

Thermal model predictions of hadron ratios

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Abstract. We present predictions of the thermal model for hadron ratios in central Pb+Pb collisions at LHC.

Hadron yields signal chemical equilibrium

- From AGS energy on, all hadron yields in central PbPb collisions reflect grand-canonical equilibration
- Strangeness suppression observed in elementary collisions is lifted

For a recent review see:

pbm, Stachel, Redlich,
QGP3, R. Hwa, editor,
Singapore 2004,
nucl-th/0304013

Thermal model description of hadron yields

Grand Canonical Ensemble

$$\ln Z_i = \frac{V g_i}{2\pi^2} \int_0^\infty \pm p^2 dp \ln(1 \pm \exp(-(E_i - \mu_i)/T))$$
$$n_i = N/V = -\frac{T}{V} \frac{\partial \ln Z_i}{\partial \mu} = \frac{g_i}{2\pi^2} \int_0^\infty \frac{p^2 dp}{\exp((E_i - \mu_i)/T) \pm 1}$$
$$\mu_i = \mu_B B_i + \mu_S S_i + \mu_{I_3} I_i^3$$

Fit at each energy provides values for T and μ_b

for every conserved quantum number there is a chemical potential μ but can use conservation laws to constrain:

- Baryon number: $V \sum_i n_i B_i = Z + N \rightarrow V$
- Strangeness: $V \sum_i n_i S_i = 0 \rightarrow \mu_S$
- Charge: $V \sum_i n_i I_i^3 = \frac{Z - N}{2} \rightarrow \mu_{I_3}$

This leaves only μ_b and T as free parameter when 4π considered for rapidity slice fix volume e.g. by dN_{ch}/dy

Hadro-chemistry at RHIC -- weakly decaying particles

All data in excellent agreement with thermal model predictions

chemical freeze-out at: $T = 165 \pm 8$ MeV

fit uses vacuum masses

most recent analysis:

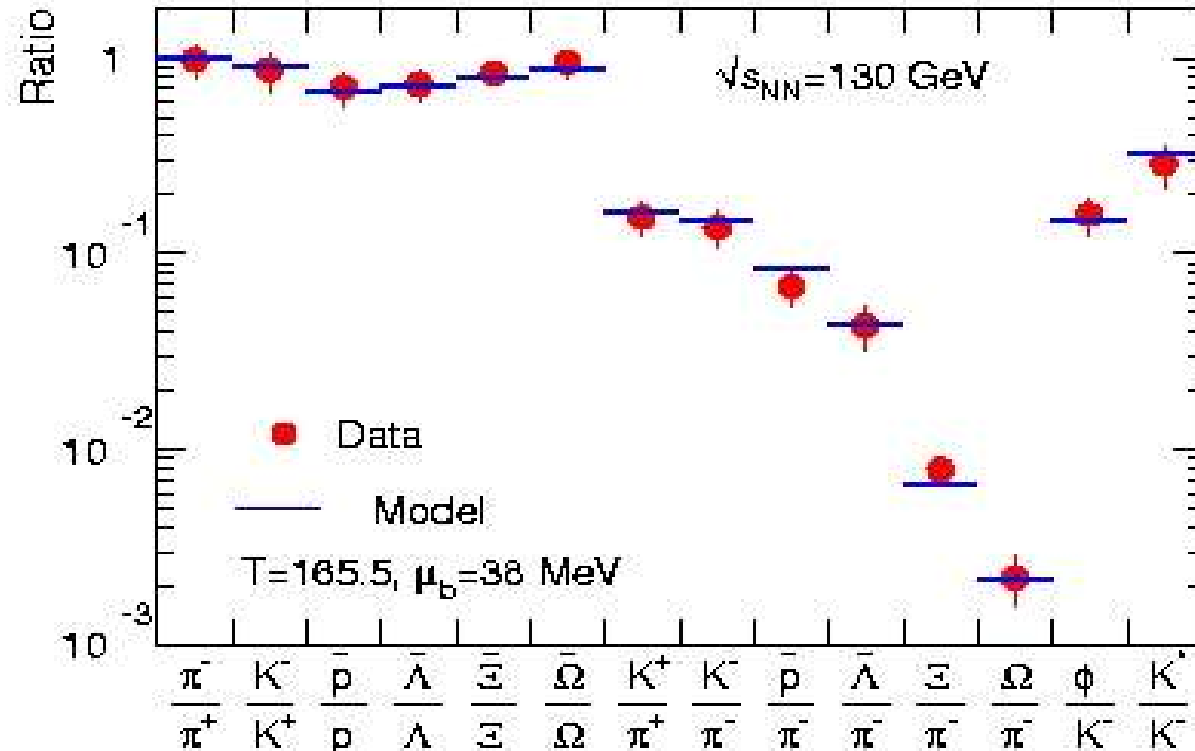
A. Andronic, pbm, J.

Stachel,

nucl-th/0511071

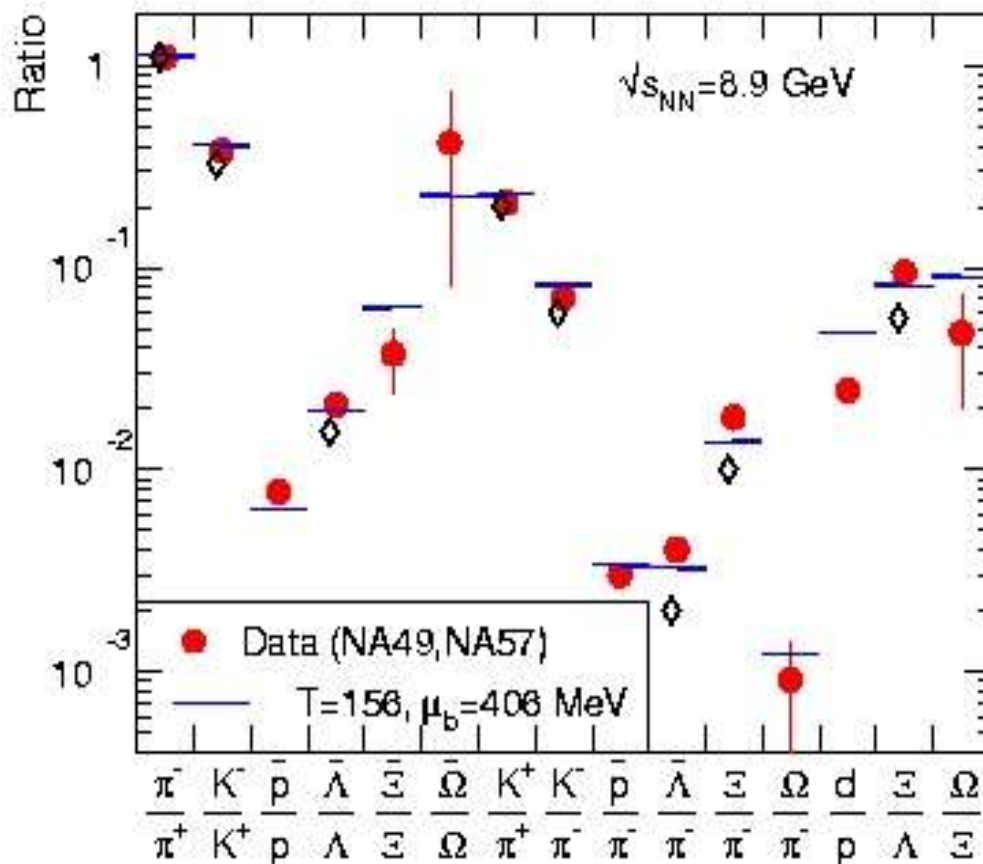
Nucl. Phys. A772

(2006) 167



pbm, d. magestro, j. stachel, k. redlich,
 Phys. Lett. B518 (2001) 41; see also Xu et al., Nucl.
 Phys. A698(2002) 306; Becattini, J. Phys. G28 (2002)
 1553; Broniowski et al., nucl-th/0212052.

Hadro-chemistry at SPS



Data at 40 GeV/u Pb+Pb
central collisions

$T = 156 \text{ MeV}$,

$\mu_b = 406 \text{ MeV}$

analysis from

Andronic, pbm,

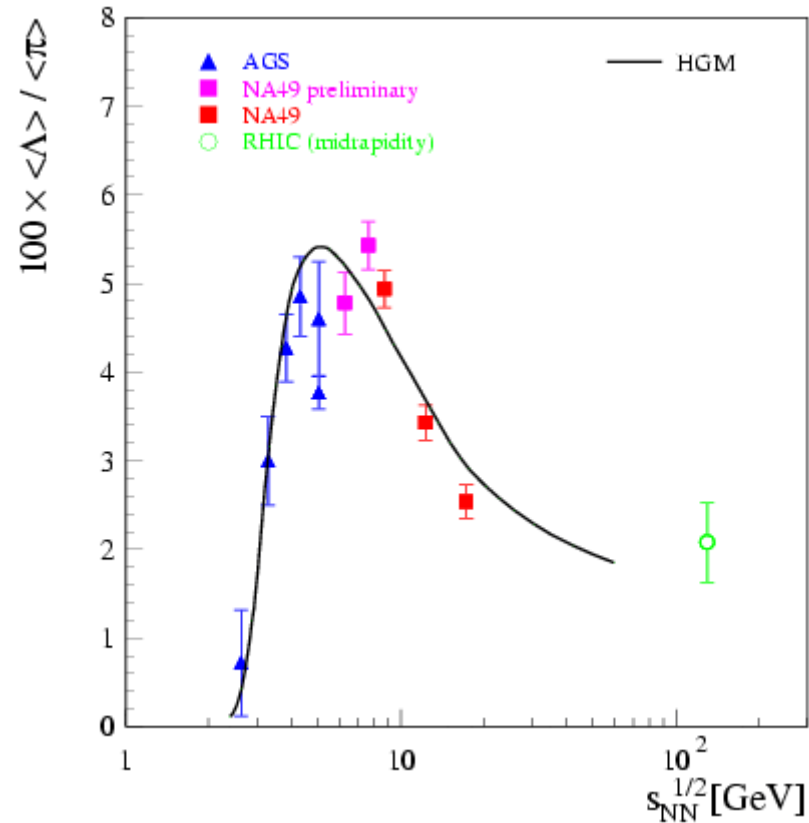
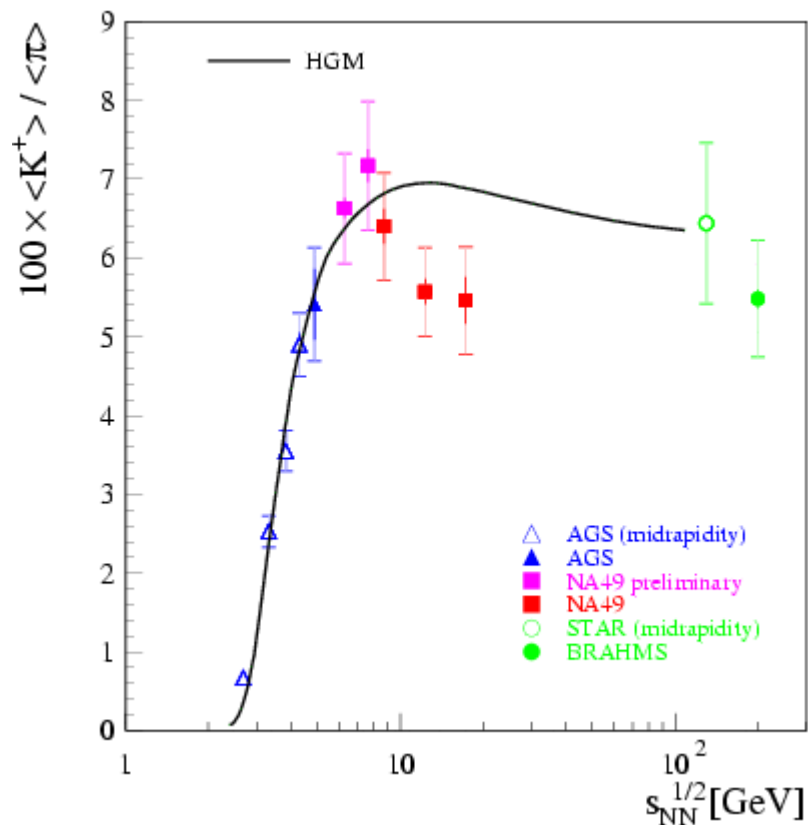
Stachel,

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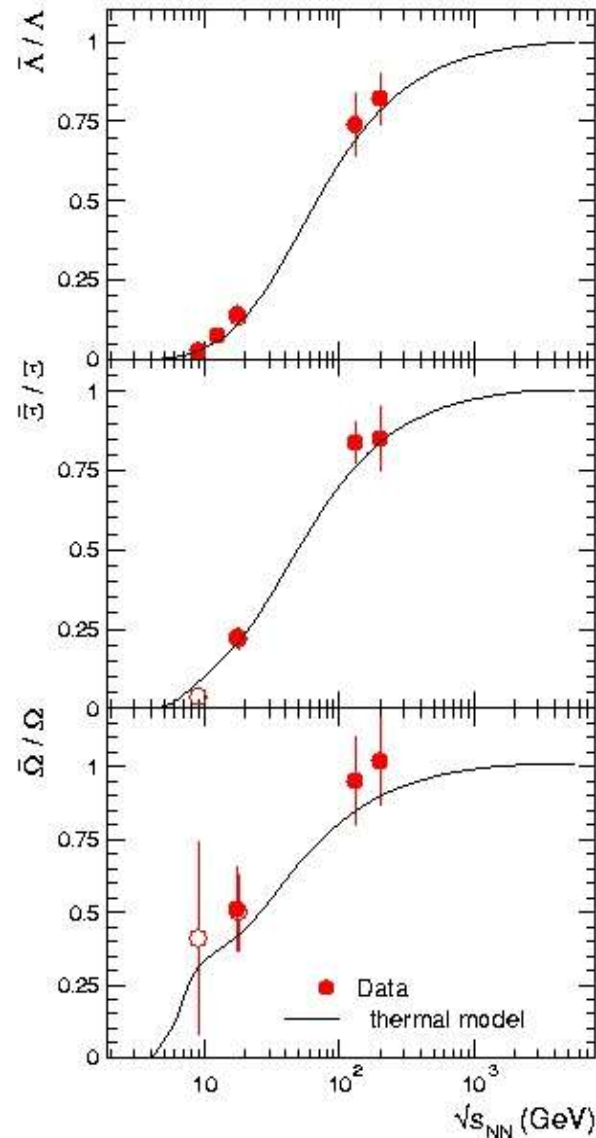
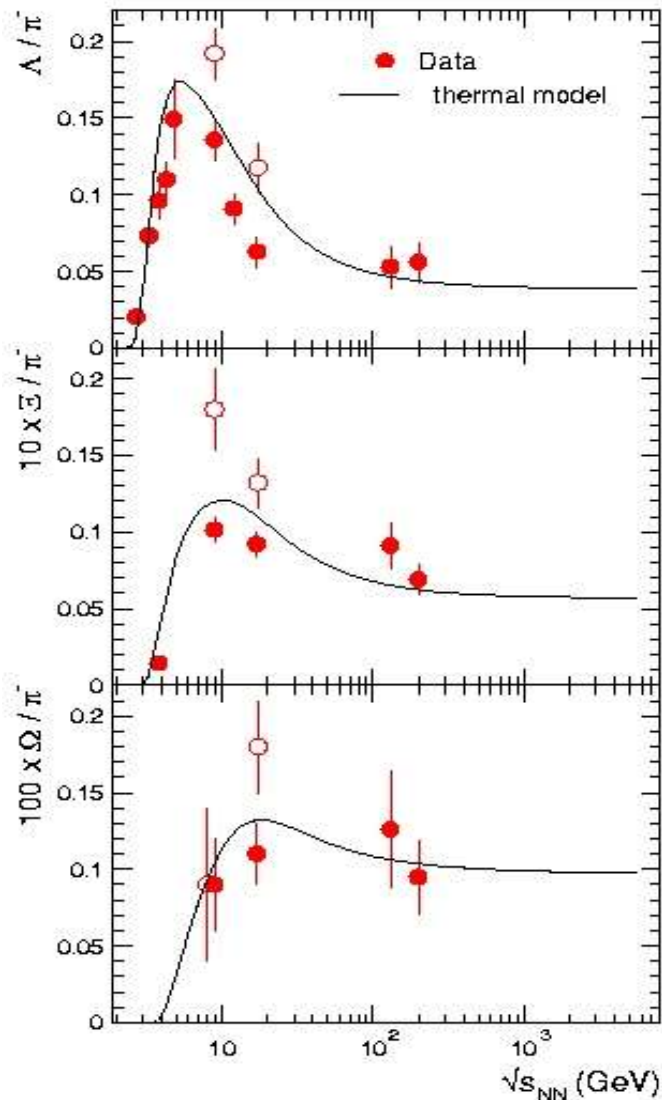
Open Issue: the NA49 „horn“ in K/ π



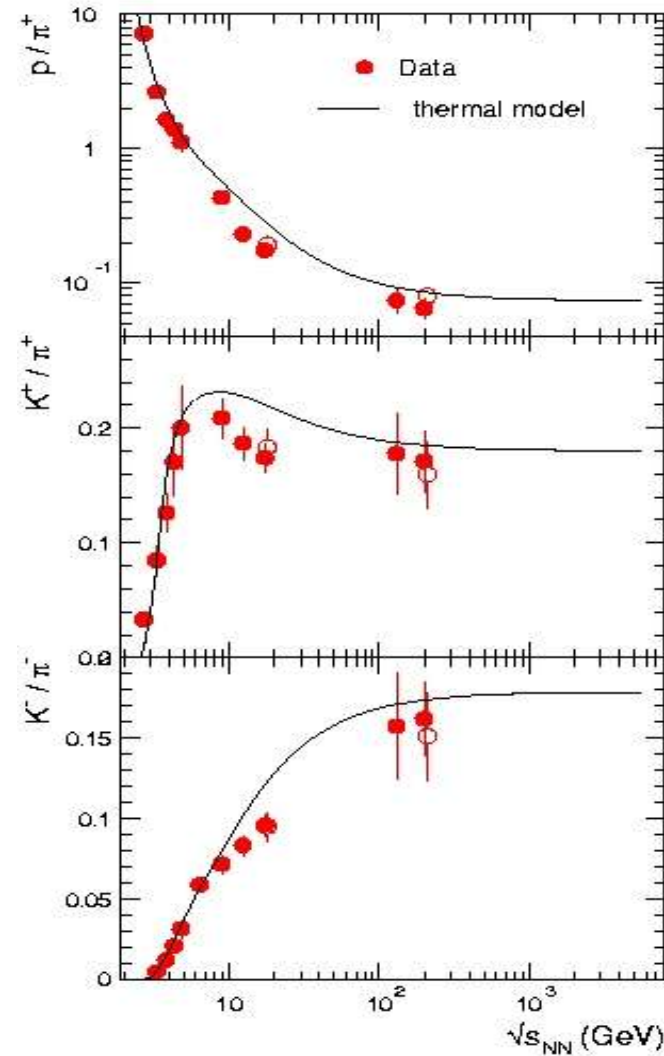
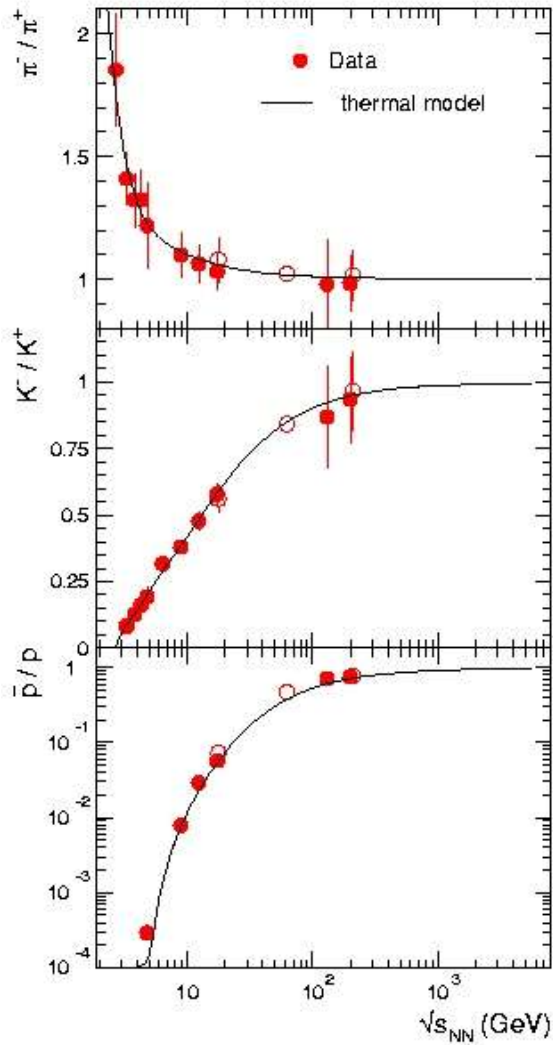
The structure near $\sqrt{s} = 8$ GeV is not reproduced but note: natural „smearing“ is ≈ 3 GeV near $\sqrt{s} = 8$ GeV

Strangeness undersaturated at 80 and 160 A GeV, saturated at all other energies?

excitation functions and thermal model predictions



excitation functions and thermal model predictions



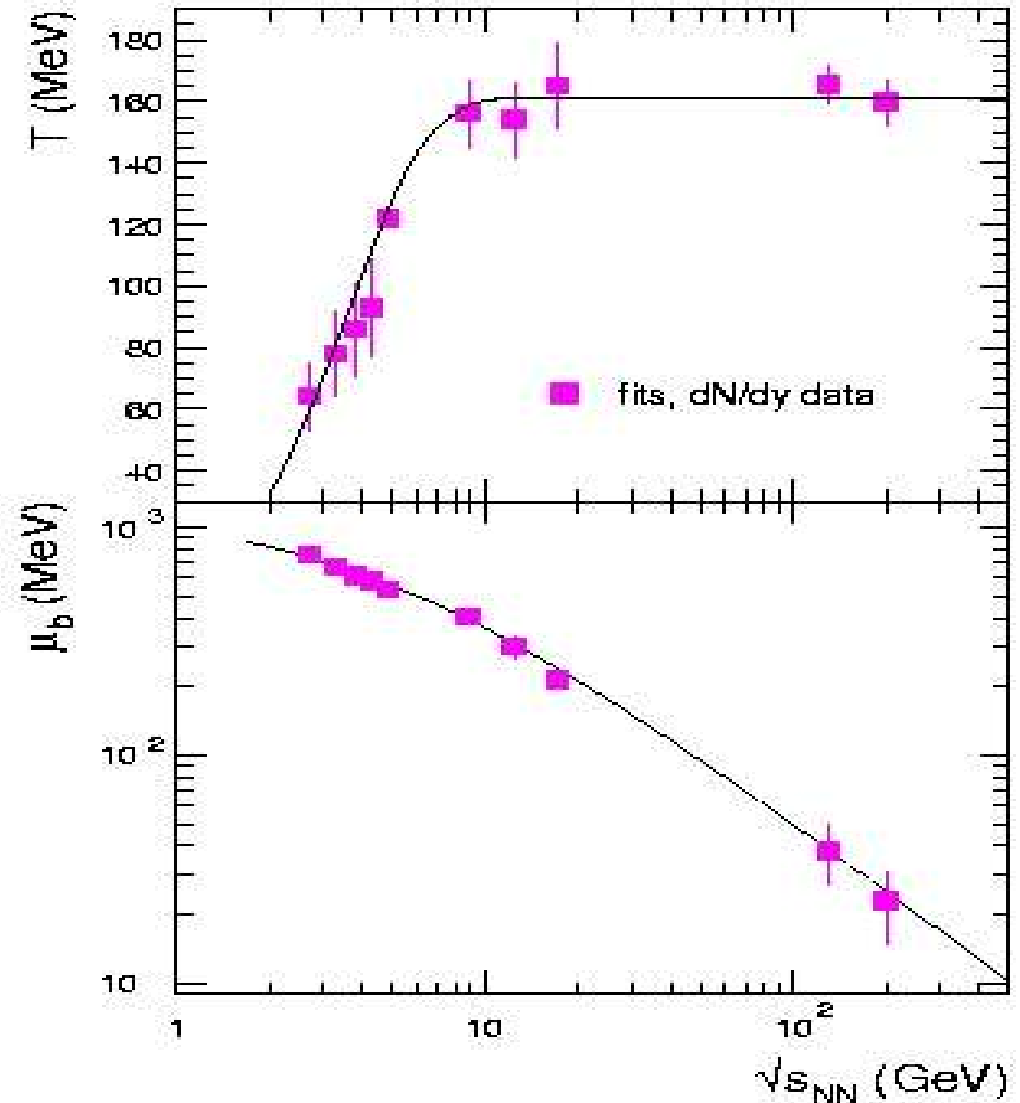
The limiting temperature is T_c

$$T_{\text{lim}} = 160 \text{ MeV}$$

$$T_c = 160 (+12 -16) \text{ MeV}$$

estimated systematic errors

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Chemical freeze-out determines T_c for small

phase transition brings multi-strange (and all other hadrons) into equilibrium

chemical freeze-out temperature closely coincides with critical temperature

determination of a fundamental QCD parameter from experiments on hadron production in ultra-relativistic nuclear collisions

$$T_c = 160 (+12 -16) \text{ MeV}$$

2 sigma discrepancy with latest lattice results of Bielefeld/Columbia/BNL group, but in agreement with Fodor et al., see also T. Hatsuda, hep-ph/0702293

first prediction of particle ratios at LHC energy

pbm, Nucl. Phys. A661 (1999) 261

invited paper, QM1999 conference, Torino, Italy

results to within 10 % in agreement with current
predictions

baryon chemical potential still unknown (10 MeV used)

from SPS and RHIC systematics, the thermal model parameters at LHC energy are estimated to be:

$$T=161\pm 4 \text{ MeV} \text{ and } \mu_b=0.8_{-0.6}^{+1.2} \text{ MeV}$$

all predictions are made for yields at mid-rapidity
in central Pb-Pb collisions

Table 1. Predictions of the thermal model for hadron ratios in central Pb+Pb collisions at LHC. The numbers in parantheses represent the error in the last digit(s) of the calculated ratios.

π^-/π^+	K^-/K^+	\bar{p}/p	$\bar{\Lambda}/\Lambda$	$\bar{\Xi}/\Xi$	$\bar{\Omega}/\Omega$
1.001(0)	0.993(4)	$0.948_{+0.008}^{-0.013}$	$0.997_{+0.004}^{-0.011}$	$1.005_{+0.001}^{-0.007}$	1.013(4)
p/π^+	K^+/π^+	K^-/π^-	Λ/π^-	Ξ^-/π^-	Ω^-/π^-
0.074(6)	0.180(0)	0.179(1)	0.040(4)	0.0058(6)	0.00101(15)

Table 2. Predictions for the relative abundance of resonances at chemical freeze-out.

ϕ/K^-	K^{*0}/K_S^0	Δ^{++}/p	$\Sigma(1385)^+/\Lambda$	Λ^*/Λ	$\Xi(1530)^0/\Xi^-$
0.137(5)	0.318(9)	0.216(2)	0.140(2)	0.075(3)	0.396(7)

predictions for other particle ratios are available upon request
from the authors