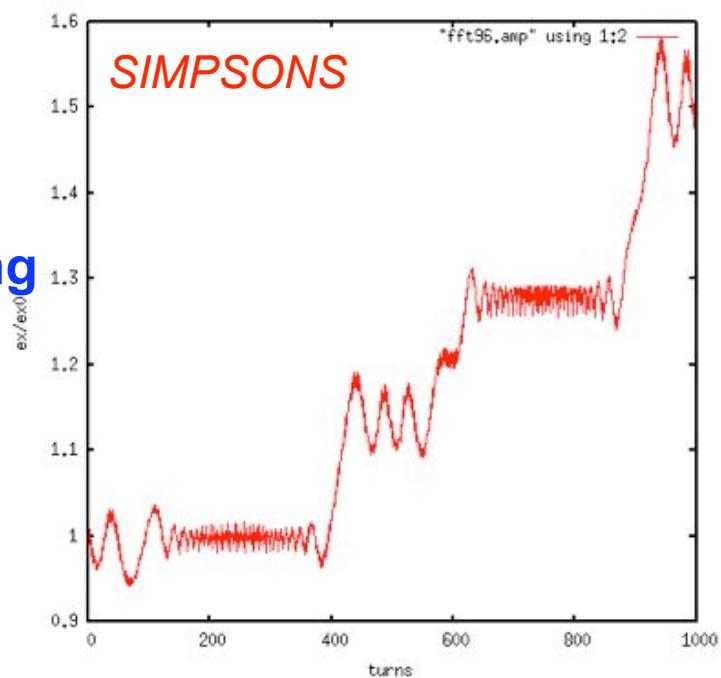
Step 7: Trapping for $N_{\text{synch}} = 10^3$

$$\begin{aligned} Q_x &= 4.3504 \\ Q_y &= 3.2 \end{aligned}$$

$$\begin{aligned} x &= 5\text{mm}, p_x = y = p_y = 0, \\ z &= 2.5\sigma_z, p_z = 0 \end{aligned}$$

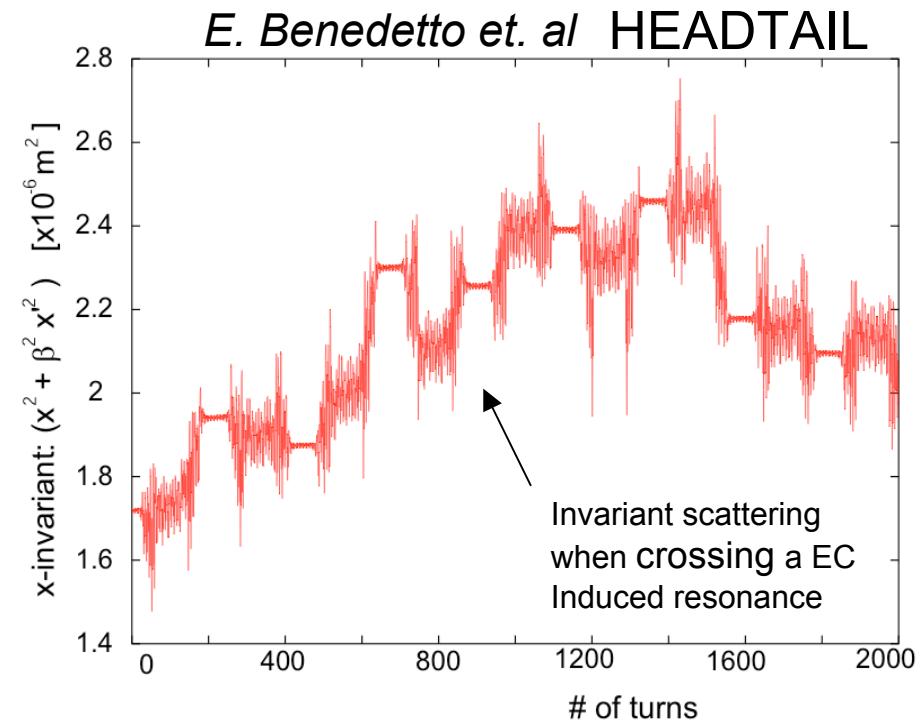
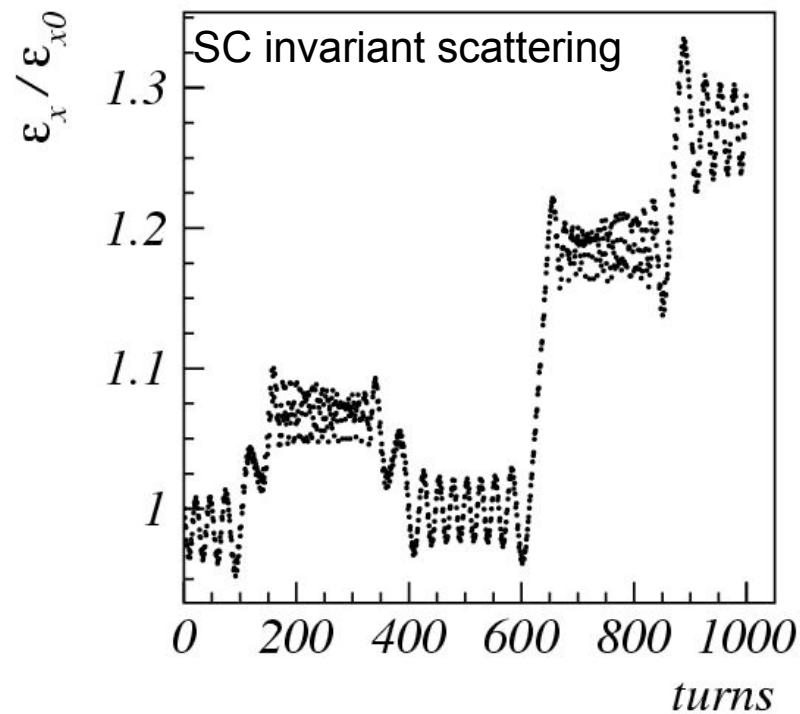


Scattering
regime



The scattering process is very sensitive to initial condition

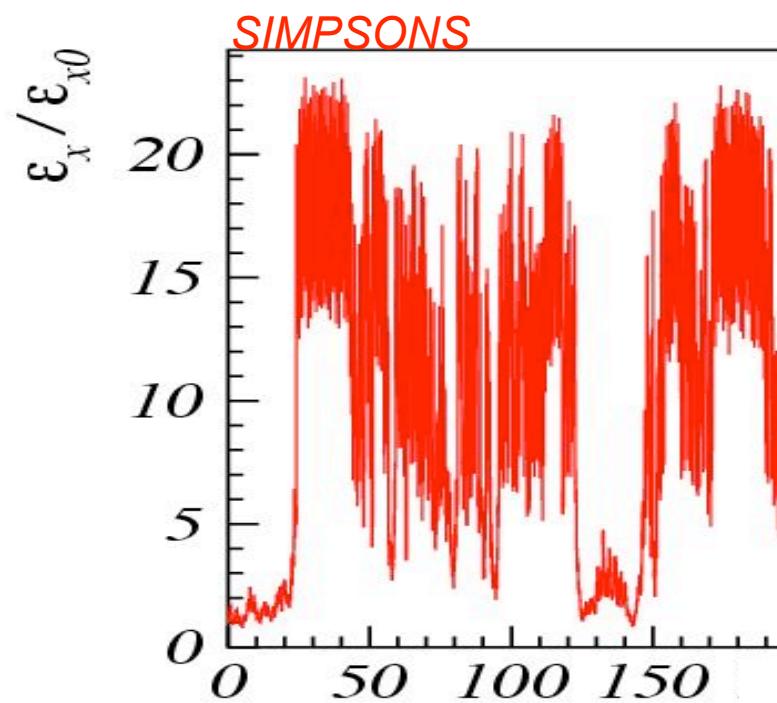
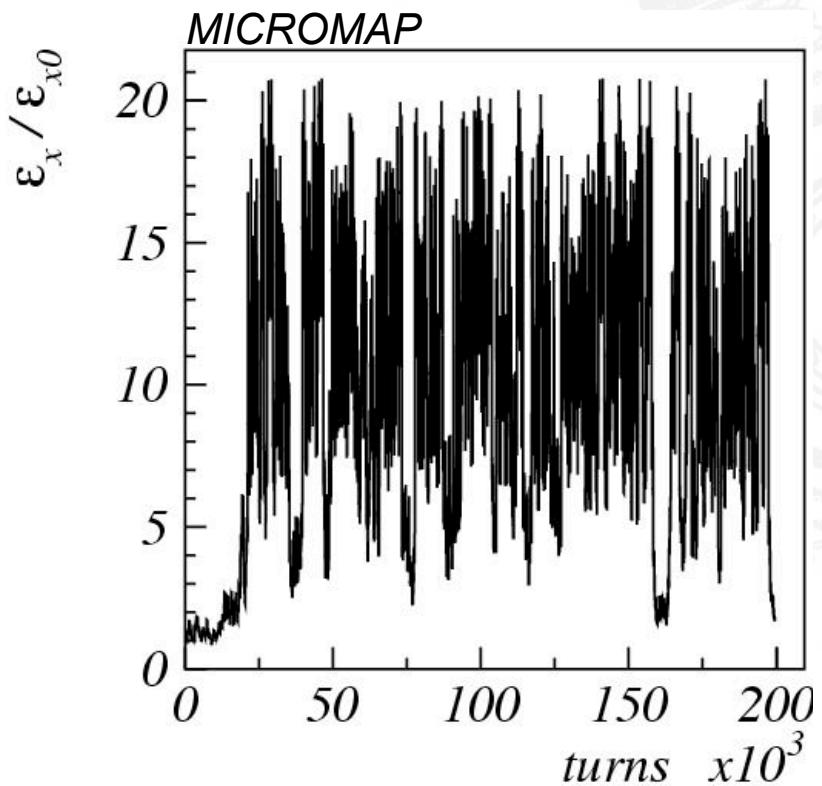
SC scattering vs. EC induced scattering



Step 8: scattering / trapping for $Q_s = 10^{-3}$ in 10^5 turns

Maximum value of the invariant
consistent with islands outer position
Step5 and Step6

Tunes and
initial condition
as in Step 7



Step 9: emittance evolution in a full bunch

Preliminary results

We change tune to increase
the number of halo particles

$Q_s = 10^{-3}$

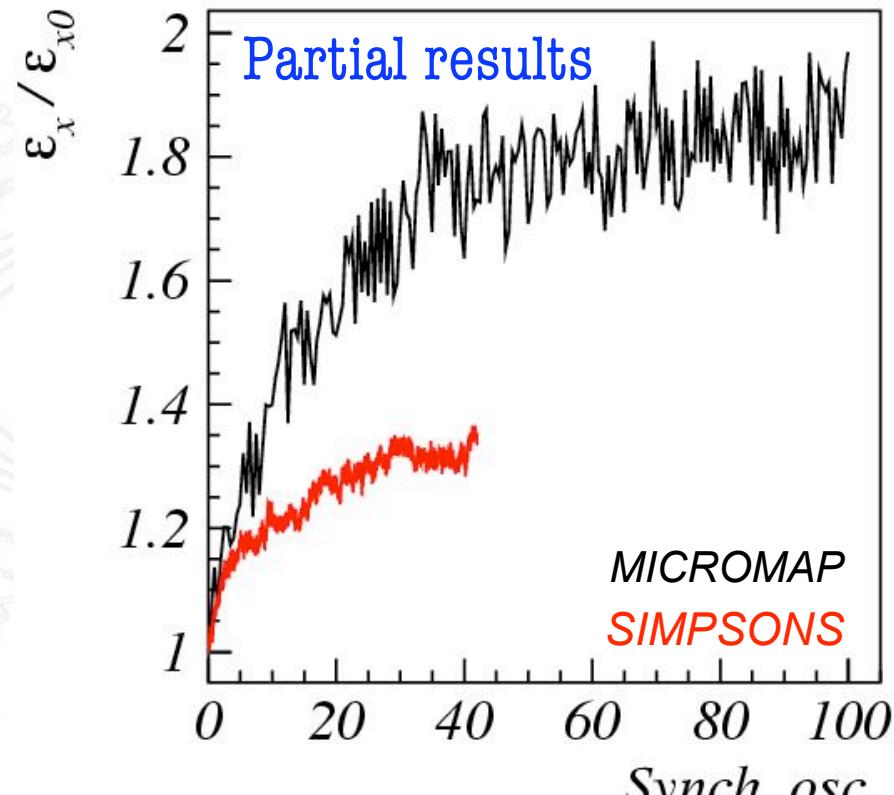
10^5 turns

10^3 macroparticles

In SIMPSONS the longitudinal
dynamics is **nonlinear**

In MICROMAP the longitudinal
dynamics is **linear**

$$Q_x = 4.3604$$



Needs to be understood... (work in progress)

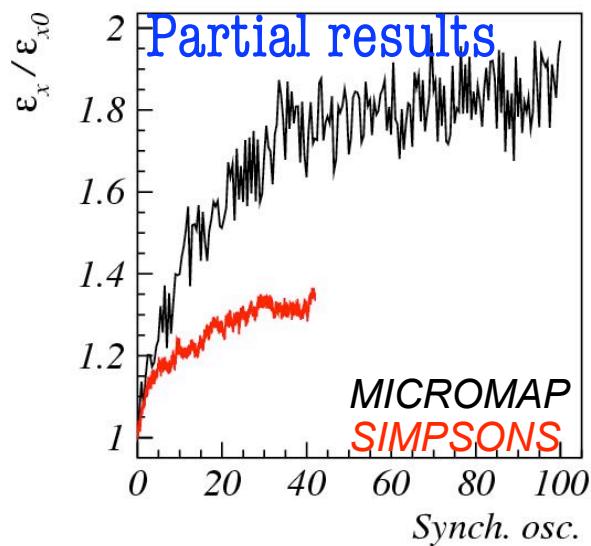
Step 9: remarks on the emittance growth

$Q_s = 10^{-3}$

10^5 turns

10^3 macroparticles

$$Q_x = 4.3604$$



Estimate of the emittance limit

$$\left\{ \begin{array}{l} \frac{E_x}{E_{x0}} = 1 - \frac{\Delta N}{N} + \frac{\epsilon_x}{E_{x0}} \frac{\Delta N}{N} \\ \frac{\Delta N}{N} = \frac{Q_x - Q_{x,res}}{\Delta Q} \end{array} \right.$$

For $Q_x = 4.3504 \rightarrow \Delta N / N = 0.27$

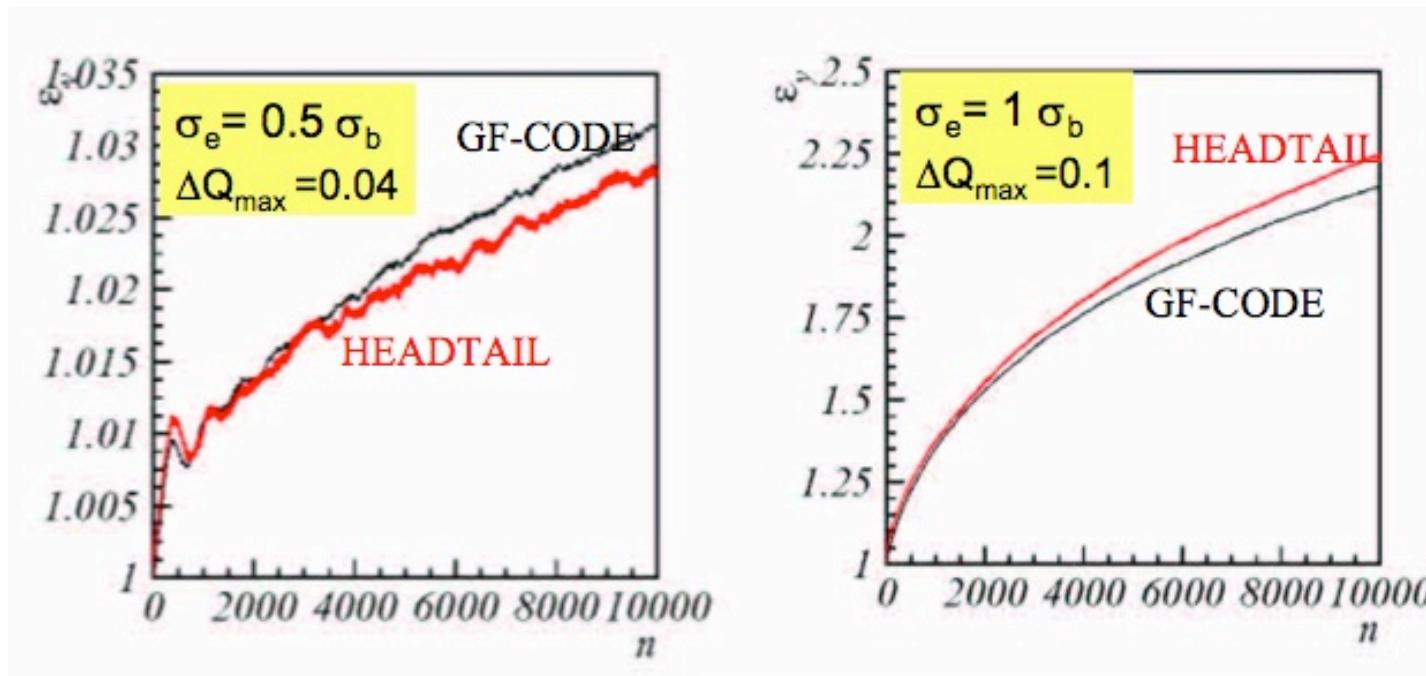
$$\epsilon_x / \epsilon_{x0} = 20 / 4 = 5$$

$$E_x / E_{x0} = 1 + 0.27 + 5 * 0.27 = 2.08$$

It makes sense !

Benchmarking not limited to SC: also EC induces resonance periodic crossing

58 synch. oscill.



from E. Benedetto's talk TUAX03

Is it really a separated
benchmark ?

Conclusion / Outlook

- 1 Trapping / scattering regimes have been successfully benchmarked;
- 2 Tests with full bunch is ongoing (partial results);

The final aim is to achieve a code-code benchmarking on the evolution of halo density / beam loss for long term storage of High intensity bunched beams.

Periodic crossing of resonances occurs also by EC kicks in IP
EC or SC induced particle trapping benchmarking are similar.

Code-Experiment benchmarking: future data from the experiment S317 @ GSI and other Labs