

# PRECISION TESTS OF QED IN STRONG FIELDS: EXPERIMENTS ON HYDROGEN- AND HELIUM-LIKE URANIUM

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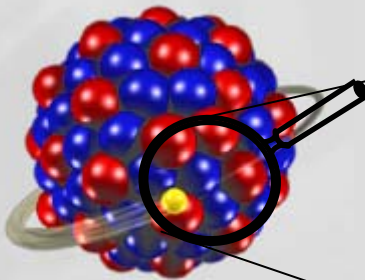
*IMP, Lanzhou, China*

*Swiatokrzyska Academy, Kielce, Poland*

*Fudan University, Shanghai, China*

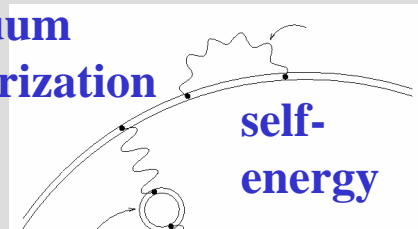
Uranium-Ion

**QED**



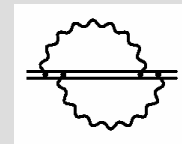
$Z=92$

**vacuum  
polarization**



**self-  
energy**

+



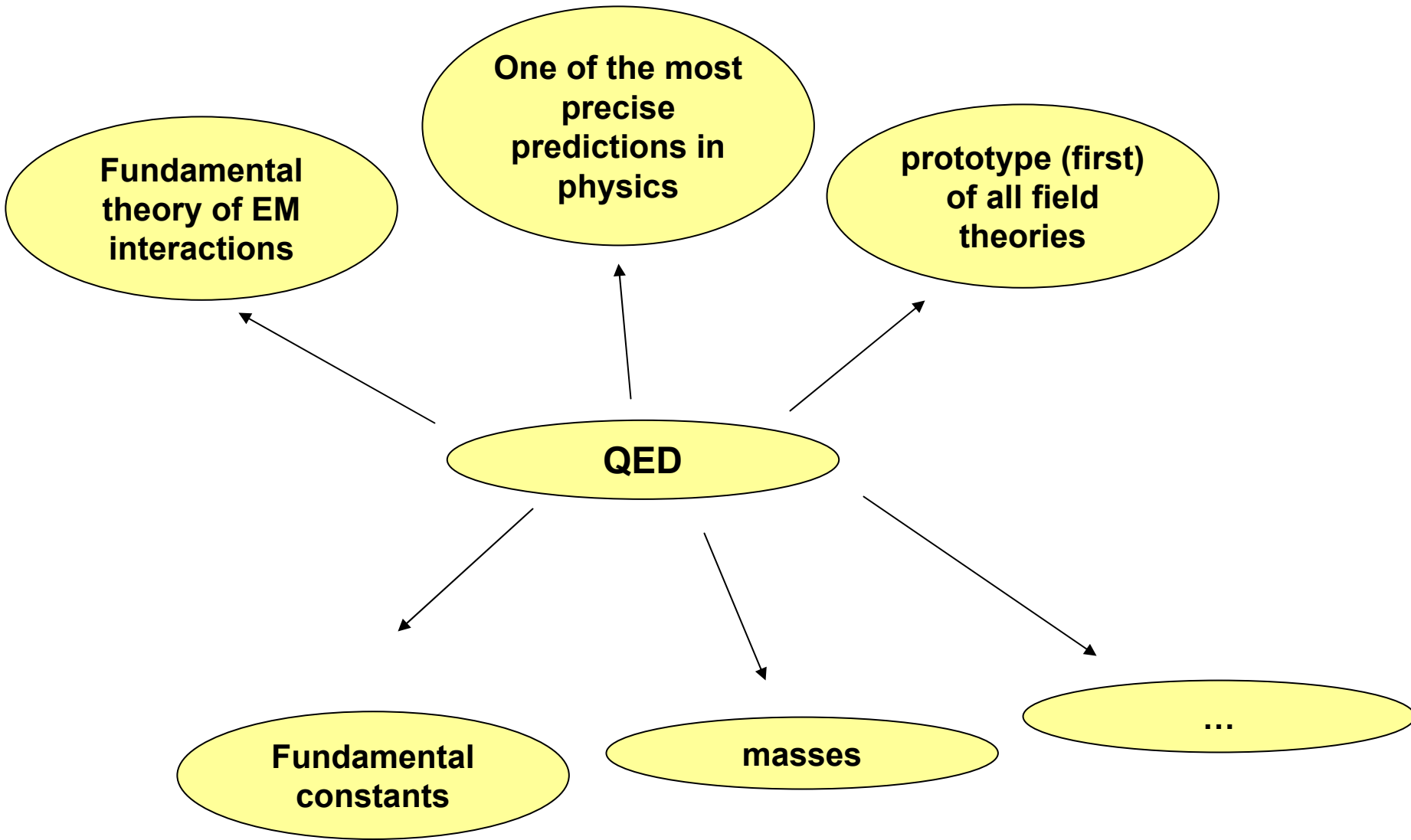
+

...

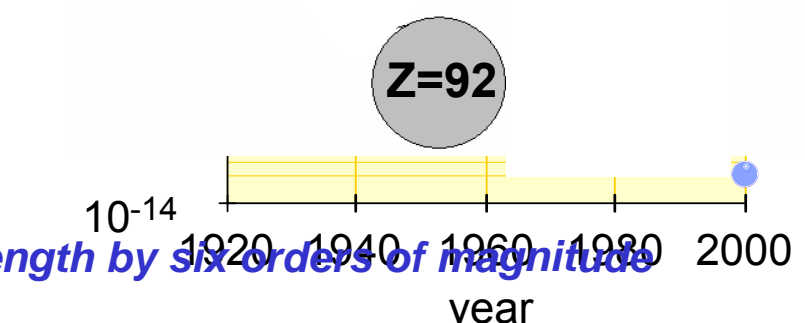
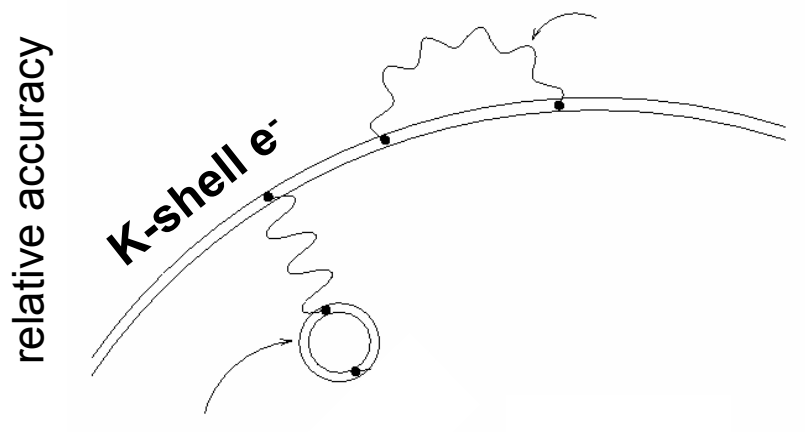
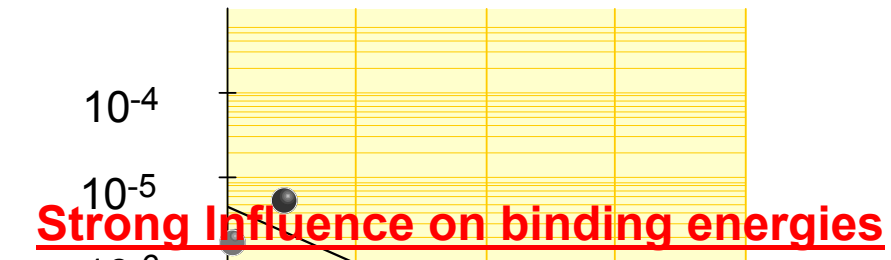
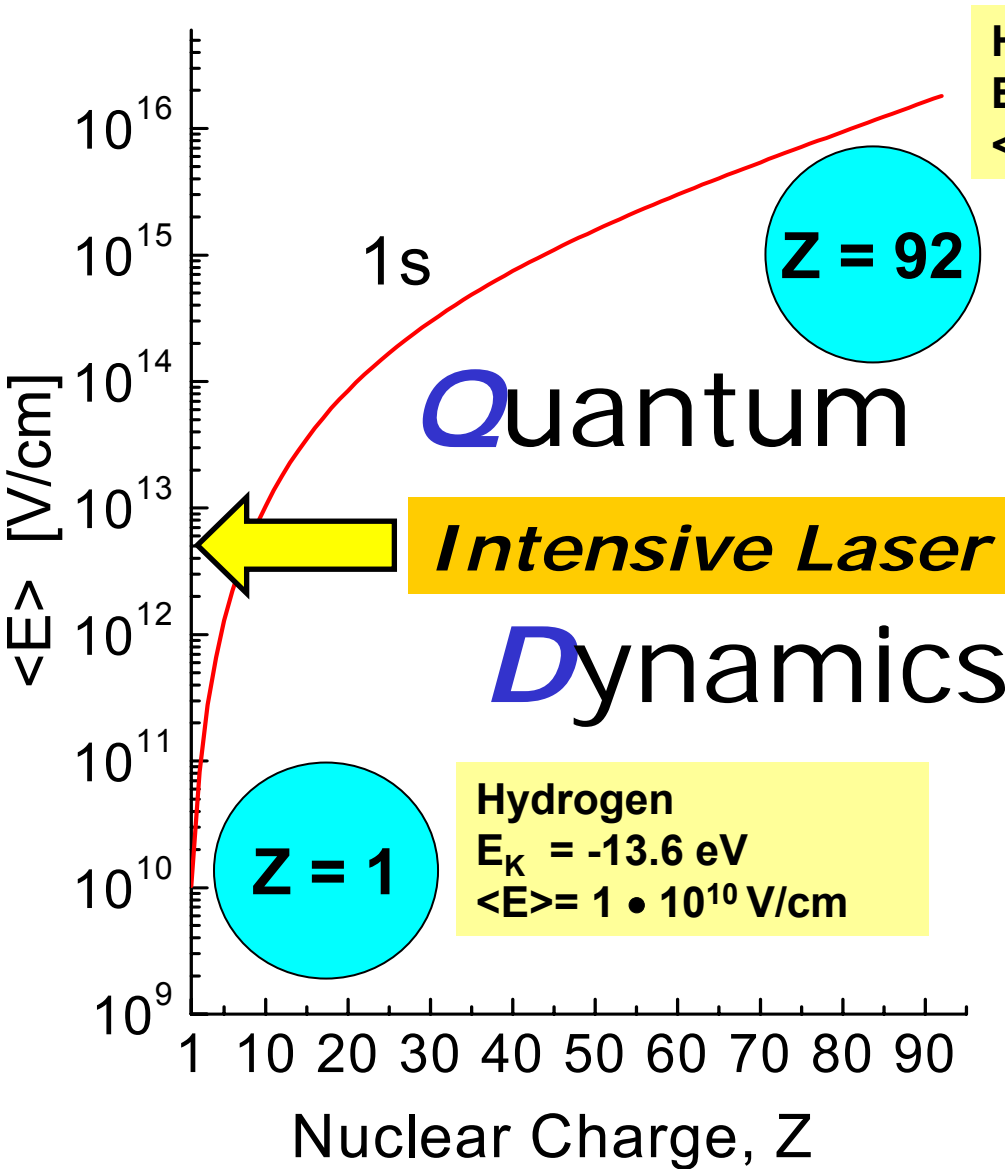
# PRECISION TESTS OF QED IN STRONG FIELDS: EXPERIMENTS ON HYDROGEN- AND HELIUM-LIKE URANIUM

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- ***Introduction:*** QED, Lamb shift and the structure of one- and two-electron systems at high-Z
- ***Experiment at the storage ring ESR at GSI***
- Production and storage of high-Z few-electron (or bare) ions
- X-ray spectroscopy at the ESR electron cooler, relativistic doppler effect
- **Results in comparison with theoretical predictions**
- ***Summary***
- ***Outlook***  
***(towards ~1 eV precision)***
- Crystal spectrometer
- Detector development

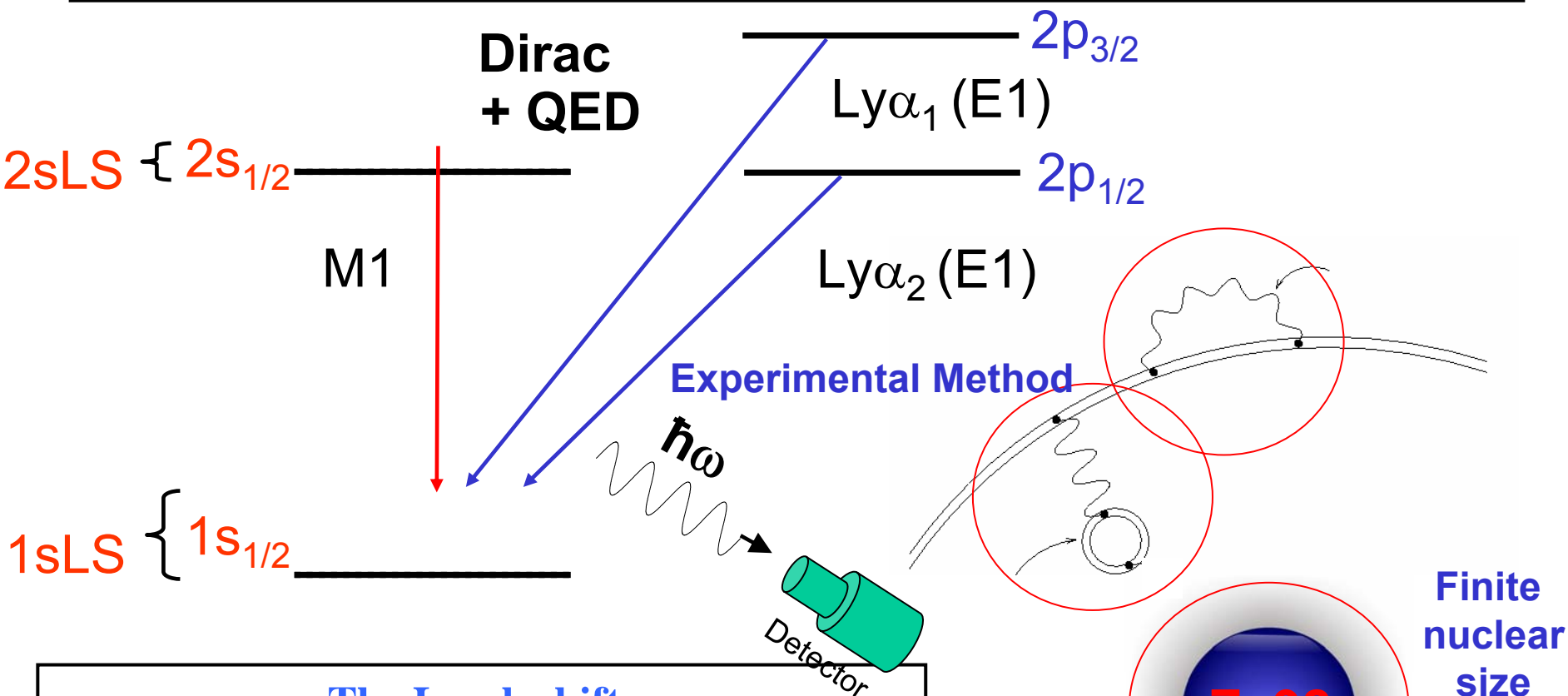


# Atomic Physics in Extremely Strong Coulomb Fields

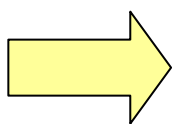


***1s-ground state: increase of the electric field strength by six orders of magnitude***

# The Atomic Structure of One-electron System



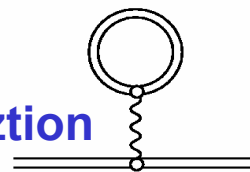
**The Lamb shift:**  
*The sum of all corrections which lead to the discrepancy from the predictions of the Dirac-Theory for a point-like nucleus.*



- Decrease of the binding energies
- dominantly for s-states

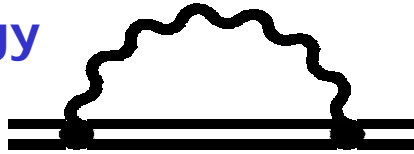


Vacuum polariztion

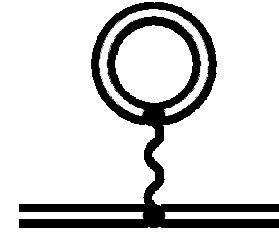


# Bound-State QED: 1s Lamb shift

Self-energy



Vacuum-polarization



$U^{91+}$	SE	VP	NS
	355.0 eV	-88.6 eV	198.7 eV

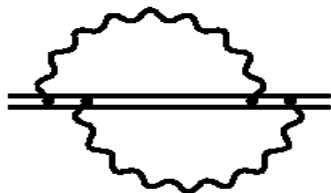
$$\Delta E = \alpha/\pi (\alpha Z)^4 F(\alpha Z) m_e c^2$$

Low Z-regime:  $\alpha Z \ll 1$

$F(\alpha Z)$ : expansion in  $\alpha Z$

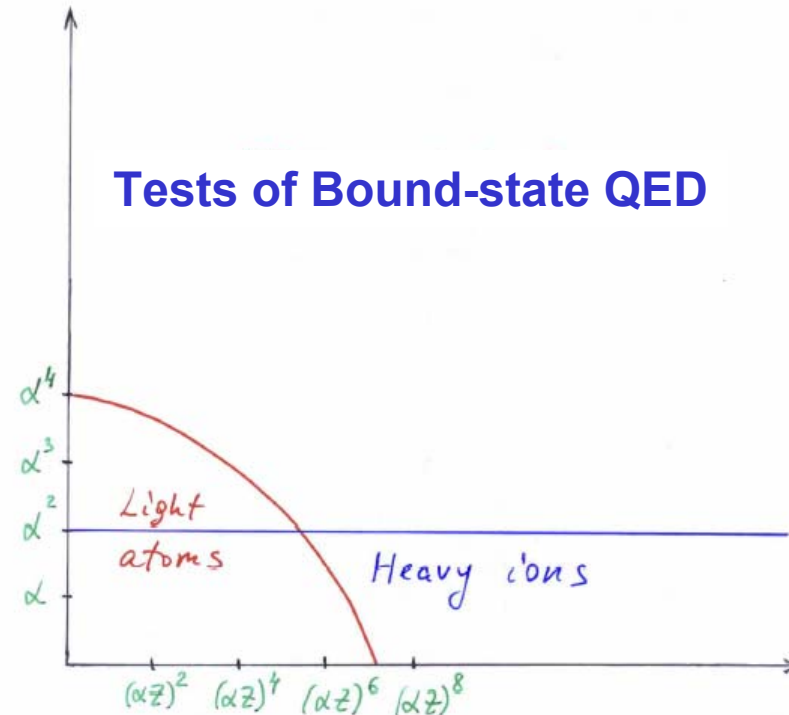
High Z-regime:  $\alpha Z \approx 1$

$F(\alpha Z)$ : expansion in  $\alpha Z$  not applicable (calculation of all orders)



$\pm 1$  eV

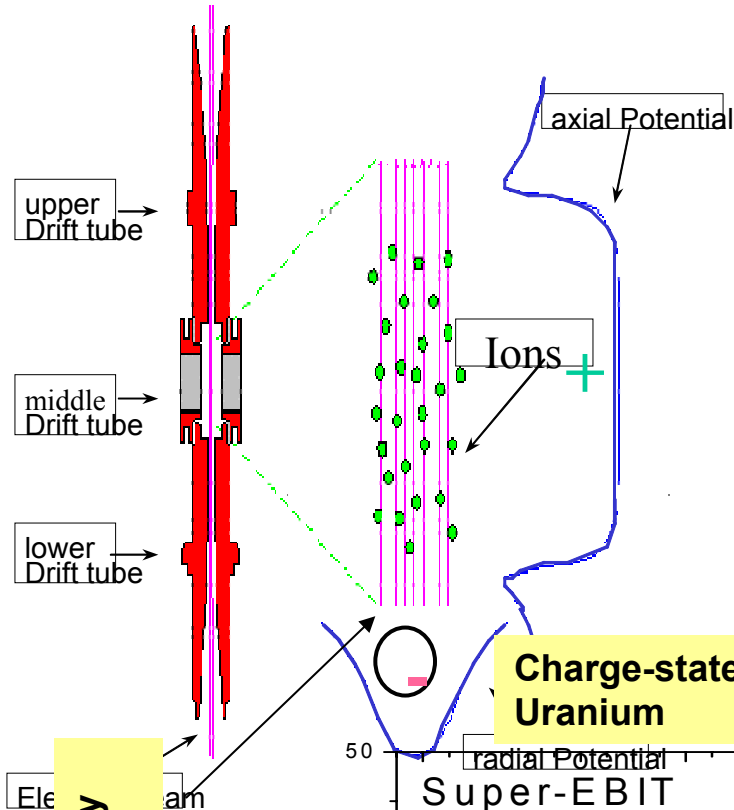
## Tests of Bound-state QED



# Production of highly charged heavy ions

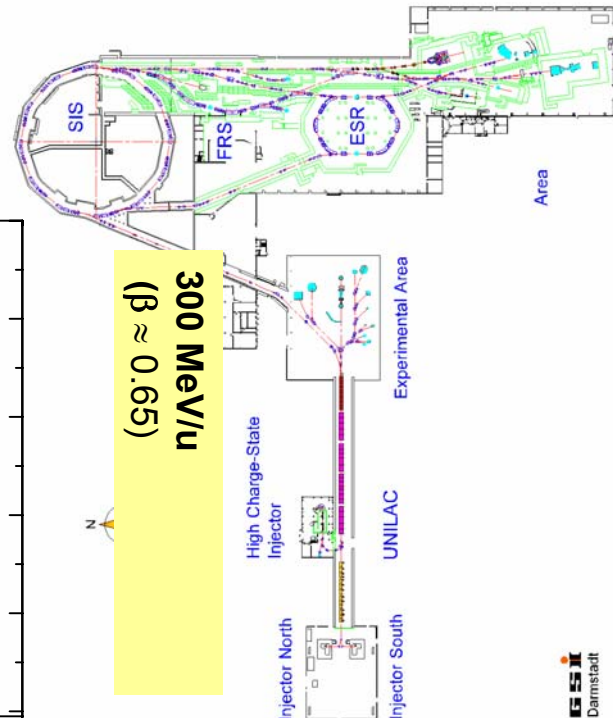
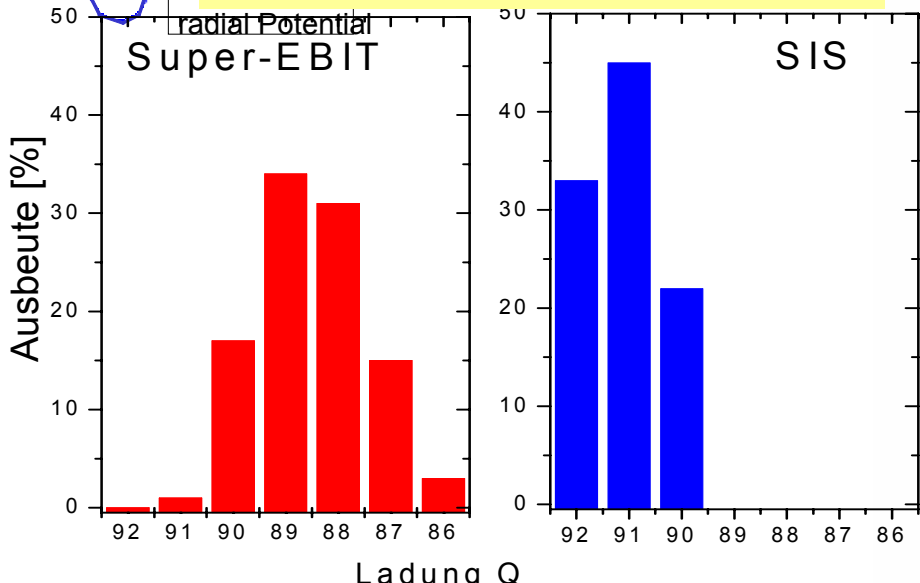
**Traps (EBIT):**  
*production of highly charged ions by collisions with high energy electron beams*

**Accelerator:**  
*production of highly-charged ions by fast collisions with target atoms.*

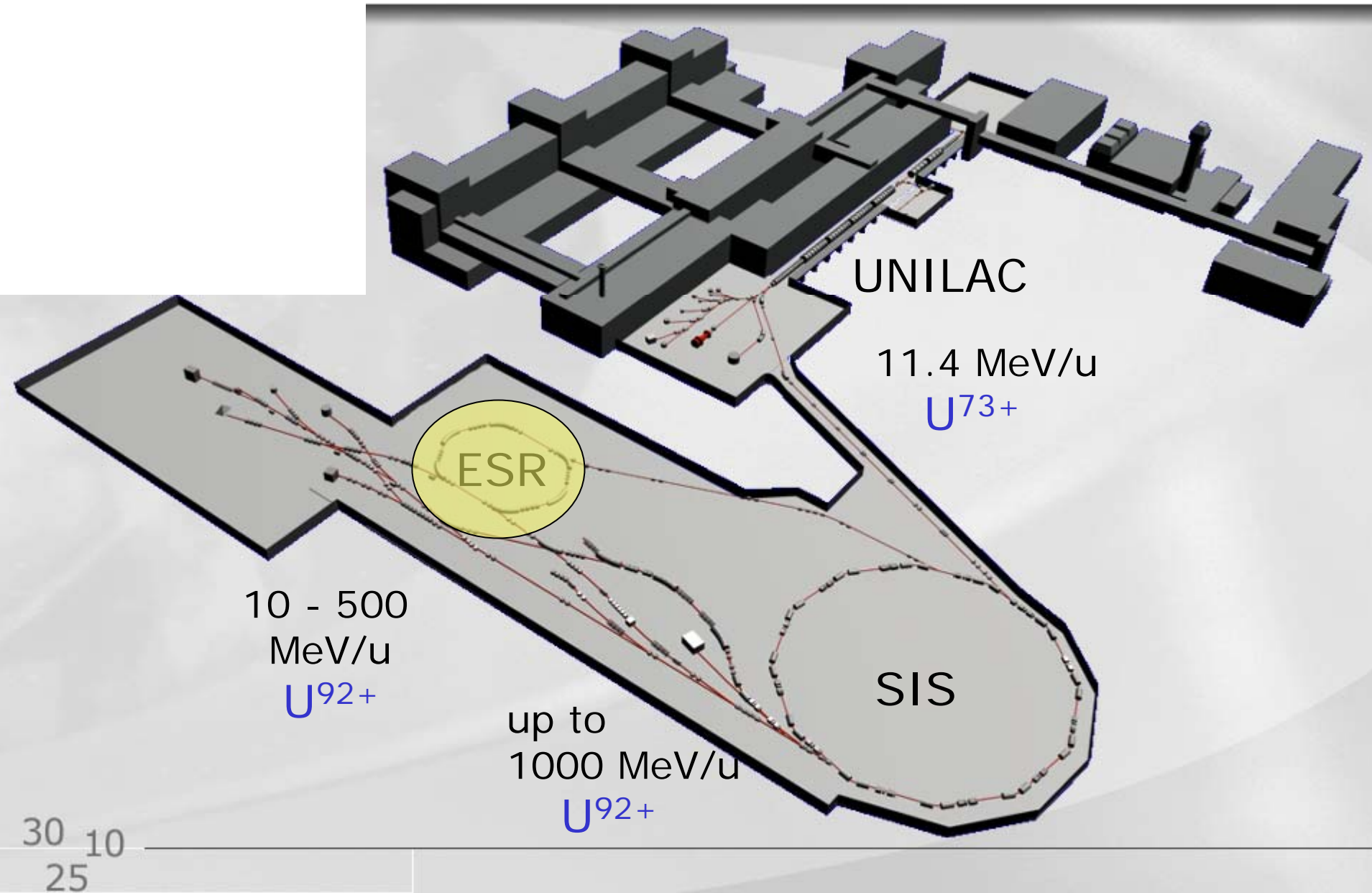


**200 keV electron energy (ions at rest)**

**Charge-state distribution for Uranium**

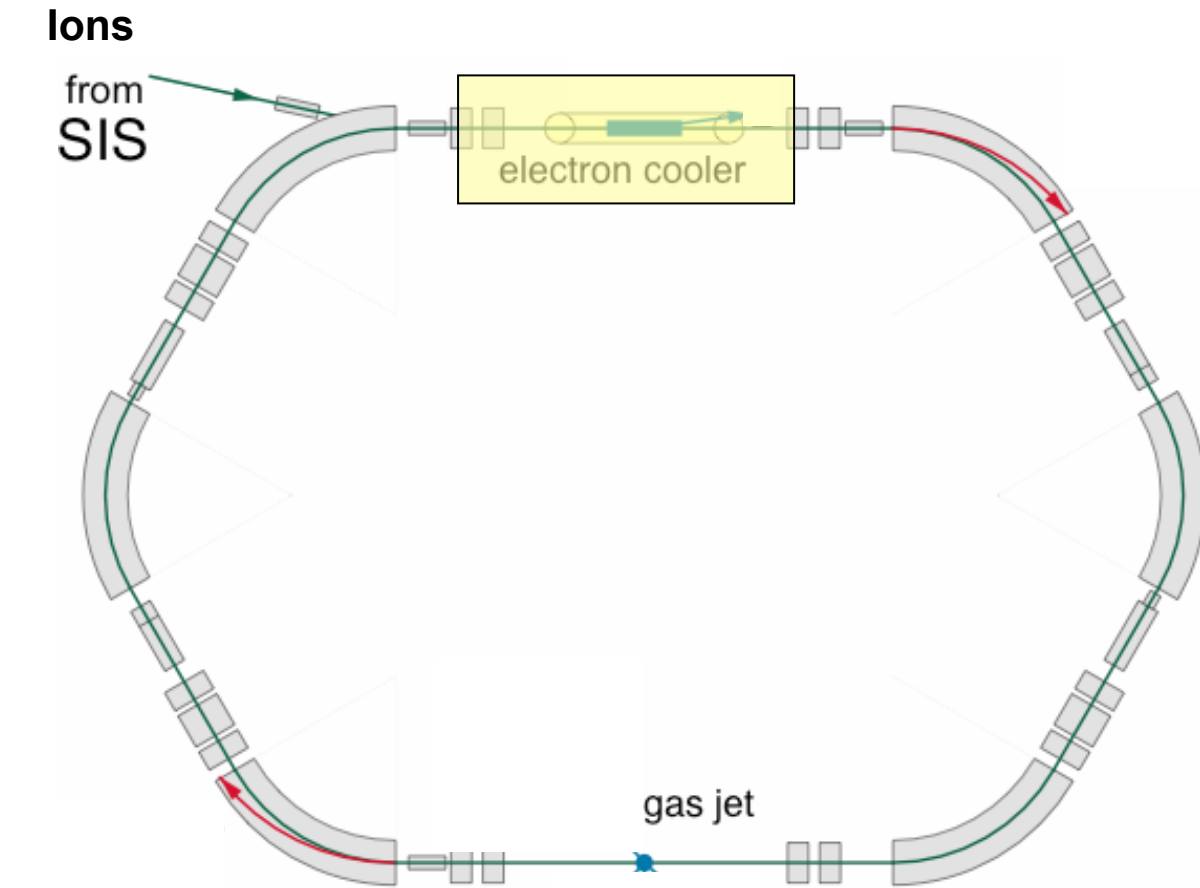


# GSI-ACCELERATOR FACILITY





# Experiments at the ESR



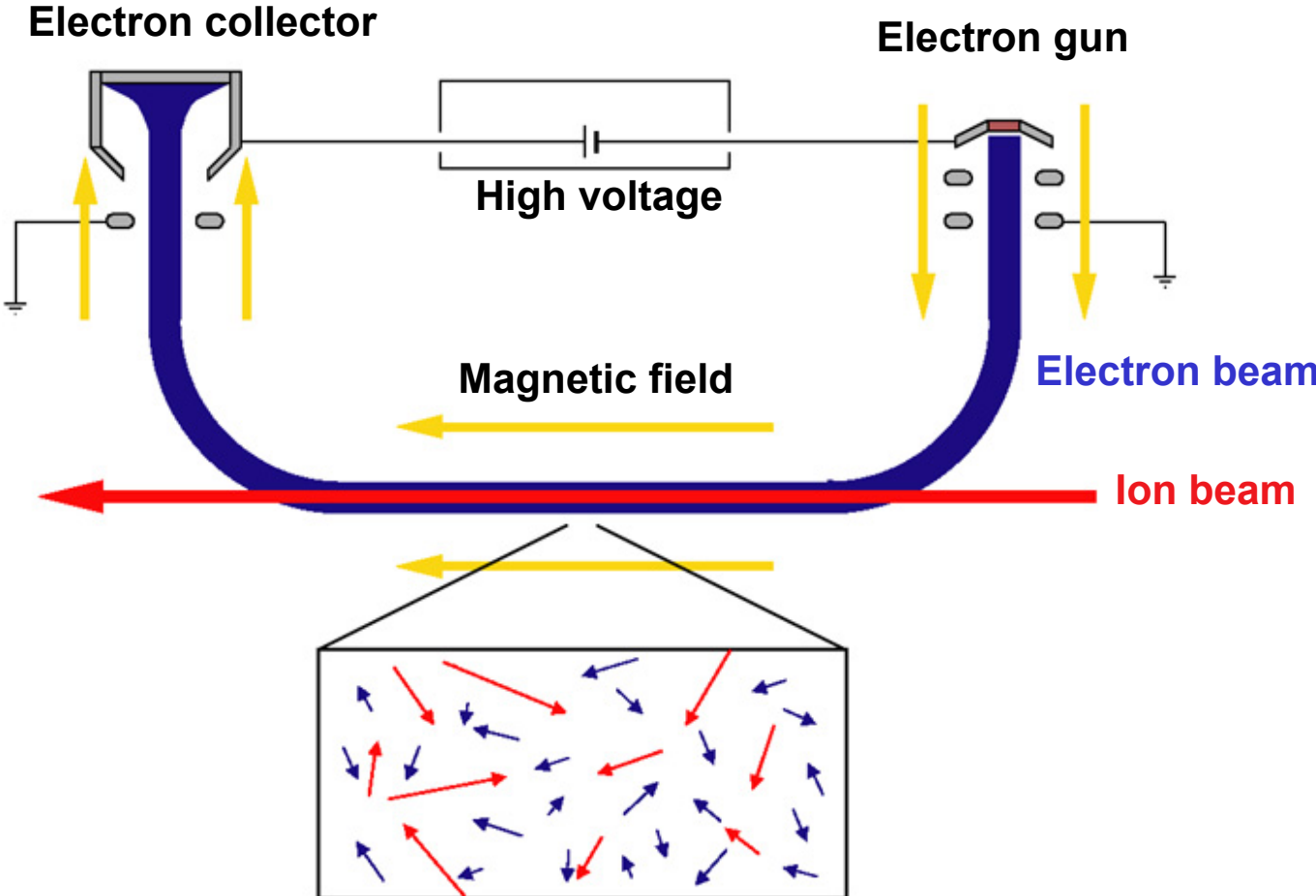
$\beta \approx 0.65$

$E \approx 300 \text{ MeV/u}$

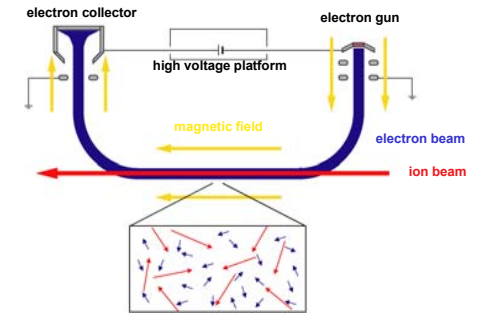
Revolution  
Frequency  
 $f: \approx 10^6 \text{ 1/s}$

**ESR**  
circumference: 108 m  
number of Ions:  $10^8$

# COOLED HEAVY-ION BEAMS



# COOLED HEAVY-ION BEAMS



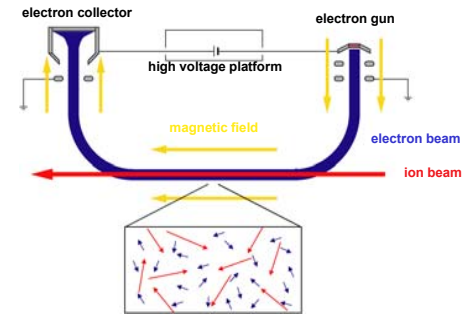
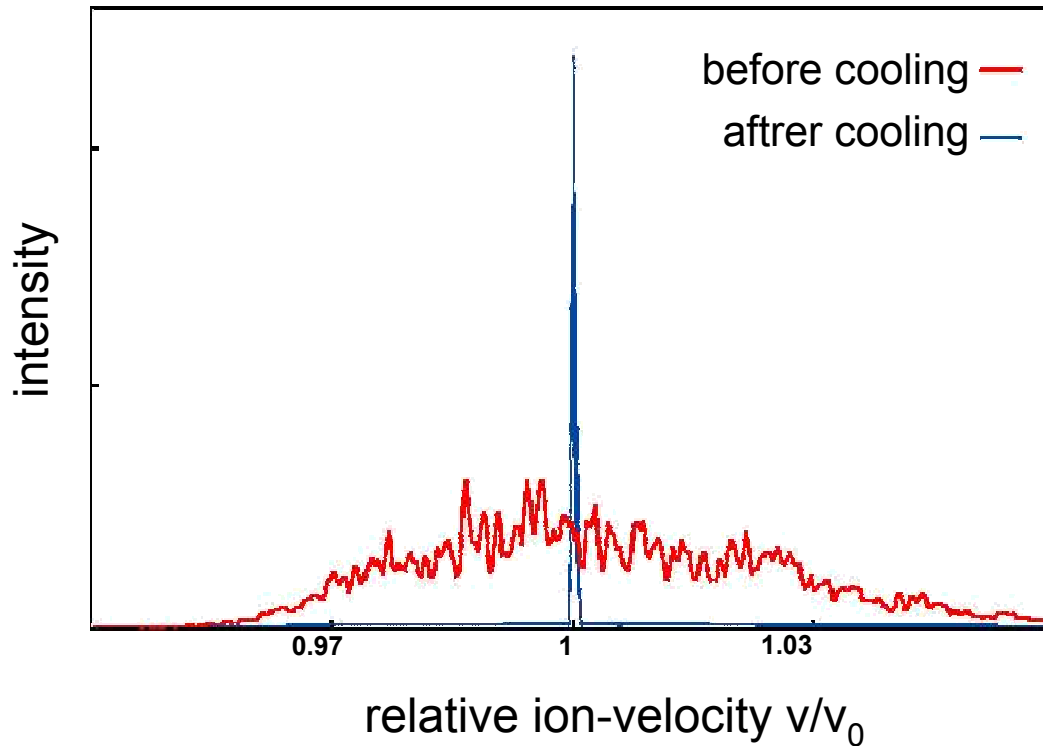
## *Electron cooler*

**Voltage: 5 to 200 kV**

**Current: 10 to 1000 mA**

**2.5 m interaction zone**

# COOLED HEAVY-ION BEAMS

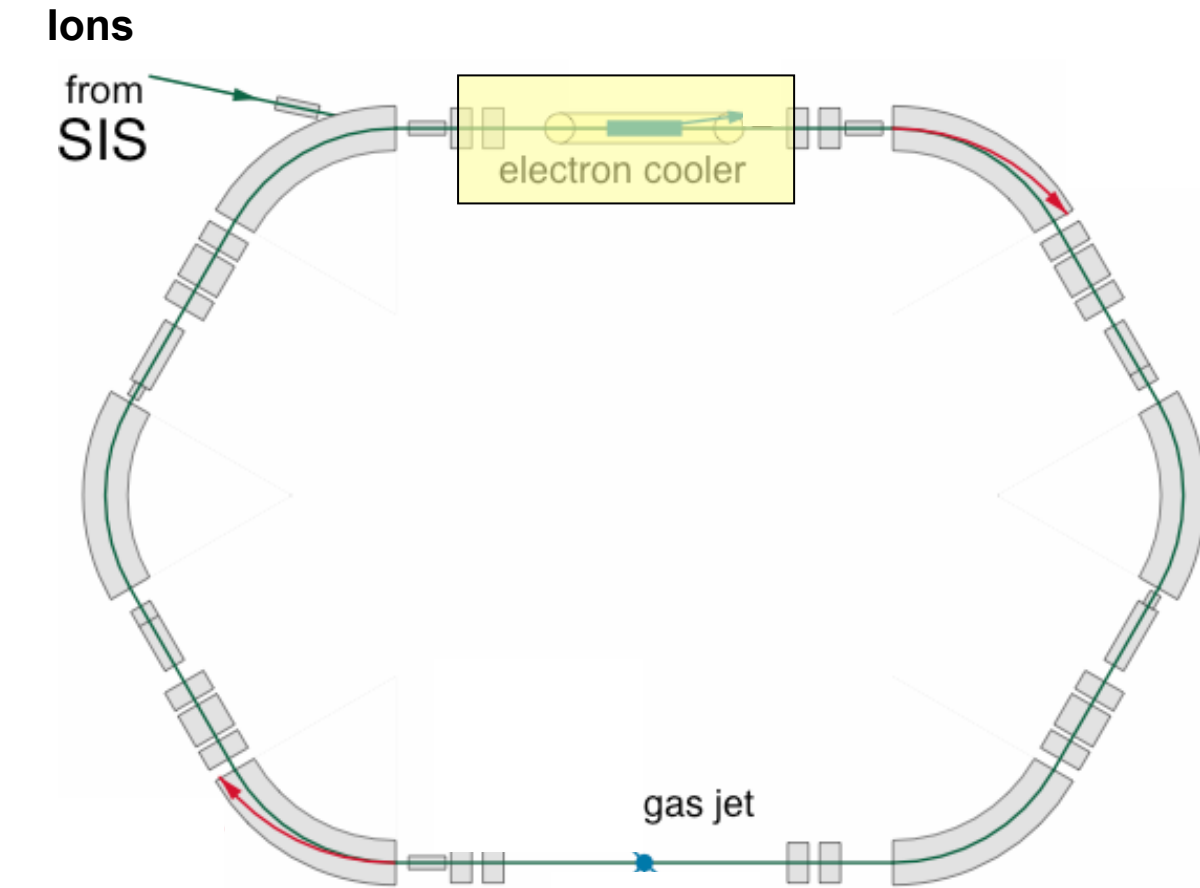


*ions interact  $10^6$  1/s with the collinear cold electron beam*

## properties of cold ion beams

momentum width  $\Delta p/p : 10^{-4} - 10^{-5}$   
size 2 mm

# Experiments at the ESR



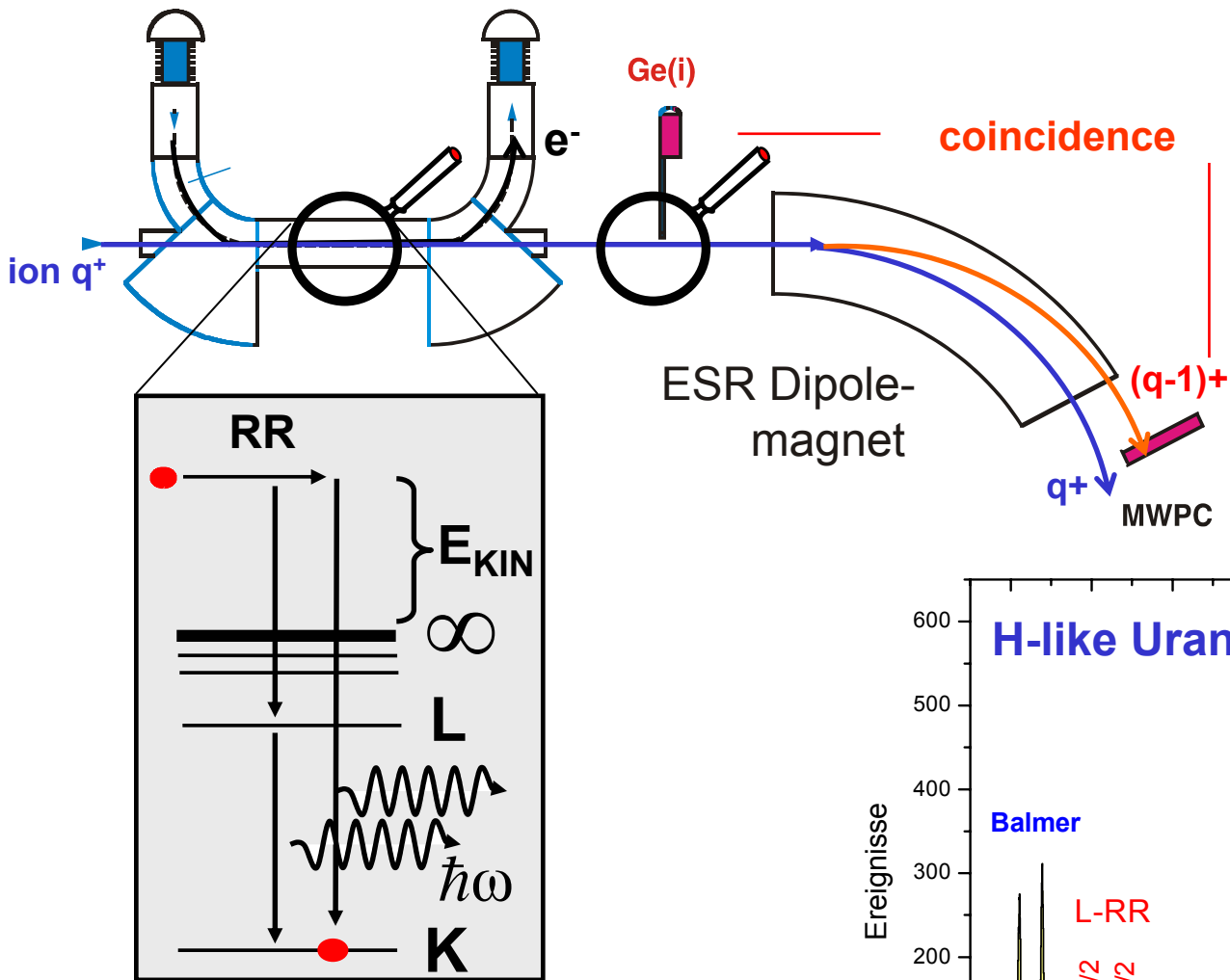
$\beta \approx 0.65$

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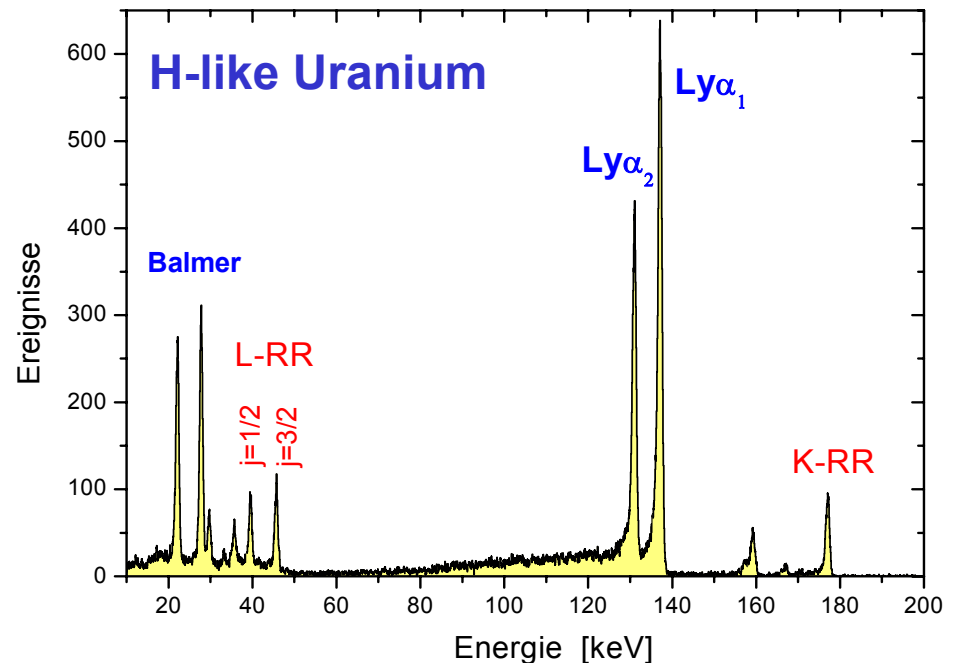
Revolution  
Frequency  
 $f: \approx 10^6 \text{ 1/s}$

**ESR**  
circumference: 108 m  
number of Ions:  $10^8$

# 0° Spectroscopy at the Electron Cooler



- maximum blueshift  
 $\beta \approx 0.29 \Rightarrow E_{lab} \approx 1.43 \times E_{proj}$
- $\Delta\theta_{LAB}$  not critical,  
 minimum Doppler broadening
- uncertainty due to  $\Delta\beta$  maximum



## Relativistic Doppler-Transformation

$$E_{\text{lab}} = \frac{E_{\text{proj}}}{\gamma \cdot (1 - \beta \cdot \cos\theta_{\text{lab}})}$$

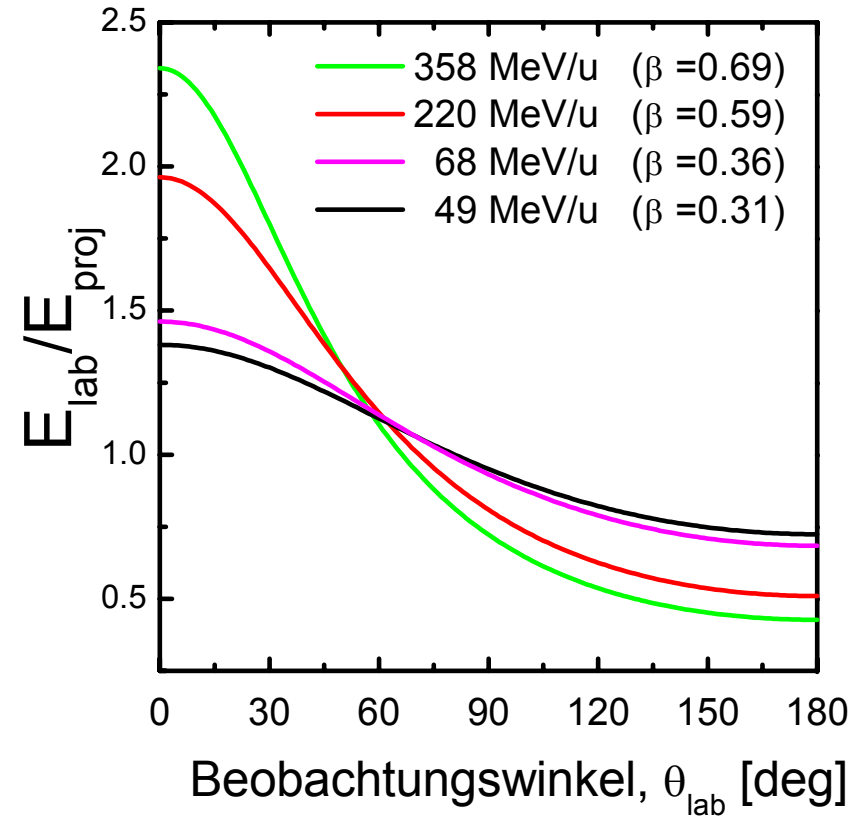
$E_{\text{lab}}$ : Photon energy in the laboratory frame

$E_{\text{proj}}$ : Photon energy in the Emitter frame

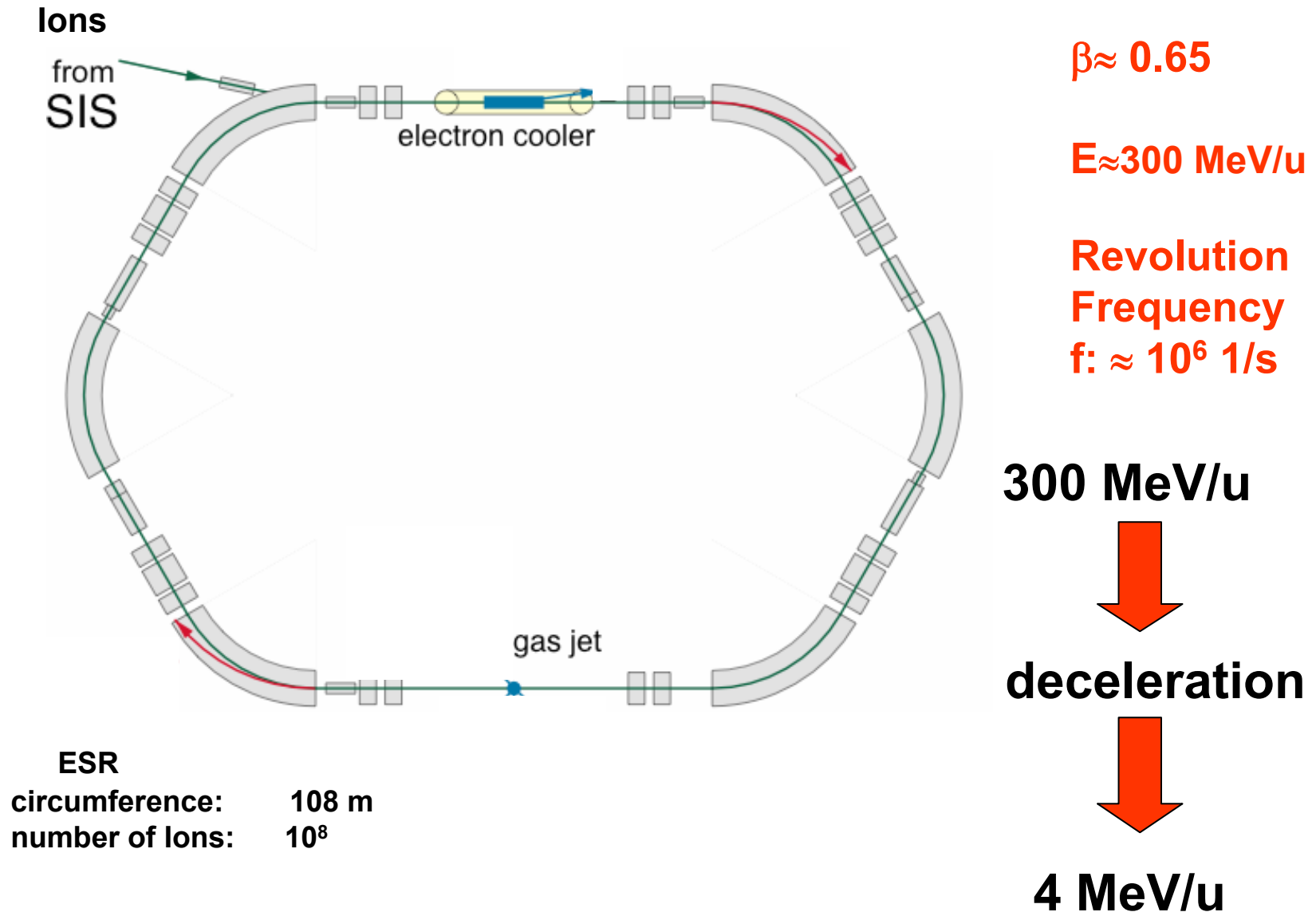
### Doppler correction

*Strong dependence on velocity  $v$   
and on observation angle  $\theta_{\text{LAB}}$*

$$\gamma = \frac{1}{\sqrt{1 - \beta^2}}; \beta = \frac{v}{c}$$



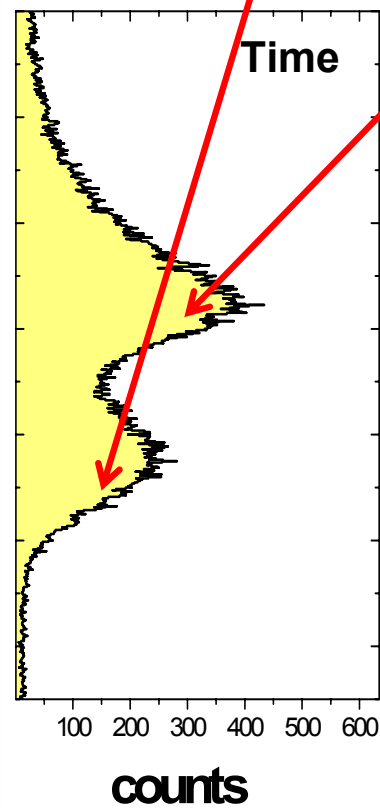
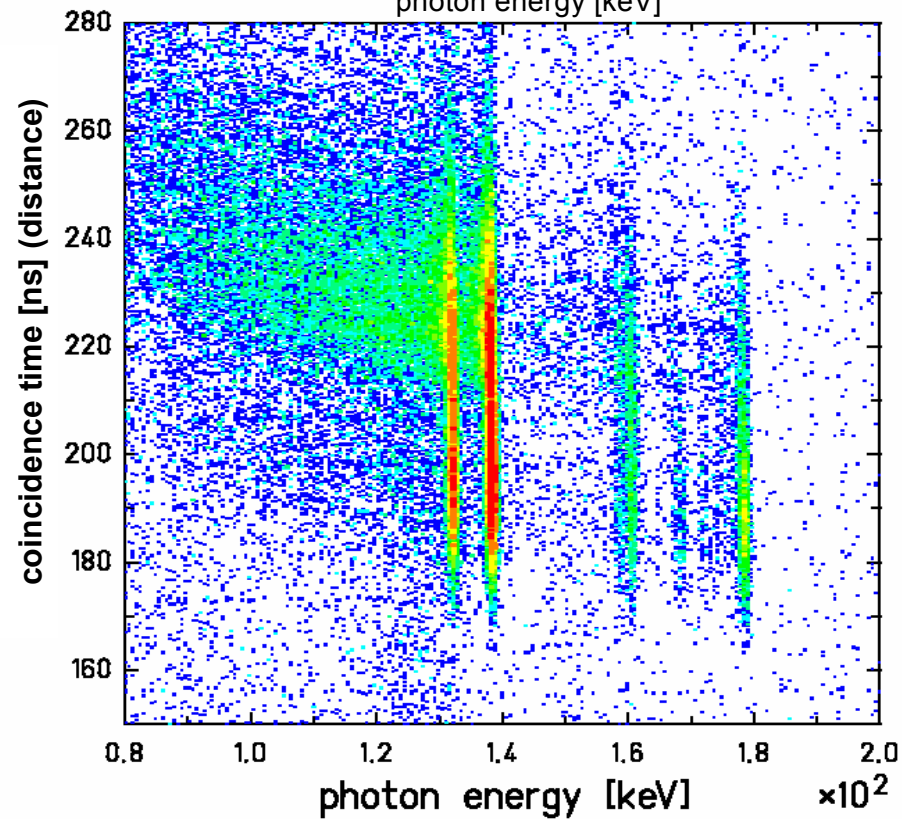
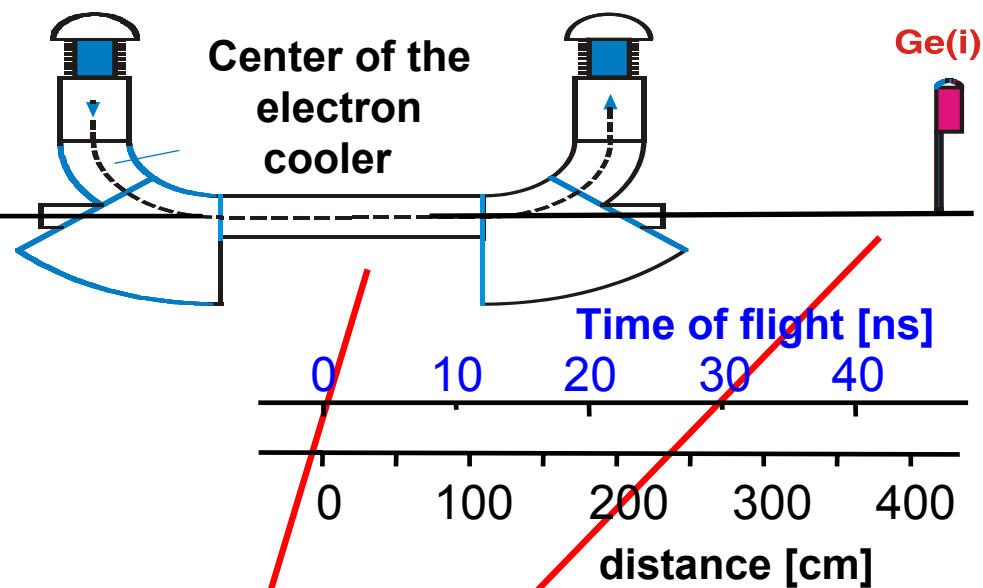
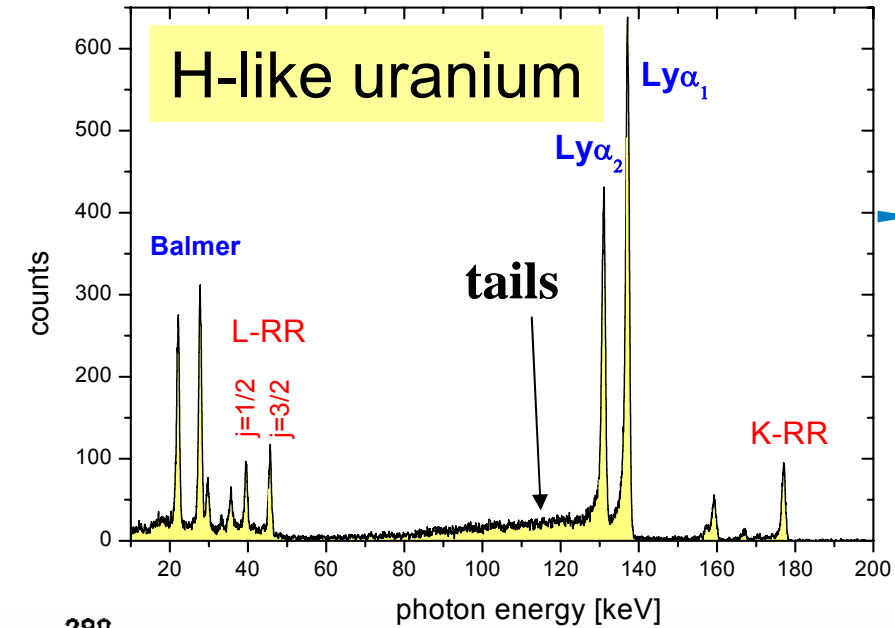
# Experiments at the ESR





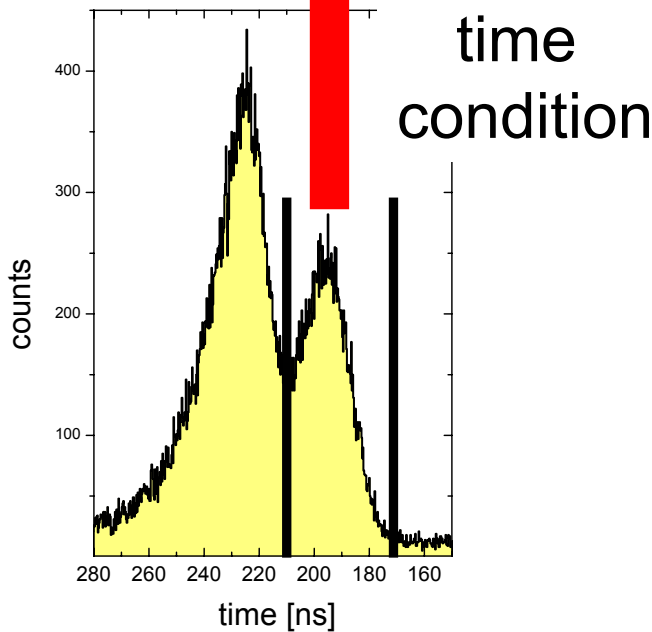
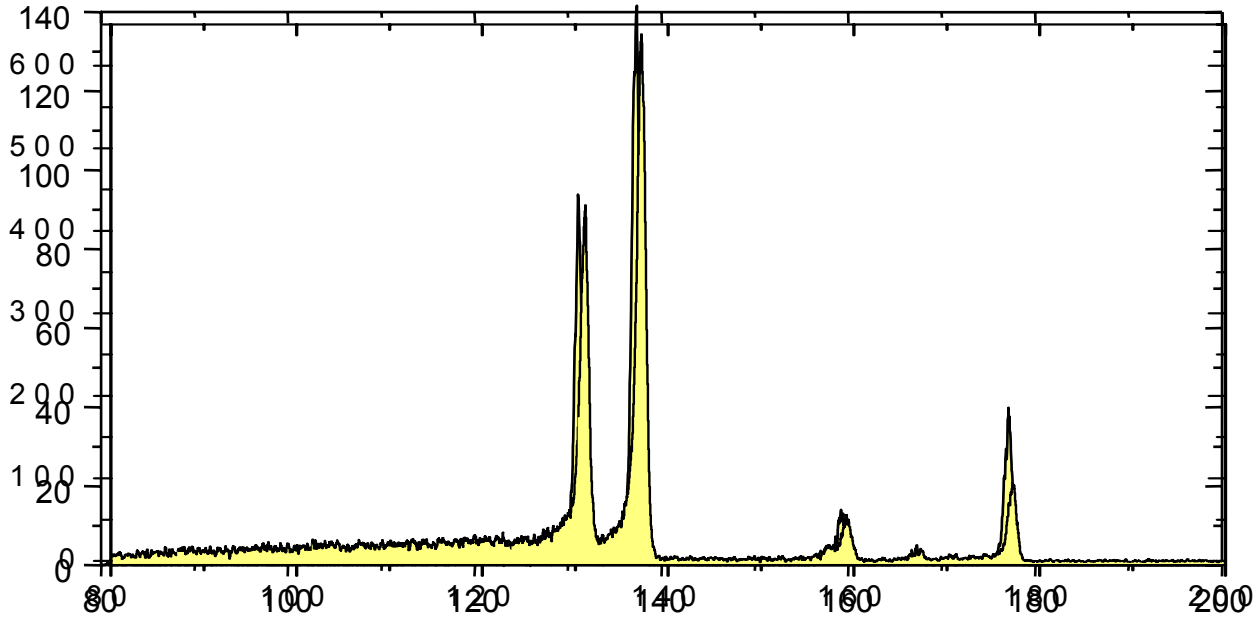
# Ge(i) Detector





Recombination into Rydberg states leads to the delayed Lyman emission, by up to microsecond.

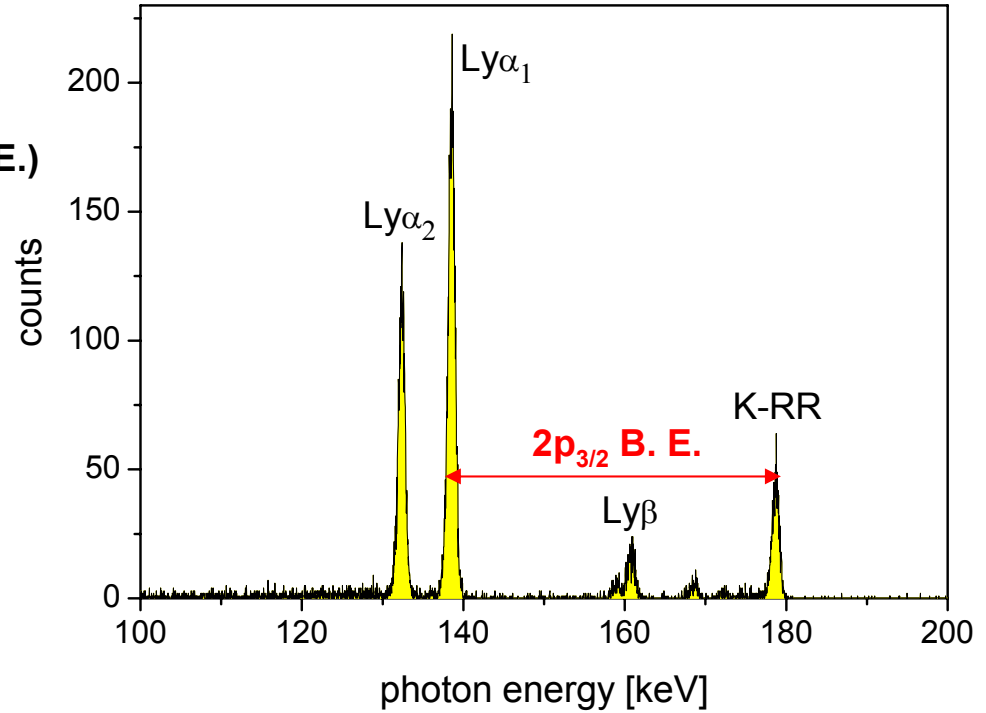
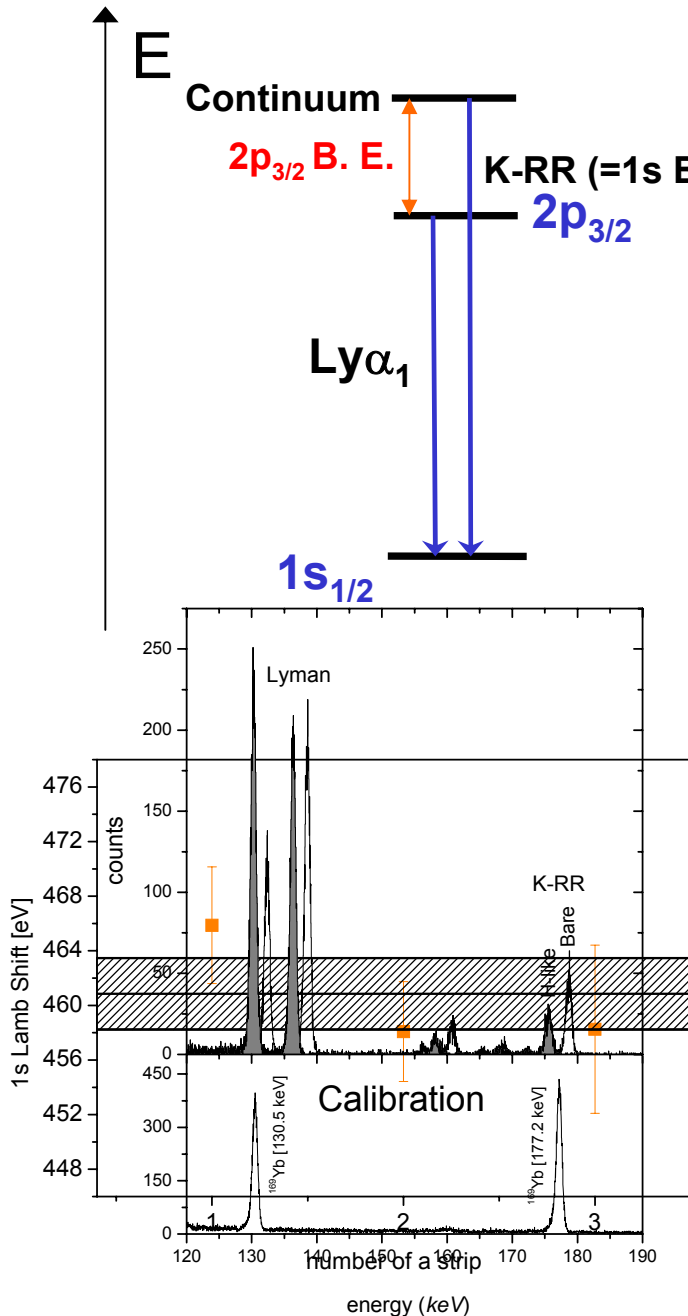
counts



time  
condition

**Tails disappear when  
one applies a proper  
condition to the time  
spectrum**

# The Ground State Lamb Shift in H-like Uranium



**1s Lamb shift in  $U^{91+}$**

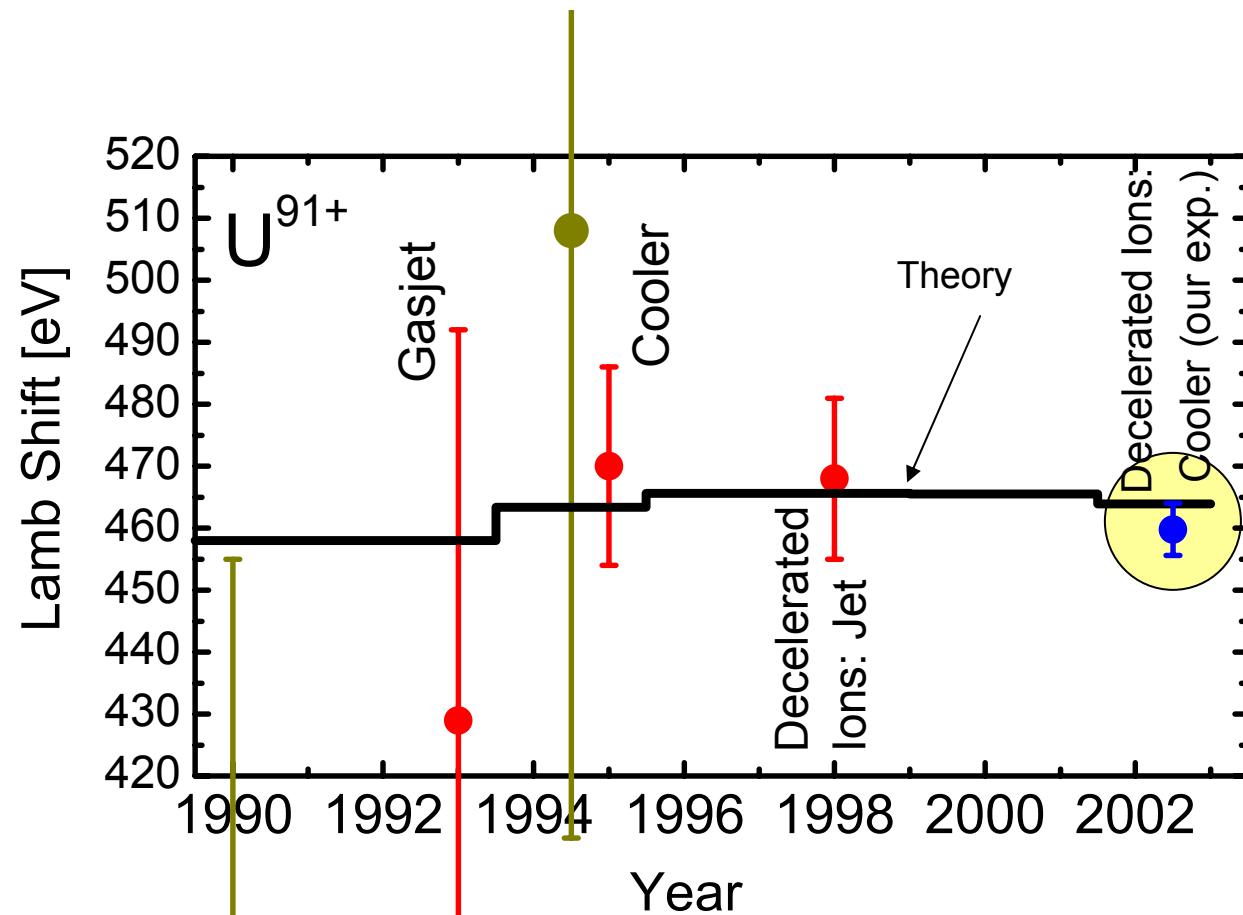
**$460.2 \pm 2.3 \pm 3.5$  eV**

statistical

**4.6 eV**

uncertainty in the  $\beta$

# Experimental Results in Comparison with Theory



**Experiment:** [460.2±4.6 eV](#)

**Theory (Yerokhin et al. 2003):** [464.26±0.5 eV](#)

SE = 355.0 eV, VP = -88.6 eV

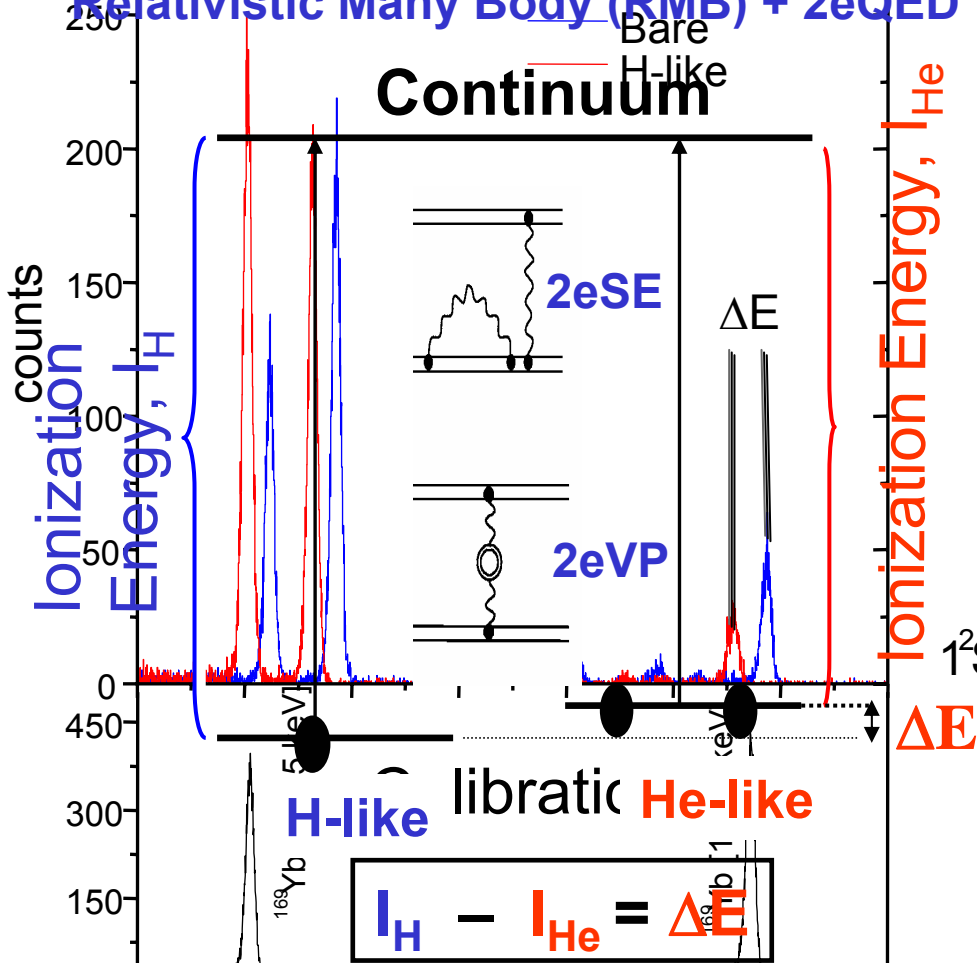
NS = 198.7 eV, HO ~ 1.8 eV

→ 1% sensitivity to the 1s Lamb shift  
4% Sensitivity to the self energy  
15% Sensitivity to the vacuum polarization

# Relative Measurement of the Two-electron Contribution to the Ground State Binding Energy in He-like Uranium

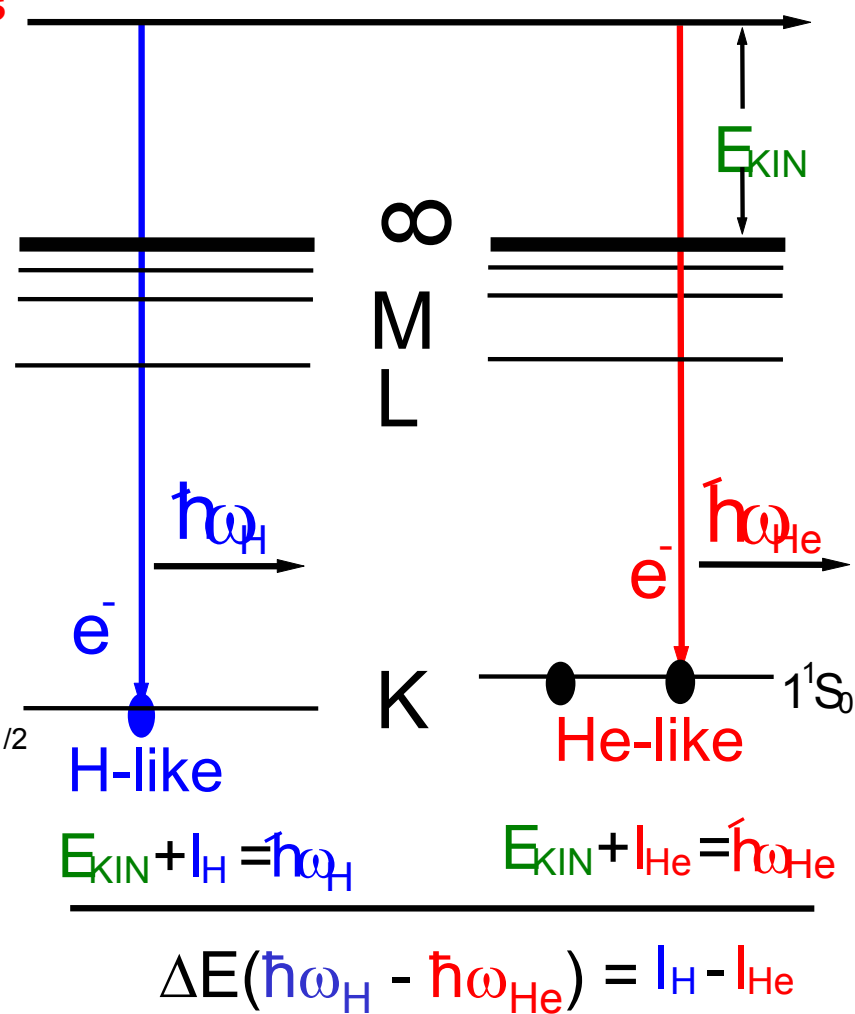
## Electron-Electron Interaction in Strong Fields

Relativistic Many Body (RMB) + 2eQED



$\Delta E$ : Two-Electron Contribution to the Ionization potential in the He-like System energy (keV)

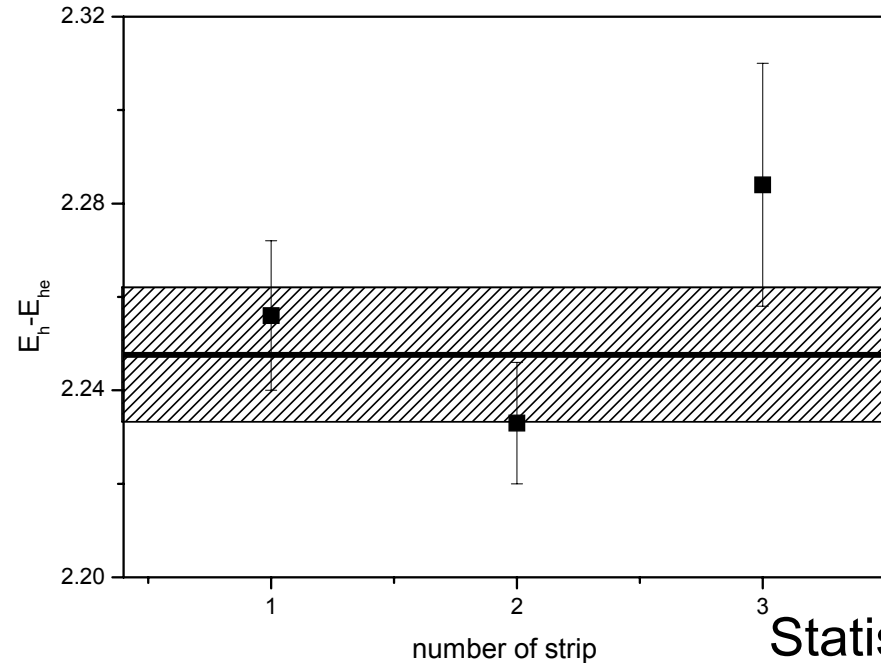
Electron beam



Relative measurement  
All one electron contributions cancel out (e.g. finite nuclear size)

# Relative Measurement of the Two-electron Contribution to the Ground State Binding Energy in He-like Uranium

- Data subdivided into several groups
- Checked for consistency



**$2248 \pm 9 \text{ eV}$**

Statistical uncertainty for  $\Delta E$ : 9 eV

~~Uncertainty caused by doppler shift:~~

**The result for the splitting  $\Delta E$  is  $2248 \pm 9 \text{ eV}$**



## Experimental Results in Comparison with Theory

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**ESR (First experiment for the two-contribution  $U^{90+}$ ):** 2248(9) eV

**Theory (Yerokhin et al. 1997):** 2246 eV

2 photon exchange  $\sim 14$  eV 2eSE  $\sim 9.7$  eV

**Super-EBIT (First measurement of the 2e contribution)**

(Marrs et al, 1995)

**But!! Results limited by counting statistics ( $Z < 83$ )**

As an example; for **Bismuth** an uncertainty of 14 eV has been achieved for the value of 1876 eV. 2eQED  $\sim 6.7$  eV

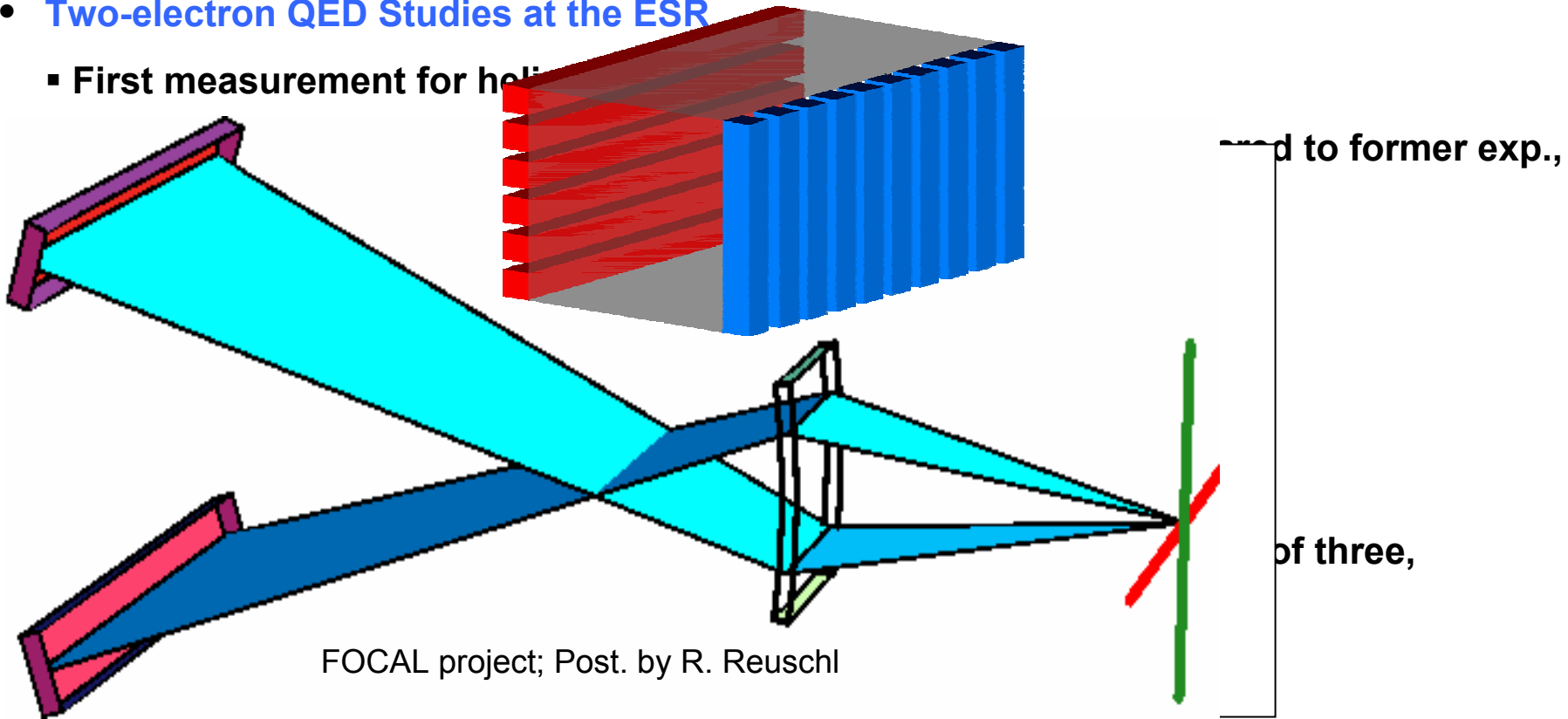
- Our result agrees well with the most recent theoretical value.
- The experimental uncertainty is of the order of two-electron QED contributions.
- Compared to the former studies at Super-EBIT in Livermore, we could substantially improve the statistical accuracy and extend studies to the higher-Z regime.



# SUMMARY AND OUTLOOK

- **Two-electron QED Studies at the ESR**

- First measurement for helicity



Simultaneous measurement at 0 and 180 deg.

High resolution detection devices; spectrometer + PSG, calorimeter

Excellent agreement between experimental results and theory for both cases

*'No test can prove a theory but any single test can disprove it.'*

*Karl Popper*