hadron production and the QCD phase boundary



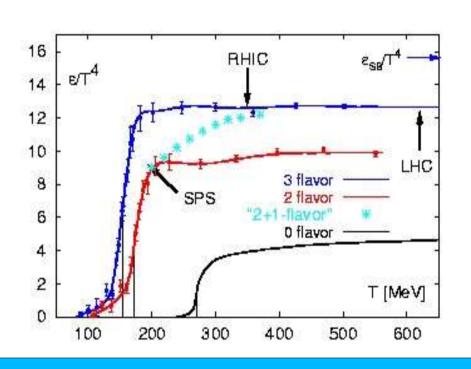
- Comments on the QCD phase transition
- Hadron production and the chemical freeze-out curve
 - hadron yields and the statistical model
 - hadron yields and the phase boundary
 - interpretation:
 - 2-body collisions don't equilibrate
 - the phase transition drives equilibration through multi-hadron collisions
 - Hagedorn states as possible intermediaries
 - Speculation about the phase boundary at large μ
- Open charm and Charmonia
- Outlook





Critical energy density and critical temperature





$$T_c = 173 \pm 12 \text{ MeV}$$

 $\epsilon_c = 700 \pm 200 \text{ MeV/fm}^3$
for the (2 + 1) flavor case:
the phase transition to the QGP
and its parameters are quantitative
predictions of QCD.

The order of the transition is not yet definitively determined.

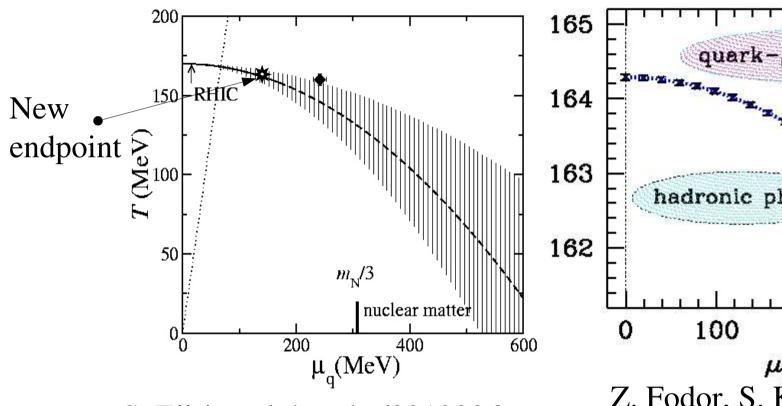
Lattice QCD calculations for μ_B = 0 Karsch et al, hep-lat/0305025



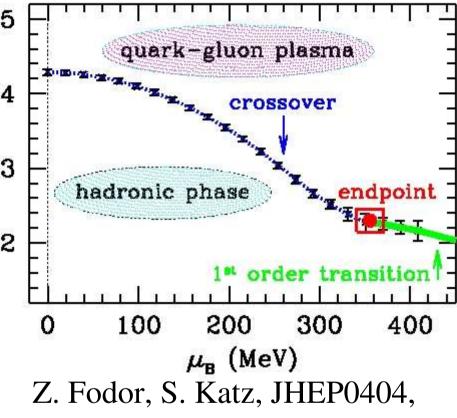


The QCD phase boundary – recent results from lattice QCD





S. Ejiri et al, hep-lat/0312006



 $(2004)\ 050;$

Note: $3 \mu_q = \mu_B$

Tri-critical point not (yet) well determined theoretically





Hadron yields signal chemical equilibrium



- From AGS energy on, all hadron yields in central PbPb collisions reflect grand-canonical equilibration
- Strangeness suppression observed in elementary collisions is lifted

For a recent review see:

pbm, Stachel, Redlich, QGP3, R. Hwa, editor, Singapore 2004, nucl-th/0304013









Fit at each

provides

values for

T and μ_b

Grand Canonical Ensemble

$$\ln Z_i = \frac{Vg_i}{2\pi^2} \int_0^\infty \pm p^2 dp \ln(1 \pm \exp(-(E_i - \mu_i)/T))$$

$$n_i = N/V = -\frac{T}{V} \frac{\partial \ln Z_i}{\partial \mu} = \frac{g_i}{2\pi^2} \int_0^\infty \frac{p^2 dp}{\exp((E_i - \mu_i)/T) \pm 1}$$
Fit at each provide
$$\mu_i = \mu_B B_i + \mu_S S_i + \mu_{I_3} I_i^3$$
provide

for every conserved quantum number there is a chemical potential μ but can use conservation laws to constrain:

$$ullet$$
 Baryon number: $V \mathop{\Sigma}\limits_{i} n_{i} B_{i} = Z + N \longrightarrow V$

$$ullet$$
 Strangeness: $V\sum\limits_{i}n_{i}S_{i}=0 \qquad \longrightarrow \mu_{S}$

$$ullet$$
 Charge: $V\sum\limits_{i}n_{i}I_{i}^{3}=rac{Z-N}{2} \longrightarrow \mu_{I_{3}}$

This leaves only μ_b and T as free parameter when 4π considered for rapidity slice fix volume e.g. by dN_{ch}/dy



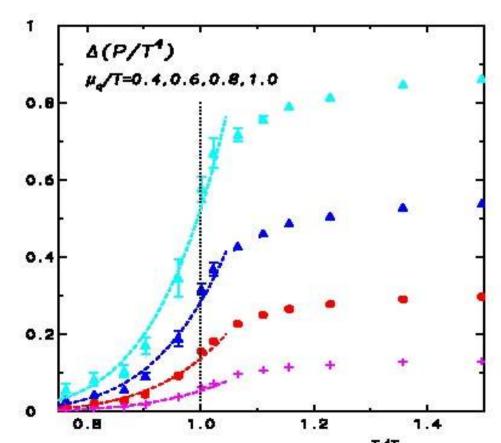


Resonance gas partition function and QCD



the resonance gas partition function contains a sum over all hadronic states

comparison between baryonic pressure from LQCD and from hadron resonance gas K. Redlich, hep-ph/0406250 and refs. there



Excellent agreement below T_c! Resonance gas approximates QCD





Hadro-chemistry at RHIC -- weakly decaying particles

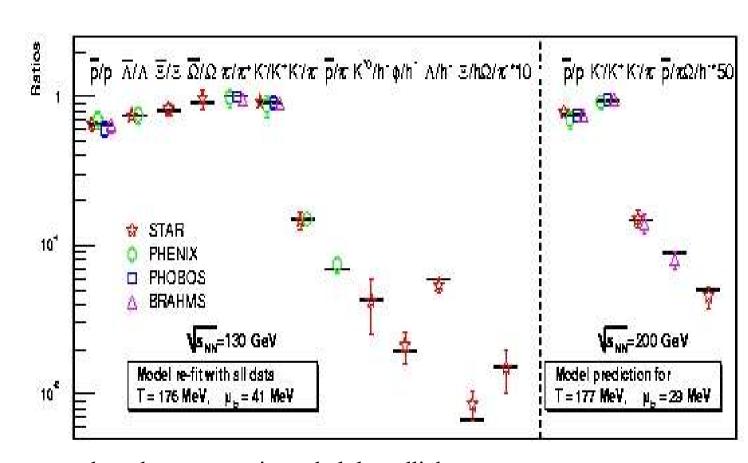


All data in excellent agreement with thermal model predictions

chemical freeze-out at: $T = 175 \pm 8 \text{ MeV}$

fit uses vacuum masses

new results from SQM04 at Cape Town consolidate this picture



pbm, d. magestro, j. stachel, k. redlich,

Phys. Lett. B518 (2001) 41; see also Xu et al., Nucl.

Phys. A698(2002) 306; Becattini, J. Phys. G28 (2002)

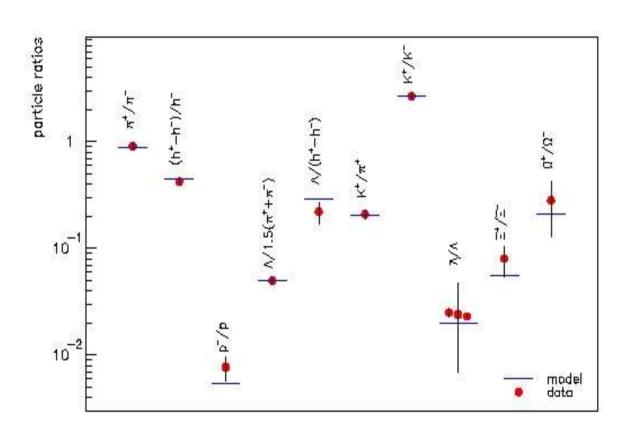
1553; Broniowski et al., nucl-th/0212052.





Hadro-chemistry at SPS





Data at 40 GeV/u Pb+Pb central collisions

T = 148 MeV,

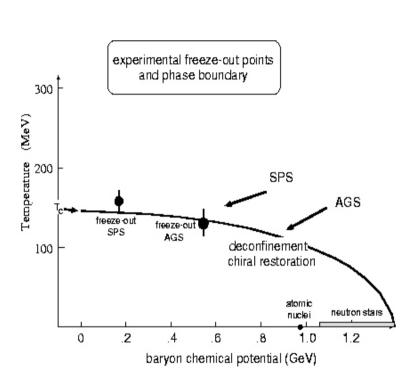
 $\mu_b = 400 \text{ MeV}$

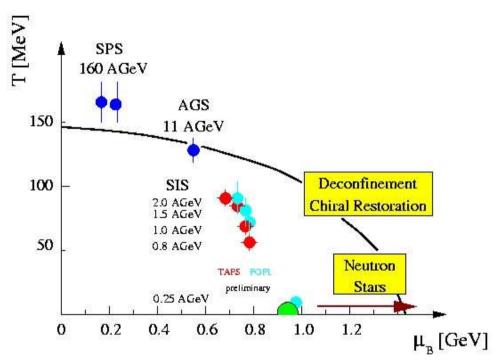
analysis from pbm, Stachel, Redlich, nucl-th/0304013 "Quark-gluon plasma 3, p. 491 – 599"



Establishing the chemical freeze-out curve







The first plot: pbm, Stachel Phys. Lett. B365 (1996)1 Nucl. Phys. A606 (1996) 320

The full curve: pbm, Stachel, QM1997 Nucl. Phys. A638 (1998)3c





Chemical freeze-out curve – the view as of 2002

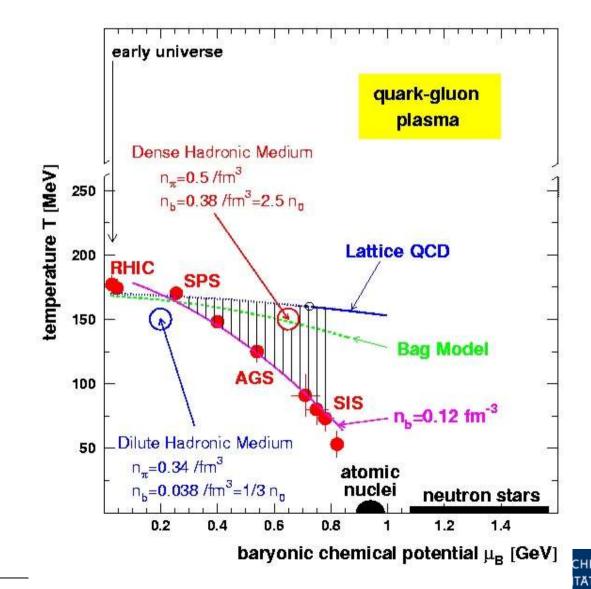


DARMSTADT

P. Braun-Munzinger, J. Stachel, J. Phys. G. 28 (2002) 1971 chem. freeze-out at constant total baryon density

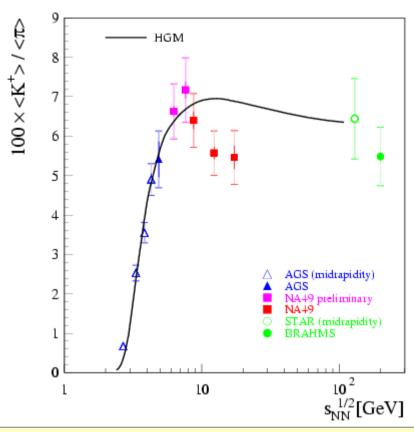
J. Cleymans, K. Redlich, Phys. Rev. Lett. 81(1998)5284 chem. freeze-out at constant energy/particle

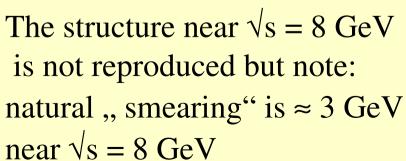
> Note: for μ < 300 MeV, LQCD phase boundary coincides with freeze-out curve

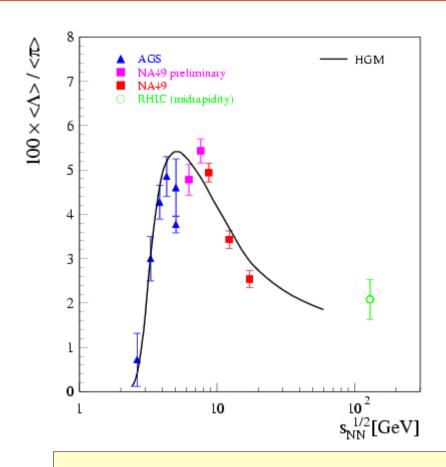


Open Issue: the NA49 ,,horn" in K/π









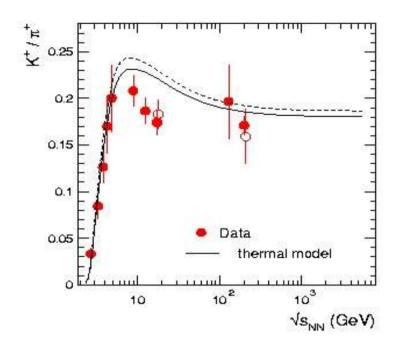
Strangeness undersaturated at 80 and 160 A GeV, saturated at all other energies?

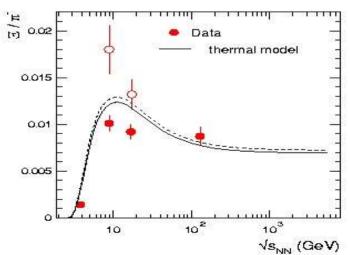


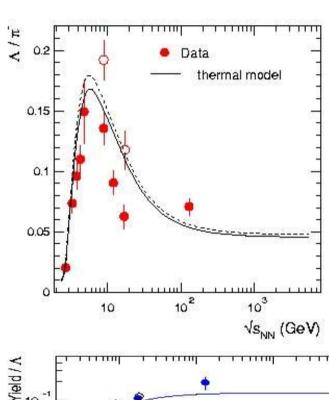


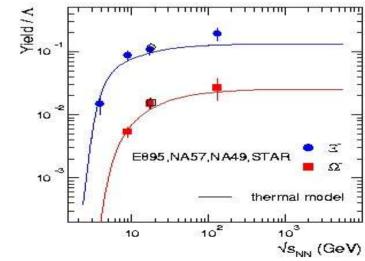
excitation functions and thermal model predictions















Strangeness equilibration at RHIC energies



- Strangeness fully saturated
- Freeze-out points are very close to phase boundary
- Deal with multi-strange baryons



Chemical Equilibration must take place in the Hadronic Phase



- Hadron yields determined by Boltzmann factors with 'free' vacuum masses.
- Particle distribution in QGP phase has no 'memory' of vacuum hadron masses .
- Relative yields are not determined by the strange quark mass but by individual strange hadron masses (at fixed T and m).
- But: the number of strange quarks is determined in the QGP phase! Equilibrium then implies redistribution of strange quarks.





How is chemical equilibration achieved? Our Scenario



- Strangeness saturation takes place in the QGP phase.
- Phase transition is crossed from above.
- Near T_c new dynamics associated with collective excitations will take place and trigger the transition.
- Propagation and scattering of these collective excitations is expressed in the form of multi-hadron scattering. Near T_c multi-hadron processes will therefore be dominant. Chemical equilibrium is reached via these multi-hadron scattering events.



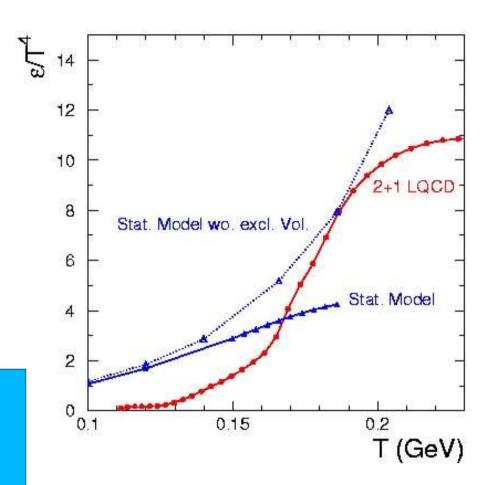


Chemical freeze-out takes place at T_c!



- Two-body collisions are not sufficient to bring multi-strange baryons into equilibrium.
- The density of particles varies rapidly with T near the phase transition.
- Multi-particle collisions are strongly enhanced at high density and lead to chem. equilibrium very near to T_c.

pbm, J. Stachel, C. Wetterich Phys. Lett. B596 (2004) 61 nucl-th/0311005



Lattice QCD calcs. By F. Karsch et al.





Evaluation of multi-strange baryon yield



consider situation at T_{ch}=176 MeV first

rate of change of density for n_{in} ingoing and n_{out} outgoing particles

$$r(n_{in}, n_{out}) = \bar{n}(\mathbb{T})^{n_{in}} |\mathcal{M}|^2 \phi$$

with

$$\phi = \prod_{k=1}^{n_{out}} \left(\int \frac{d^3 p_k}{(2\pi)^3 (2E_k)} \right) (2\pi)^4 \delta^4 \left(\sum_k p_k^{\mu} \right)$$

- ullet The phase space factor ϕ depends on \sqrt{s} needs to be weighted by the probability f(s) that multiparticle scattering occurs at a given value of \sqrt{s} evaluate numerically in Monte-Carlo using thermal momentum distribution
- typical reaction: $\Omega + \bar{N} \rightarrow 2\pi + 3K$ assume cross section equal to measured value for $p + \bar{p} \rightarrow 5\pi$ relevant $\sqrt{s} = 3.25 \text{ GeV} \rightarrow \sigma = 6.4 \text{ mb}$
- ullet compute matrix element and use for rate of $2\pi+3K
 ightarrow \Omega+ar{N}$





Evaluation of multi-strange baryon yield



reaction
$$2\pi+3K\to\Omega+N$$
 leads to
$${\rm r}_\Omega=0.00014~{\rm fm}^{-4}~{\rm or}~{\rm r}_\Omega/{\rm n}_\Omega=1/\tau_\Omega=0.46/{\rm fm}$$

 \Rightarrow can achieve final density starting from 0 in 2.2 fm/c!

similarly one obtains

for
$$3\pi + 2K \rightarrow \Xi + \bar{N}$$

$$au_{\Xi}=0.71~\mathrm{fm/c}$$

and

for
$$4\pi + K \rightarrow \Lambda + \bar{N}$$

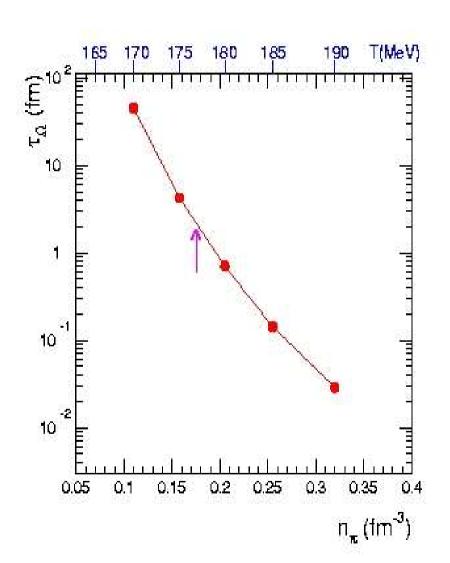
$$\tau_{\Lambda} = 0.66 \text{ fm/c}$$





Density dependence of characteristic time for strange baryon production





- Near phase transition particle density varies rapidly with T.
- For small μ_b , reactions such as $KKK\pi\pi \rightarrow \Omega N_{bar}$ bring multi-strange baryons close to equilibrium.
- Equilibration time $\tau \propto T^{-60}$!
- All particles freeze out within a very narrow temperature window.

pbm, J. Stachel, C. Wetterich Phys. Lett. B596 (2004) 61 nucl-th/0311005





Hagedorn states as intermediaries



Recent work by C. Greiner, H. Stoecker et al. hep-ph/0412 095, following up on our approach:

- multi-hadron collisions are channeled through heavy (~ 1-2 GeV) Hagedorn doorway states
- detailed balance is applied through-out
- decay of the Hagedorn states leads to rapid production of (multi-strange) baryons
- nucleon production less problematic

As in our approach, multi-particle plasma correlations near T_c lead to complete strangeness saturation. Chemical freeze-out takes place at the phase boundary.





What about pp and e+e- collisions?



- Thermal fits describe hadron yields with T ~ 160 MeV
- Hadronization may be pre-thermalization process
- But: multi-strange baryons can only be reproduced by ad-hoc strangeness suppression factor implying incomplete equilibration



pp and e+e- continued



- Suppression factor of 2 implies Omega baryons are factor 8 off the equilibrium value
- Suppression is not due to canonical thermodynamics (phi problem, K. Redlich)
- Multi-meson fusion not effective since no high density phase
- Temperature' in pp and e+e- reflects hadronization but not phase transition.
- The existence of a medium in AA collisions also leads to the result that T is not universal (at T = 160 MeV as in e+e- and pp) but varies with μ : T=140 MeV at μ = 400 MeV, e.g.



Analysis of pp collisions

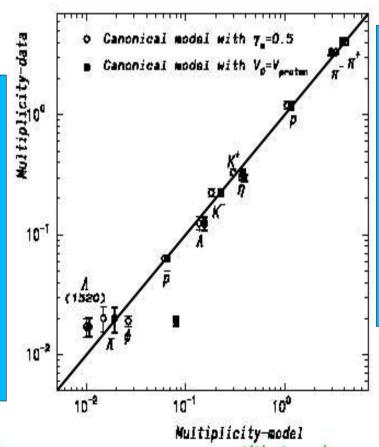


F. Becattini, Z. Phys. C69 (1996) 485; F. Becattini and U. Heinz, Z. Phys. C76 (1997) 269 pp data, $\sqrt{s} = 27.6 \text{ GeV}$

canonical (volume) suppression vs γ_s factor (non-equilibrium), T=165~MeV

Analysis by K. Redlich, see pbm, Stachel, Redlich, nucl-th/0304013

 γ_s factor needed to describe ϕ production



Observed strangeness suppression is **not** described by equilibrium thermodynamics

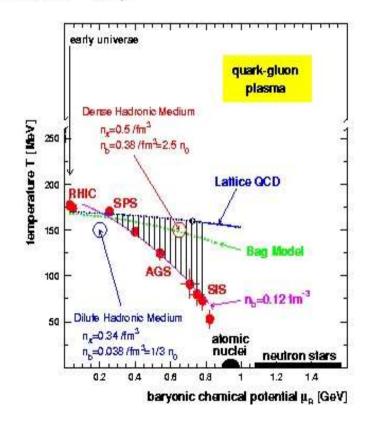




What about lower beam energies?



- at top SPS energy numbers work out nearly the same as at RHIC
- at 40 A GeV/c pion and kaon densities lower by $1/3 \rightarrow \tau_{\Omega}$ increases by factor 12
- but: other reactions involving baryons must come into play at high baryon density: $N\rho KKK \to \Omega\pi$ or $N\pi\pi KKK \to \Omega\rho$





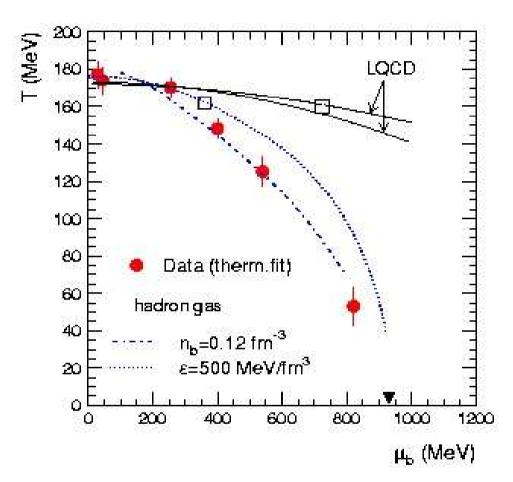


The QCD phase diagram and chemical freeze-out



Data are nearly described by curve of constant critical energy density

Conjecture: chemical freeze-out points delineate the QCD phase boundary also at larger μ down to AGS energy







A remark on critical energy density



- Along the Fodor-Katz phase boundary, critical energy density increases with increasing μ
- At $\mu = 0$, $\varepsilon_{crit} = 0.6 \text{ GeV/fm}^3$
- At T = 160 MeV and μ = 650 MeV, $\epsilon_{crit} \approx 2.7 \text{ GeV/fm}^3$ calc. within hadron resonance gas model, no excluded volume correction
- There are 1.46 baryons/fm³ and 0.44 mesons/fm³ at this point

Phase boundary at $\mu = 650$ MeV is very likely at lower T





Extra slides



2-body collisions are not enough



typical densities at T_{ch} : $\rho_{\pi} = 0.174/\text{fm}^3$ (incl. res.) $\rho_{\rm K} = 0.030/\text{fm}^3$ $\rho_{\Omega} = 0.0003/\text{fm}^3$

• To maintain equilibrium even for 5 MeV below T_{ch} need relative rate change

$$\left|\frac{\bar{r}_{\Omega}}{n_{\Omega}} - \frac{\bar{r}_{K}}{n_{K}}\right| = \tau_{\Omega}^{-1} - \tau_{K}^{-1} = (1.10 - 0.55)/\text{fm} = 0.55/\text{fm}.$$

So, Ω density needs to change by 100 % within 1 fm/c

Typical reactions with large cross sections of 10 mb and relative velocity of 0.6 give

$$\Omega + \pi \rightarrow \Xi + K$$
 \rightarrow $\bar{r}_{\Omega}/n_{\Omega} = n_{\bar{\pi}} \langle v_{\tau} \sigma \rangle = 0.086/\mathrm{fm}$ $\pi + \pi \rightarrow K + \bar{K} \ (\sigma = 3\mathrm{mb})$ \rightarrow $\bar{r}_{K}/n_{K} = 0.18/\mathrm{fm}$

i.e. much too slow to maintain equilibrium even over $\Delta T = 5$ MeV!

- Even much more difficult: to produce large Ω abundancy assume hadronization like in pp, factor 8 too few Ω s, to produce them within 1 fm/c need reactions that provide $\bar{r}_{\Omega}/n_{\Omega}{=}1.0$ \Rightarrow not with 2-body reactions
- Consensus in the literature: Koch, Müller, Rafelski, Phys. Rep. 142(1986), C. Greiner,
 S. Leupold, J.Phys.G27(2001)L95; P. Huovinen, J. Kapusta, nucl-th/0310051





Check numerics via detailed balance



- \bullet Initially manifestly nonequilibrium situation start with practially zero Ω density
- As equilibrium is approached rates $3{\sf K}+2\pi\to\Omega+\bar{N}$ and $\Omega+\bar{N}\to3{\sf K}+2\pi$ have to become equal
- back and forth reactions scale very differently with pion density
 → only at one density can they be equal
- to explicitly check these rates now use pion, kaon, nucleon densities before strong decays, i.e. without resonance feeding
 (for all resonances corresponding rates have to be calculated accordingly)
- find: creation of Ω with $r_{\Omega}/n_{\Omega}=3.4\ 10^{-3}/\mathrm{fm}$ and annihilation of Ω with $r_{\Omega}/n_{\Omega}=1.4\ 10^{-3}/\mathrm{fm}$

for equal rates reduce density by 25 % reduce T by 2-3 MeV or excluded volume a bit larger





Variation of fireball temperature with time



Values chosen appropriate for RHIC Au + Au collisions

- Assume: T_{ch}=176 MeV
 density decrease between chemical and thermal freeze-out: 30 %
- Two-pion correlation data: $R_{\text{side}} = 5.75 \text{ fm}$, $R_{\text{long}} = 7.0 \text{ fm}$, mean $\beta_t = 0.5$, $\beta_{\text{long}} = 1$
- Isentropic expansion $\rightarrow \tau_f = 0.9$ 2.3 fm, $T_f = 158$ 132 MeV (uncertainty due to variation in density profile)
- Near T_c : rate of decrease in temperature $|T/T| = \tau_T^{-1} = (13 \pm 1) \%$ /fm





What about centrality dependence of chemical equilibration?



- Apparent chemical temperature depends little on centrality.
- The importance of multiple collisions should decrease with decreasing particle density, i.e. lower centrality.
- This is expressed in the data as change in γ_s .
- Note: $\gamma_s = 0.8$ reduces Ω yield by factor of 2.



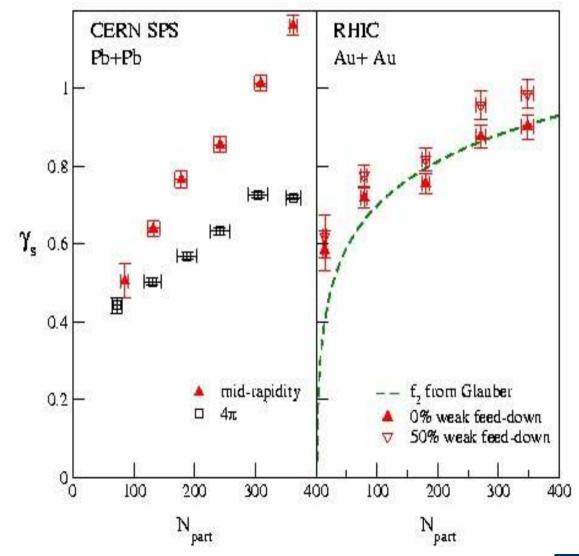
Centrality dependence of γ_s



Cleymans, Kämpfer, Steinberg, Wheaton, hep-ph/0212335

Fit μ_B and γ_S to π , K, p yields

 f_2 fraction of N_{part} with multiple collisions

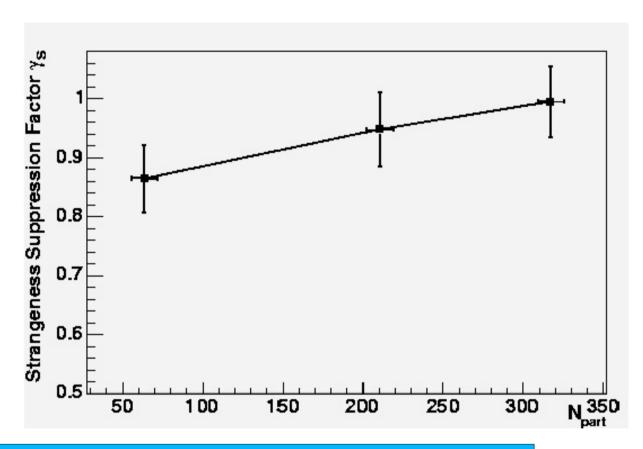






Centrality dependence of γ_s





S. Wheaton et al, SQM04, Au+Au analysis, RHIC energy increasing $N_{part} \rightarrow$ increasing particle density \rightarrow chemical equilibration is reached



