

Präzisionsexperimente am wasserstoffähnlichen Uran

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Einführung

Die atomare Struktur im hohen Z Bereich

**QED-Beitrag zum Grundzustand
in schweren H-ähnlichen Ionen**

Die 1s Lamb-Verschiebung

**QED-Beitrag zum Grundzustand
in schweren He-ähnlichen Ionen**

Zwei-Elektronen QED

Zusammenfassung und Ausblick

Collaboration

Experiment

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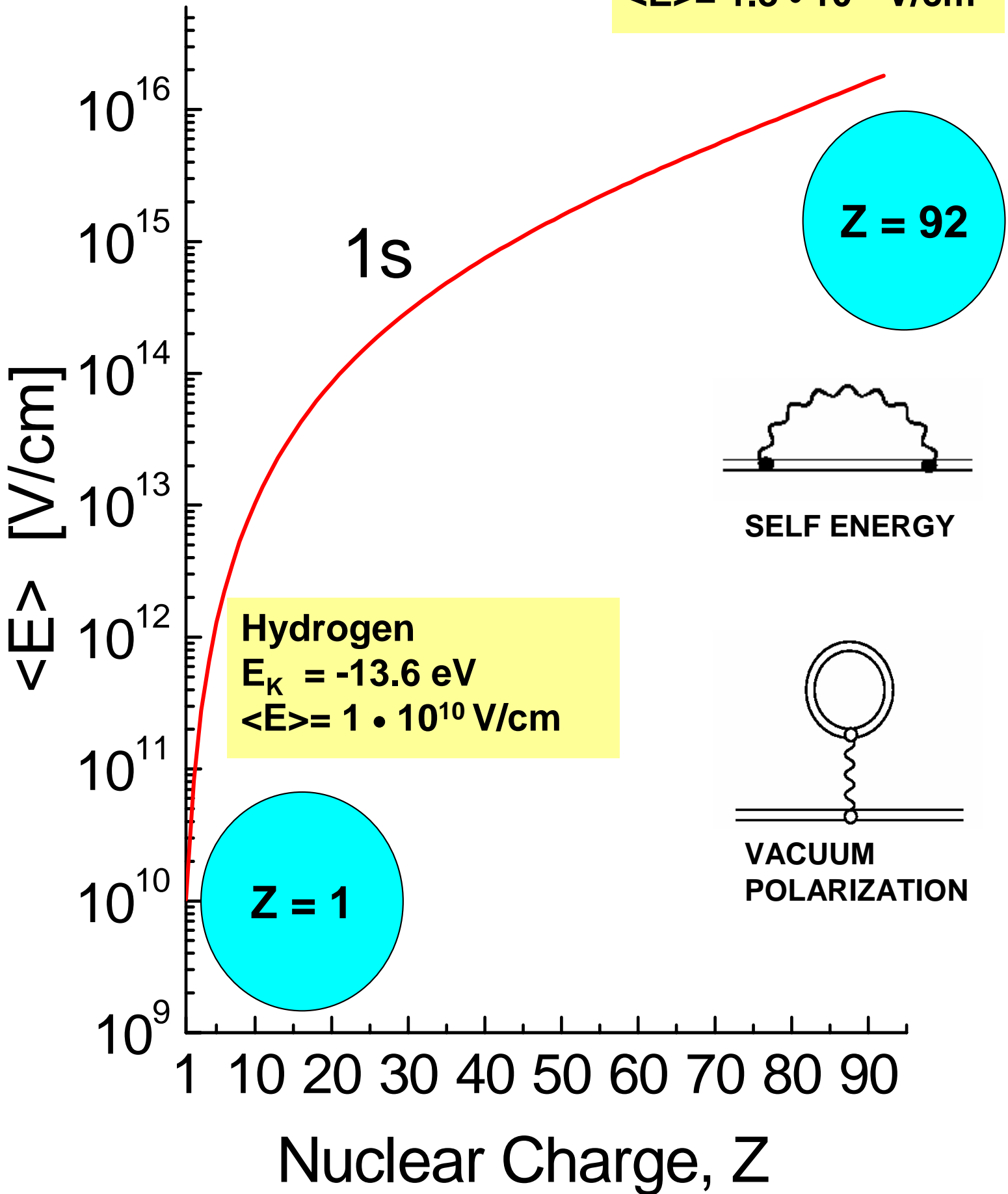
GSI-Darmstadt, Germany

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Atomic Physics in Extremely Strong Coulomb Fields

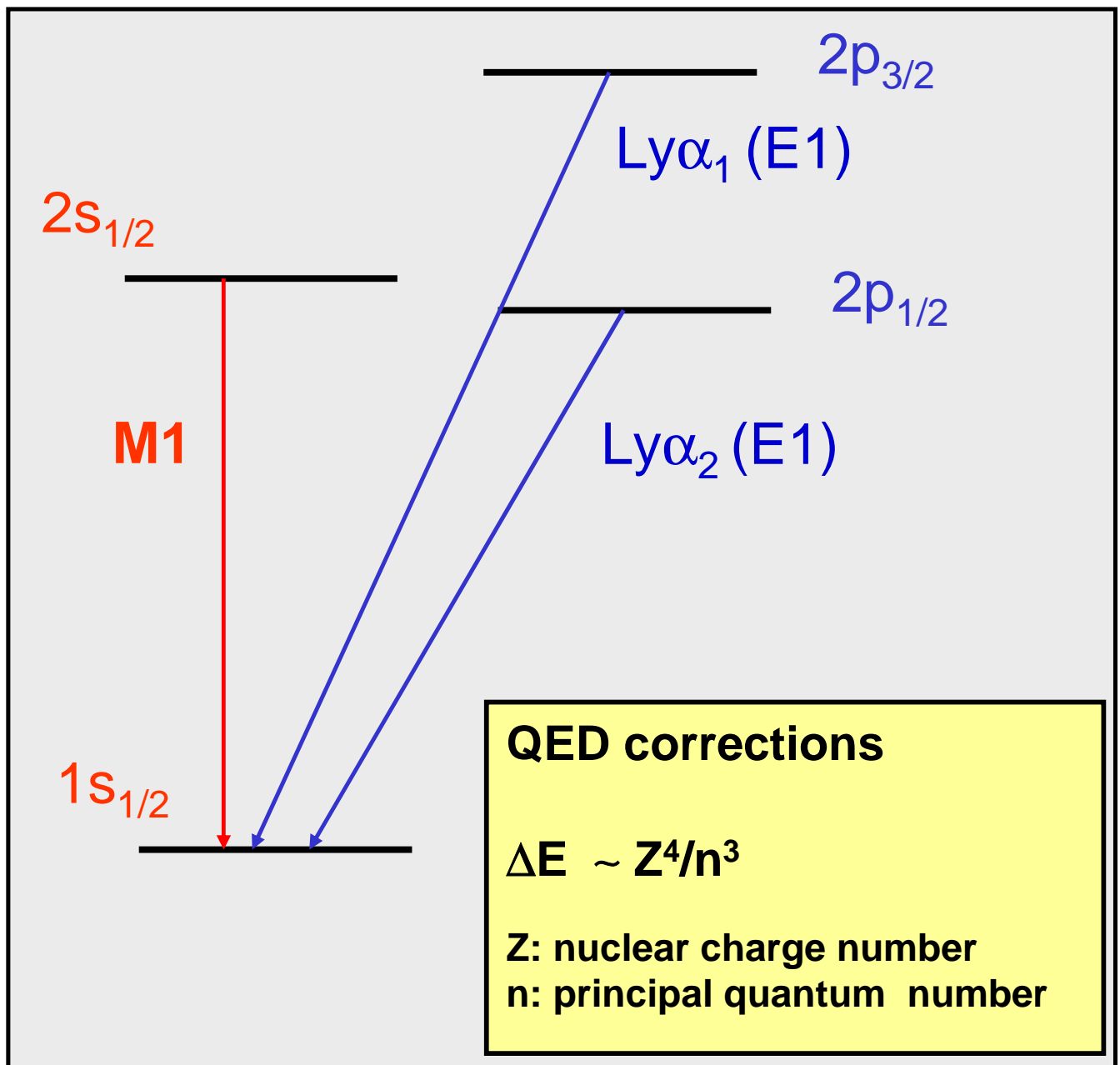
H-like Uranium

$E_K = -132 \cdot 10^3 \text{ eV}$
 $\langle E \rangle = 1.8 \cdot 10^{16} \text{ V/cm}$



1s-ground state: increase of the electric field strength by six orders of magnitude

The Structure of One-Electron Systems

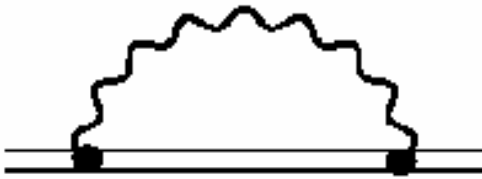


Atomic systems at high-Z

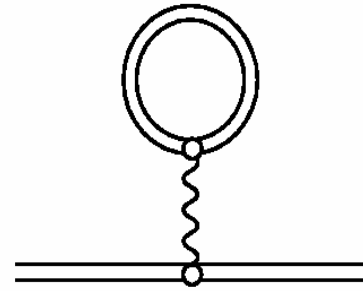
- Large relativistic effects on energy levels and transition rates (e.g. shell and subshell splitting)
- Large QED corrections
- Transition energies close to 100 keV

Bound-State QED: 1s Lamb Shift

Self energy



Vacuum polarization



Sum of all corrections, leading to deviations from the Dirac theory for a point like nucleus

U^{92+}

SE

VP

NS

355.0 eV

-88.6 eV

198.7 eV

$$\Delta E = \alpha/\pi (\alpha Z)^4 F(\alpha Z) m_e c^2$$

Low Z-Regime: $\alpha Z \ll 1$

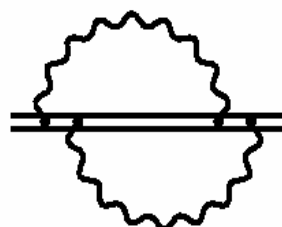
$F(\alpha Z)$: series expansion in αZ

High Z-Regime: $\alpha Z \approx 1$

$F(\alpha Z)$: series expansion in αZ

not appropriate

Goal:



± 1 eV

Test of Bound-State QED at high-Z



Experiments

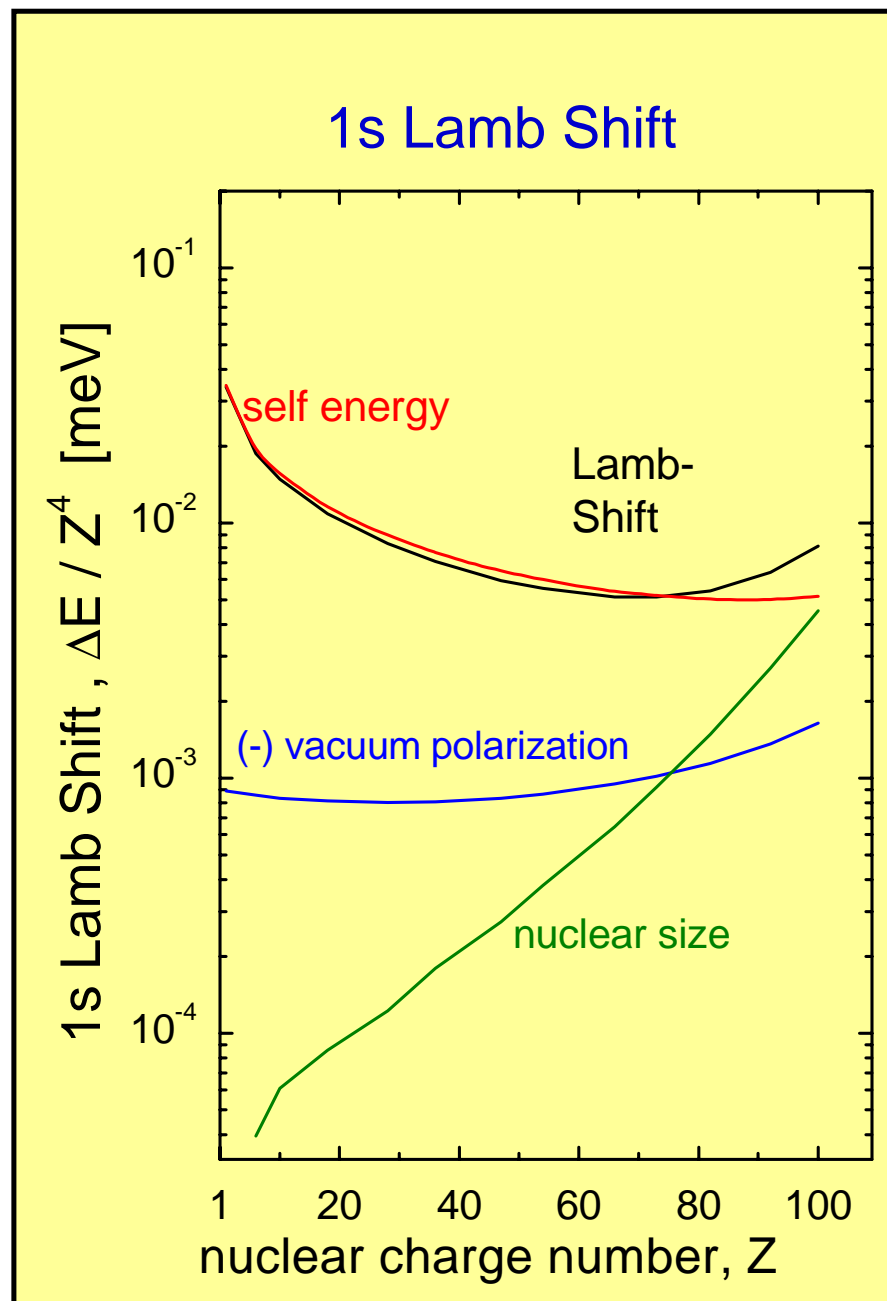
1s Lamb Shift

hyperfine-structure

g-factor of bound electrons

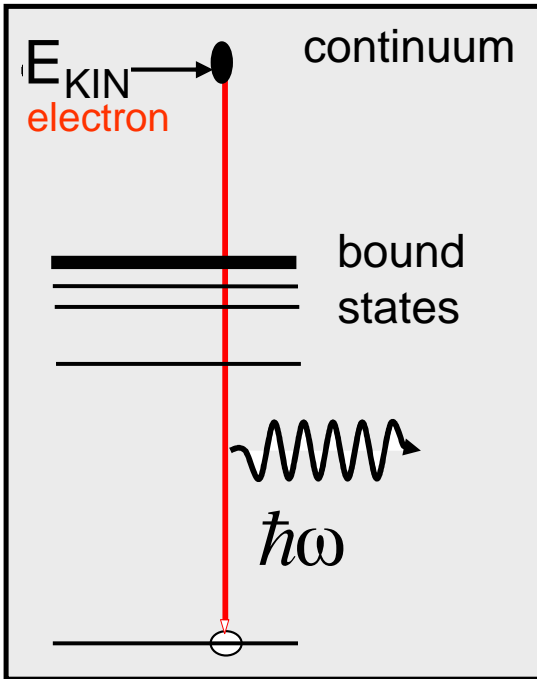
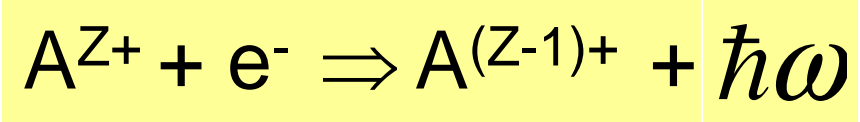
2s-2p transitions in Li-like heavy ions

2eQED for He-like ions



Electron Pickup Processes of HCl in Collisions with Electrons (Dynamic Processes)

Radiative Recombination/Electron Capture

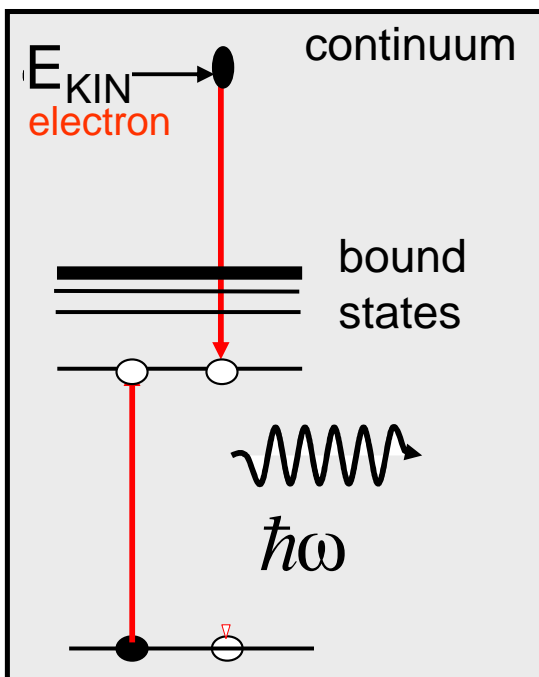


- **Electron capture into a bound ionic state by emission of a photon**

$$\hbar\omega = E_B + E_{KIN}$$

- **Time-reversed photionization**
- **Only possible capture/recombination process for bare ions colliding with electrons**

Dielectron Recombination/Electron Capture

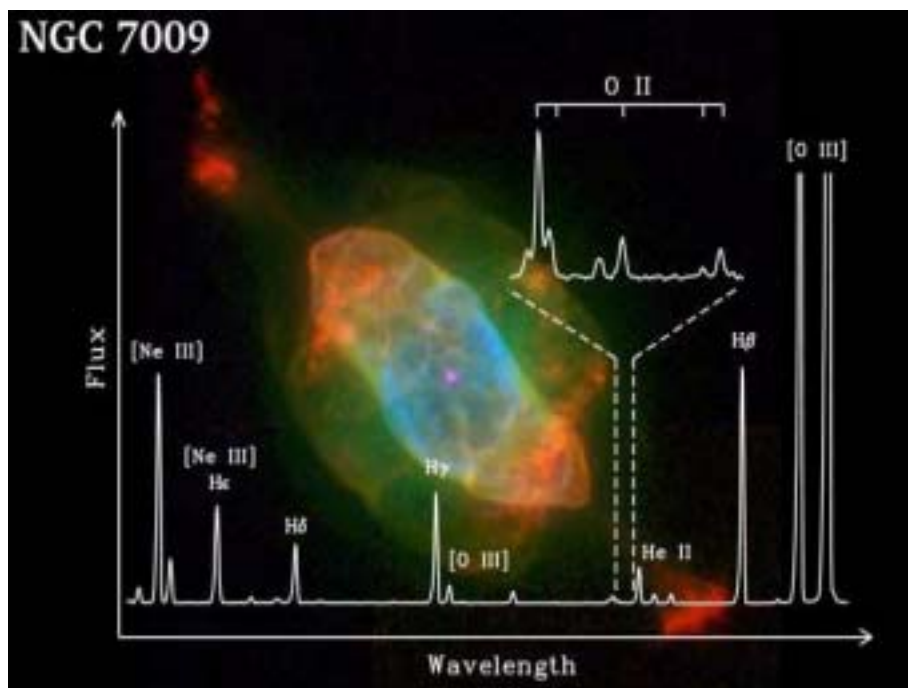


- **Resonant (non-radiative) capture of an electron into a bound state**
- **Time-reversed Auger process**
- **Important charge exchange process for multi-electron ions**

Recombination Processes: Elementary Atomic Physics Process and of Outmost Importance when Dealing with Highly Ionized Matter

e.g.

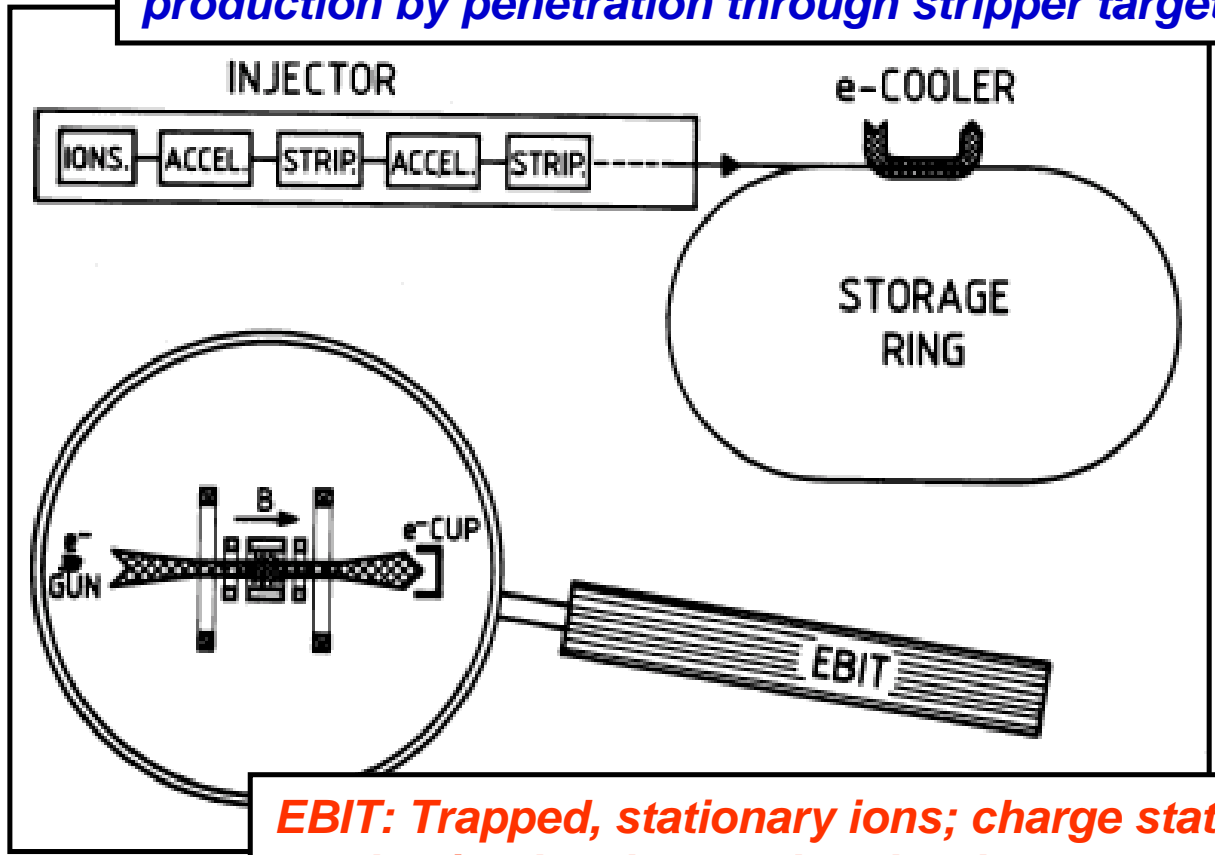
- **ion sources**
- **accelerator**
- **charge state development /distributions of HCl in matter**
- **photon emission and absorption characteristic of plasma sources**
- **astrophysics**



The spectra of ionized planetary Nebulae are dominated by strong H and He recombination lines, emitted following structure

Production of Highly Charged Heavy Ions

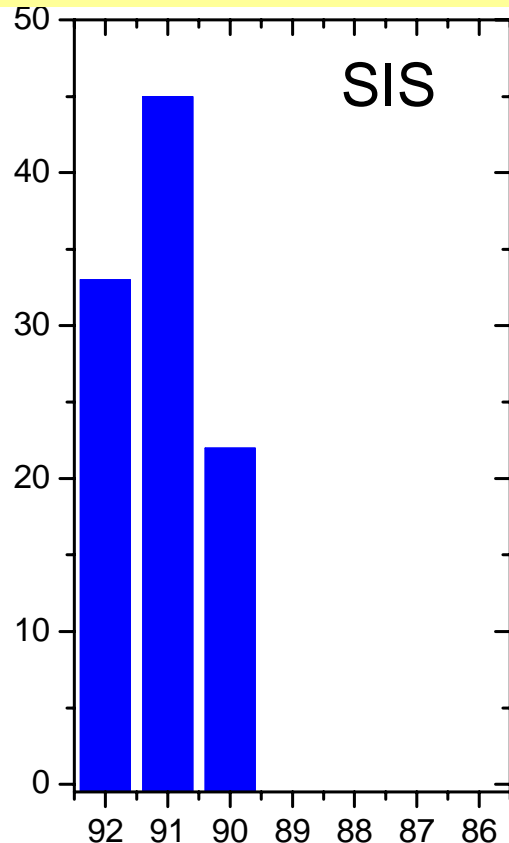
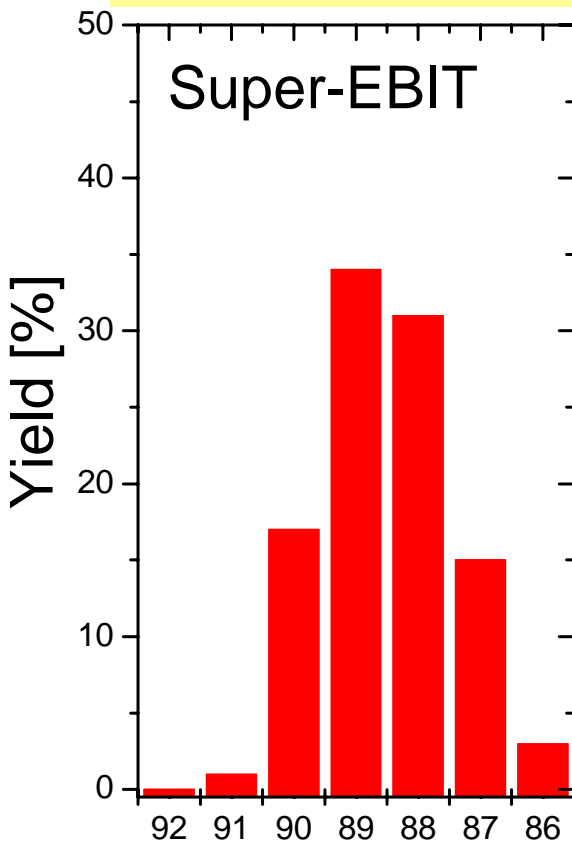
Accelerator: Fast moving ions, charge state production by penetration through stripper targets



EBIT: Trapped, stationary ions; charge state production by electron bombardment

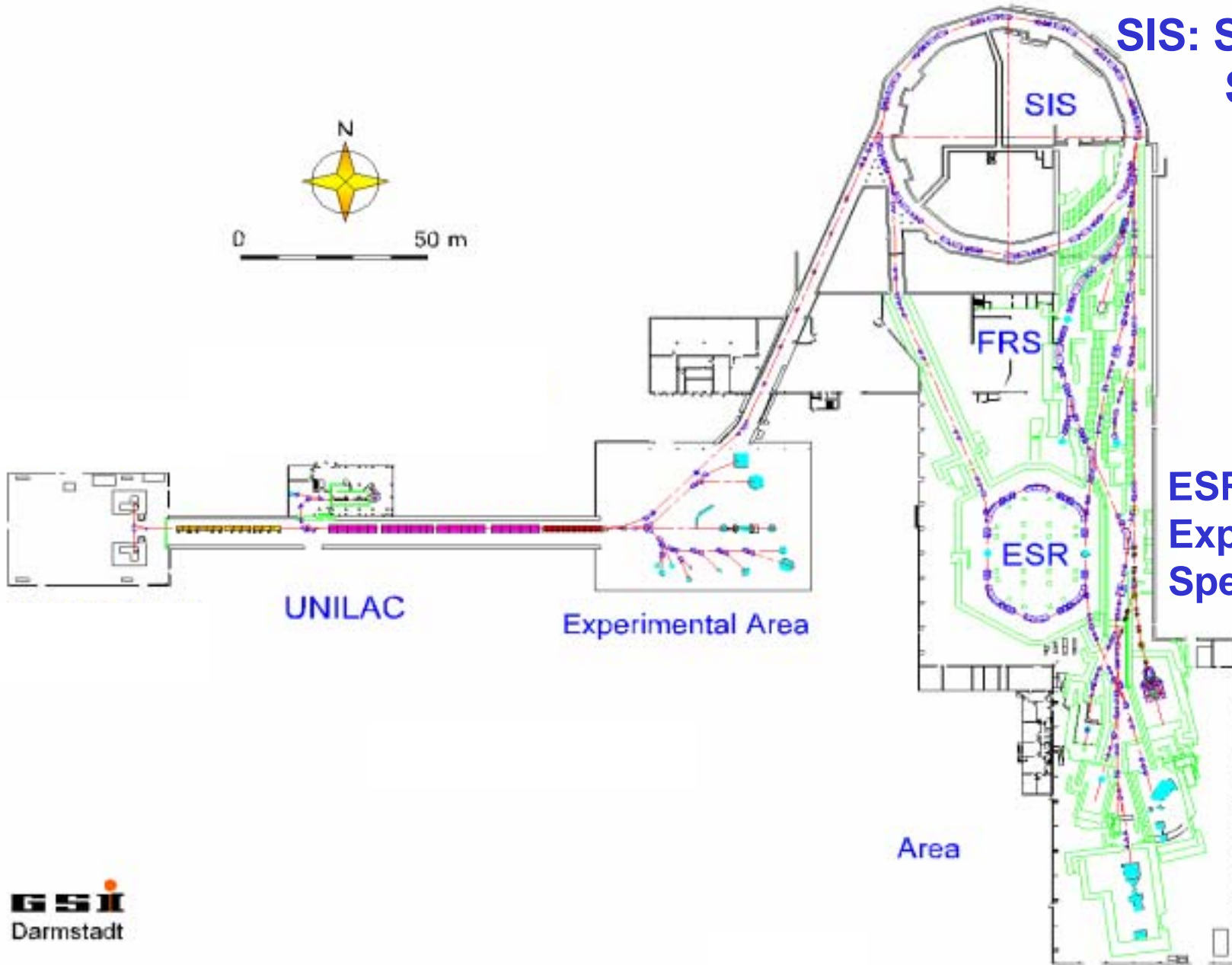
Charge State Distributions for Uranium

**200 keV electron energy
(ion at rest)**



300 MeV/u ($\beta \approx 0.65$)

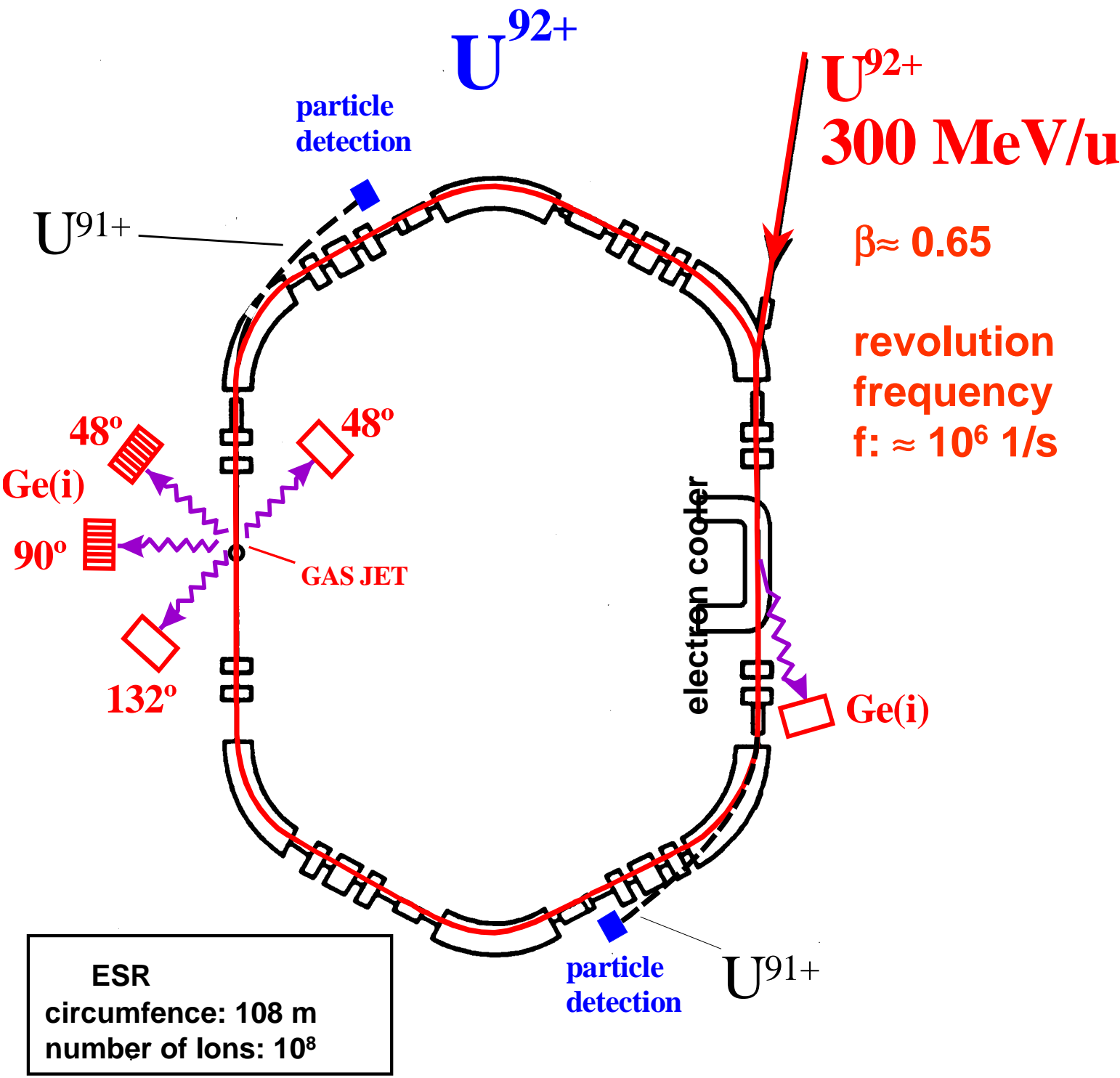
charge state Q



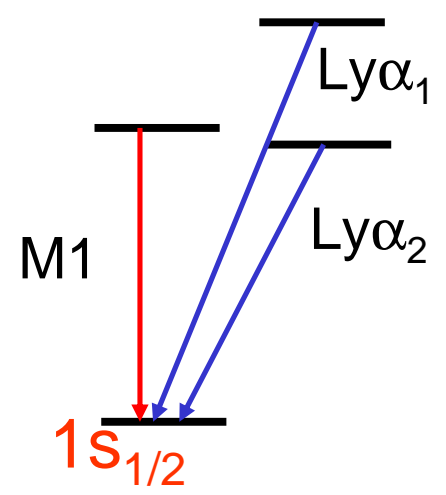
**SIS: Schwerionen
Synchrotron**

**ESR:
Experimentier
Speicherring**

Lamb-Shift Studies for High-Z Ions: X-ray Spectroscopy at the ESR Storage Rings



At the ESR, production of characteristic x-rays by electron capture into the bare ions (electron cooler or jet-target)



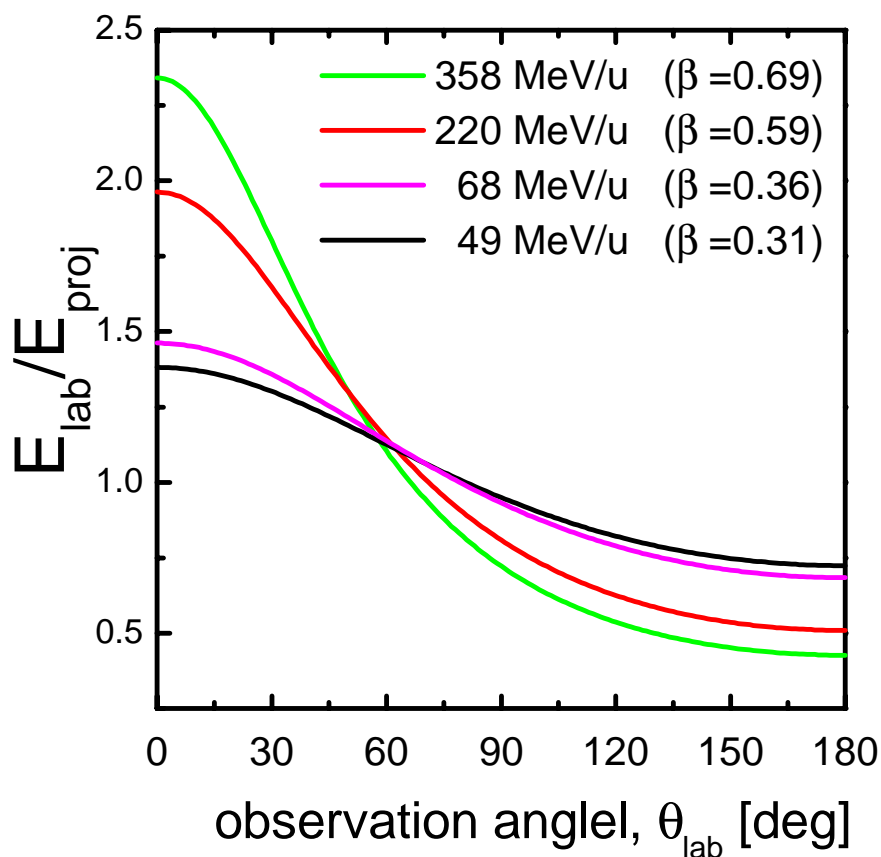
The Experimental Challenge

Relativistic Doppler-Transformation

$$E_{\text{lab}} = \frac{E_{\text{proj}}}{\gamma \cdot (1 - \beta \cdot \cos\theta_{\text{lab}})}$$

E_{lab} : Photon energy in the laboratory system

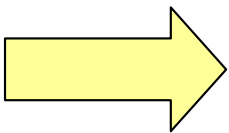
E_{proj} : Photon energy in the emitter system



Doppler-Correction: *Strong dependence on velocity and the observation angle θ_{LAB}*

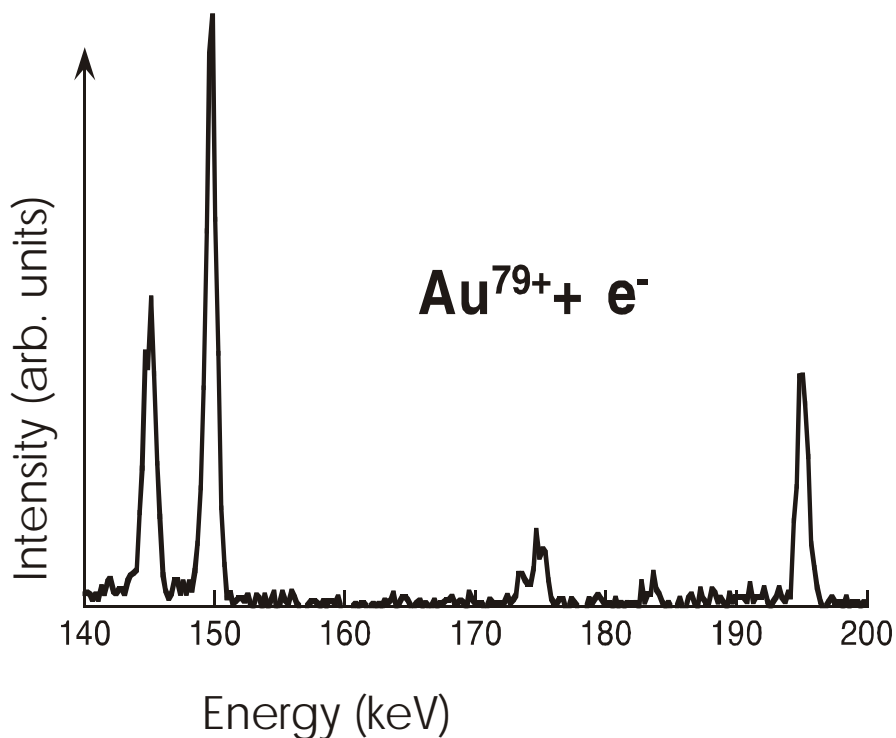
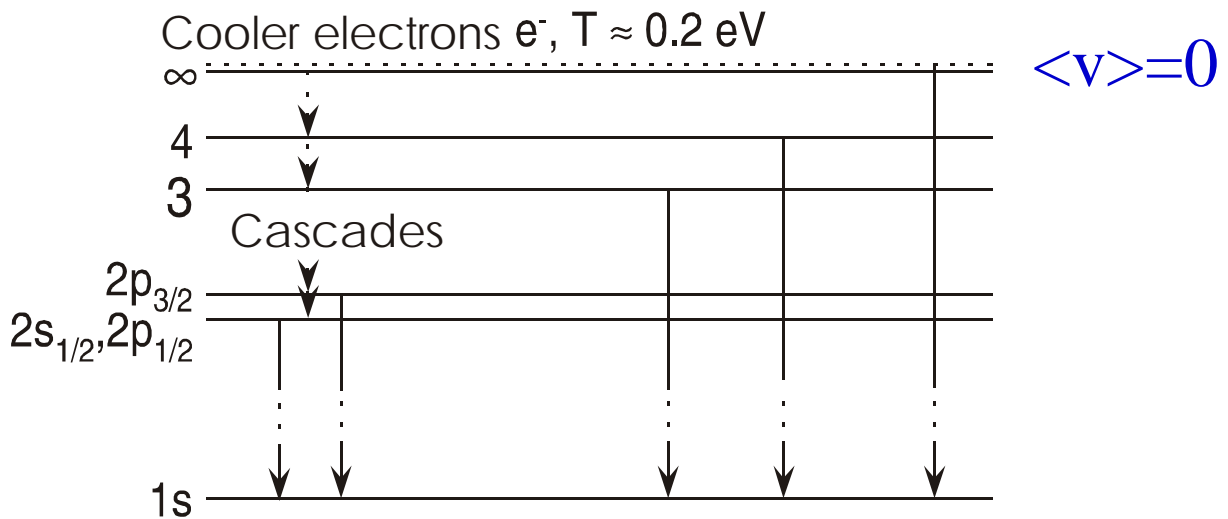
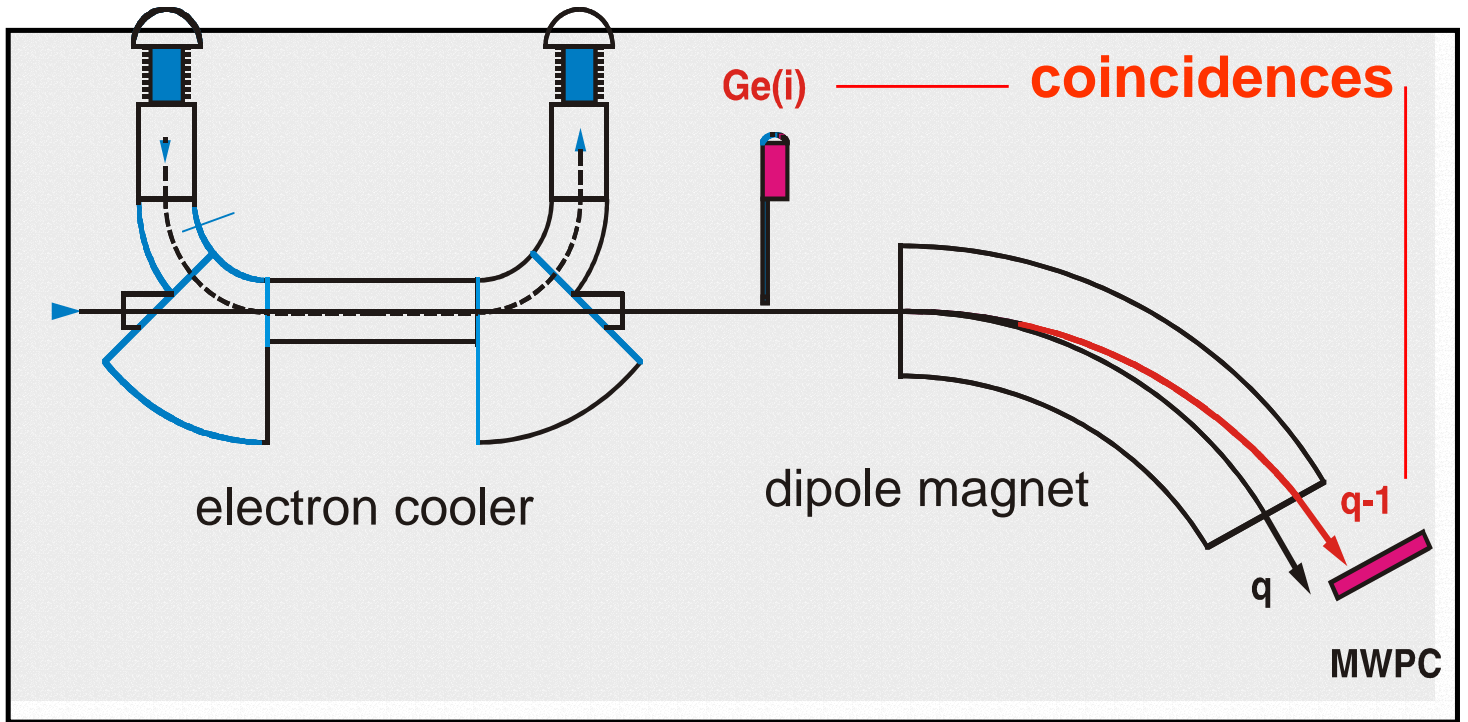
Principle of LS Experiments at ESR

- 1. Production of bare ions*
- 2. Stacking and cooling*
- 3. Electron capture in excited states
(jet-target or electron cooler)*
- 4. Detection of x-rays*
- 5. Doppler correction*
- 6. Comparison with Dirac theory*



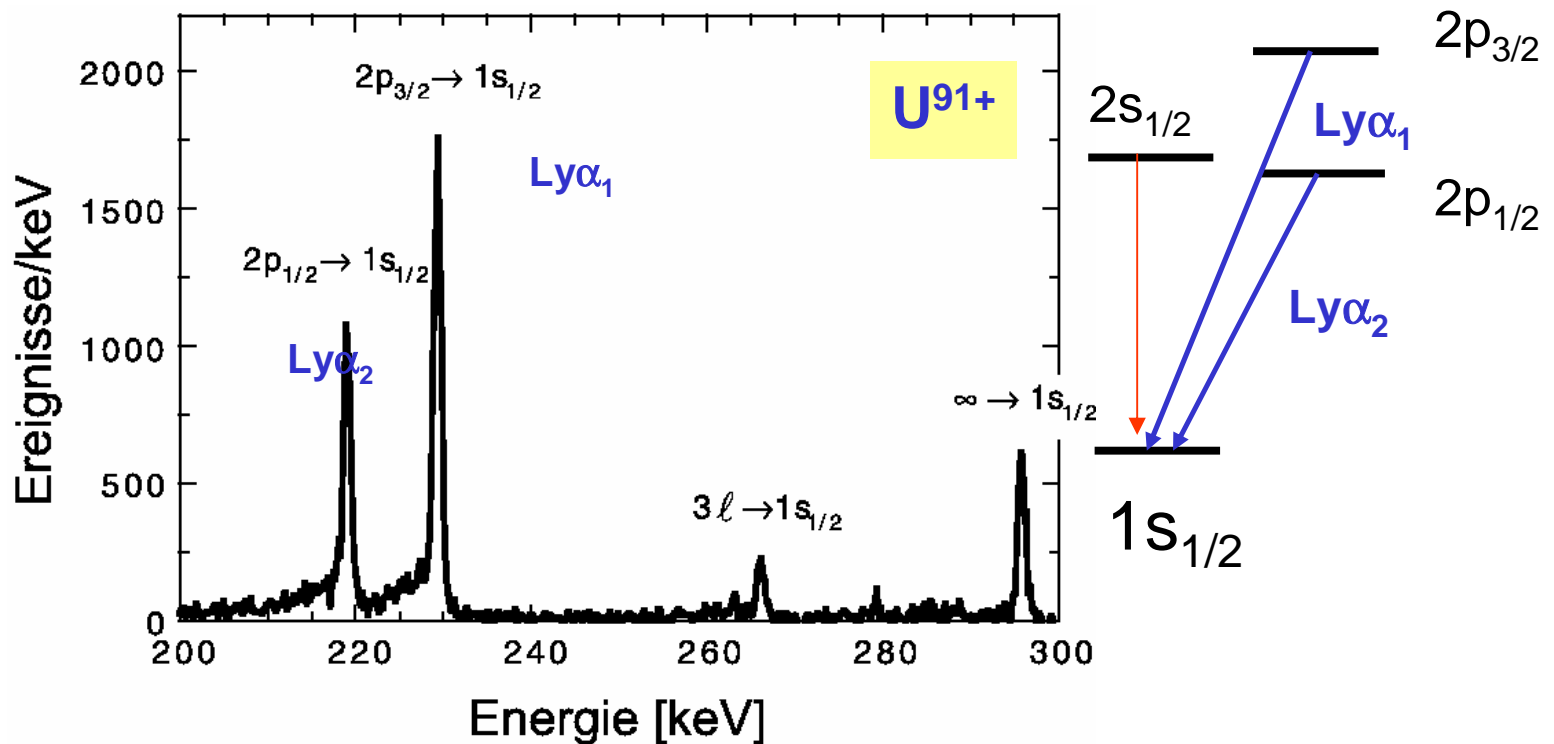
1s Lamb Shift

Experimental Scenario at the Electron Cooler



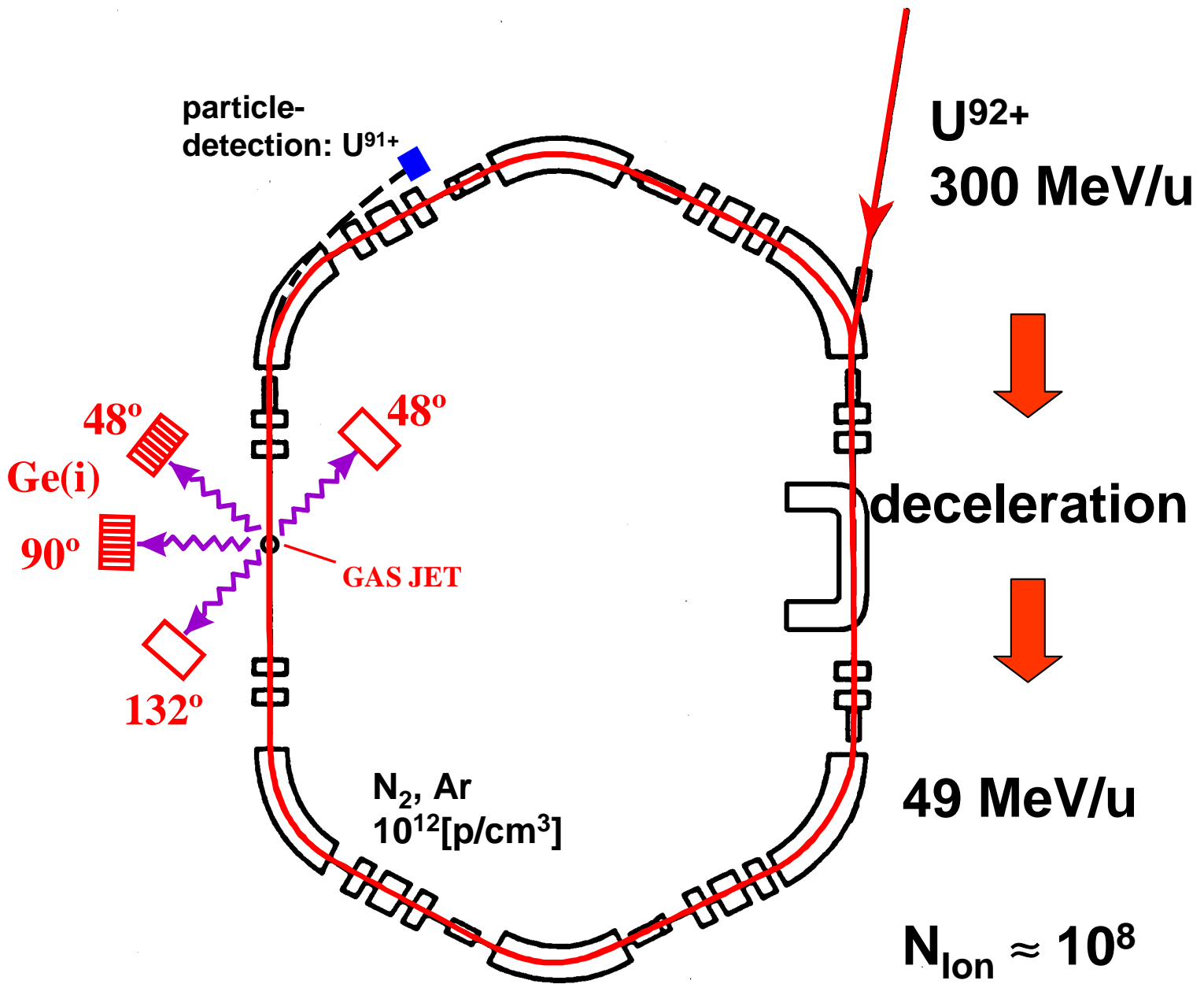
0° Spectroscopy at the Electron Cooler

- strongest blue shift
 $\beta \approx 0.65 \Rightarrow E_{\text{lab}} \approx 2.2 \times E_{\text{proj}}$
- $\Delta\theta_{\text{LAB}}$ not critical, Doppler width has its minimum
- Uncertainty is caused by $\Delta\beta$



Exp.: - $131\,810 \pm 16$ eV Dirac: - $132\,280$ eV
LS: $470 \text{ eV} \pm 16 \text{ eV}$

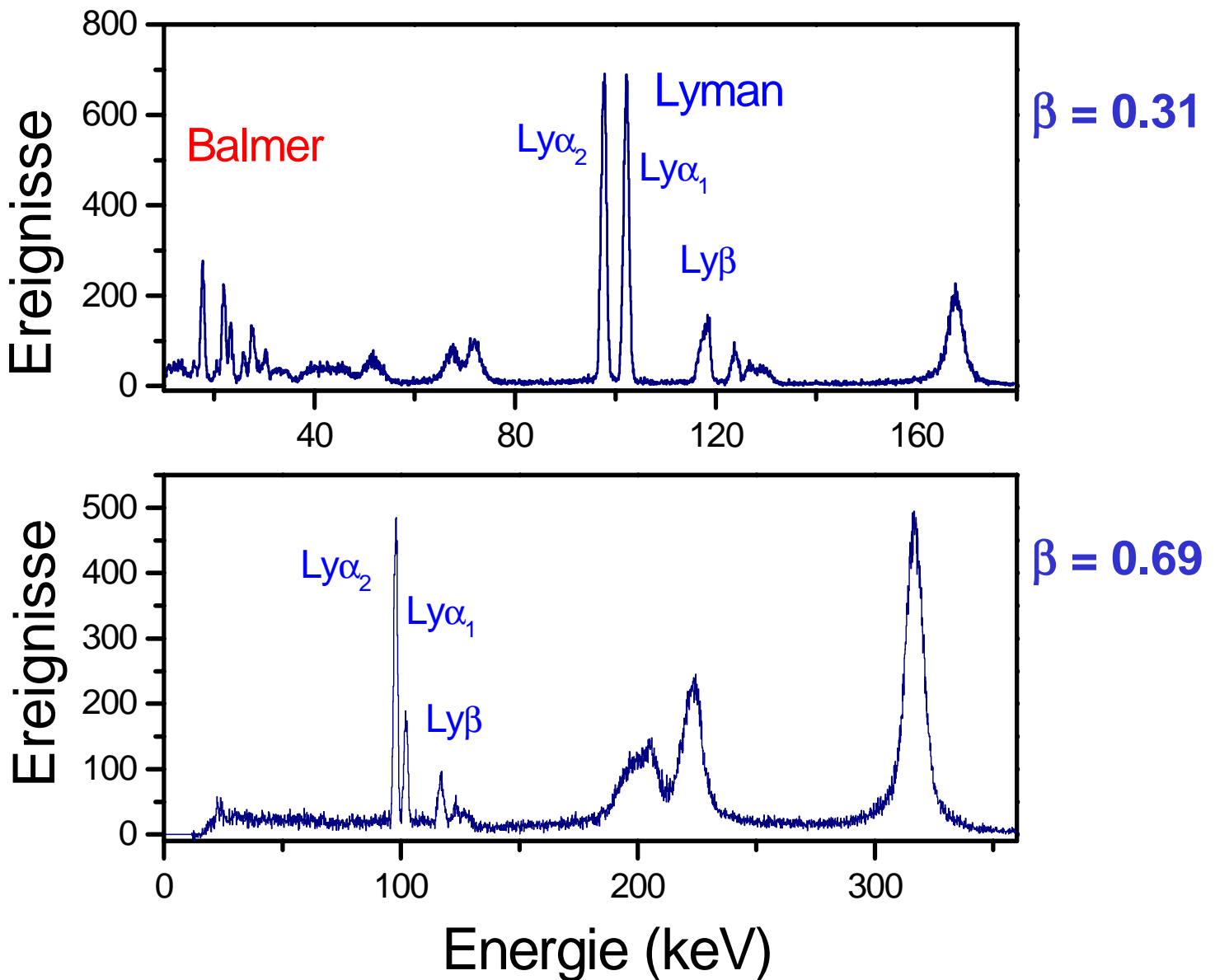
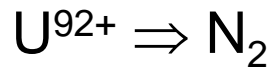
X-Ray Spectroscopy at the Jet-Target



$$E_{lab} = \frac{E_{proj}}{\gamma \cdot (1 - \beta \cdot \cos \theta_{lab})}$$

E_{lab} : Photon energy in laboratory system
 E_{proj} : Photon energy in emitter system

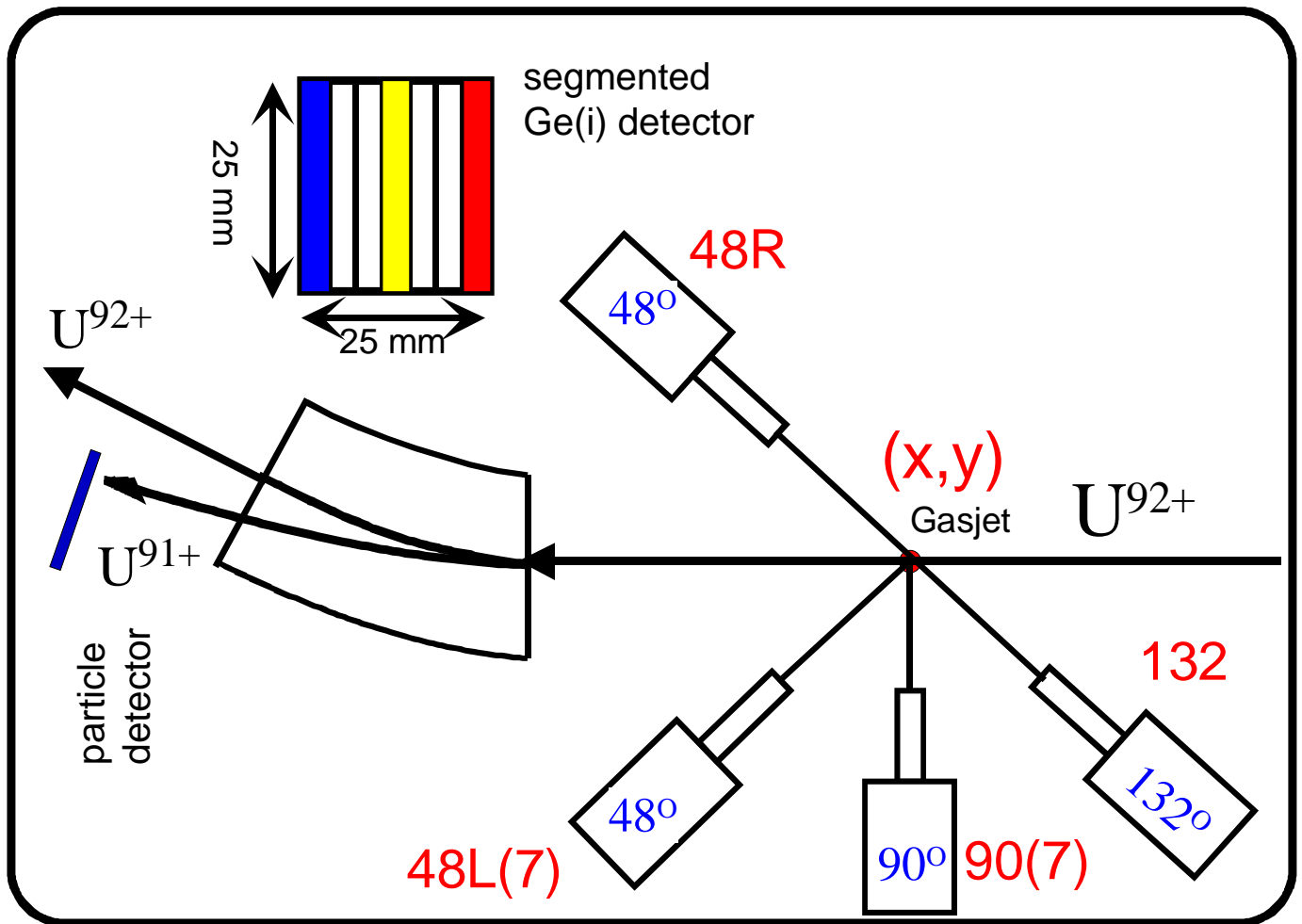
X-ray spectra of decelerated, bare uranium ions



decelerated ions:

- *efficient production of characteristic x-rays (Lyman- and Balmer transitions)*
- *improved energy resolution (reduced Doppler broadening).*

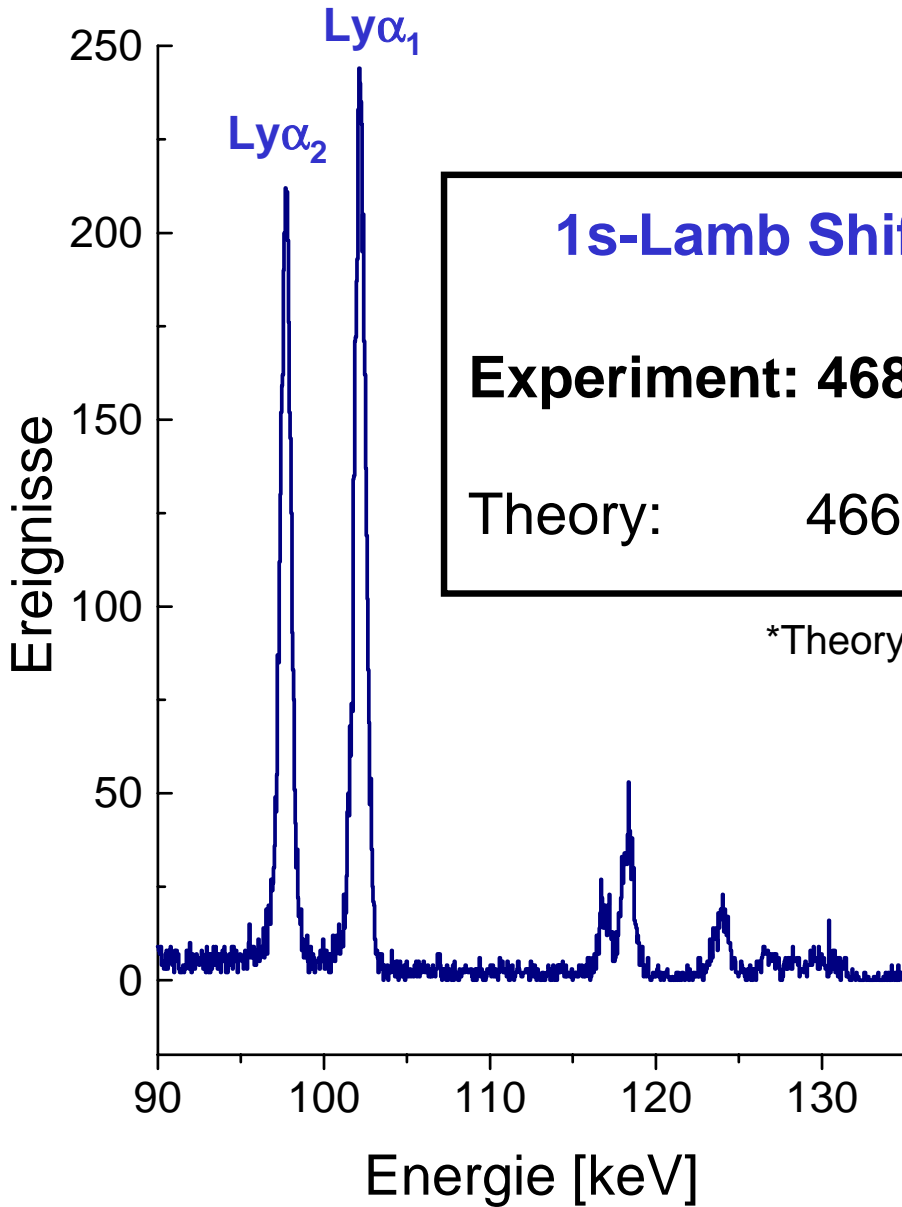
LS-Experiment at the Jet-Target



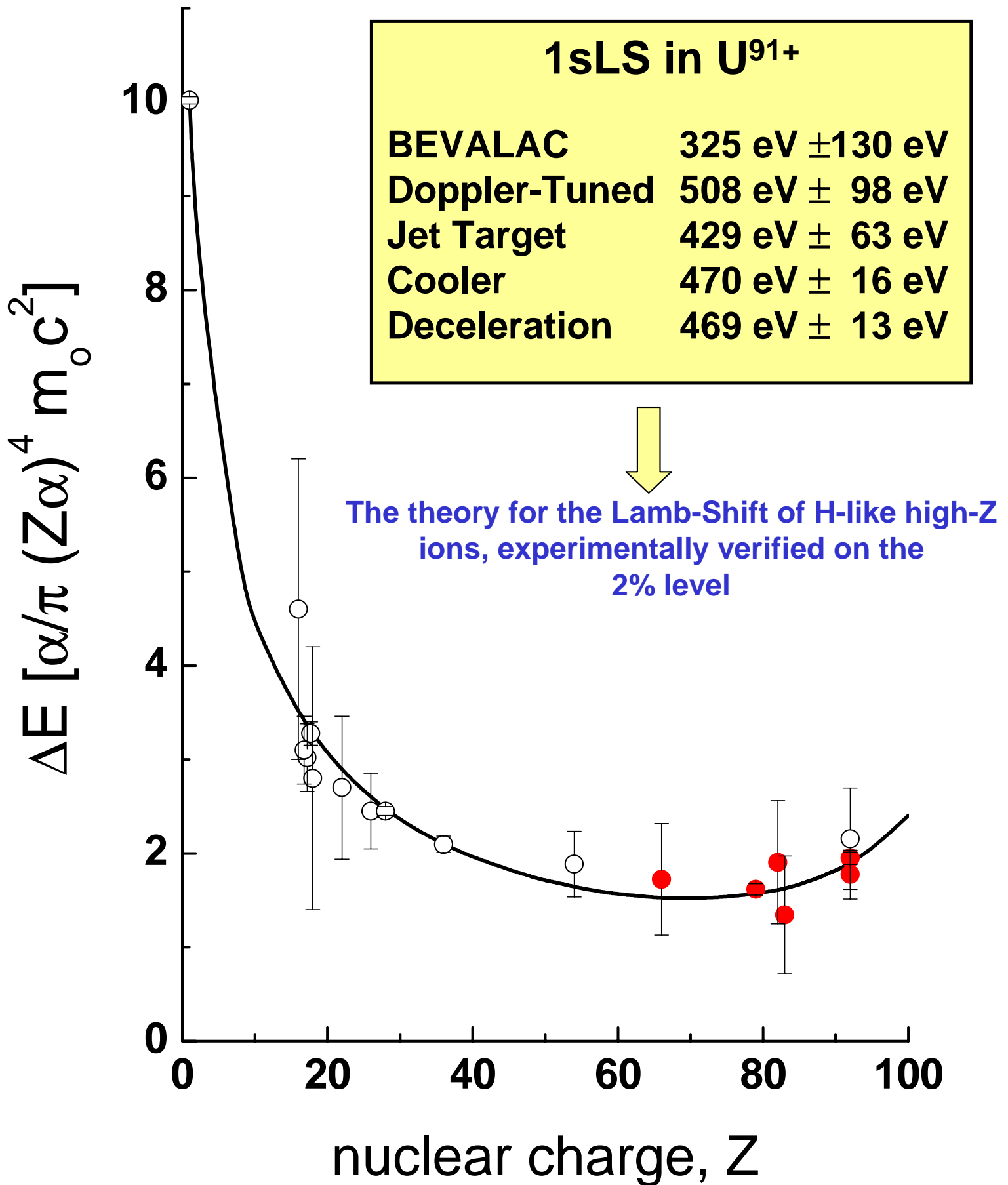
- ***Decelerated ions***
- ***Precise measurement of the relative detector geometry***
- ***Simultaneous observation at various angles***
- ***Forward/Backward symmetry***
- ***Left/Right symmetry***

Experiments at the Jet-Target

Geometry ± 8.5 eV $\Delta\beta$ ± 2.6 eV **Fit** ± 9.7 eV $\text{Ly}\alpha_1$ ($2p_{3/2} \rightarrow 1s_{1/2}$) $102\,171 \pm 13.2$ eV



Goal of future experiments



Additional improvement by one-order of magnitude (1 eV level) !!!

Towards an Accuracy of 1 eV

Detector and Spectrometer Development

High Resolution X-Ray Spectrometer (50 eV to 100 eV resolution at 100 keV)

	<i>Resolution</i>	<i>Accuracy</i>
Cristal spectrometer	≤ 50 eV	1 - 10 eV
Bolometer	≤ 50 eV	1 - 10 eV
Absorption edge spectroscopy (Doppler tuned)		1 - 10 eV

and position sensitive x-ray detectors (200 μm)

Slow ions or ions at rest

Deceleration of the ions in the ring \Rightarrow small Doppler correction
(energies between 50 MeV/u and 3 MeV/u)

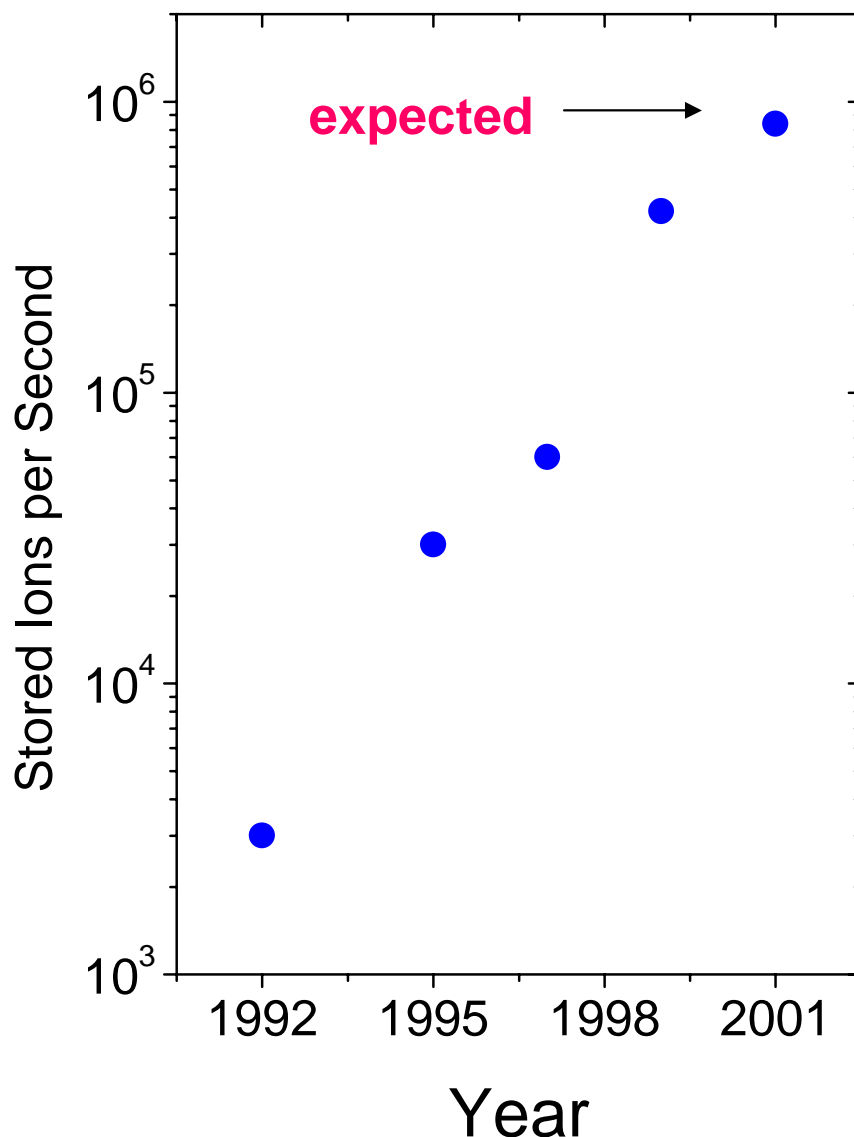
The Status of the Deceleration Technique at the ESR

1995: Deceleration down to **50 MeV/u** routinely available

1999: First experiment with bare high-Z ions (Pb^{82+}) at **25 MeV/u**

2000: Deceleration of U^{92+} down to **9 MeV/u** (M. Steck et al.)

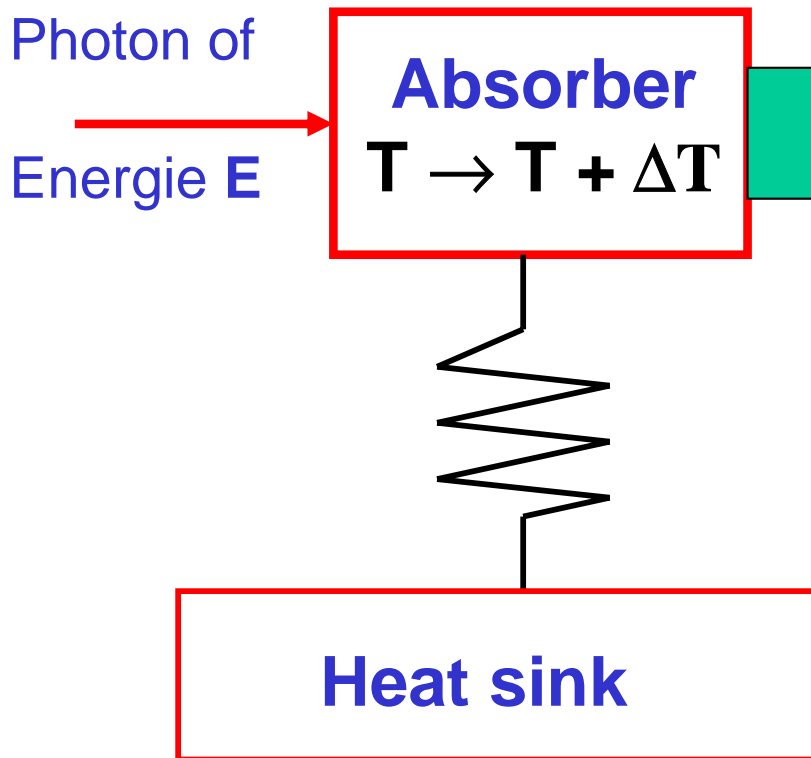
Intensity Increase at the ESR



*Increase
by more
than
two-orders
of magnitude*

Development of a Bolometer System for the High Energy Regime

Detection of Photons instead of Electrons



Thermo-
meter
 $\Delta T = E / C$



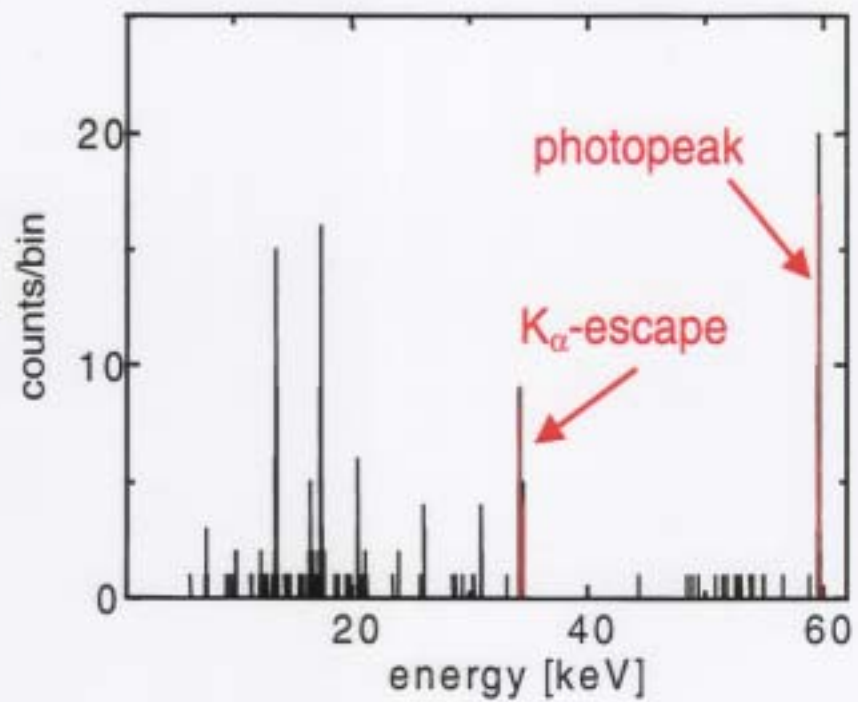
Heat capacity: $C = c \cdot m$
 $C \sim T^3$
Specific heat capacity : c
Detector mass: m

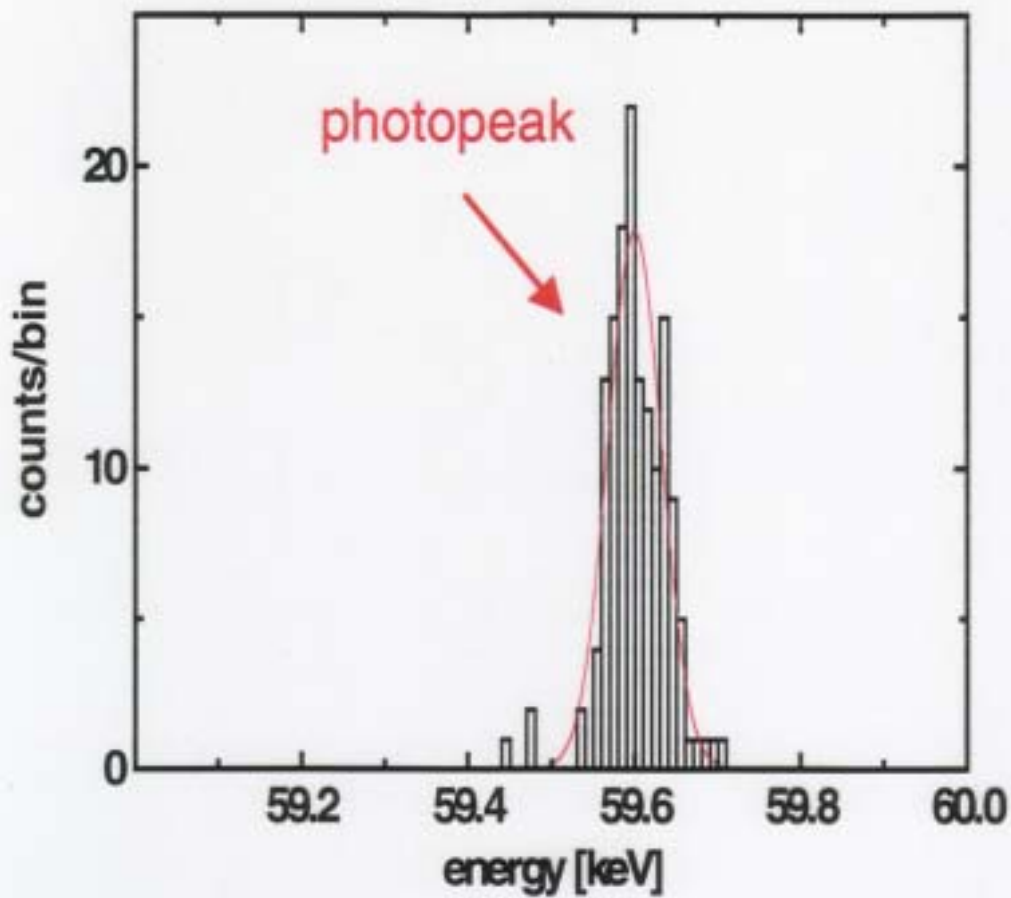
P. Egelhof et al., 1999

Detector operates at temperatures of 50 mK

energy spectrum for an ^{241}Am -source:

detector: Sn-absorber ($V = 0.3 \text{ mm}^2 \times 66 \text{ }\mu\text{m}$)





energy resolution for $E_\gamma = 59.6$ keV:

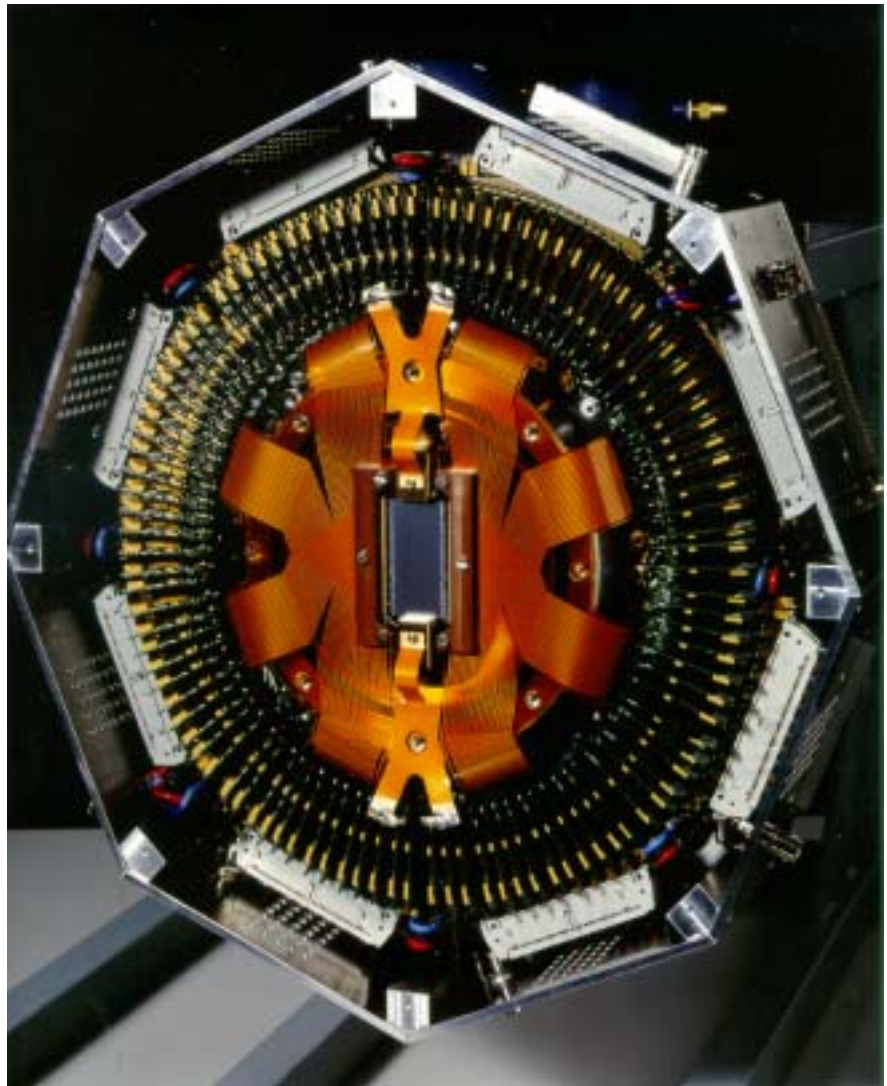
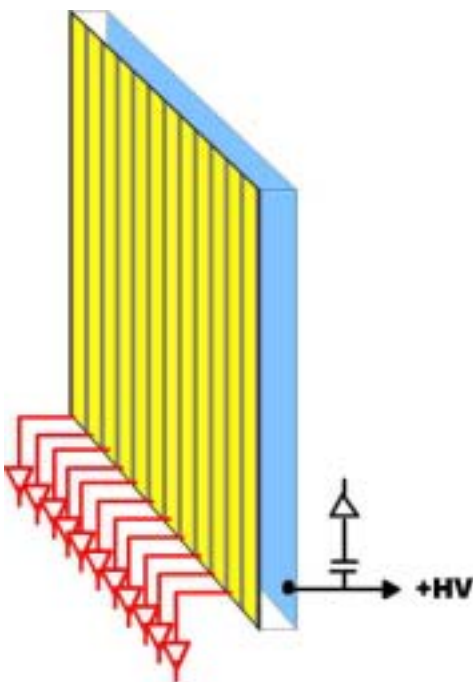
$$\Delta E = 75 \text{ eV}$$

(theoretical limit for conventional
Si-semiconductor detector: $\Delta E \geq 350$ eV)

Position Sensitive Ge(i) Detectors

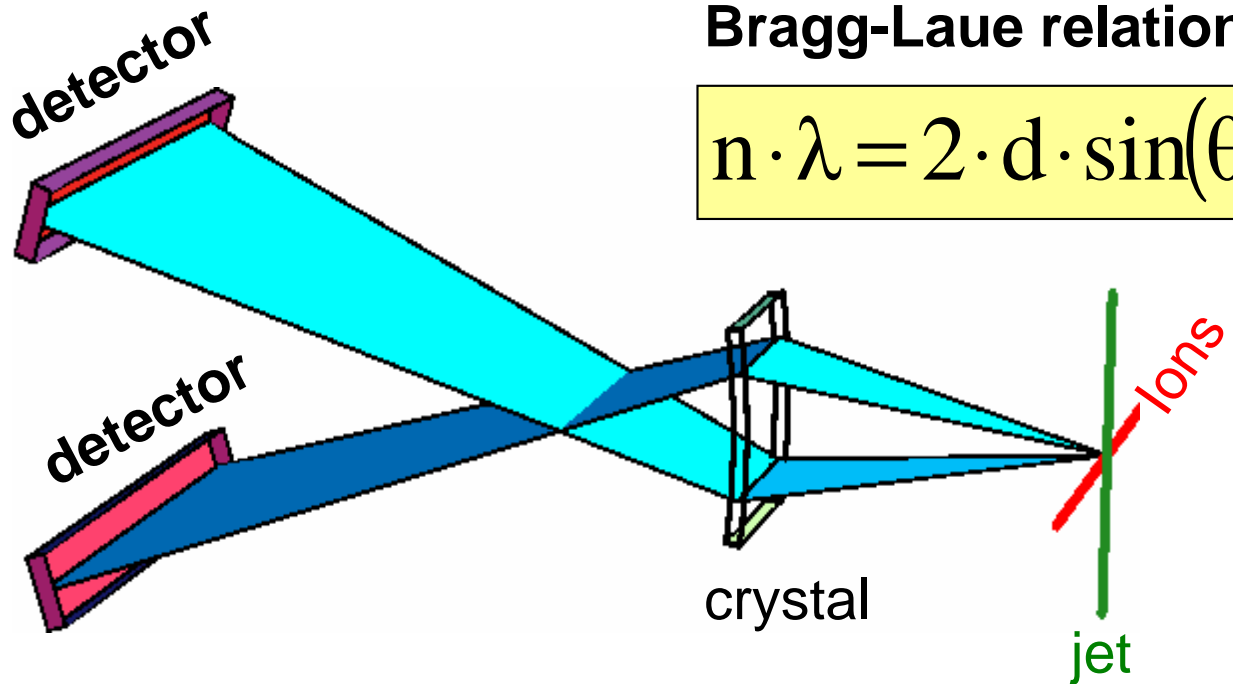
Micro-Strip Germanium Detector Development:

Energy Resolved X-Ray Imaging, Timing,
Multi-Hit Capability

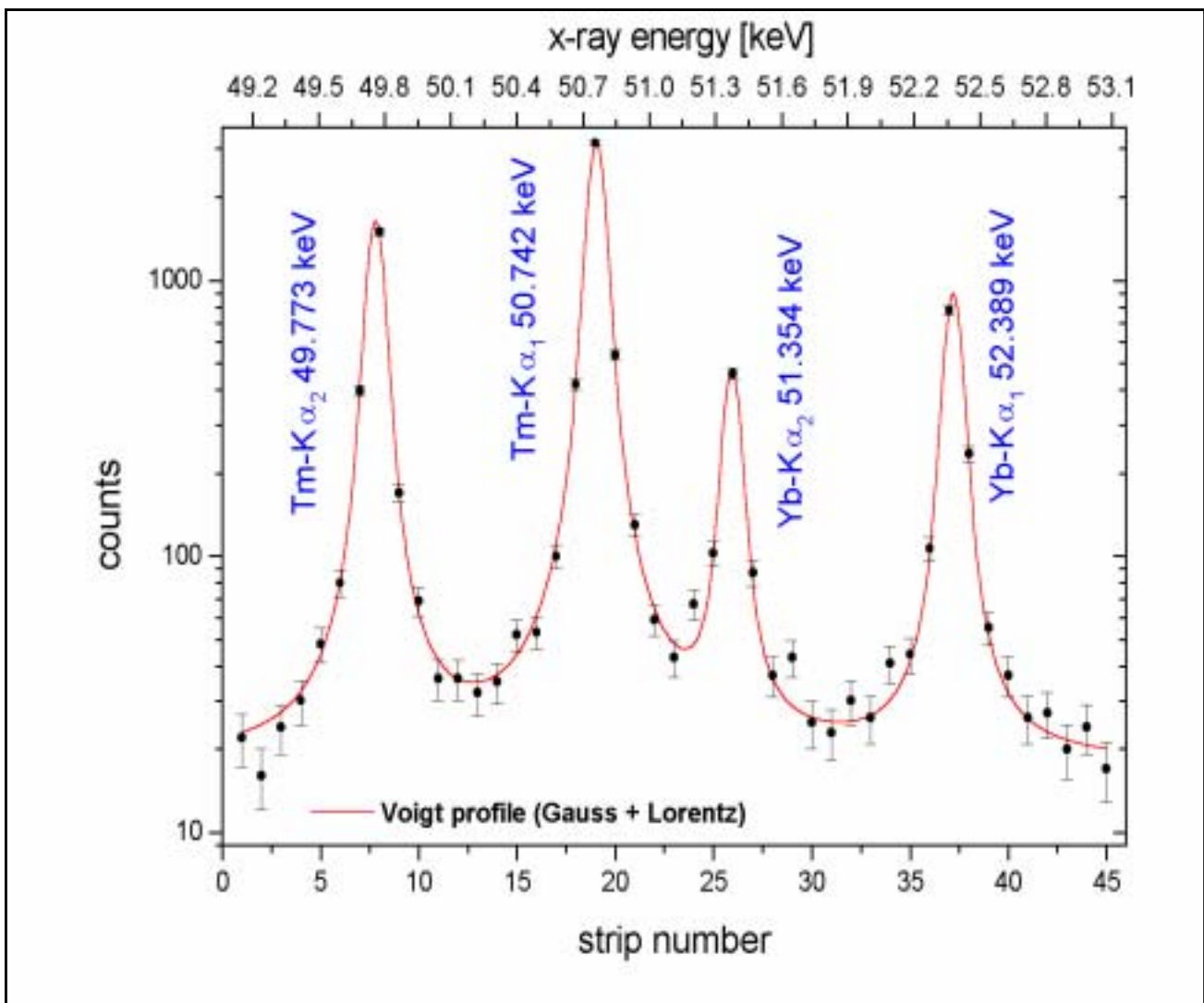


- crystal spectrometer
- doppler tuned
- polarization studies

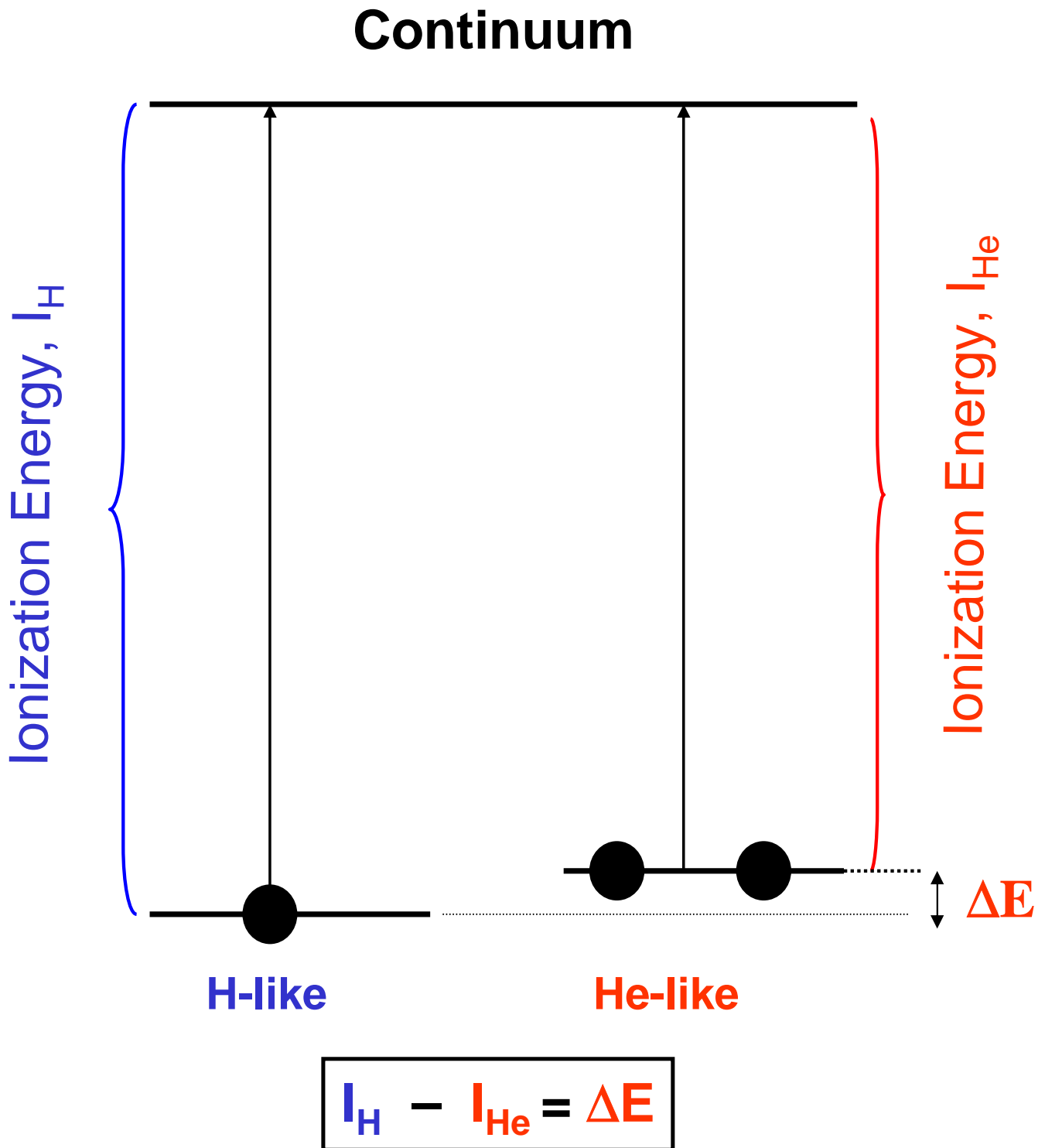
Transmission crystal spectrometer



H.F. Beyer et al., GSI Report 2000

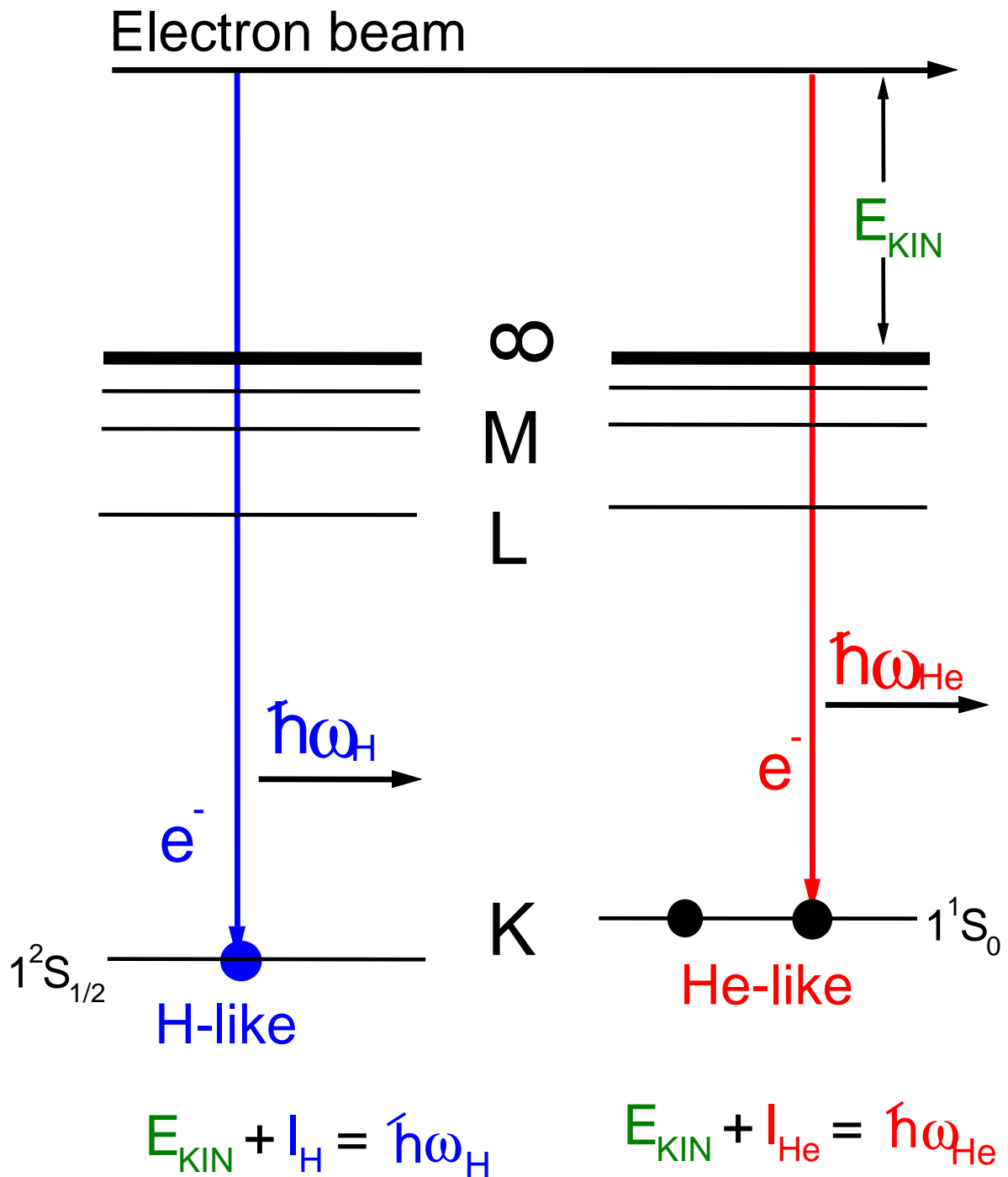


Electron-Electron Interaction in Strong Fields



ΔE : Two-Electron Contribution to the Ionization Potential in the He-like System: **Second Order in α**

The Method



$$\Delta E(\hbar\omega_H - \hbar\omega_{He}) = I_H - I_{He}$$

Advantage of relative measurement:
All one electron contributions cancel out

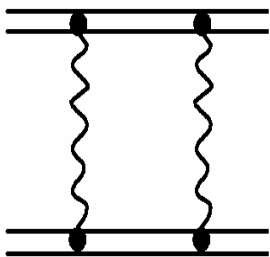
Electron-Electron Interaction in Strong Fields

Measurement of the 2eQED for Uranium at

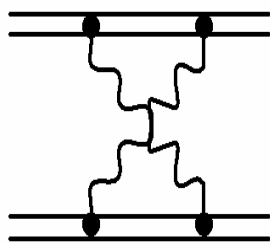
Accuracy:
2 eV; $\Delta E/E \approx 0.1\%$

Z=92

Two-Electron Contribution: **2246.0 eV**

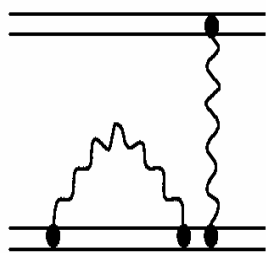


a)

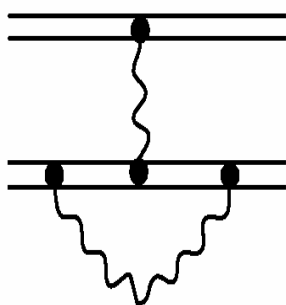


b)

a,b) Non-Radiative QED
+1.3 eV [U⁹⁰⁺]
0.06%

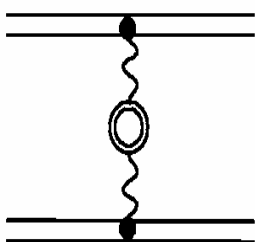


c)

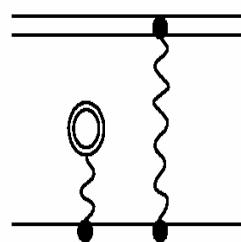


d)

c,d) Two-Electron
Self Energy
-9.7 eV [U⁹⁰⁺]
0.4%



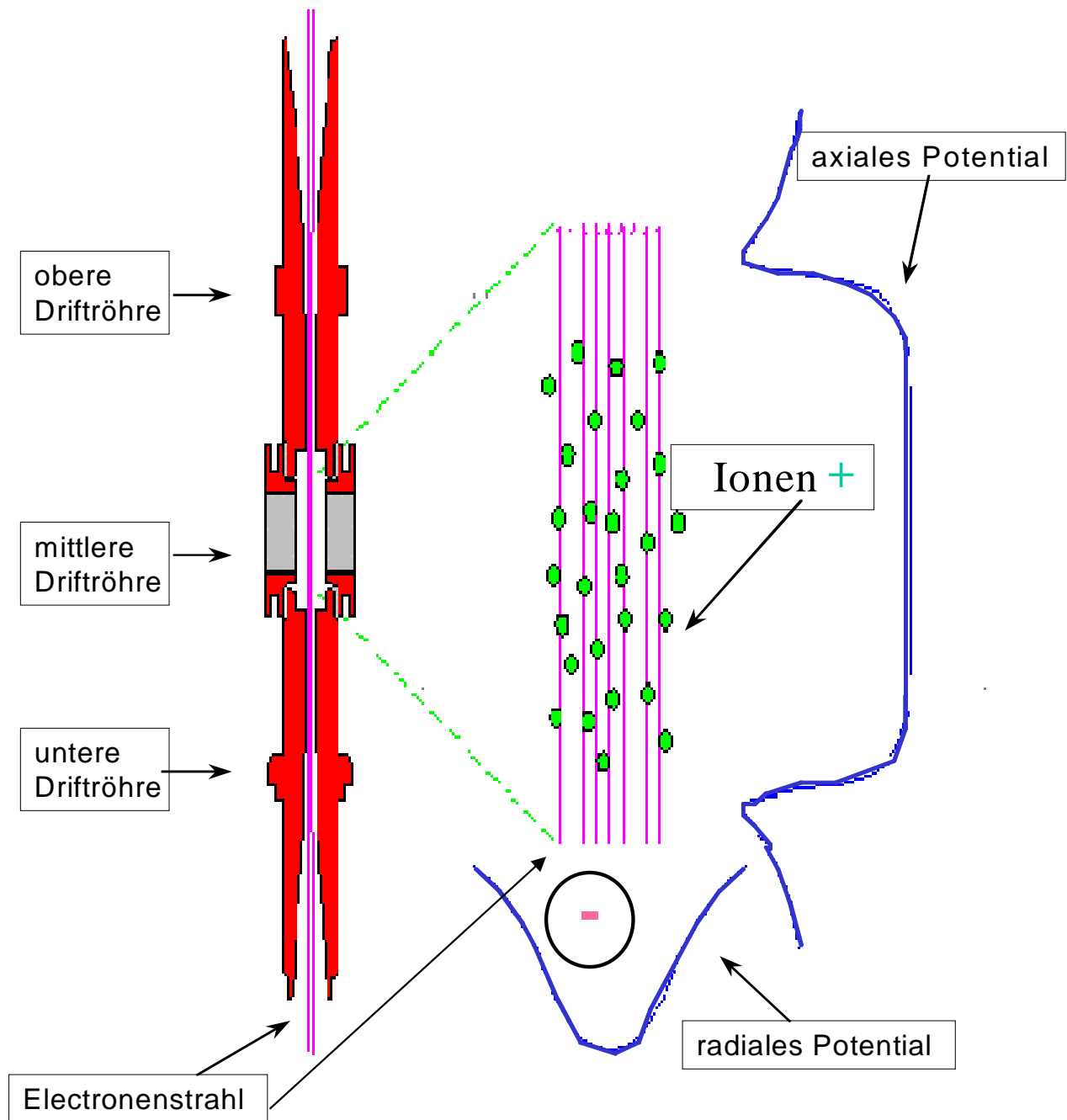
e)



f)

e,f) Two-Electron
Vacuum Polarization
+2.6 eV [U⁹⁰⁺]
0.1%

Super-EBIT (Electron Beam Ion Trap)

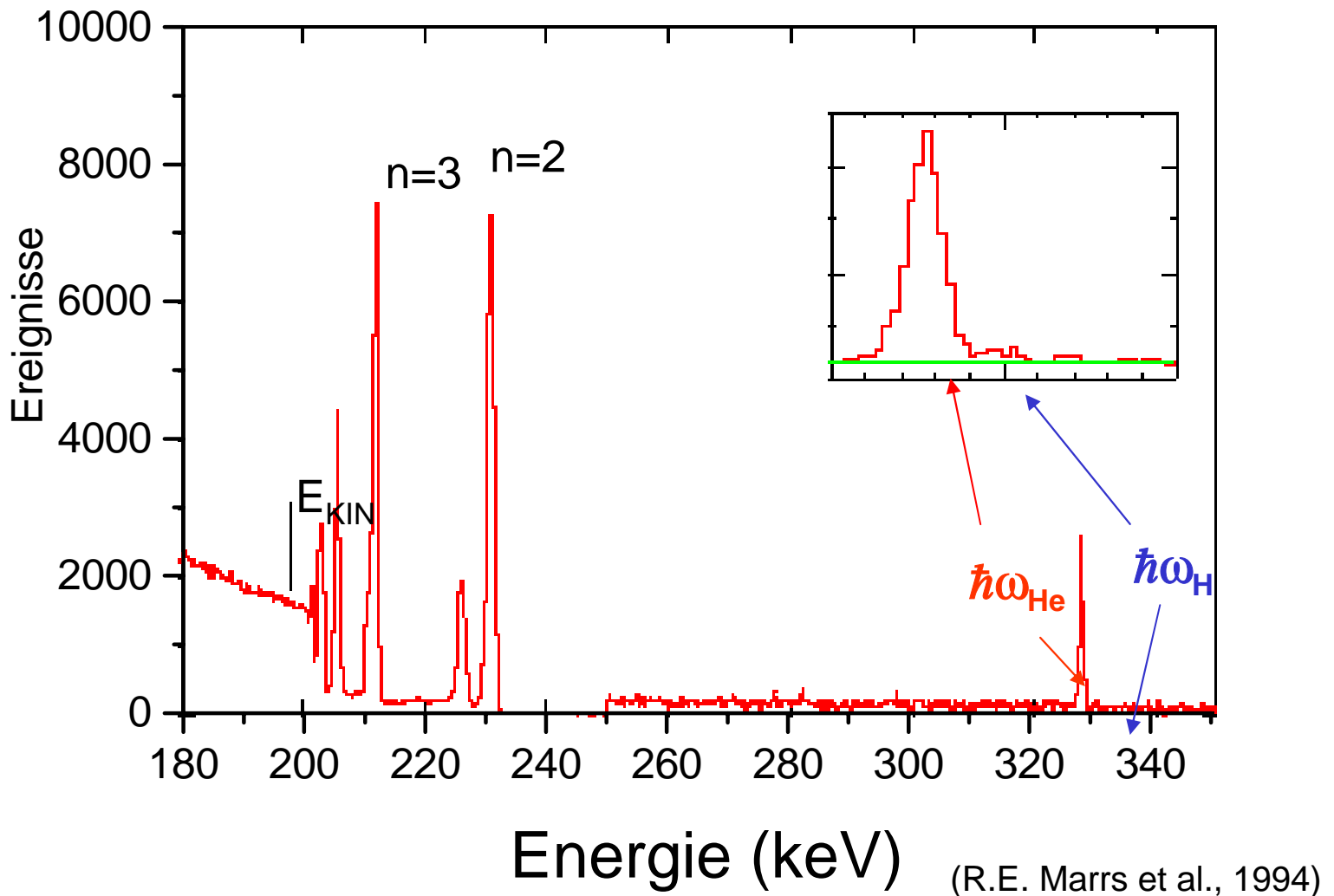


(S.R. Elliott: Nucl. Instr. and Meth, B98, 114 (1995))

EBIT- Parameter

- **Elektronenstrahlenergie:** 10 –210 keV
- **Max. Elektronenstrom:** 200 mA
- **Strahlradius:** 50 μ m
- **Stromdichte:** 5000 A/cm²
- **Magnetfeld:** 3 T

Erzeugung stationärer, nackter Uranionen



EBIT Einstellung:

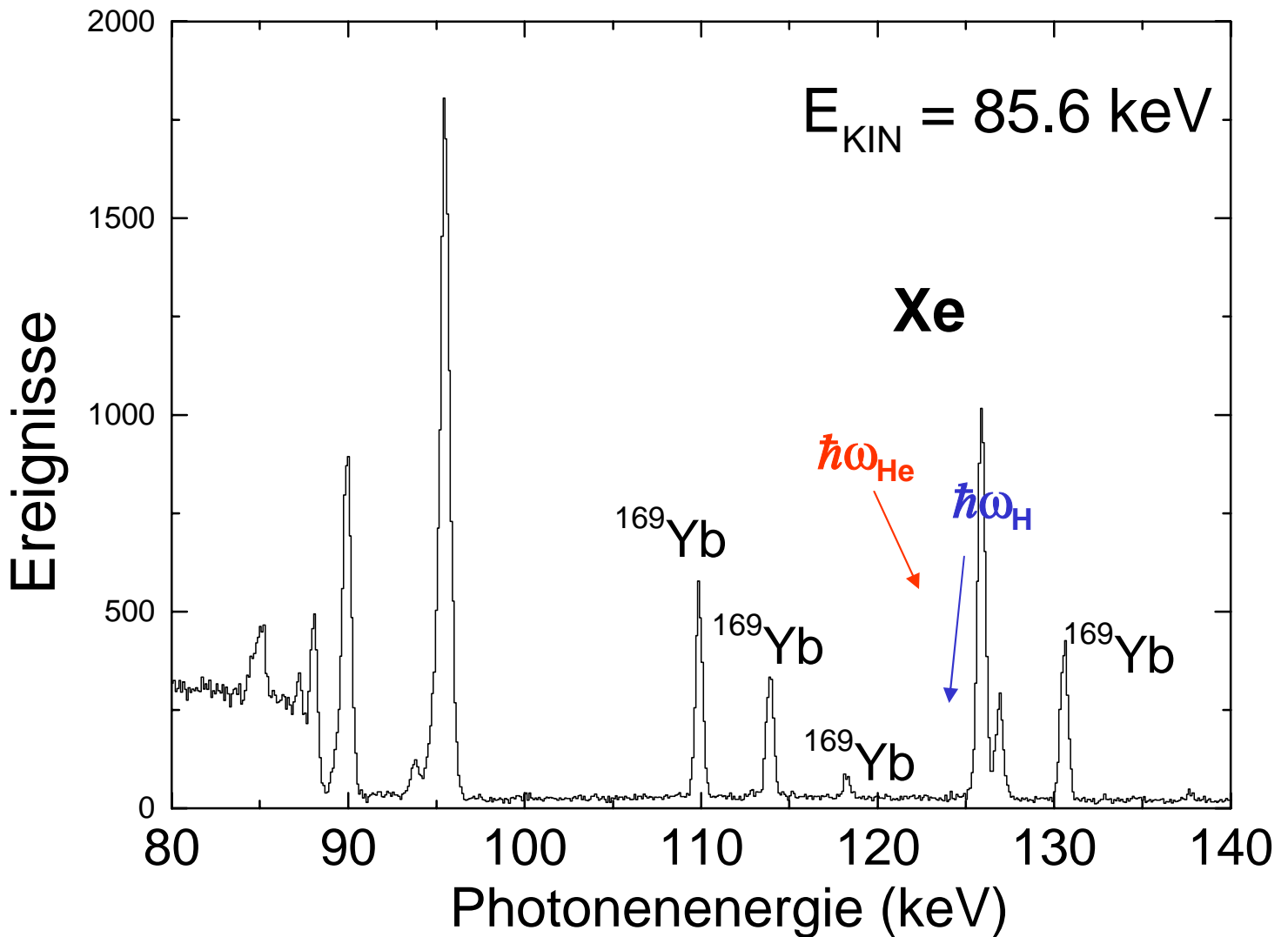
Spannung	198 kV
Strom	200 mA

$\hbar\omega_{\text{He}}$: Einfang in den Grundzustand H-artiger Ionen

$\hbar\omega_{\text{H}}$: Einfang in den Grundzustand nackter Ionen

**Vorteil der Super-EBIT für die Spektroskopie:
Stationäre Ionen, d.h. keine Dopplerkorrekturen.**

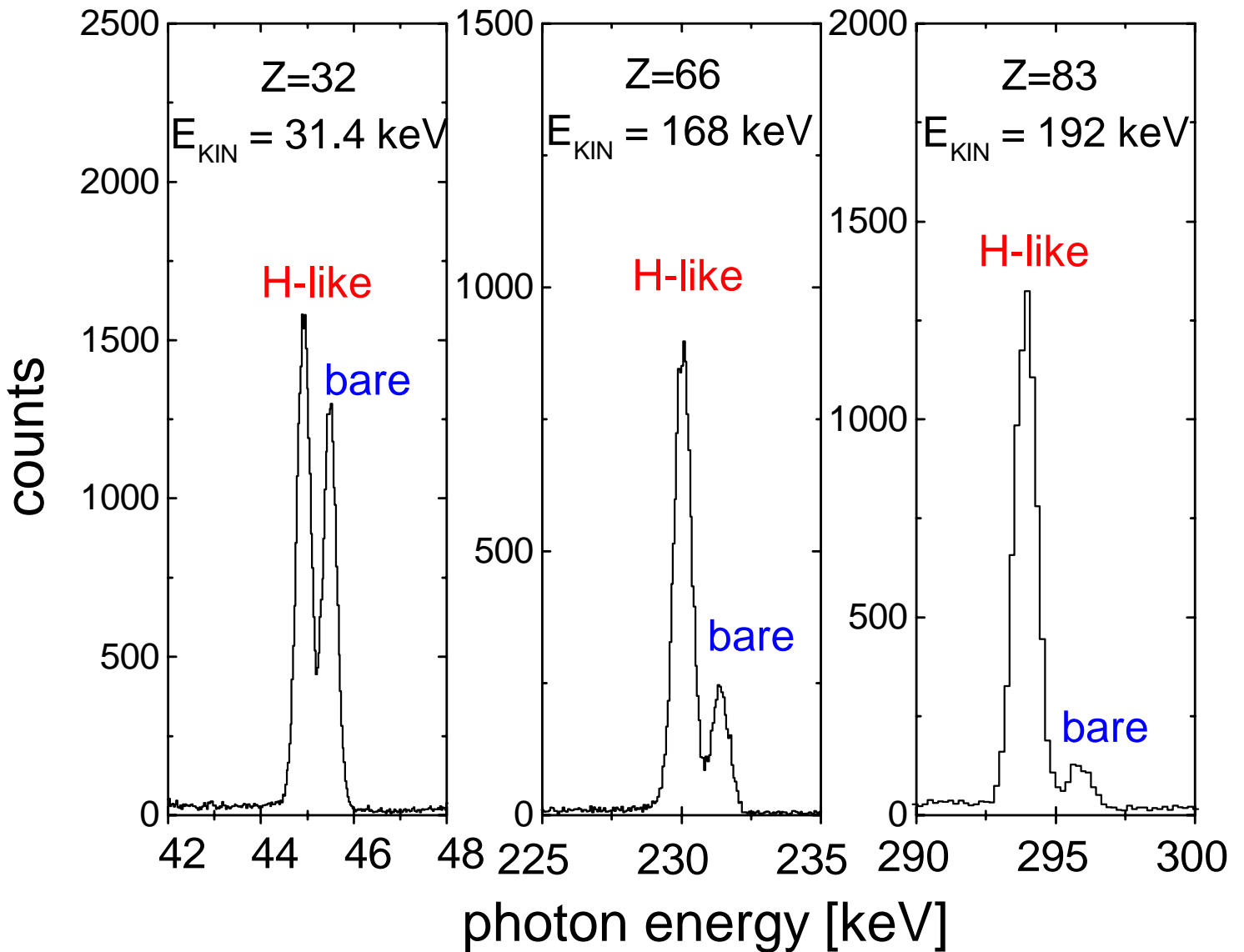
Typical X-ray spectrum



Insgesamt wurde die Messung an sechs verschiedenen Elementen durchgeführt:

*Ge(Z=32), Xe(Z=54), Dy(Z=66),
W(Z=74), Os (Z=76), Bi(Z=83)*

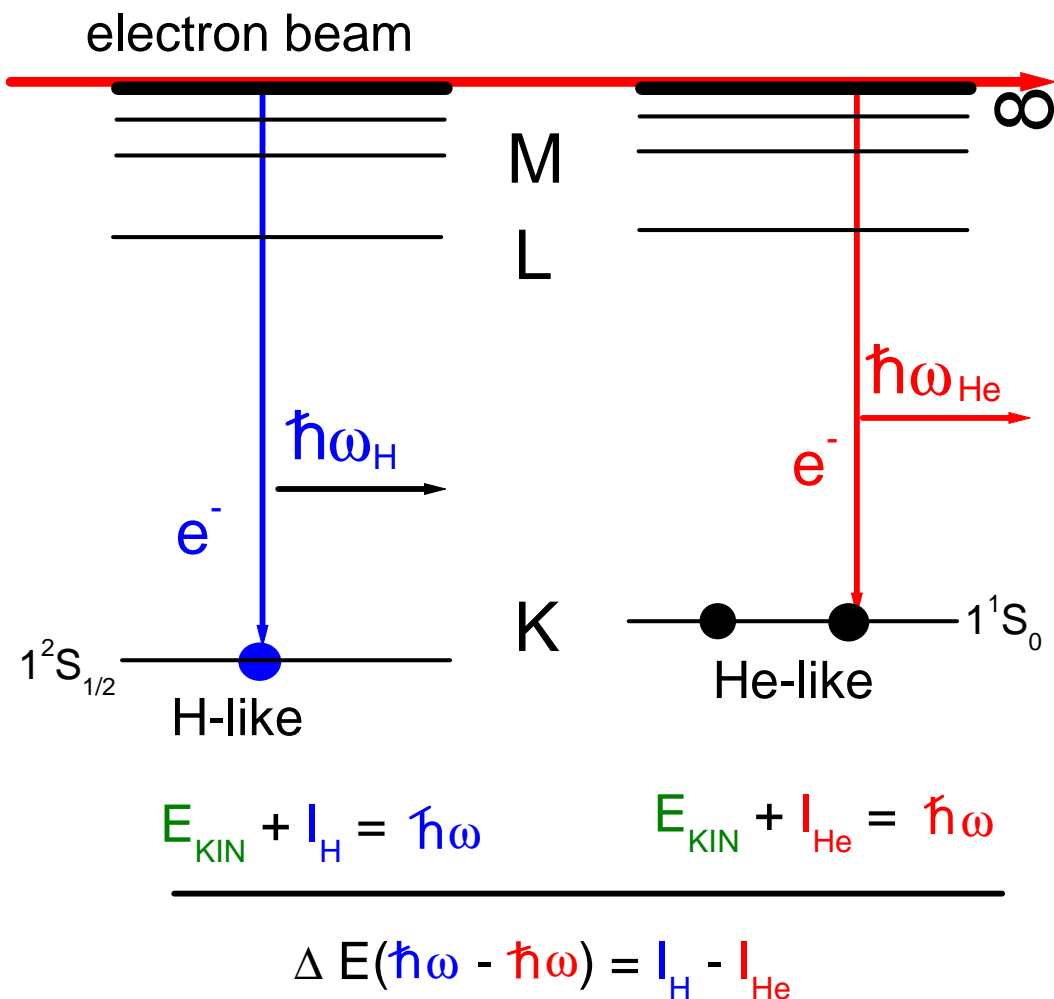
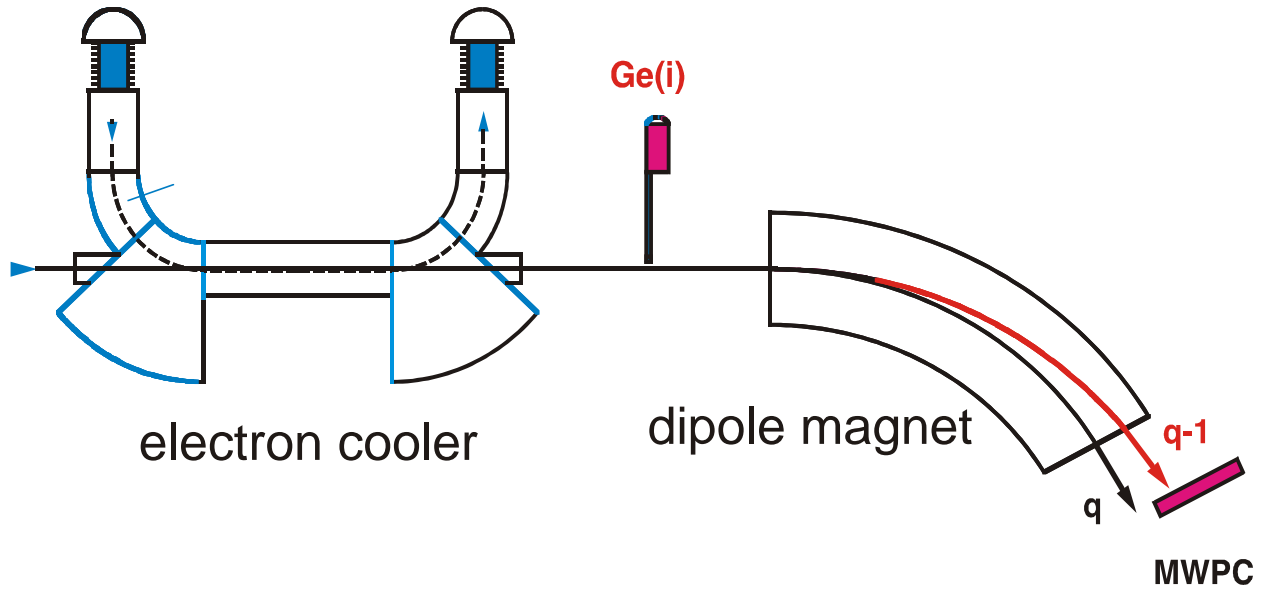
Results from Super-EBIT



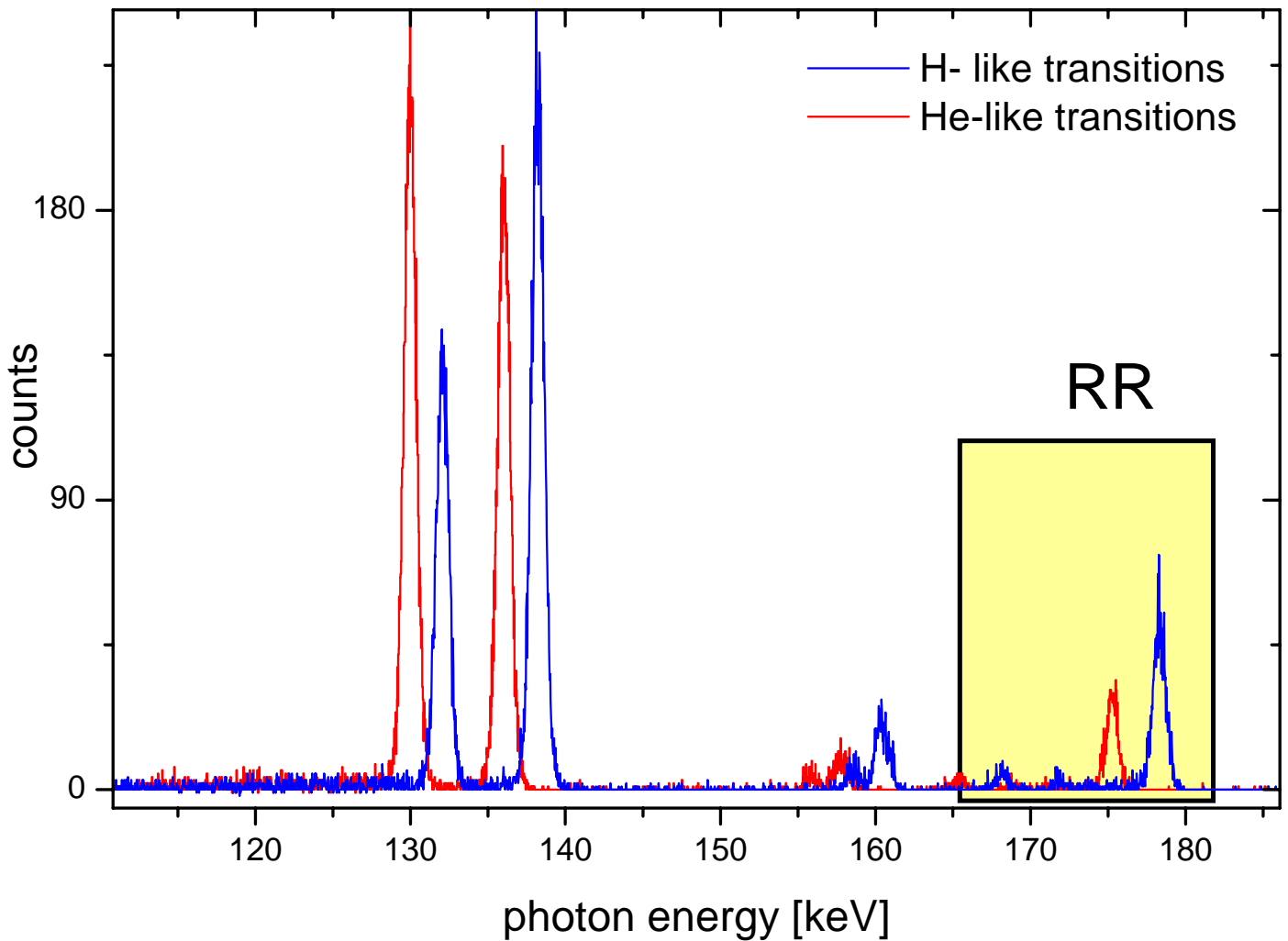
Z	32	54	66	74	76	83
Exp. [eV]	562.6 ± 1.6	1027.2 ± 3.5	1341.6 ± 4.3	1568.9 ± 15	1608 ± 20	1876 ± 14
$\Delta E/E$	2.8 $\times 10^{-3}$	3.4 $\times 10^{-3}$	3.0 $\times 10^{-3}$	1 $\times 10^{-2}$	1.2 $\times 10^{-2}$	0.7 $\times 10^{-3}$

Results are only limited by counting statistics

2eQED Studies for the Ground State



Relative measurement at the electron cooler



Estimated statistical uncertainty
for RR into H- and He-like uranium: $\approx 7\text{eV}$

~~Uncertainty caused by doppler
shift:~~

Additional systematic errors: ?

Two Electron

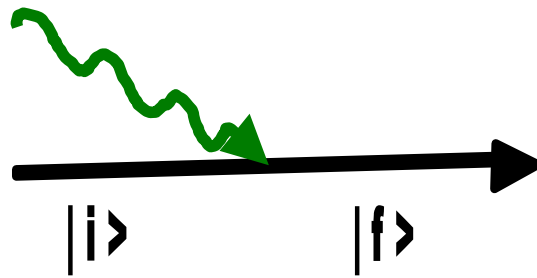
Self Energy

$-9.7\text{ eV [U}^{90+}]$

Vacuum Polarization

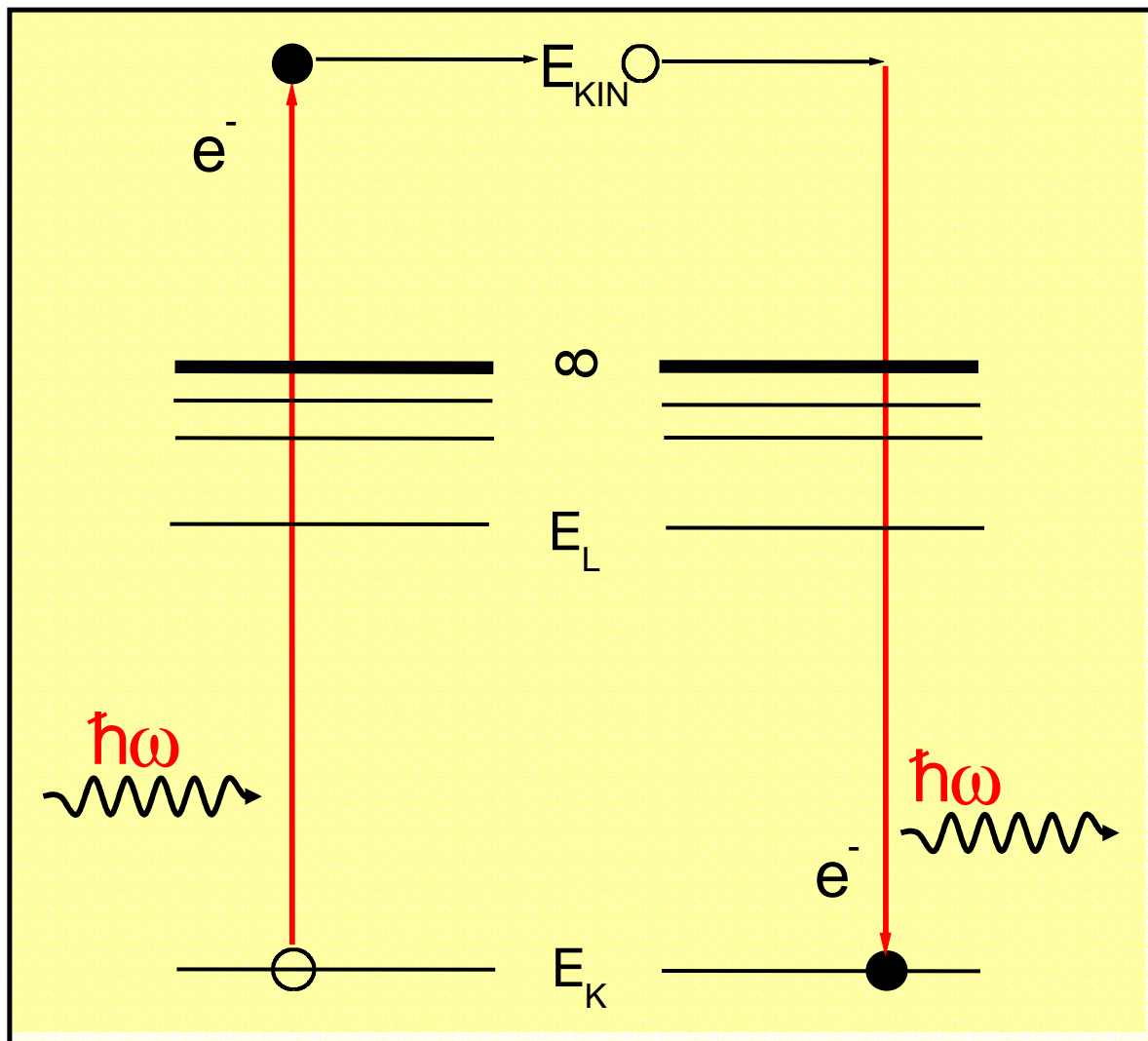
$+2.6\text{ eV [U}^{90+}]$

Photon-Matter Interaction in the Relativistic Regime: *Radiative Electron Capture*



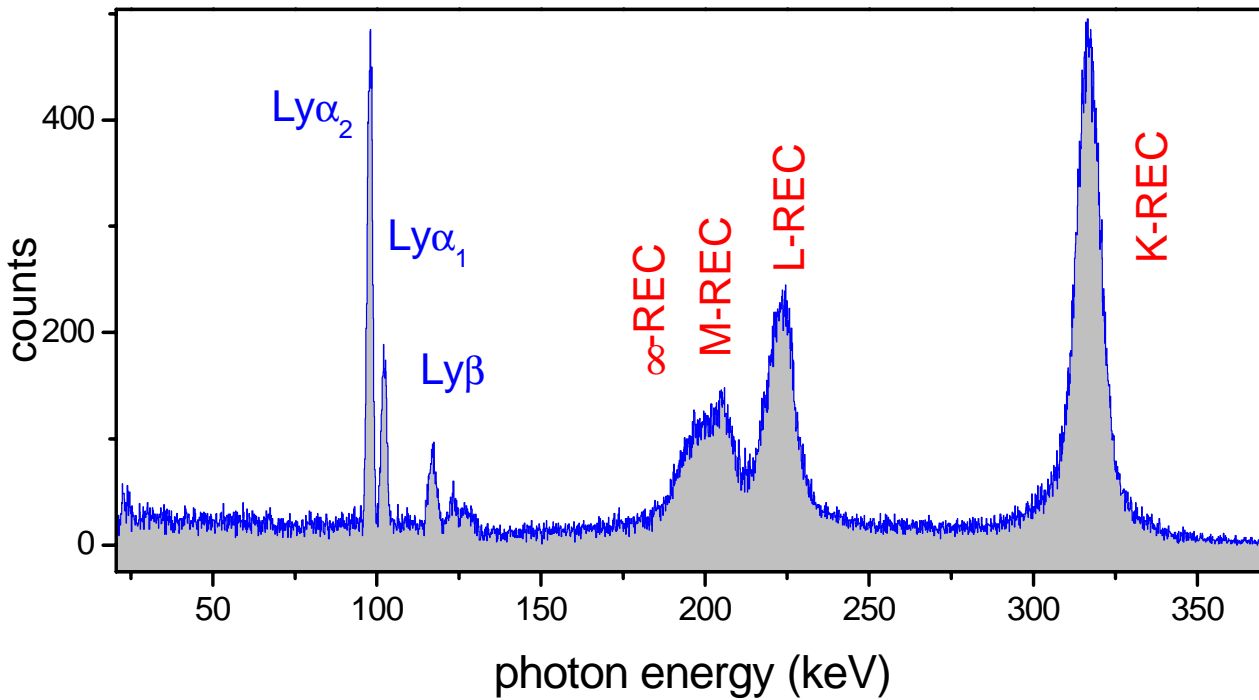
Photoionization

Radiative Electron Capture



Radiative Electron Capture Capture of Quasifree Targetelectrons

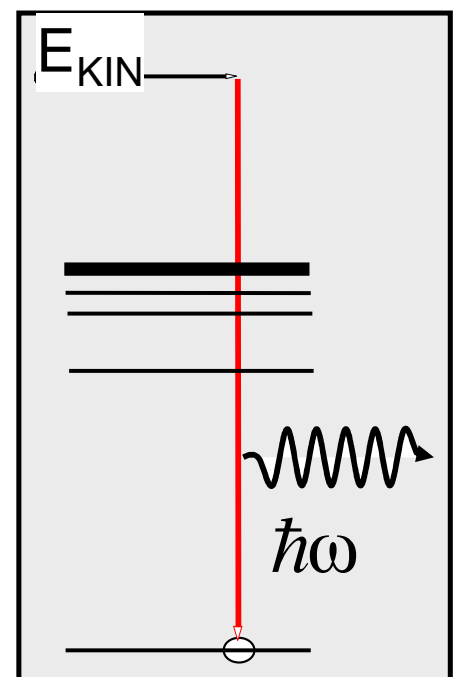
$U^{92+} \Rightarrow N_2, 358 \text{ MeV/u}$



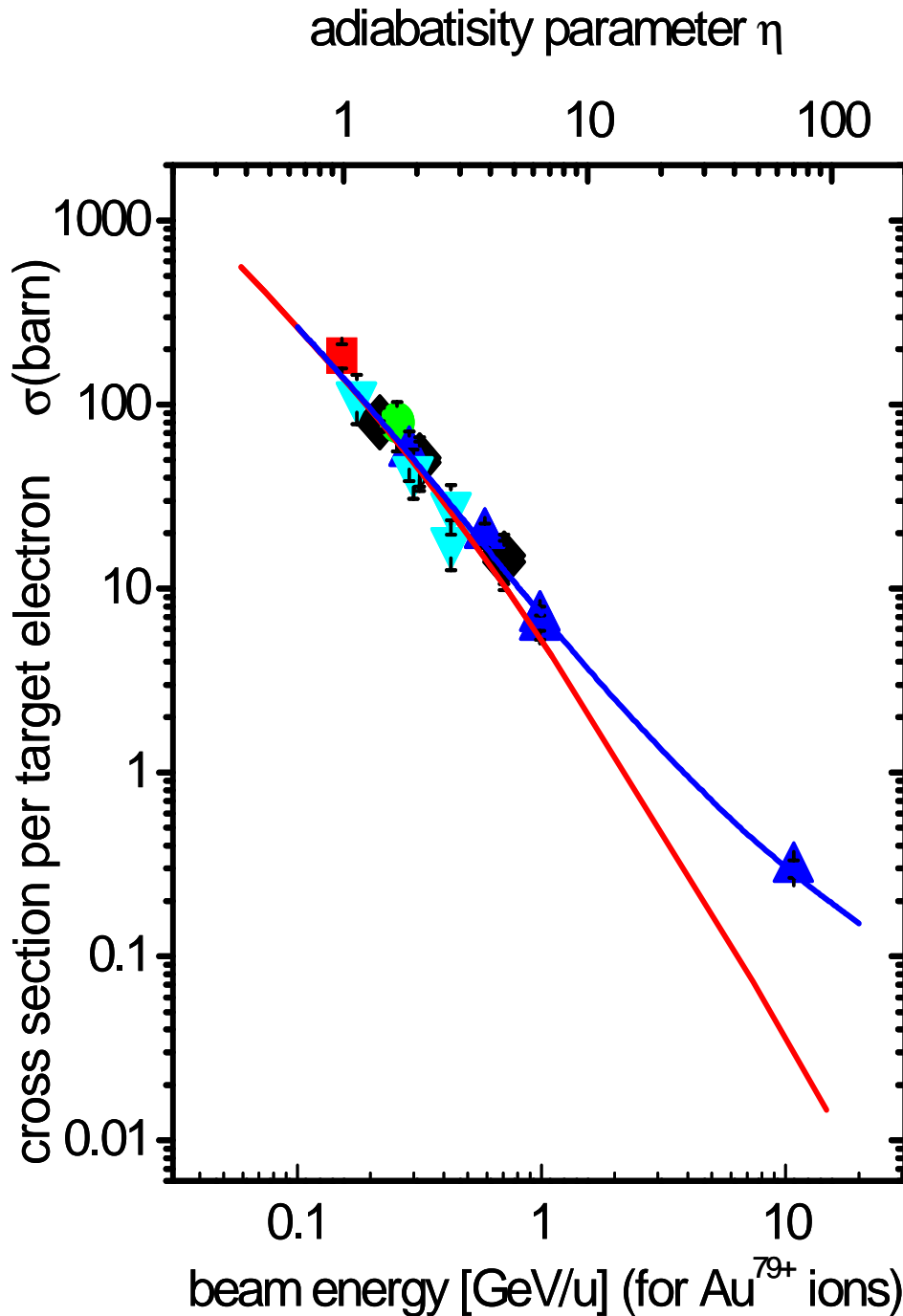
REC photon energy

$$\hbar\omega_{\text{REC}} = E_B + m_e c^2 (\gamma - 1) + \gamma(v_i p_z - E_T)$$

Shape and width of REC lines are determined by the **momentum distribution** of the target electrons



Total REC cross sections for bare ions



$$\eta = \frac{E_{\text{KIN}}}{E_{\text{K}}}$$

E_{K} :
K-shell binding energy

E_{KIN} :
kinetic projectile energy

Data cover the Z
range between
Z=54 to 92

(BEVALAC,
SIS/FRS/ESR,
BROOKHAVEN)

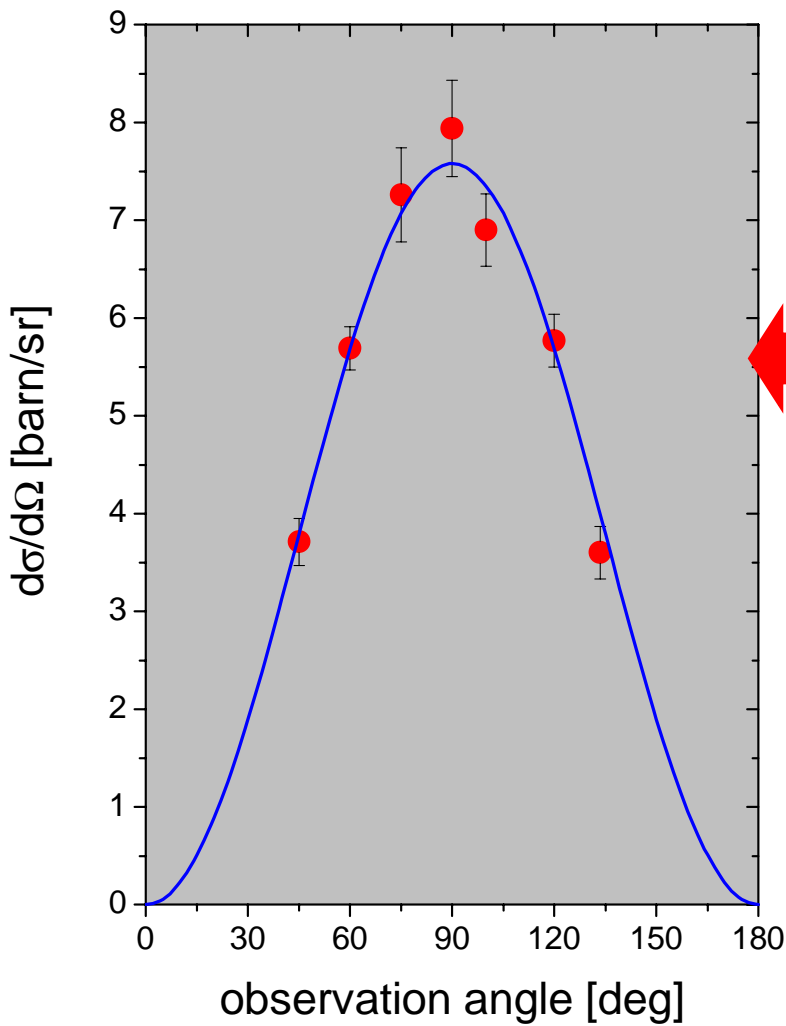
— complete relativistic calculations for Au^{79+} (Eichler et. al)

— dipole approximation

The simple non-relativistic dipole approximation provides an accurate tool for cross section predictions (below 1 GeV/u)

K-REC Distribution for Xe^{54+} (200 MeV/u)

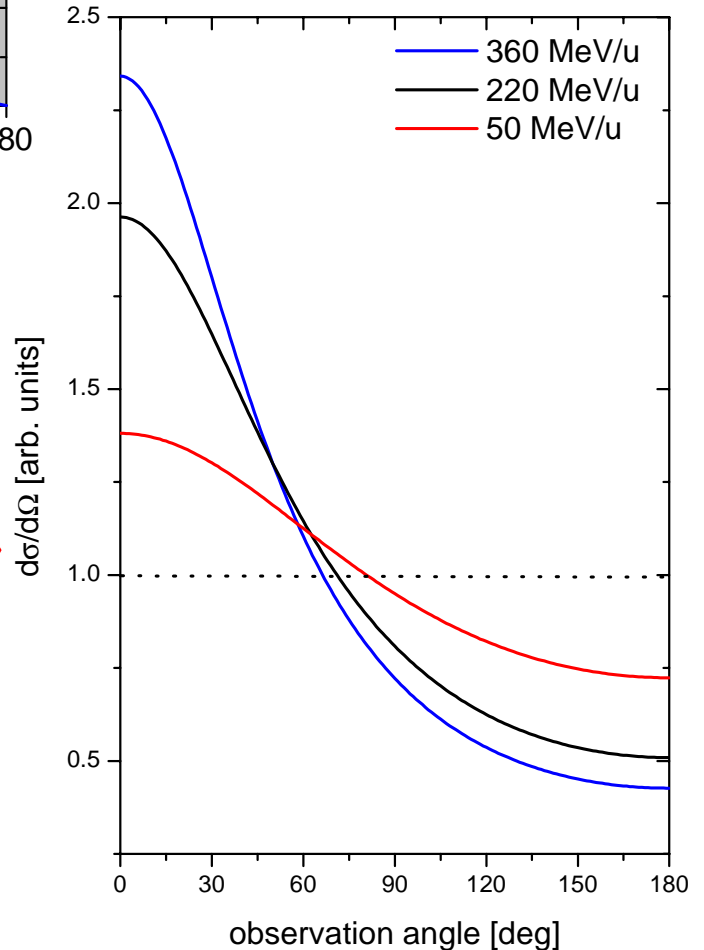
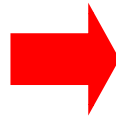
K-REC angular distribution



R. Anholt (1984)
BEVALAC experiment

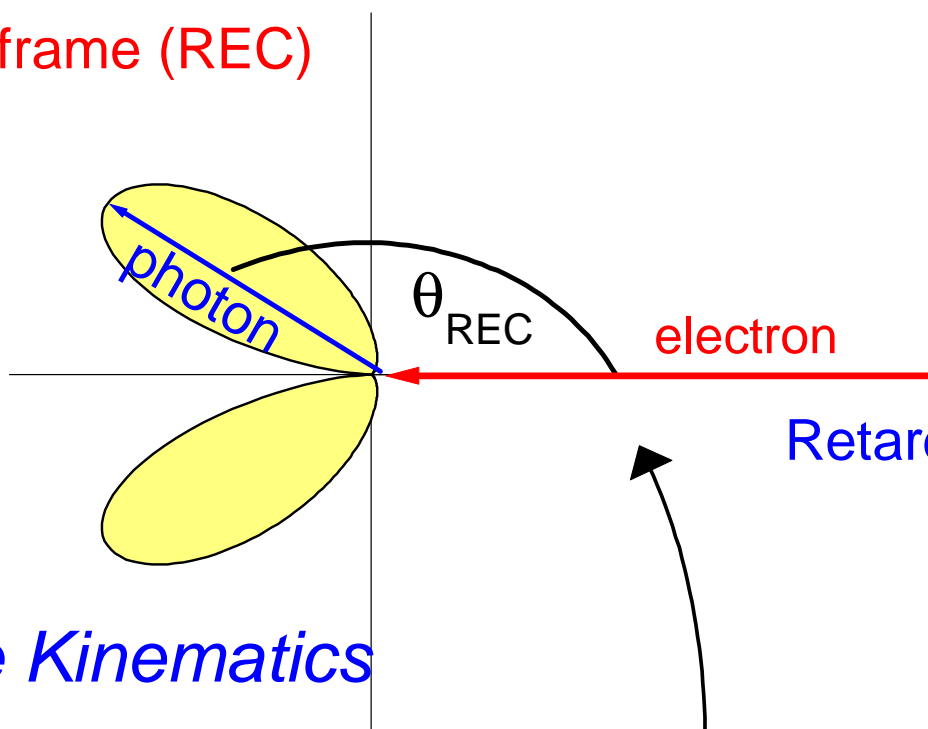
$$\left. \frac{d\sigma}{d\Omega} \right|_{LAB} \propto \sin^2 \vartheta_{lab}$$

Lab. angular distribution
of an isotropic transition
in the projectile frame

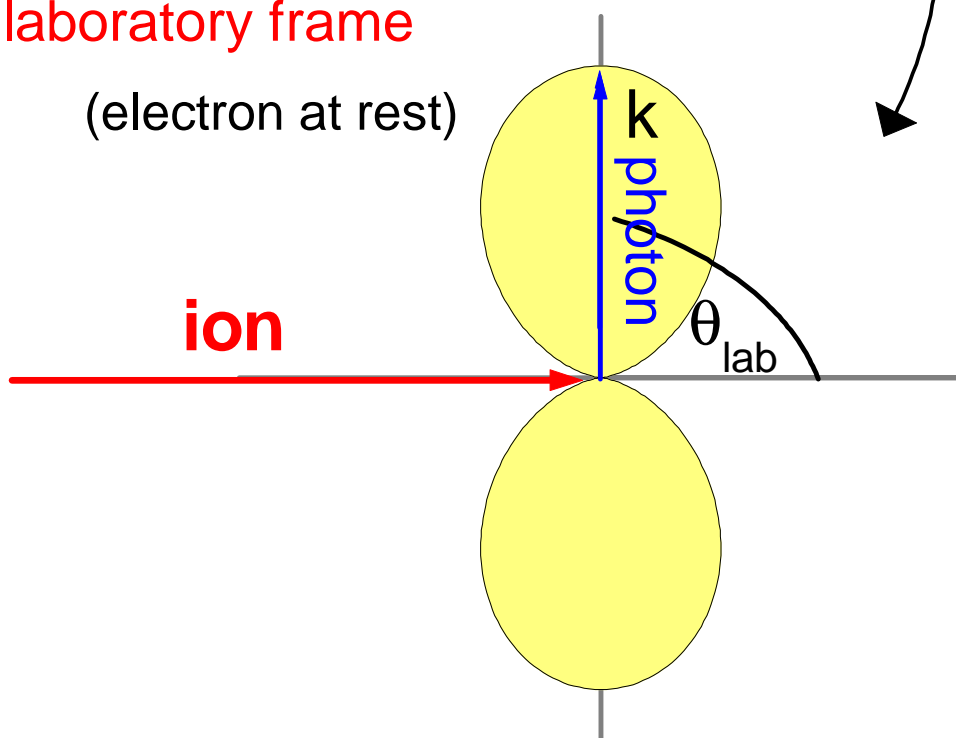


Recombination and Photoionisation of s-States

projectile frame (REC)



laboratory frame
(electron at rest)

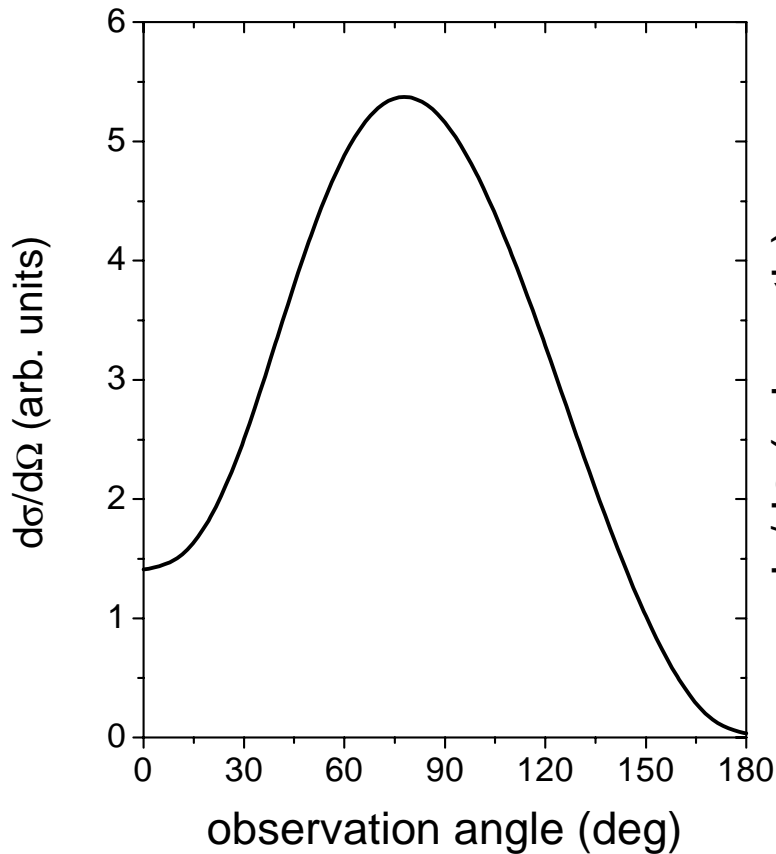


Retardation

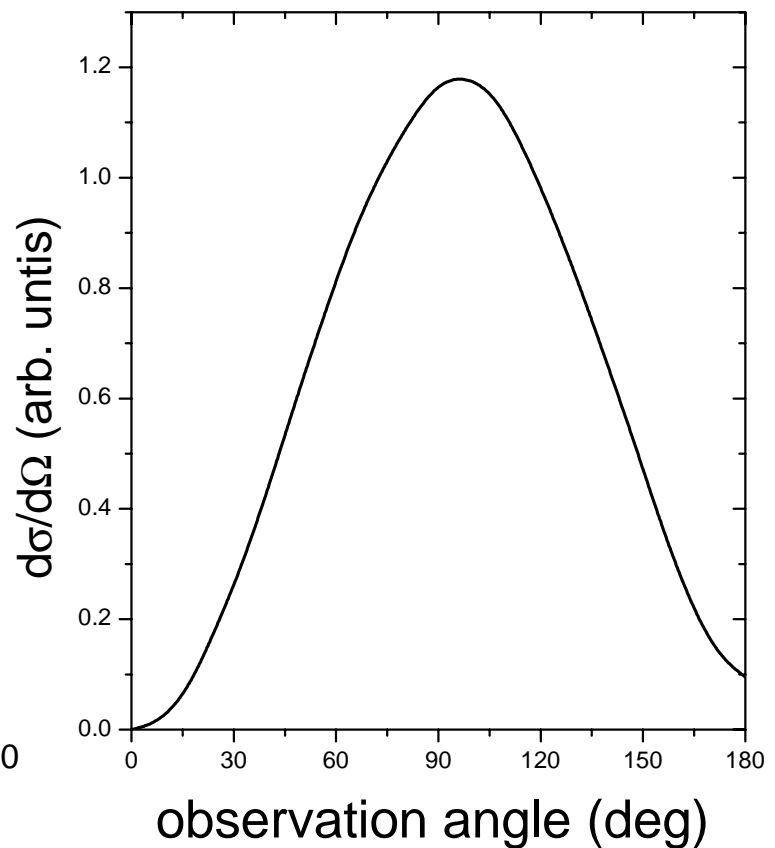
Lorentz transformation

Using non-relativistic wave functions, complete cancellation between retardation and Lorentz transformation occurs (verified by Anholt for $197 \text{ MeV/u Xe}^{54+} \Rightarrow \text{Be}$)

K-Shell Angular Distribution Studies for U^{92+} close to 500 MeV/u



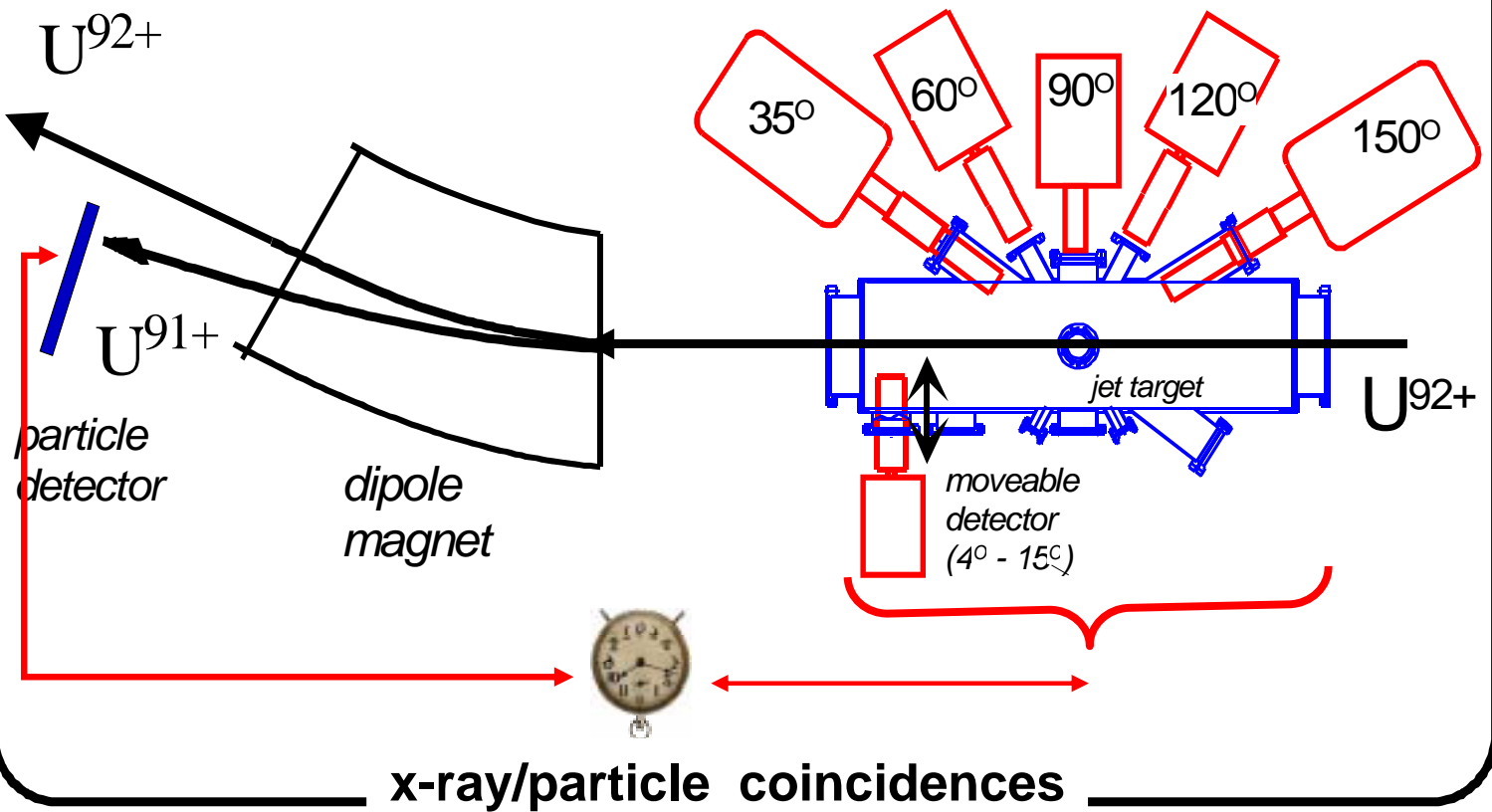
Eichler, PRA (1995)
rigorous all order relativistic
calculations



Hino and Watanabe, PRA (1989)
Relativistic Born approximation

Photon Angular Distribution Studies

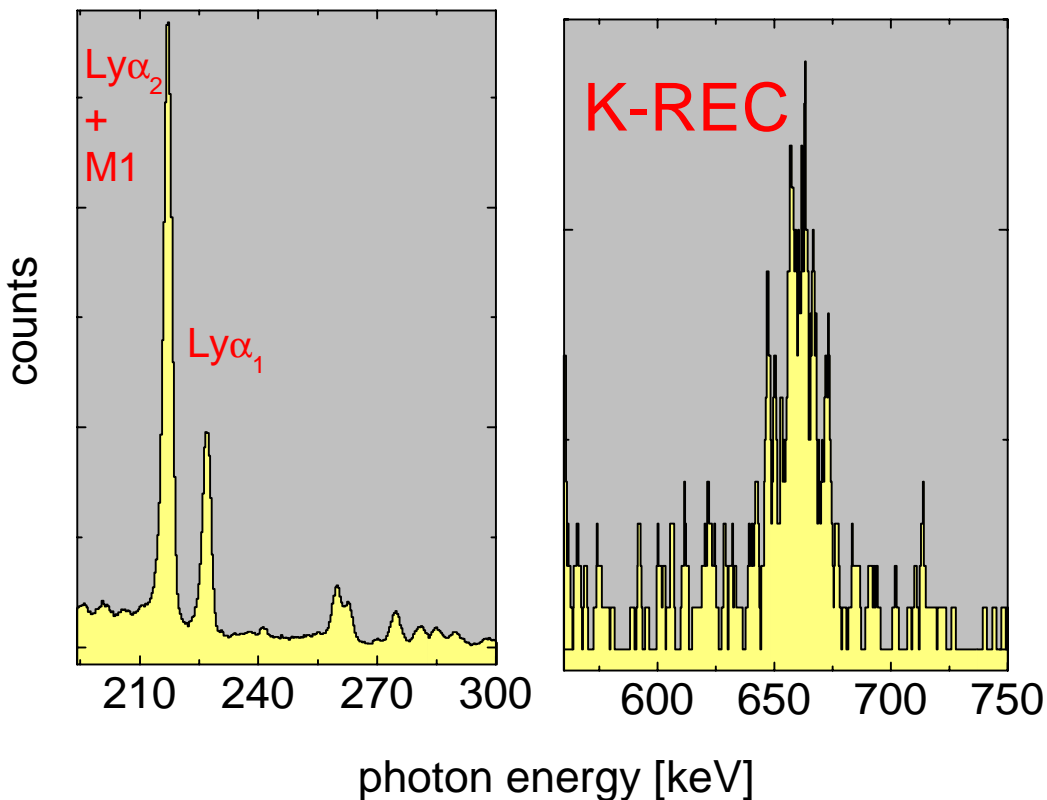
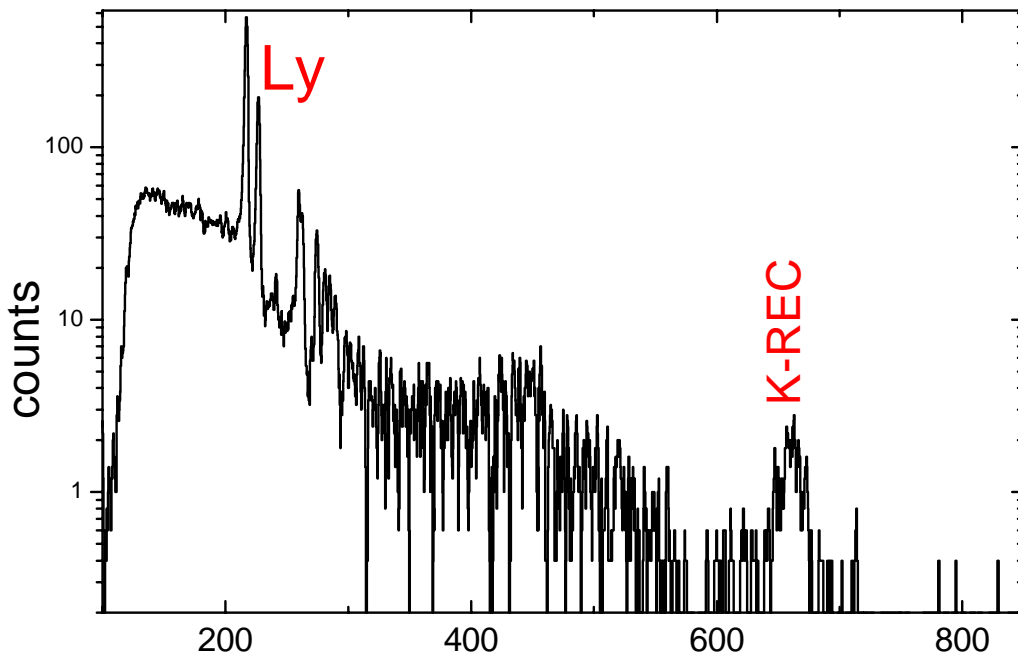
Experimental Setup at the Gas-Jet Target



Photon Emission Close to Zero Degree

$U^{92+} \Rightarrow N_2, 310 \text{ MeV/u}$

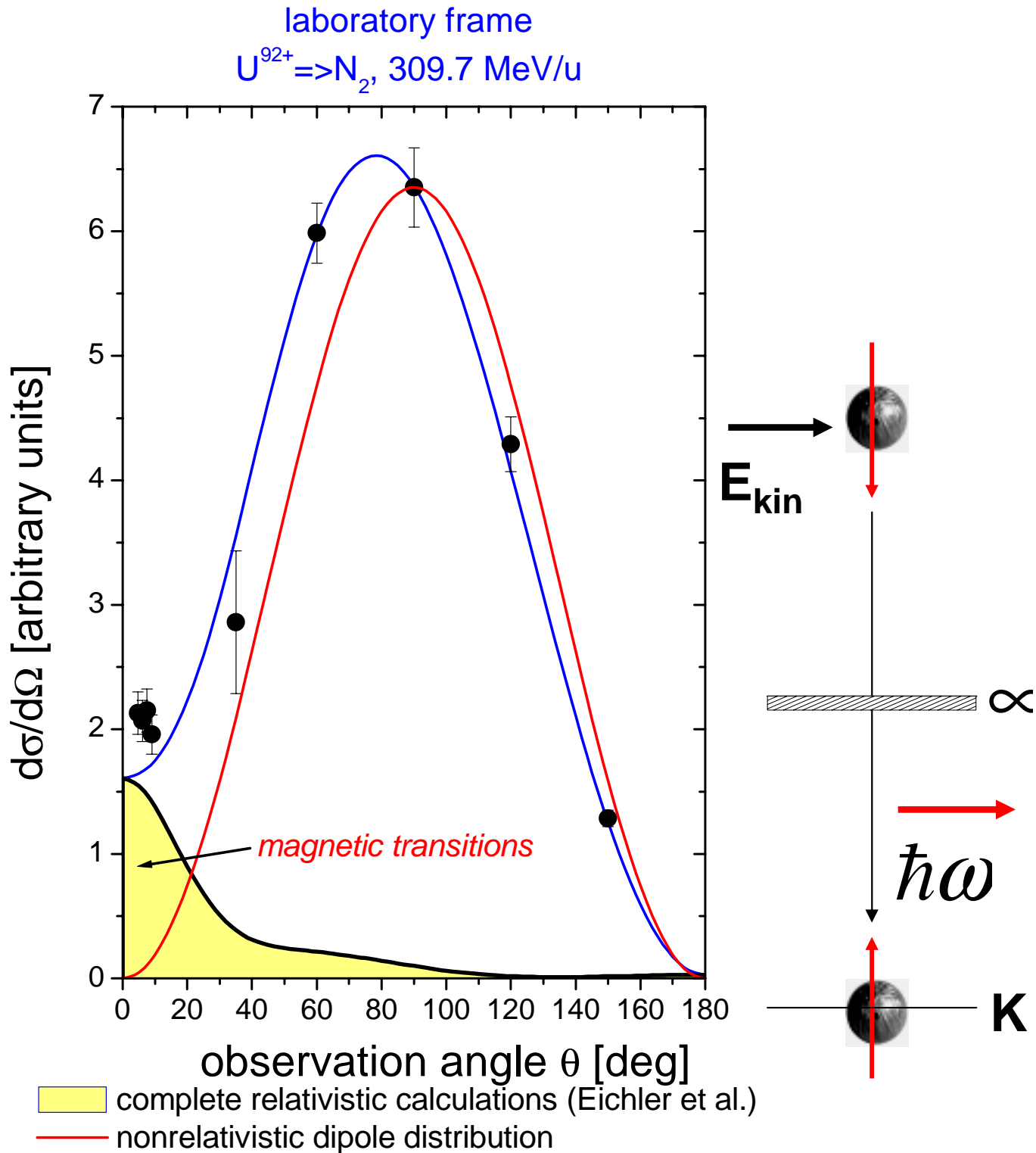
$\theta_{\text{LAB}} = 4 \text{ deg}$



normalization to the Ly α_2 +M1 intensity:

- a) angular distribution of the REC radiation in the emitter frame
- b) almost all systematic uncertainties cancel out completely

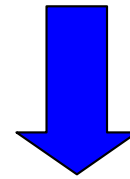
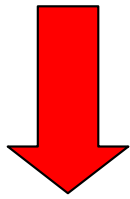
Kinematical Identification of Spin-Flip Transitions from Continuum States into the 1s-Ground State



zero degree emission: $(\alpha Z)^2$ correction to the magnetic emission

Angular Distribution

radiative capture into U^{92+} and photoionization of U^{91+}

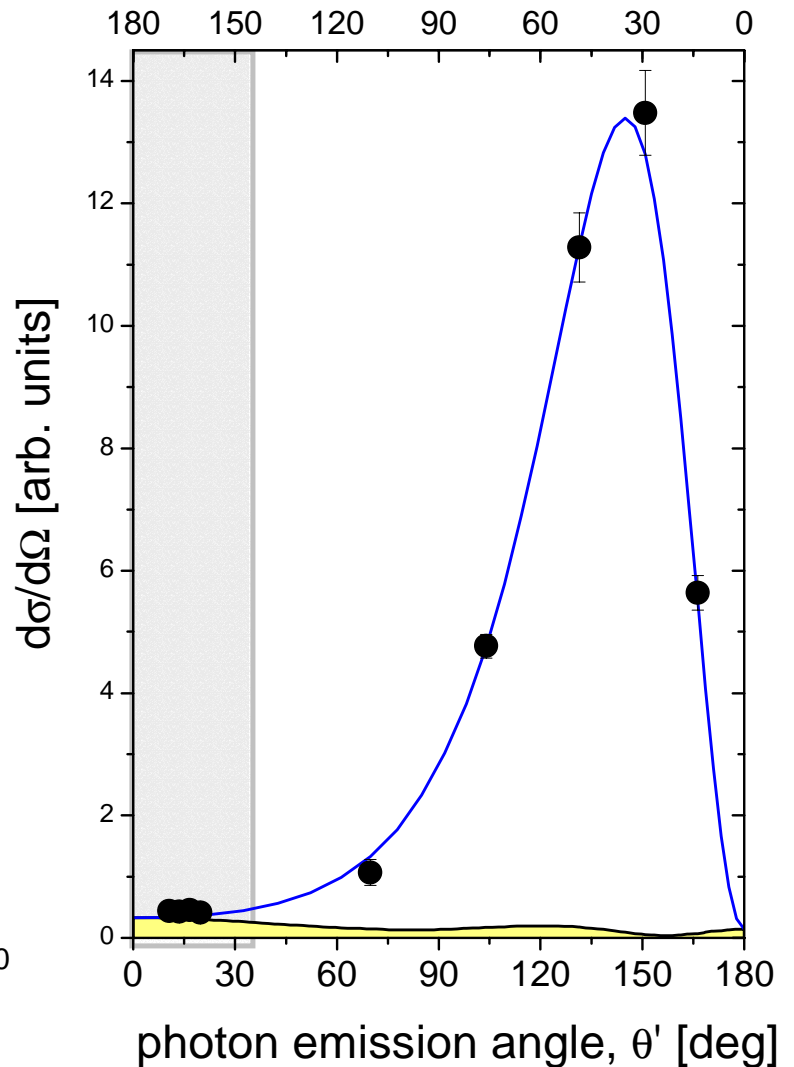
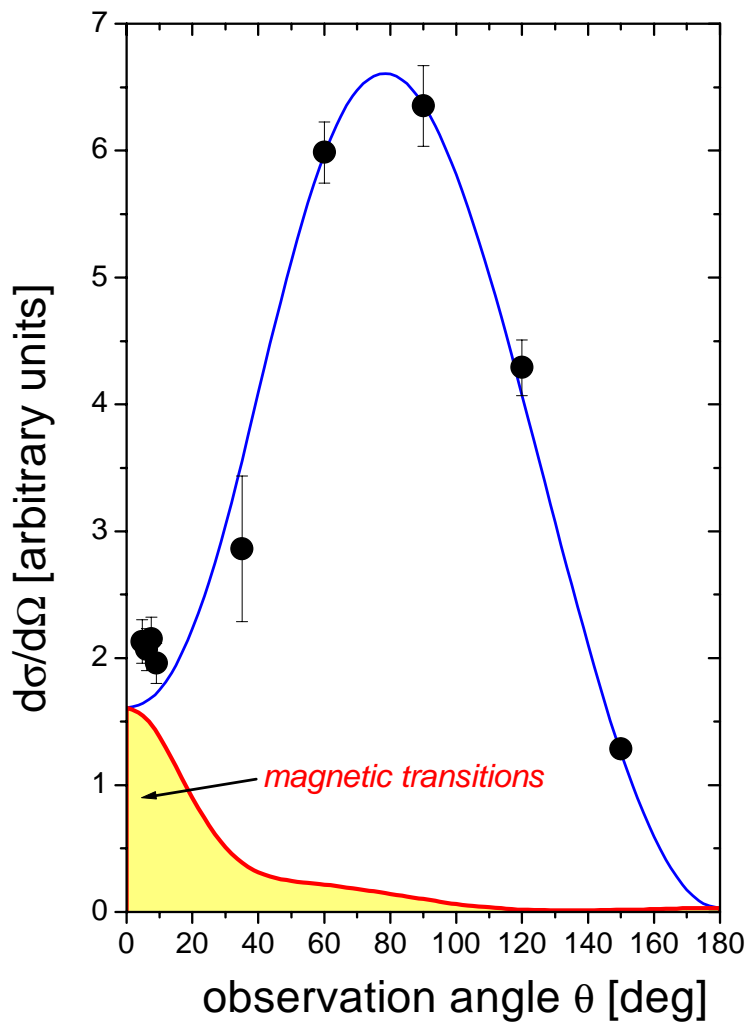


Time reversal

laboratory frame

emitter frame

electron emission angle, $\pi - \theta'$ [deg]



Angle and solid angle transformation

Open Questions

Angular distributions for few-electron ions
close to the threshold (decelerated ions)
(no appropriate theories available)

Polarization of the emitted photons
(no experimental information available)

Almost 100% linear polarization predicted

Summary

- **Storing and cooling of highly charged ions delivers brilliant beams for experiments**
- **The ESR provides ideal conditions for accurate atomic structure studies**
- **1s-LS experiments at the ESR allowed to improve the experimental accuracy by an order of magnitude**
- **Study of 2eQED provides a test of QED in the strong field limit which is not blended by nuclear effects**
- **The study of elementary atomic processes for highly-charged heavy ions via their time-reversal**

Outlook

- **Implementation of new spectroscopic tools and techniques which are currently in preparation may provide a further gain of accuracy towards the 1 eV limit**
- **Expansion of collision studies to few-electron ions**
- **Polarisation and x-x correlation studies**
- **Combined photon, electron and recoil ion momentum spectroscopy**
- **Structure and Collision Studies at High- γ**