

# *Relativistic Quantum Dynamics Explored in Atomic Collisions of High-Z Ions*

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in collaboration with

## *Experiment*

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## *Theory*

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*JAERI, Japan*  
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# *Relativistic Quantum Dynamics*

## **Introduction**

Atomic structure at high-Z

## **Test of Bound-State QED for the Groundstate in H- and He-Like Ions**

1s Lamb Shift

Two-Electron QED

## **Relativistic Effects in Electron-Ion Recombination and Electron Capture**

Photon correlation studies

Population of magnetic sub-levels

Multipole-Mixing

Photon polarization studies

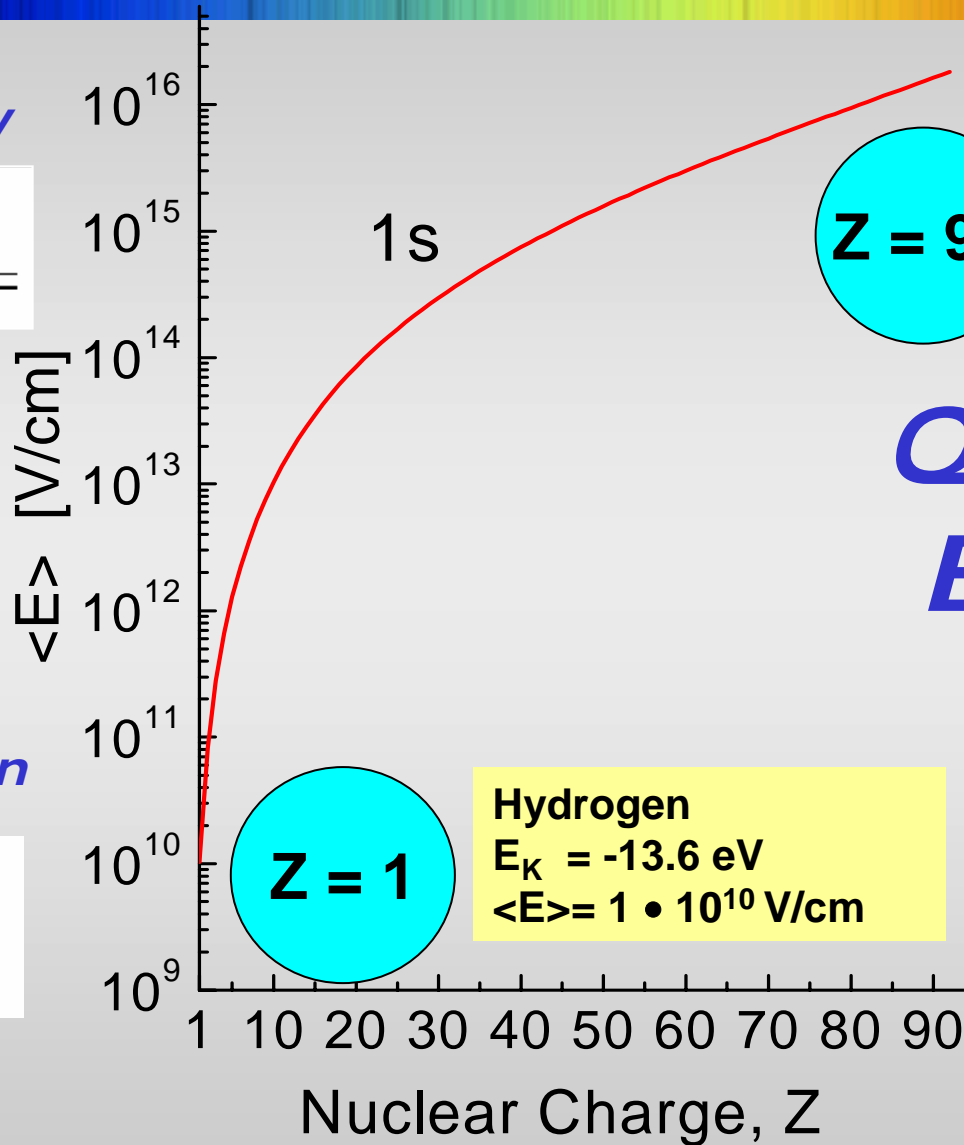
3D x-ray/compton cameras

## **Summary and Outlook**

# Atomic Physics in Extremely Strong Coulomb Fields

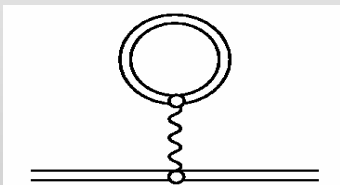
H-like Uranium  
 $E_K = -132 \cdot 10^3 \text{ eV}$   
 $\langle E \rangle = 1.8 \cdot 10^{16} \text{ V/cm}$

Self Energy



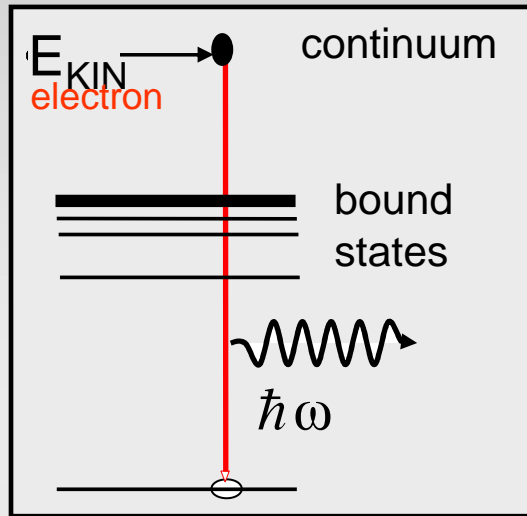
Quantum  
 Electro-  
 Dynamics

Vacuum Polarization



1s-ground state: increase of the electric field strength by six orders of magnitude

## Radiative Recombination/Electron Capture

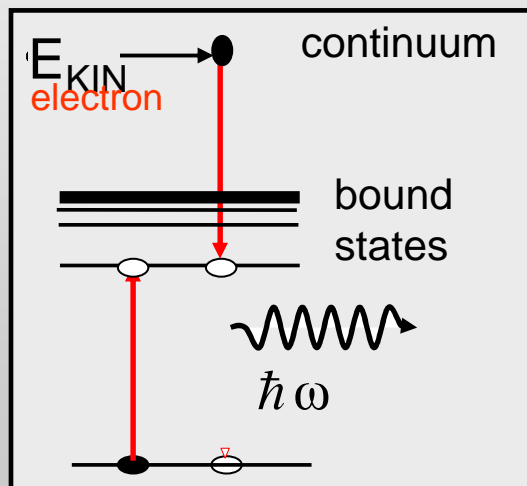


- *Electron capture into a bound ionic state by emission of a photon*

$$\hbar\omega = E_B + E_{KIN}$$

- *Time-reversed photionization*
- *Only possible capture/recombination process for bare ions colliding with electrons*

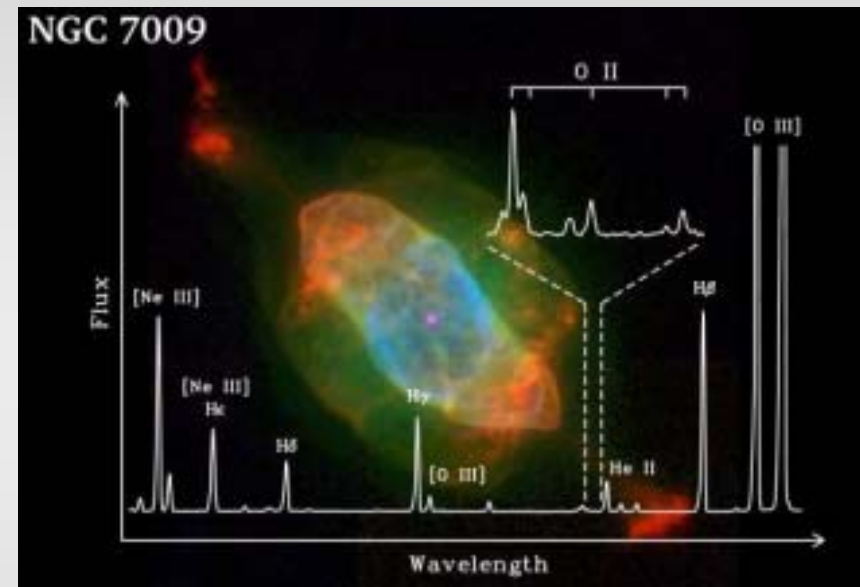
## Dielectronic Recombination/Electron Capture



- *Resonant (non-radiative) capture of an electron into a bound state*
- *Time-reversed Auger process*
- *Important charge exchange process for multi-electron ions*

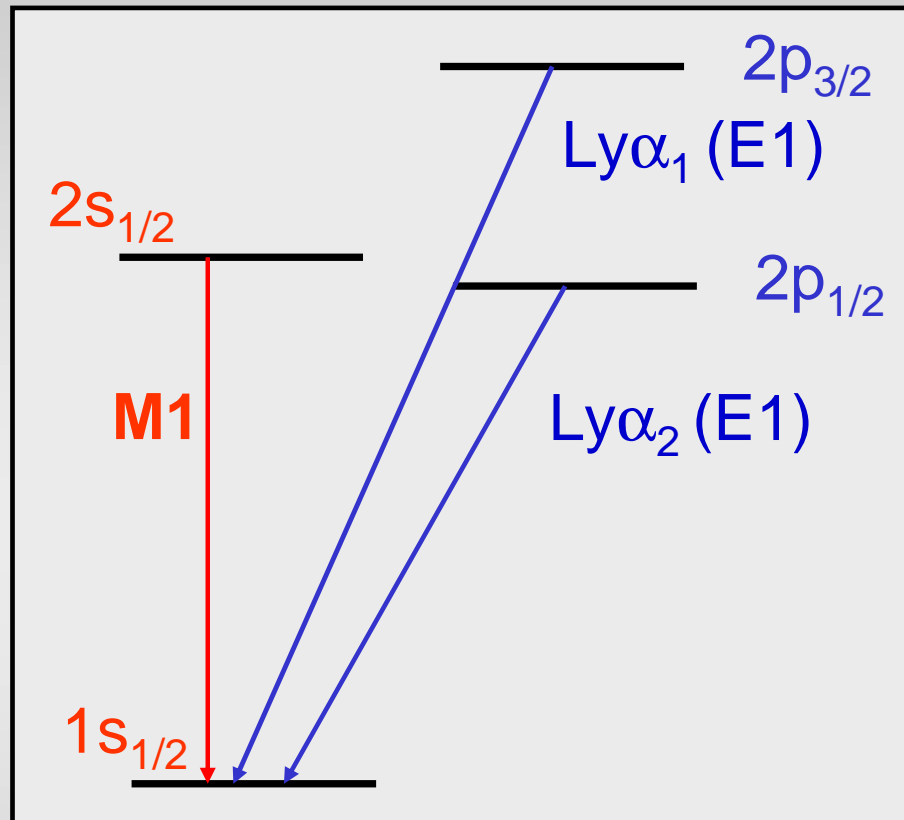
e.g.

- *ion sources*
- *accelerator*
- *charge state distributions of HCl in matter*
- *photon emission and absorption characteristic of plasma sources*
- *astrophysics*



*The spectra of ionized planetary nebulae are dominated by strong H and He recombination lines, emitted following capture*

# The Structure of One-Electron Systems



## QED corrections

$$\Delta E \sim Z^4/n^3$$

**Z:** nuclear charge number  
**n:** prinzipal quantum number

Atomic systems at high-Z

- Large relativistic effects on energy levels and transition rates (e.g. shell and subshell splitting)
- Large QED corrections
- Transition energies close to 100 keV

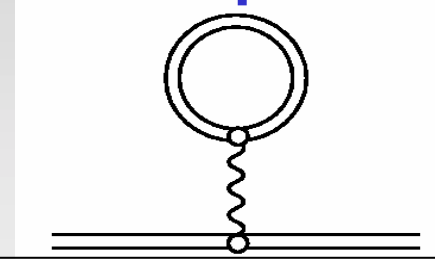
# Bound-State QED: 1s Lamb Shift

*Sum of all corrections, leading to deviations from the Dirac theory for a point like nucleus*

Self energy



Vacuum polarization



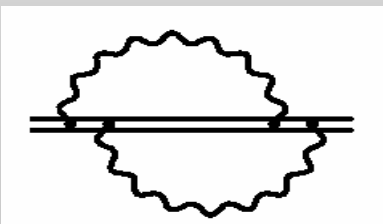
$U^{92+}$	SE	VP	NS
	355.0 eV	-88.6 eV	198.7 eV

$$\Delta E = \alpha/\pi (\alpha Z)^4 F(\alpha Z) m_e c^2$$

**Low Z-Regime:**  $\alpha Z \ll 1$   
 $F(\alpha Z)$ : series expansion in  $\alpha Z$

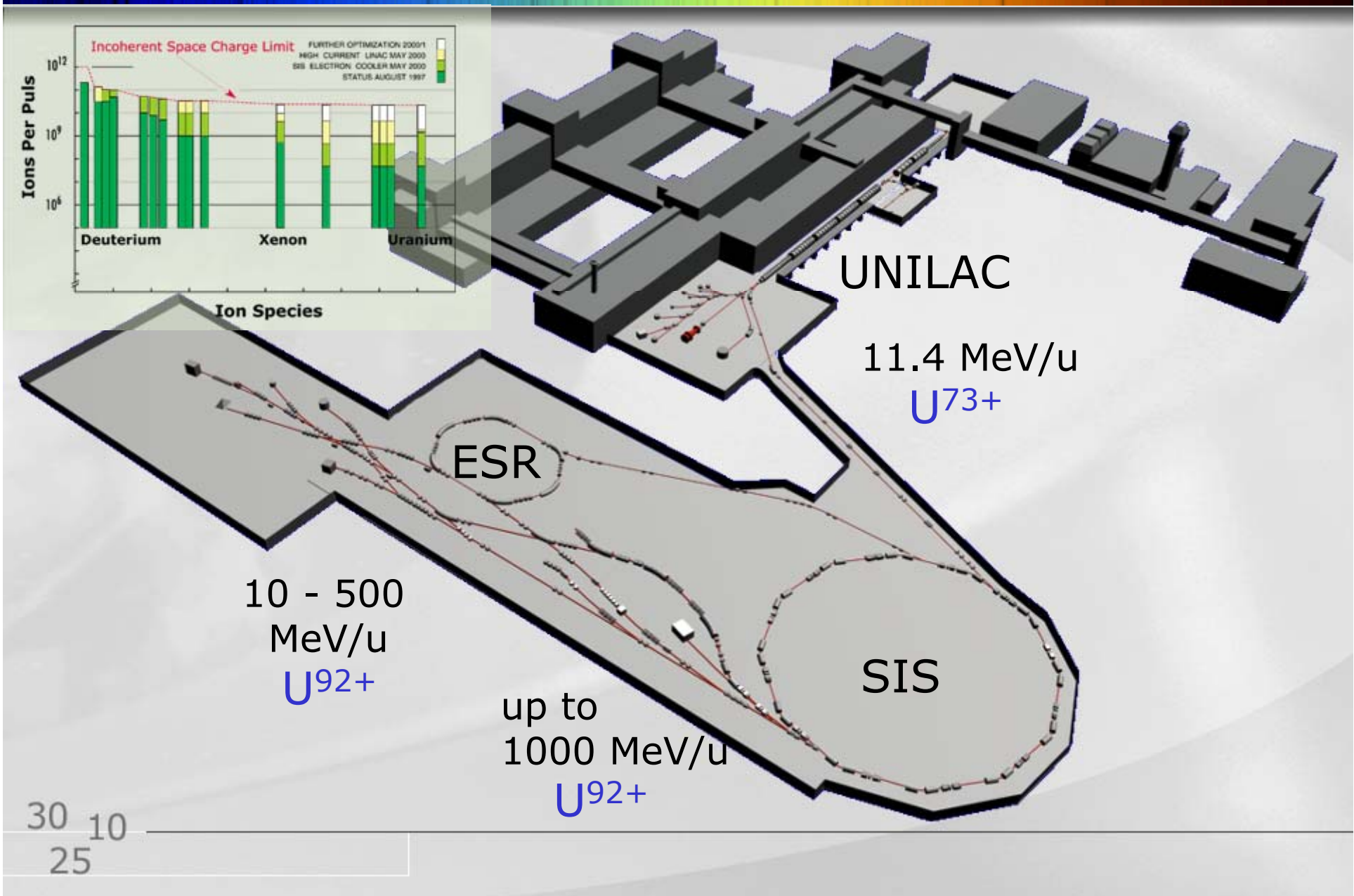
**High Z-Regime:**  $\alpha Z \approx 1$   
 $F(\alpha Z)$ : series expansion in  $\alpha Z$  not appropriate

**Goal:**



$\pm 1$  eV

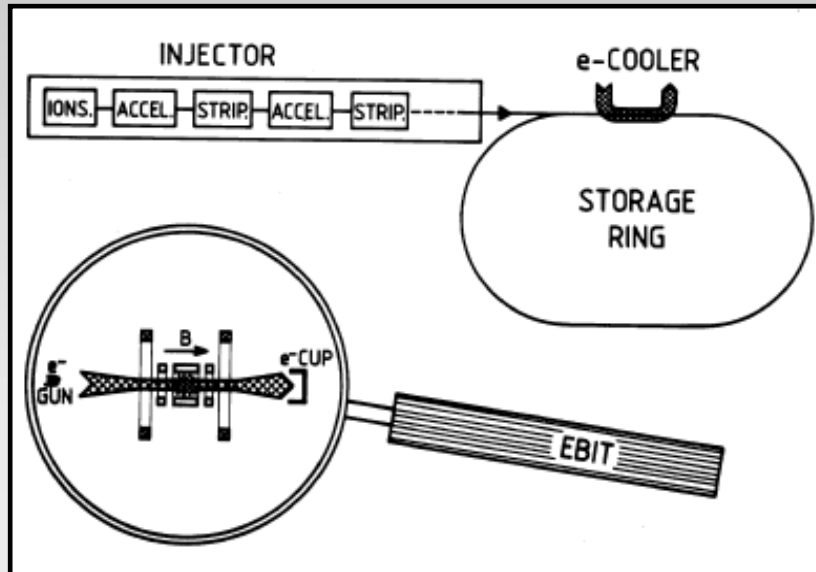
# GSI - Accelerator Facility





# Production of Highly Charged Heavy Ions

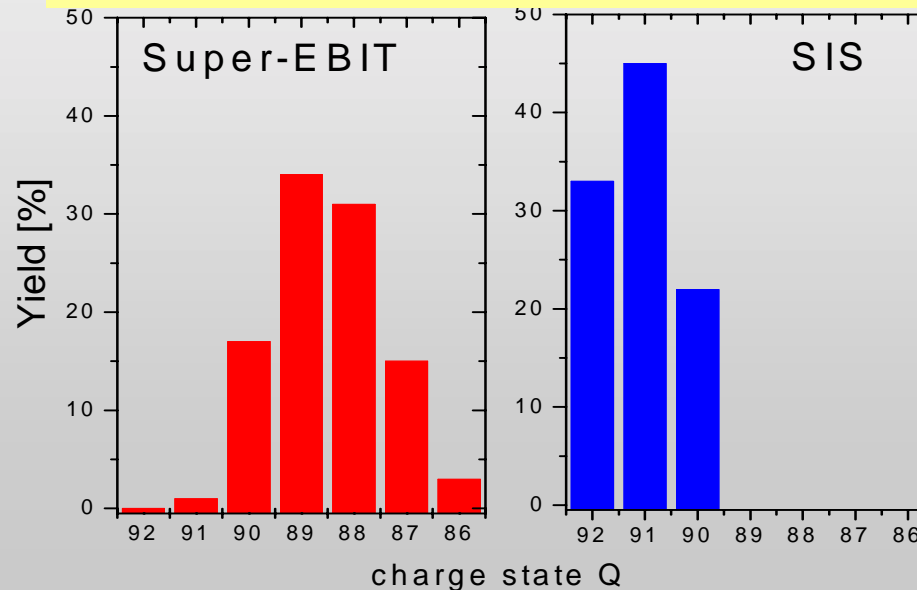
**EBIT: Trapped, stationary ions; charge state production by electron bombardment**



**Accelerator: Fast moving ions, charge state production by penetration through stripper targets**

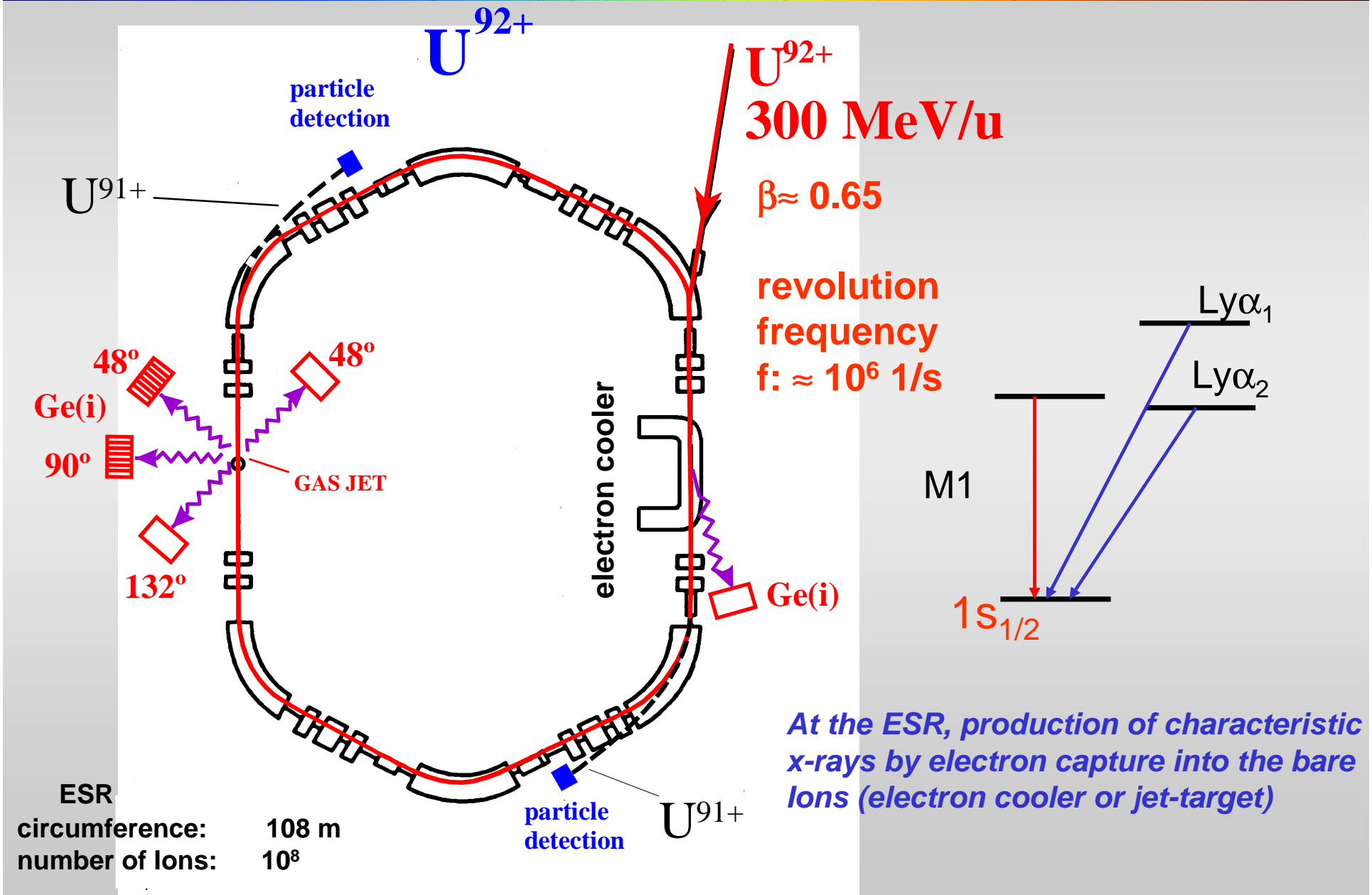
## Charge State Distributions for Uranium

**200 keV electron energy (ion at rest)**



**300 MeV/u ( $\beta \approx 0.65$ )**

# Lamb-Shift Studies for High-Z Ions: X-ray Spectroscopy at the ESR Storage Rings



# The Experimental Challenge

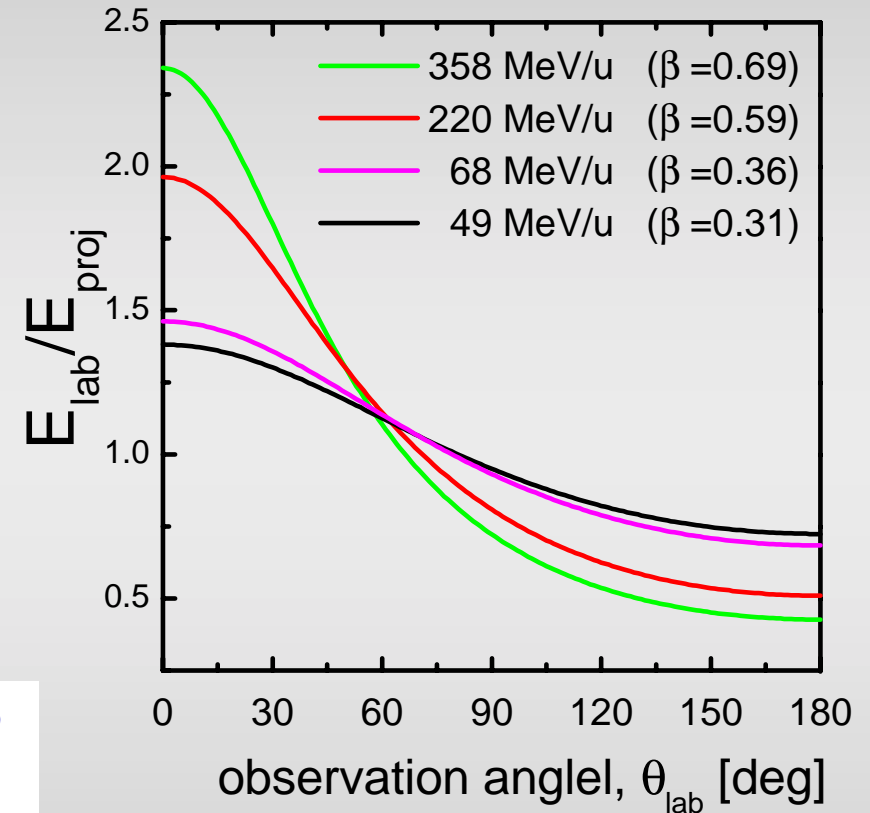
## Relativistic Doppler-Transformation

$$E_{\text{lab}} = \frac{E_{\text{proj}}}{\gamma \cdot (1 - \beta \cdot \cos\theta_{\text{lab}})}$$

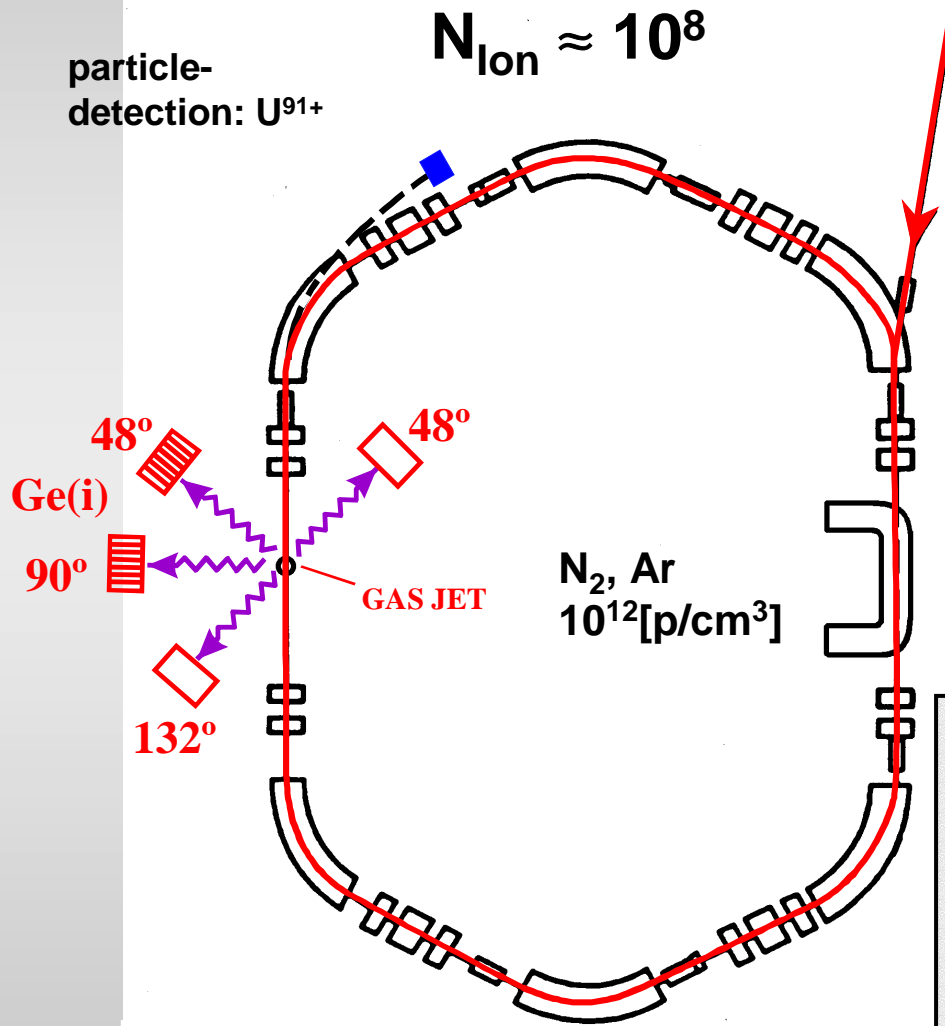
$E_{\text{lab}}$ : Photon energy in the laboratory system

$E_{\text{proj}}$ : Photon energy in the emitter system

**Doppler-Correction:** *Strong dependence on velocity and the observation angle  $\theta_{\text{LAB}}$*



# X-Ray Spectroscopy at the Jet-Target



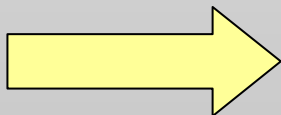
$$E_{\text{lab}} = \frac{E_{\text{proj}}}{\gamma \cdot (1 - \beta \cdot \cos \theta_{\text{lab}})}$$

$E_{\text{lab}}$ : Photon energy in laboratory system

$E_{\text{proj}}$ : Photon energy in emitter system

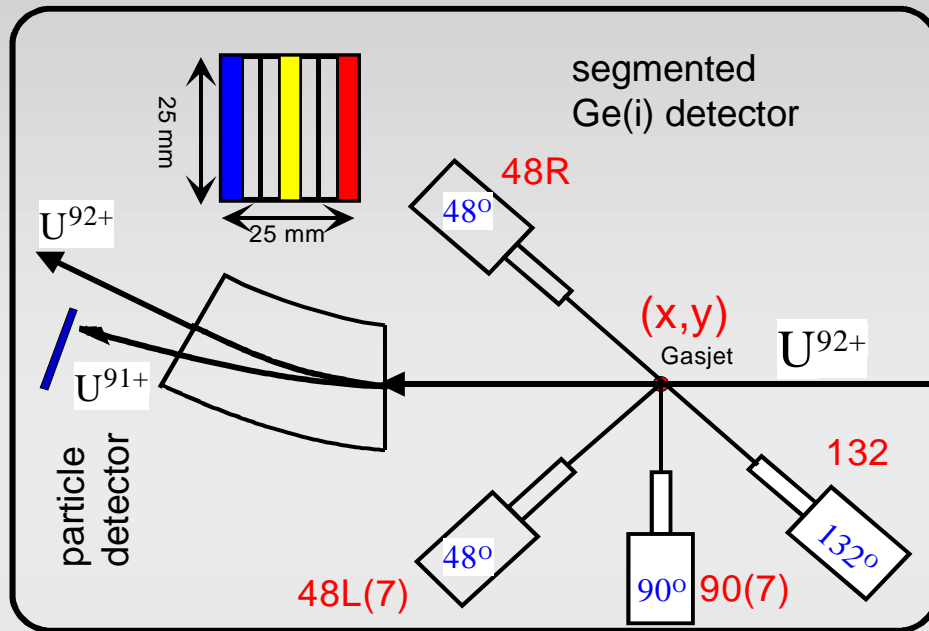
## Principle of LS Experiments at ESR

- 1. Production of bare ions*
- 2. Stacking and cooling*
- 3. Electron capture in excited states  
(jet-target or electron cooler)*
- 4. Detection of x-rays*
- 5. Doppler correction*
- 6. Comparison with Dirac theory*

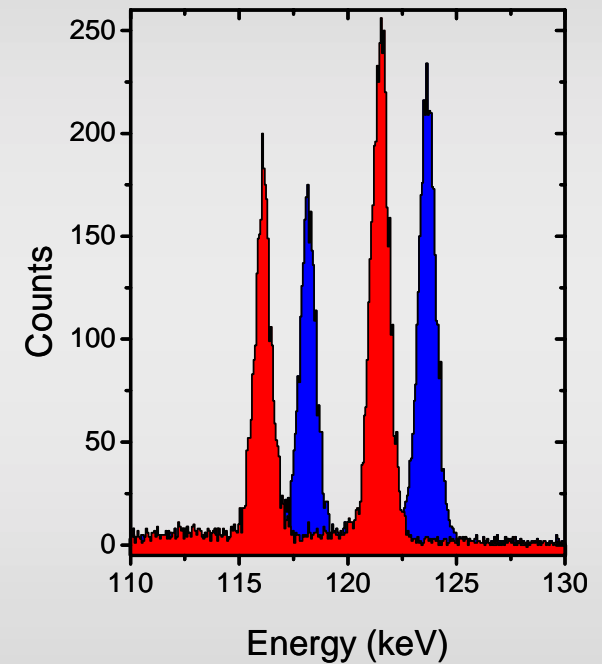


**1s Lamb Shift**

# Lamb Shift-Experiment at the Jet-Target



$Ly\alpha_1$  ( $2p_{3/2} \rightarrow 1s_{1/2}$ )  
 $102\,171 \pm 13.2$  eV



$\Delta\theta \approx 3.0$  deg

- *Simultaneous observation at various angles*
- *Forward/Backward symmetry*
- *Left/Right symmetry*

## 1s-Lamb Shift

**Experiment:  $468$  eV  $\pm$   $13$  eV**  
 Theory:  $466$  eV\*

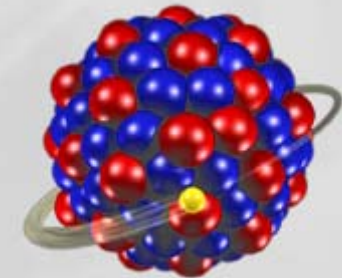
## Test of Quantum Electrodynamics (1s-LS)

### Hydrogen-Atom

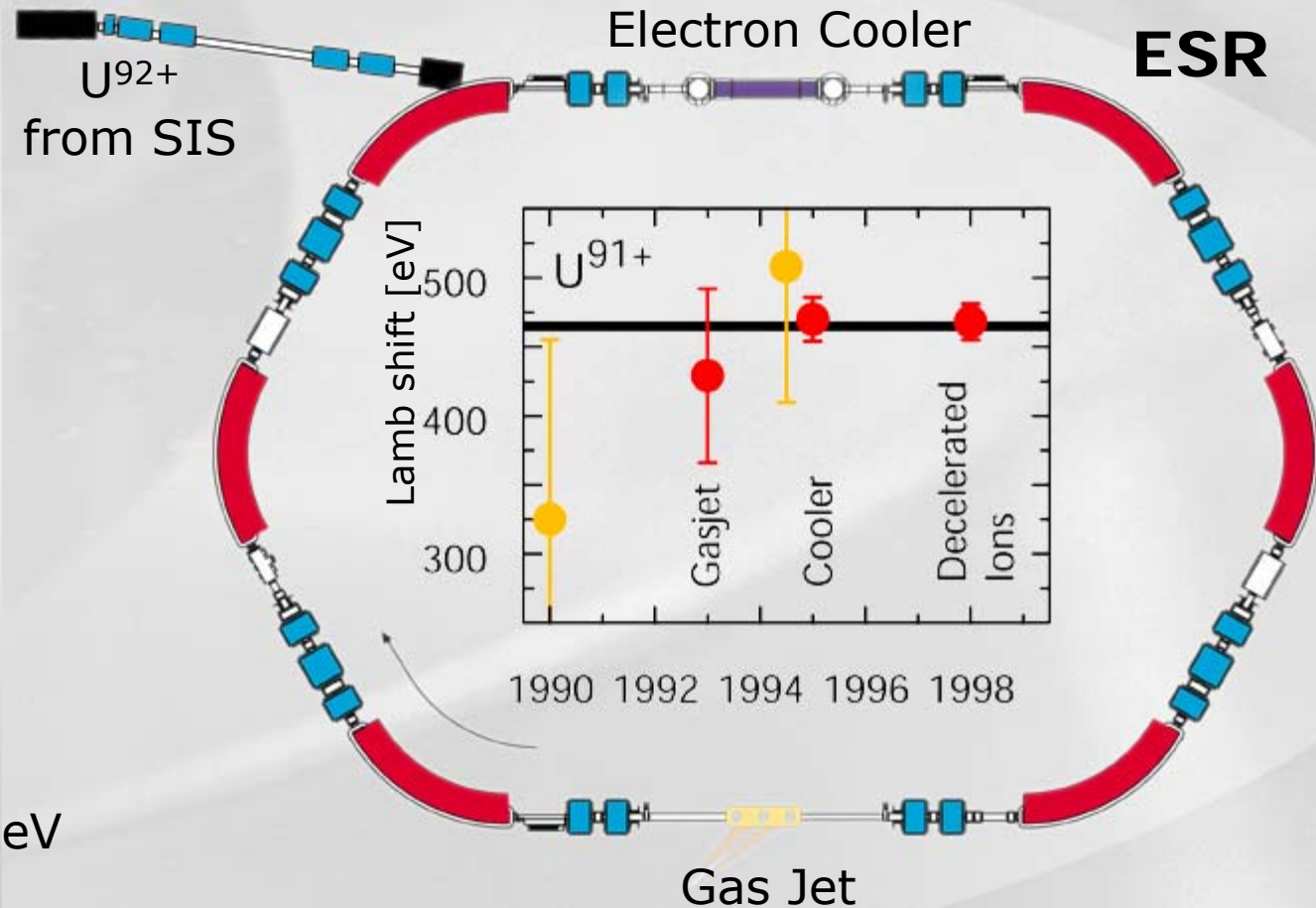


$Z=1$ ;  $E_b = 13.6 \text{ eV}$   
 $Z \cdot \alpha \ll 1$

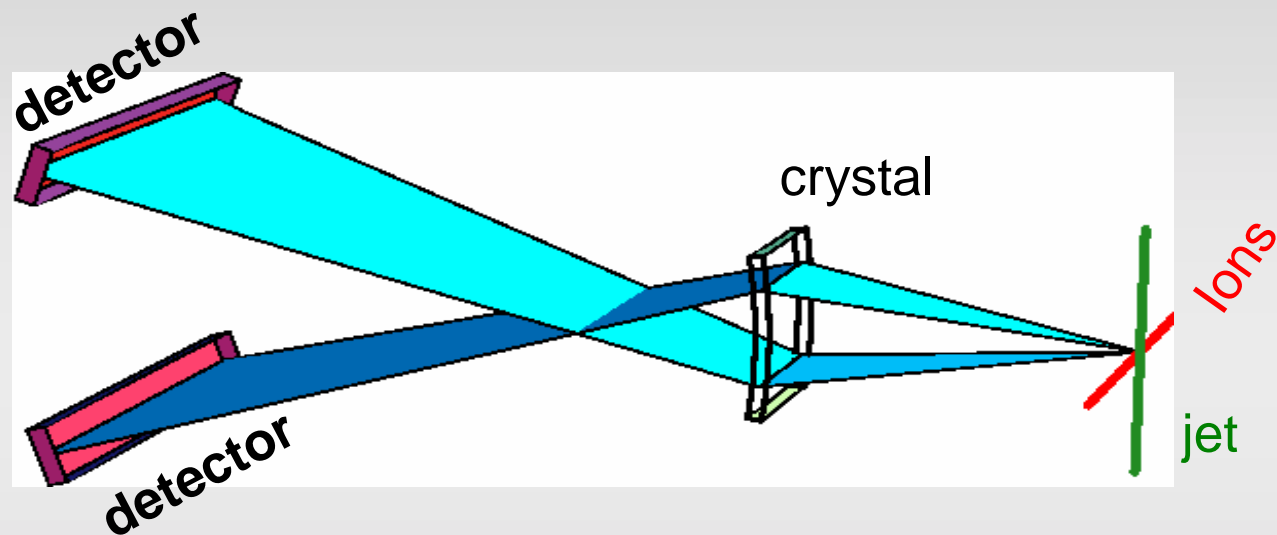
### Uranium-Ion



$Z=92$ ;  $E_b = 132 \text{ KeV}$   
 $Z \cdot \alpha \approx 1$



# Transmission crystal spectrometer: *towards an accuracy of 1 eV*

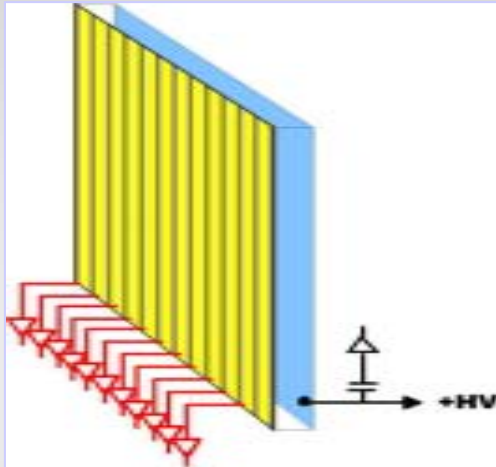


Bragg-Laue relation

$$n \cdot \lambda = 2 \cdot d \cdot \sin\theta$$

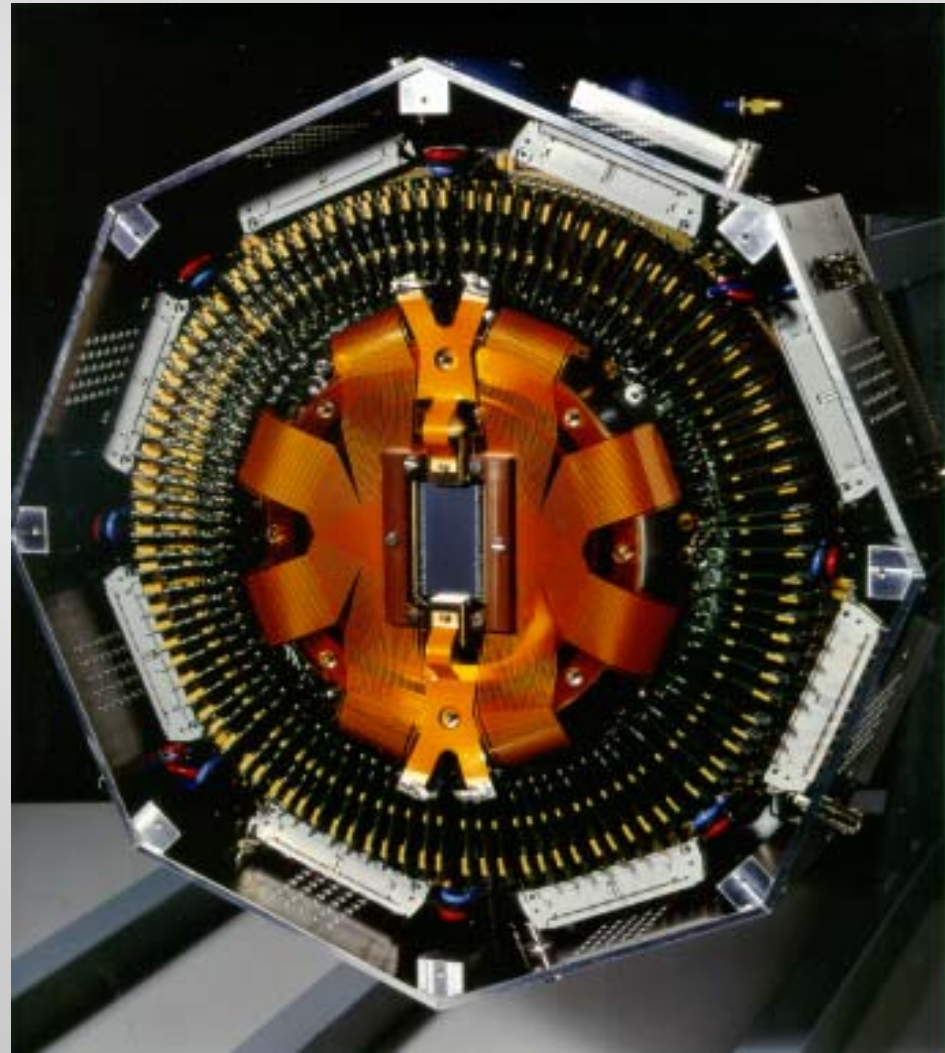


## Micro-Strip Germanium Detector Development: Energy Resolved X-Ray Imager, Timing, Multi-Hit Capability



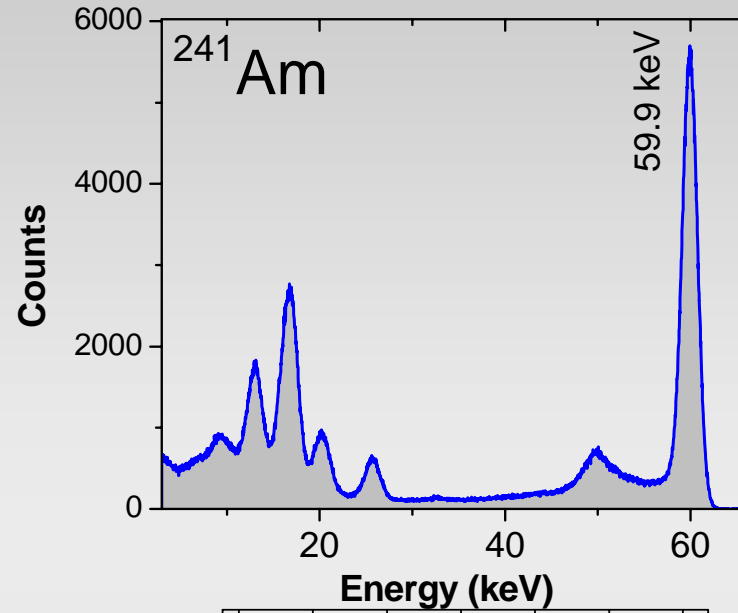
- crystal spectrometer
- doppler tuned
- polarization studies
- Compton cameras

D. Protic et al., IEEE in print (2001)

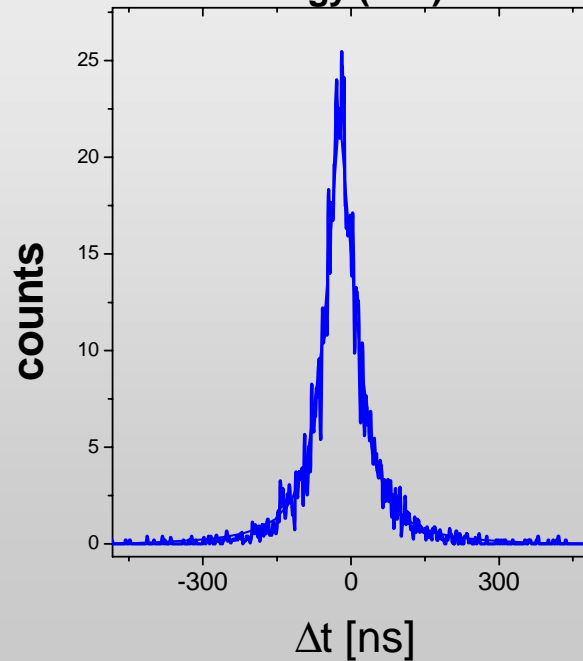
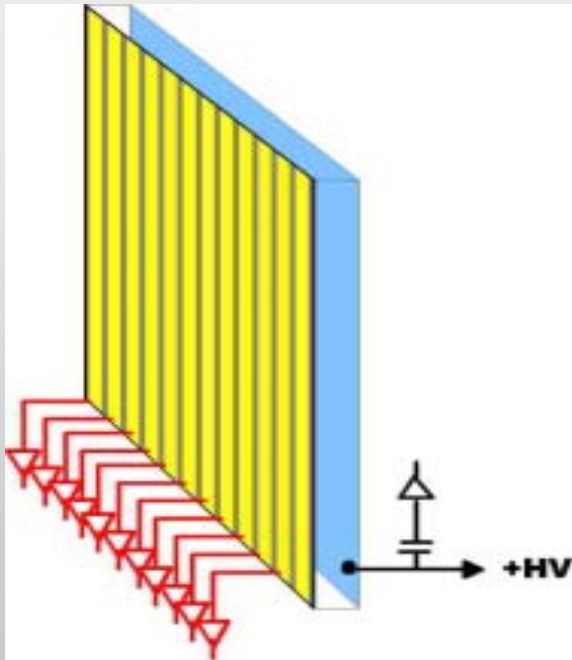


# Micro-Strip Germanium Detectors: Position Sensitive X-ray Spectroscopy

**Energy resolution**  
 1.6 keV @ 60 keV  
  
**Position resolution**  
 200  $\mu\text{m}$   
  
**Time resolution**  
 50 ns

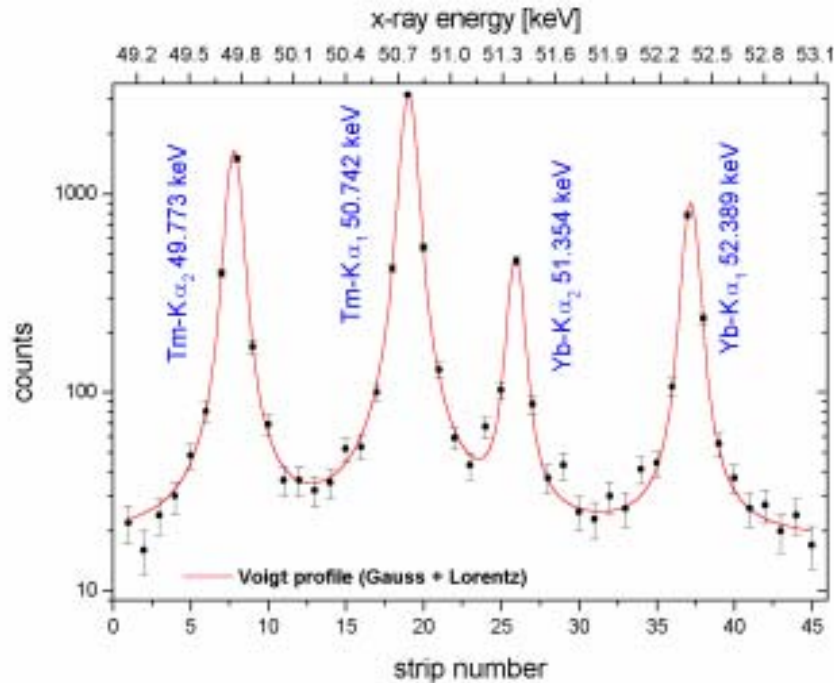
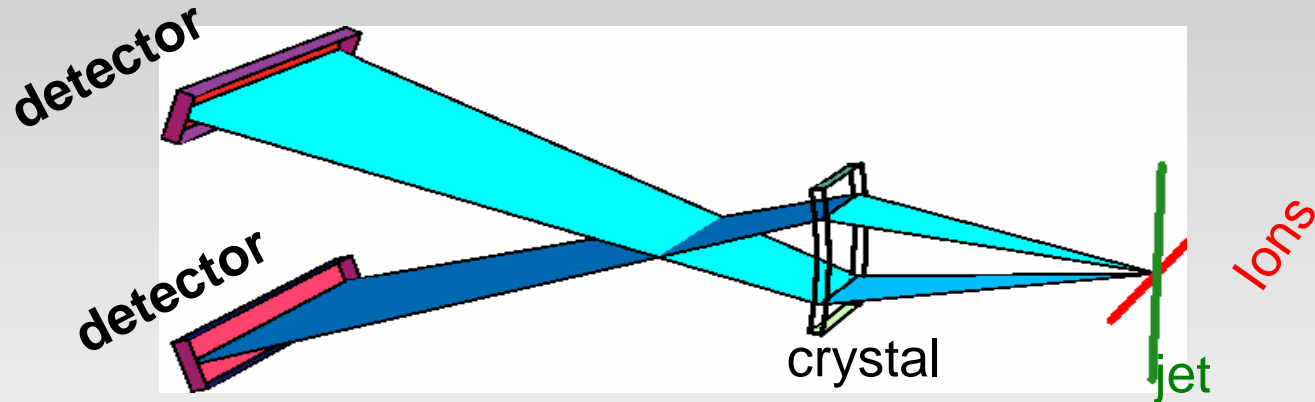


Energy



Timing

# Transmission crystal spectrometer towards an accuracy of 1 eV

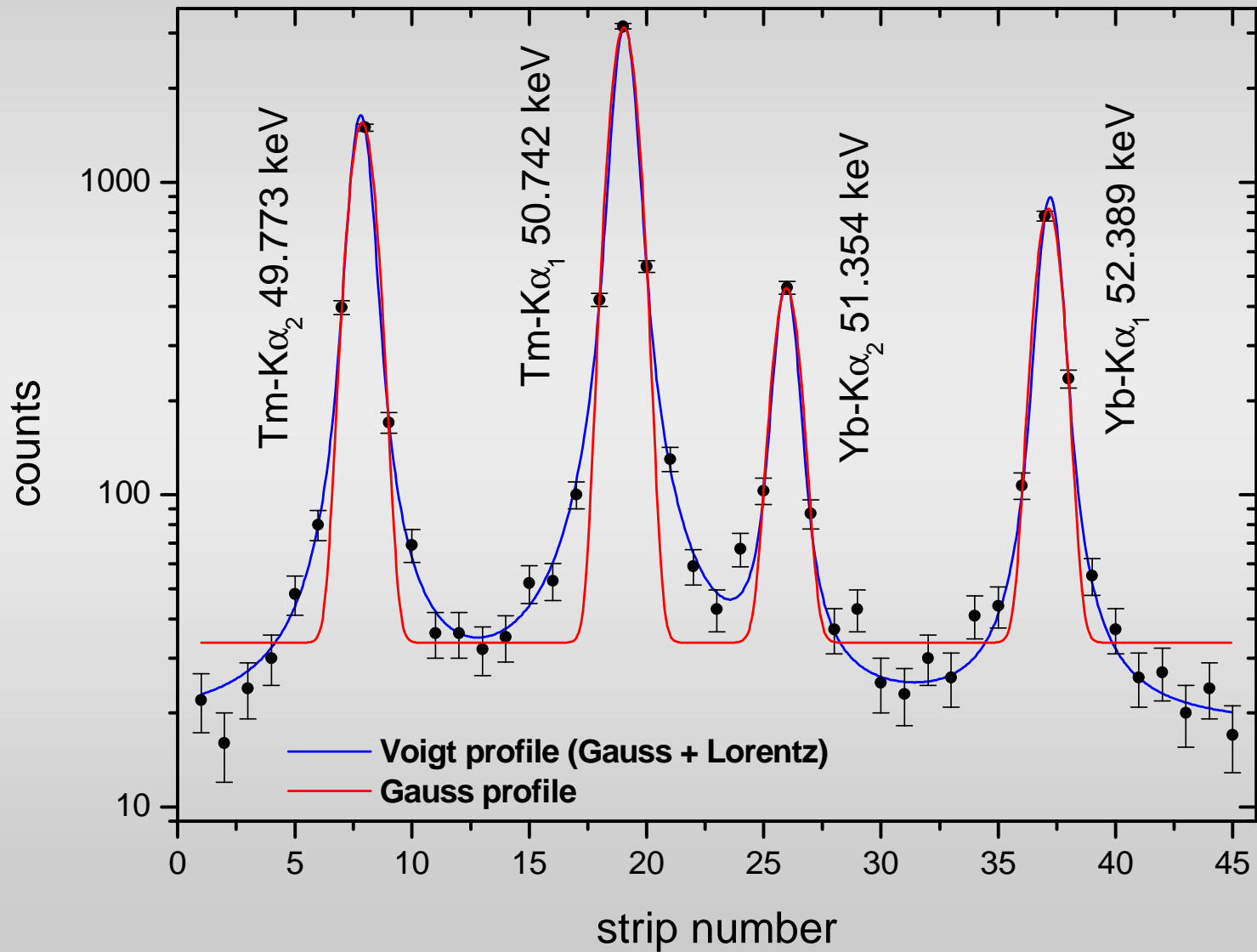


H.F. Beyer et al., GSI Report 2000

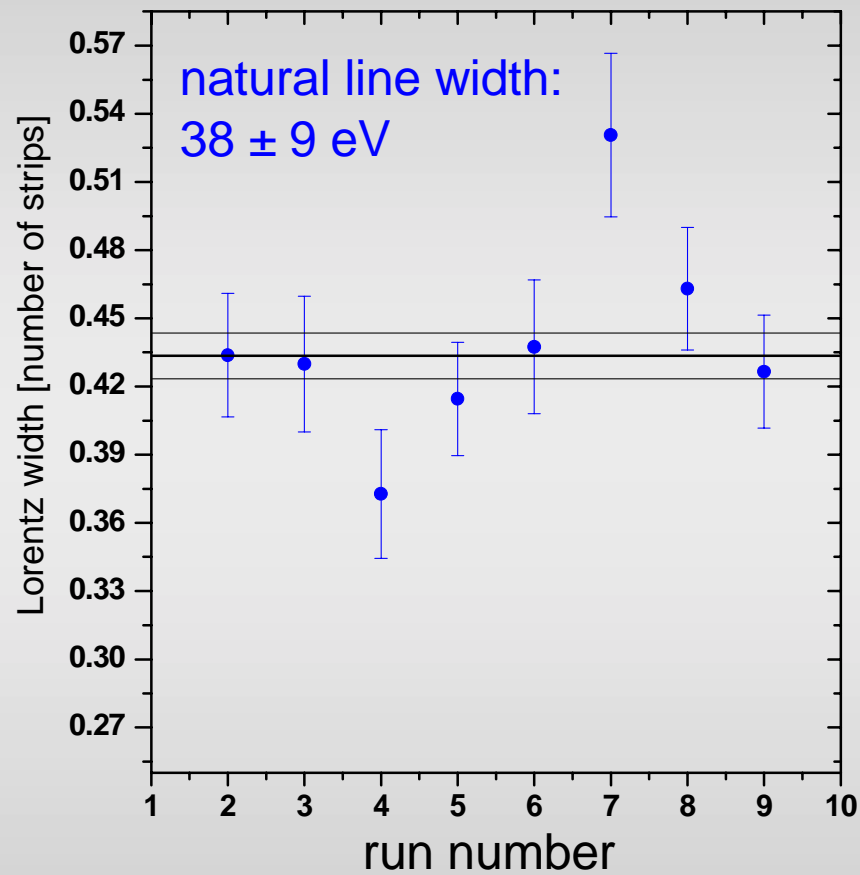
Bragg-Laue relation

$$n \cdot \lambda = 2 \cdot d \cdot \sin\theta$$

# Transmission crystal spectrometer towards an accuracy of 1 eV



# using micro-strip detectors, lifetimes of atomic states are accessible (natural line width)



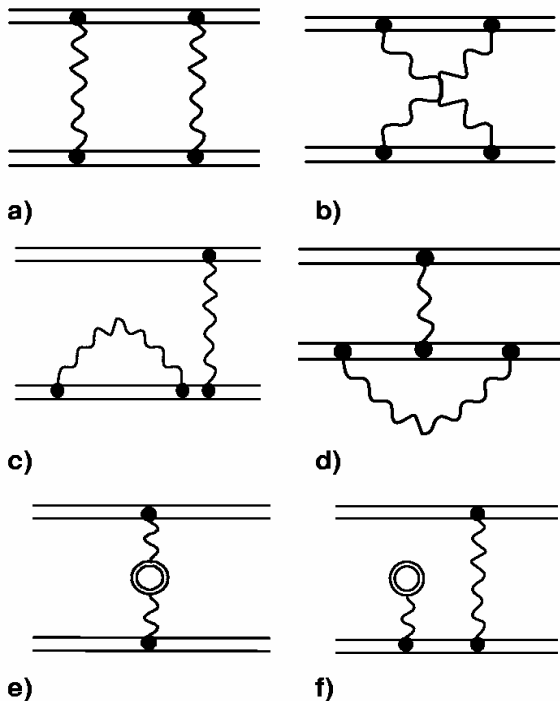
natural line width  
theory: 30 eV

# Electron-Electron Interaction in Strong Fields

*Measurement of the 2eQED for Uranium at*  
**Accuracy: 2 eV;  $\Delta E/E \approx 0.1\%$**

**Z=92**

**Two-Electron Contribution: 2246.0 eV**



**a,b) Non-Radiative QED**

**+1.3 eV [U<sup>90+</sup>]**

**0.06%**

**c,d) Two-Electron Self Energy**

**-9.7 eV [U<sup>90+</sup>]**

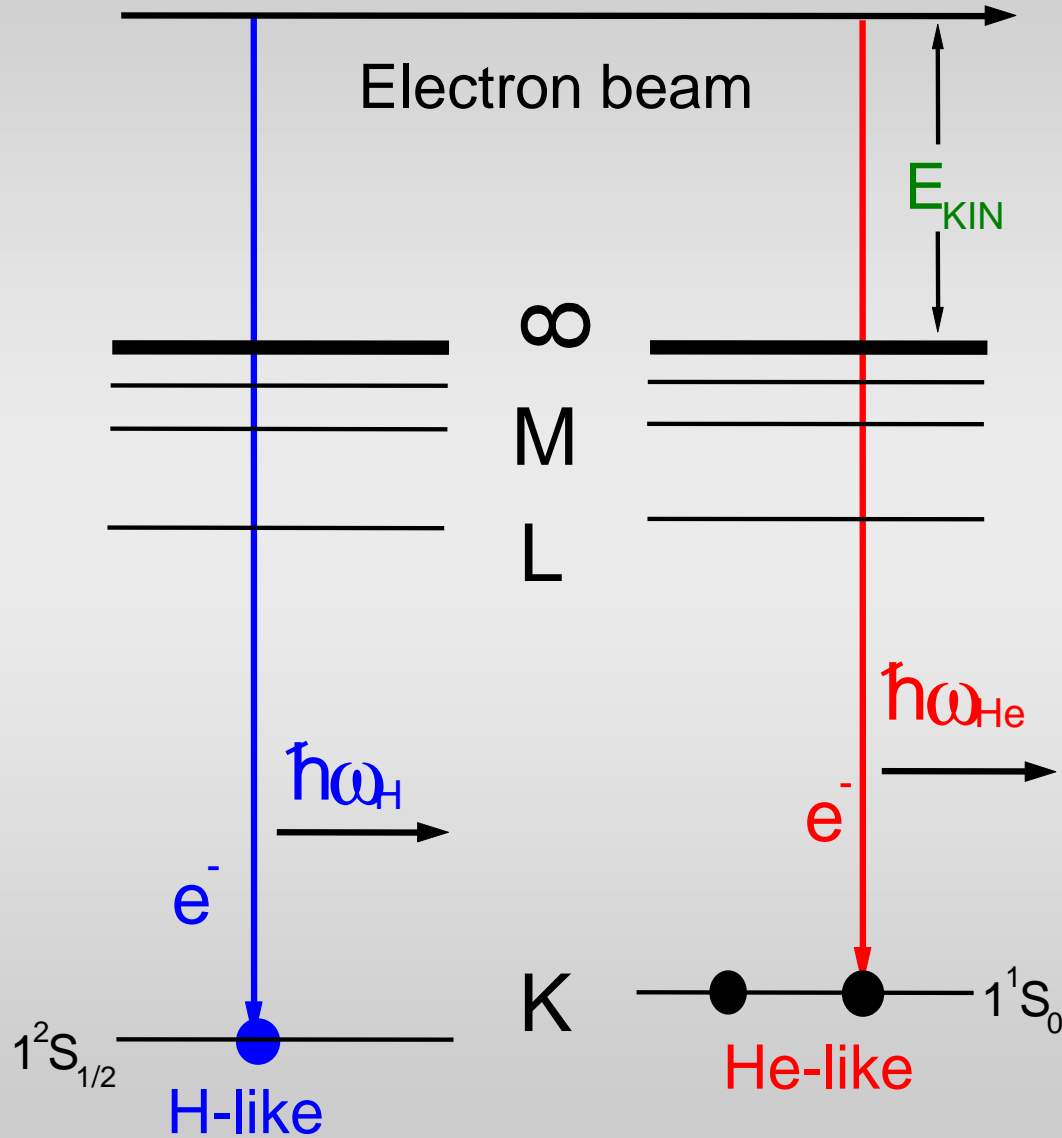
**0.4%**

**e,f) Two-Electro Vacuum Polarization**

**+2.6 eV [U<sup>90+</sup>]**

**0.1%**

# The Method



H-like:

$$E_{KIN} + I_H = \hbar\omega_H$$

He-like:

$$E_{KIN} + I_{He} = \hbar\omega_{He}$$


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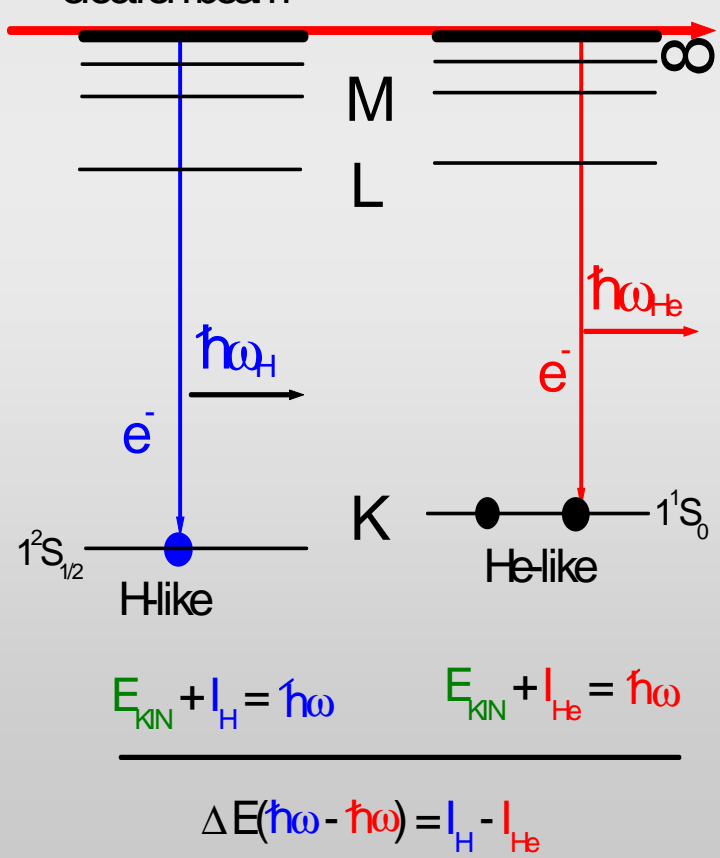
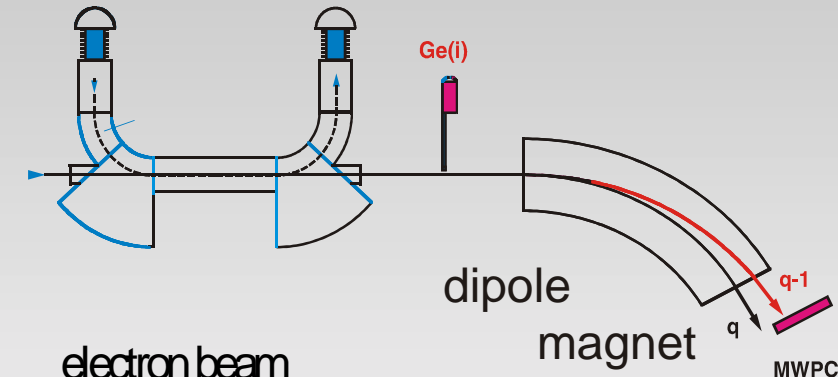

$$E(\hbar\omega_H - \hbar\omega_{He}) = I_H - I_{He}$$

Advantage of relative measurement:

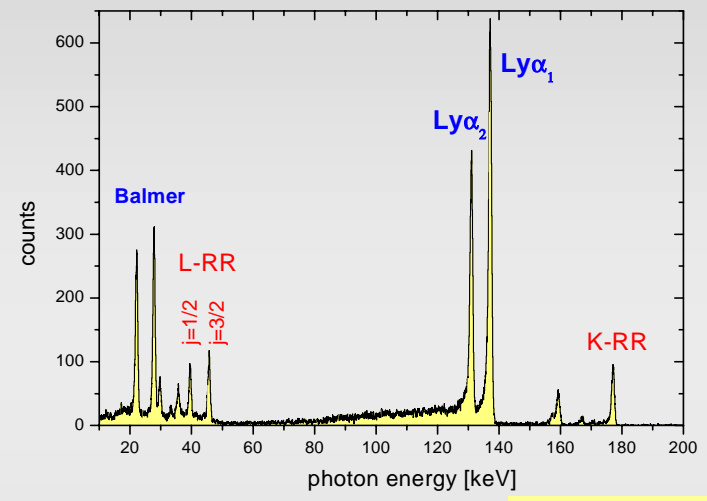
*All one electron contributions cancel out e.g. nuclear size*

# 2eQED Studies for the Ground State

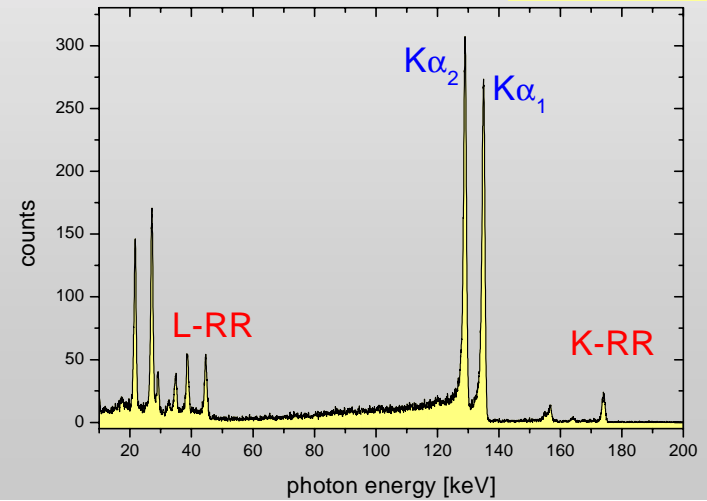
## 0 deg spectroscopy at the electron cooler



H-like uranium

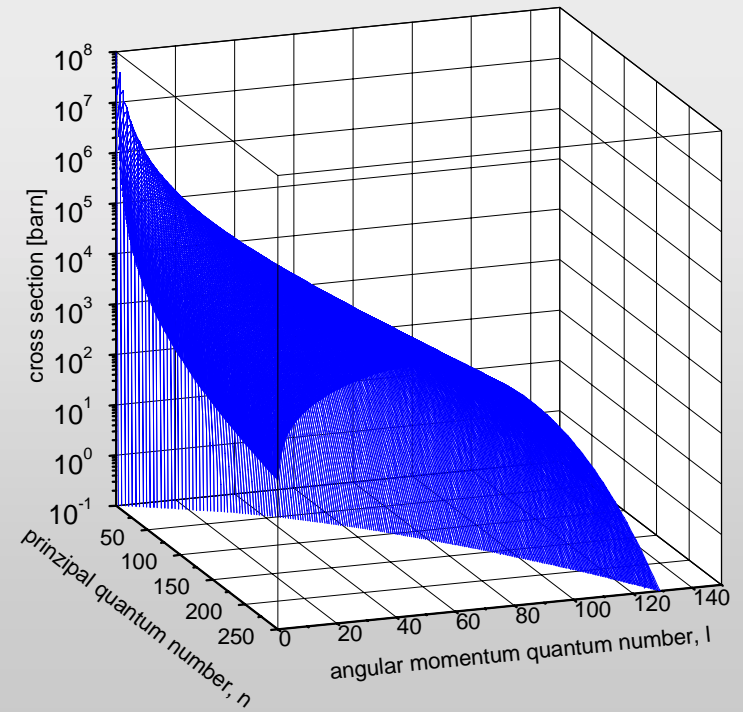
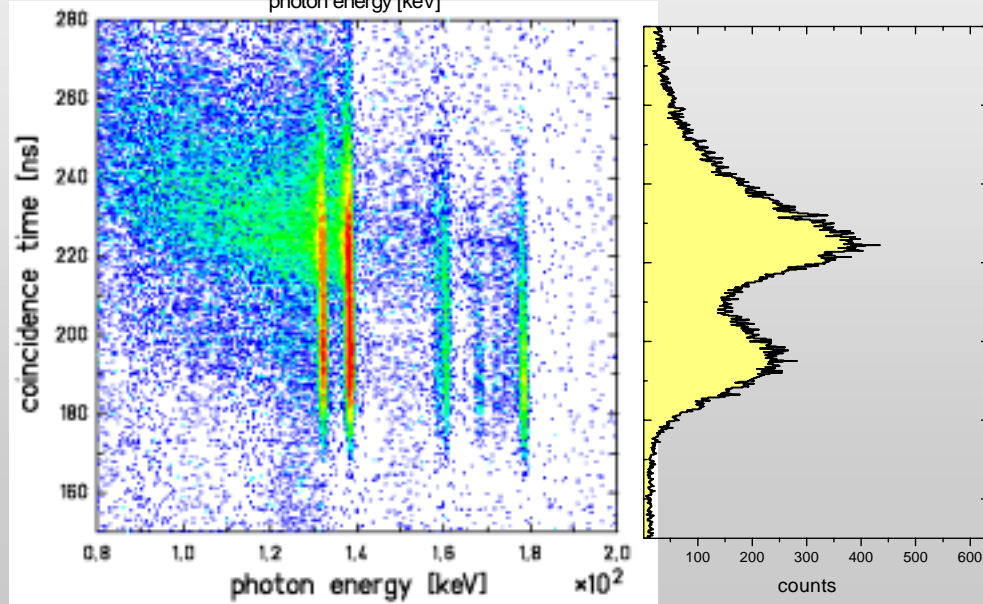
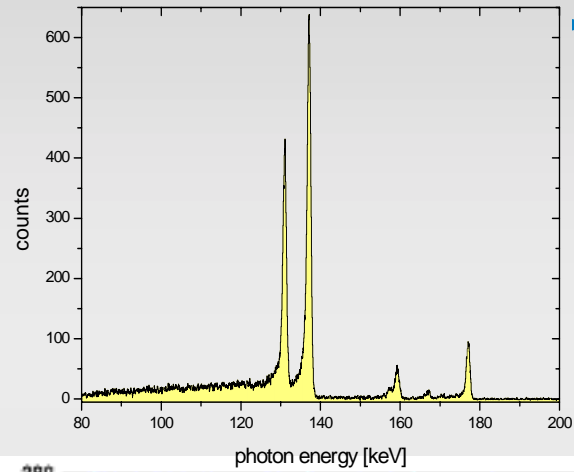
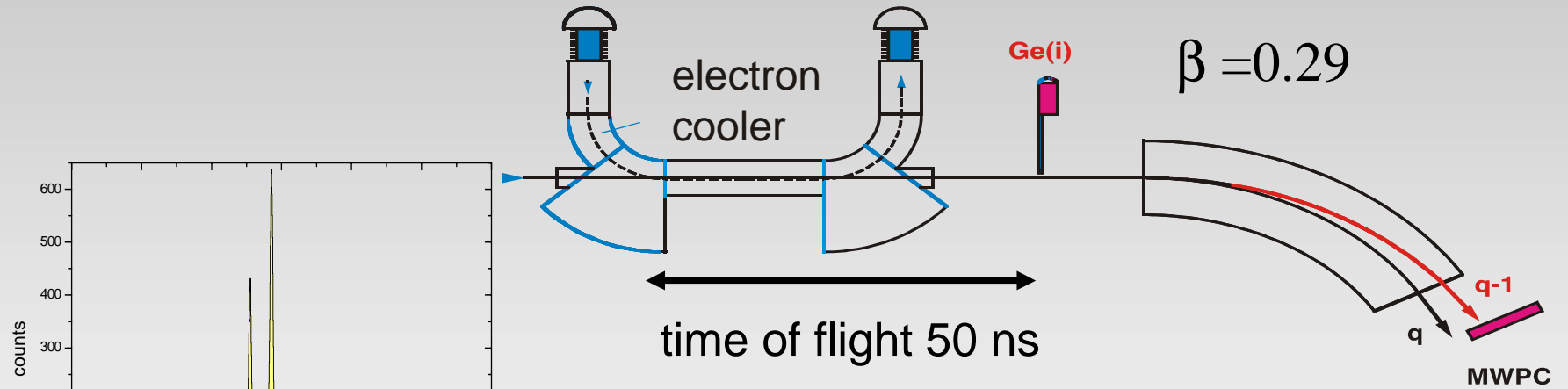


He-like uranium

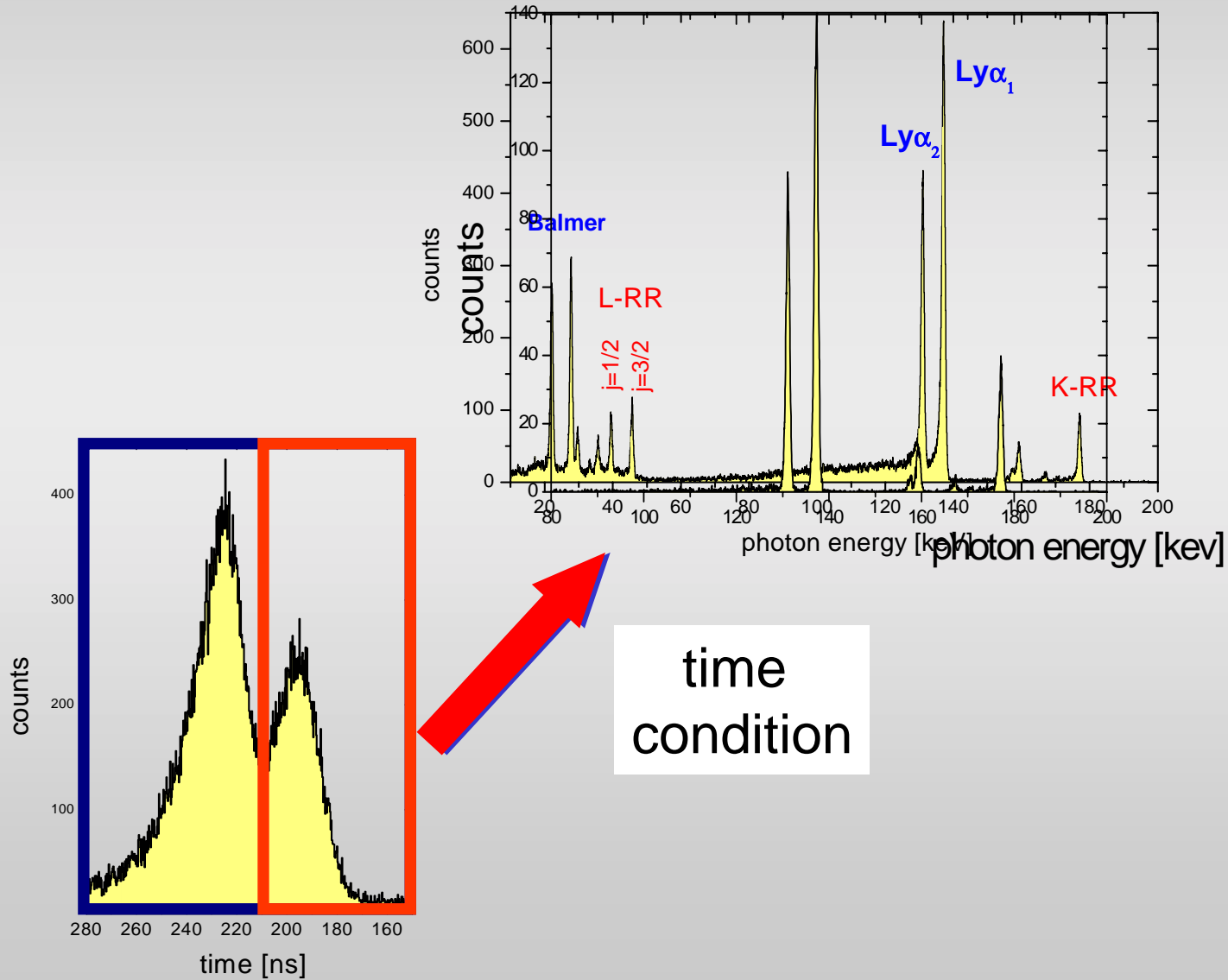




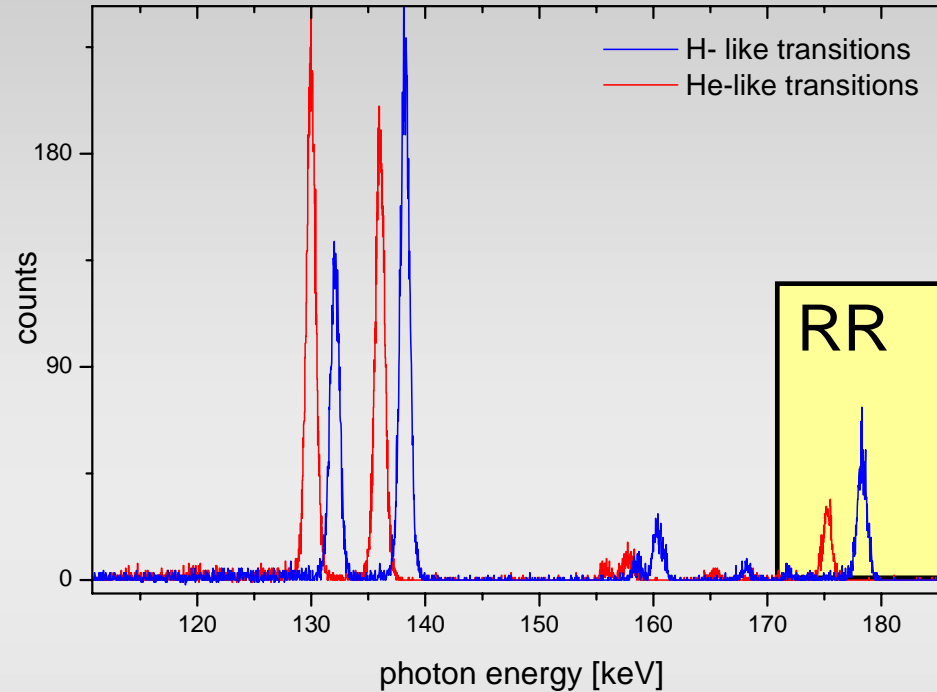
# 0 deg spectroscopy at the electron cooler



# 0 deg spectroscopy at the electron cooler



# Relative measurement at the electron cooler



RR

Prel. Result

$2.248\text{keV} \pm 9\text{ eV}$

A. Gumberidze

Estimated statistical uncertainty  
for RR into H- and He-like uranium:  $\approx 9\text{ eV}$

~~Uncertainty caused by doppler  
shift:~~

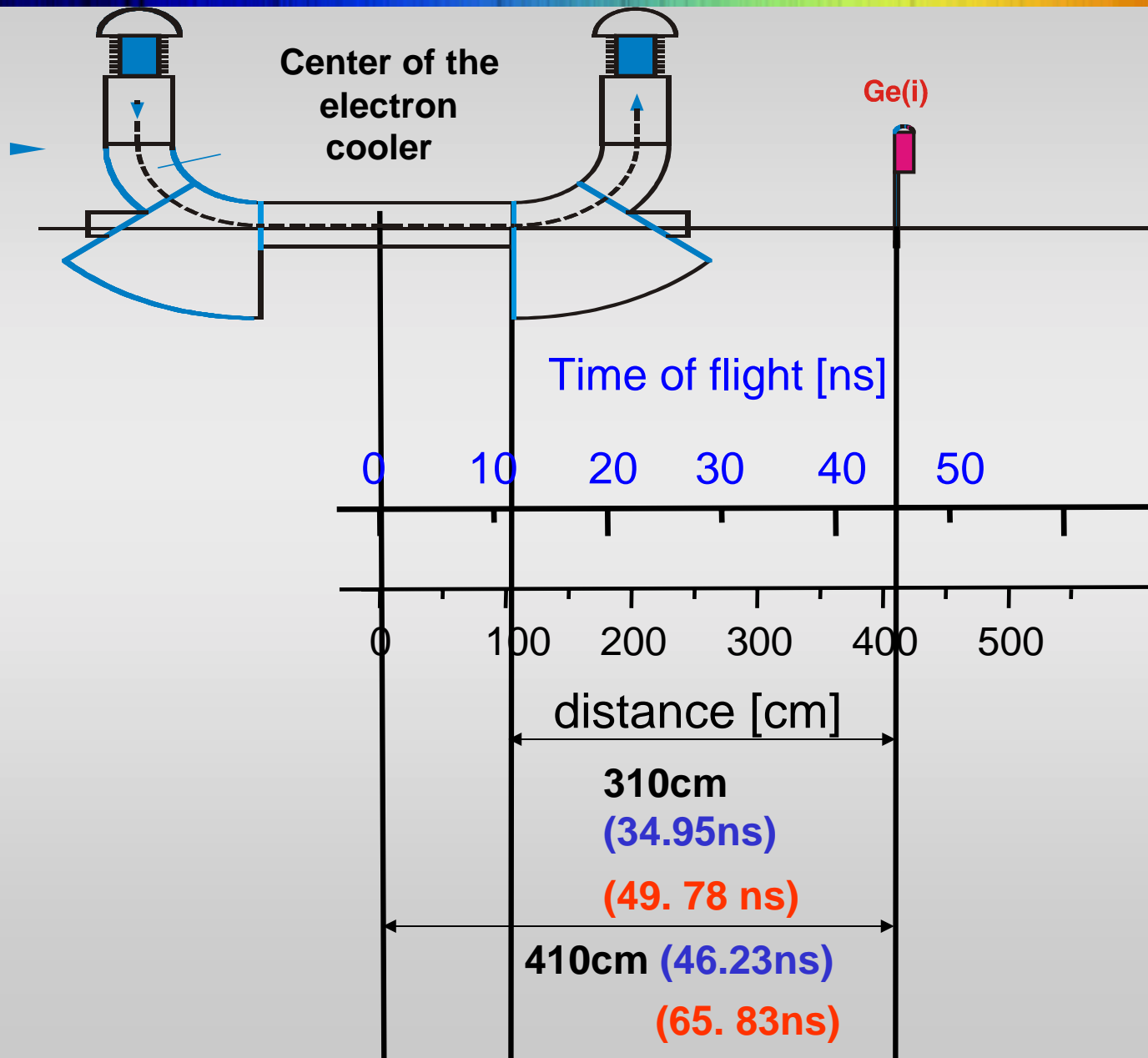
Additional systematic errors: ?

Two  
Electron

SE  
-9.7 eV [U<sup>90+</sup>]

VP  
+2.6 eV [U<sup>90+</sup>]

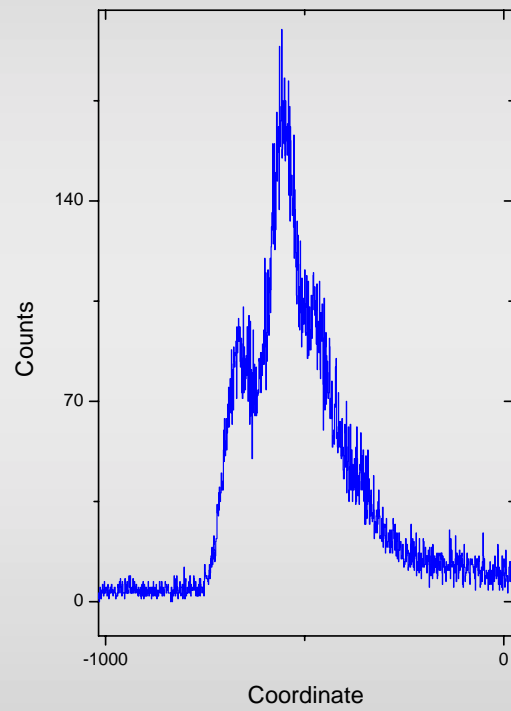
# 0 deg spectroscopy at the electron cooler



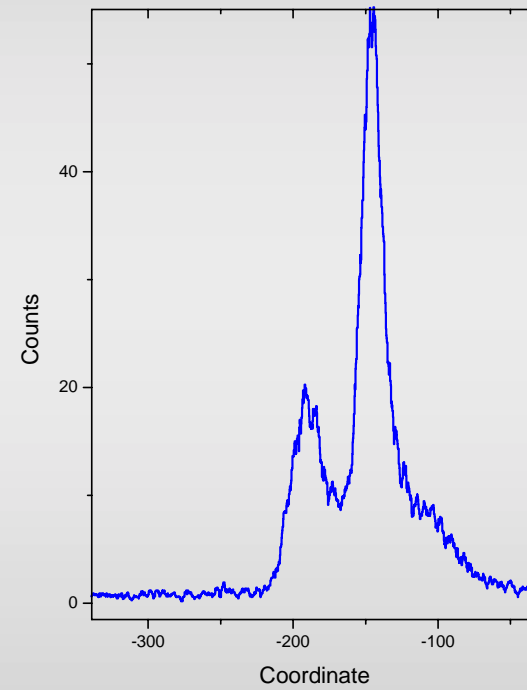
$E=43.5904 \text{ MeV/u}$   
 $\beta = 0.29565$   
 $\gamma=1.0468$

$E=20.74 \text{ MeV/u}$   
 $\beta=0.20761$   
 $\gamma=1.0223$

# 0 deg spectroscopy at the electron cooler



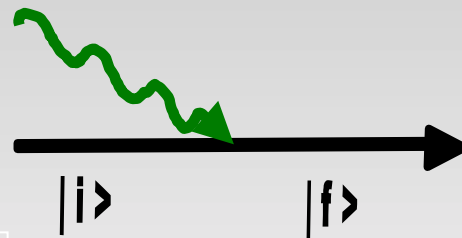
43 MeV/u



21 MeV/u

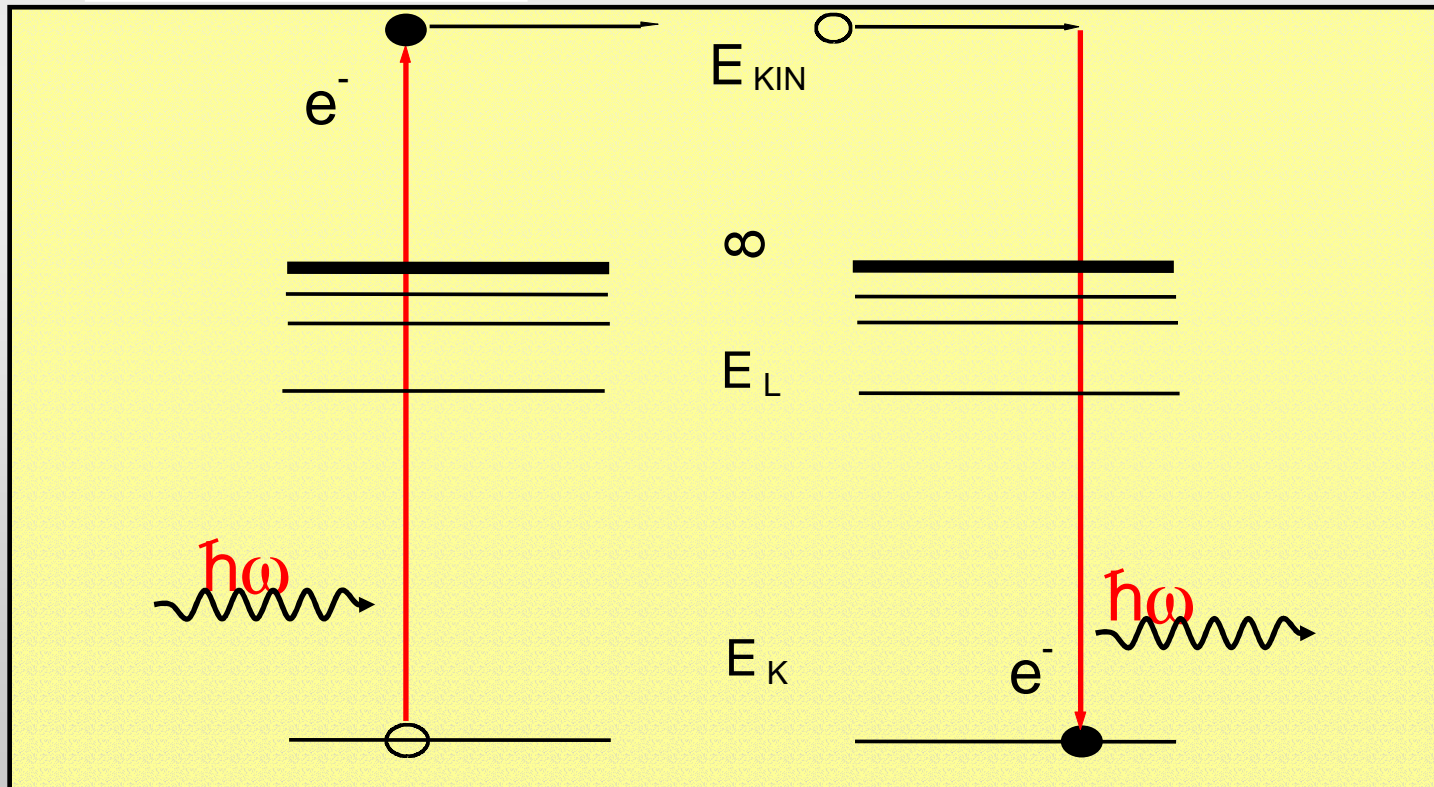
# Photon-Matter Interaction in the Relativistic Regime

## *Radiative Electron Capture*

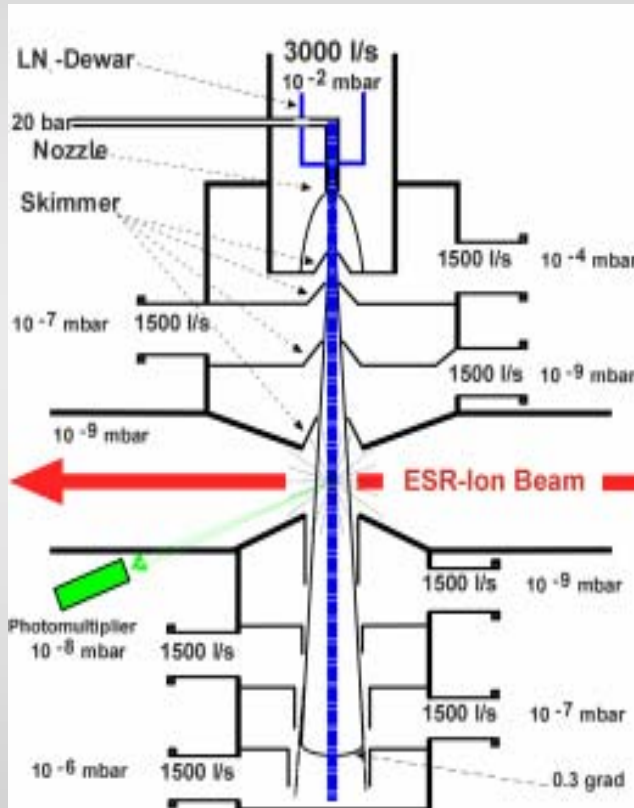


Photoionization

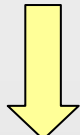
Radiative Electron Capture



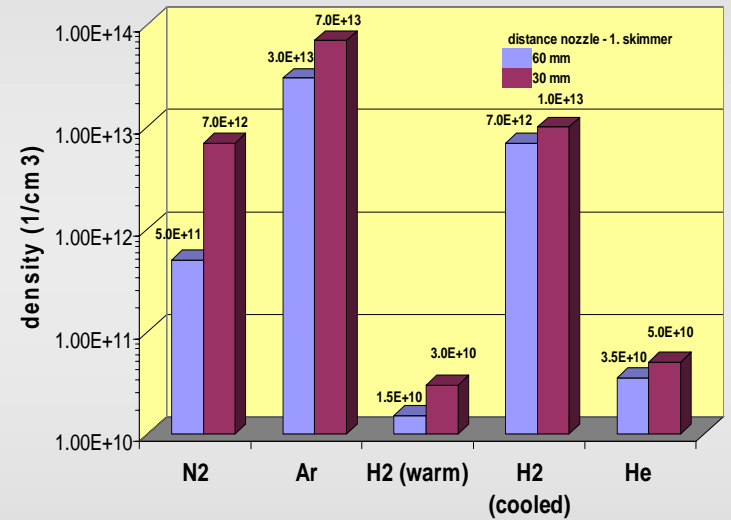
## The Jet-Target



**Target densities**  
 $10^{12} - 10^{14} \text{ p/cm}^3$

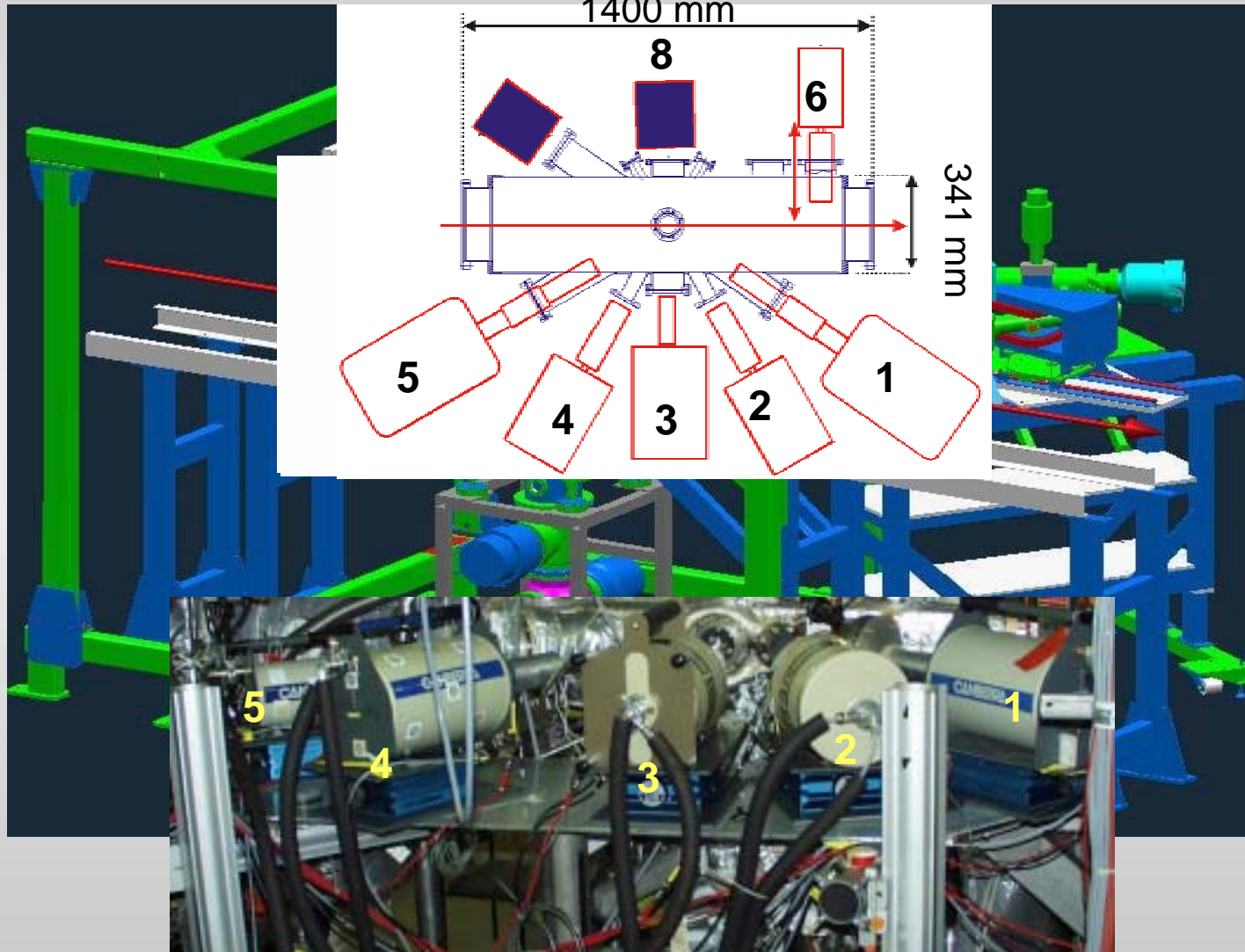


**Single collision conditions**



**Supersonic jet, operates in ultra high vacuum environment ( $10^{-11}$  mbar)**

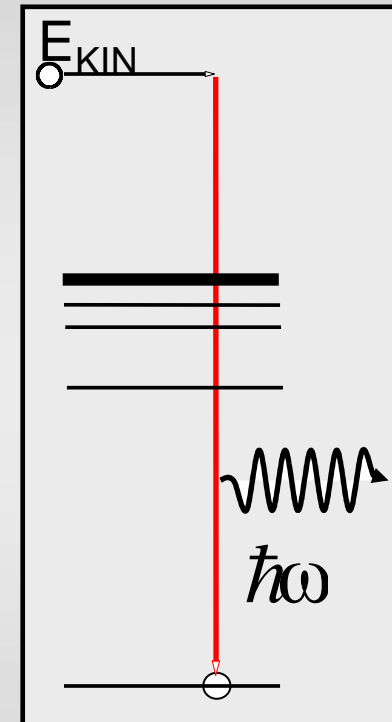
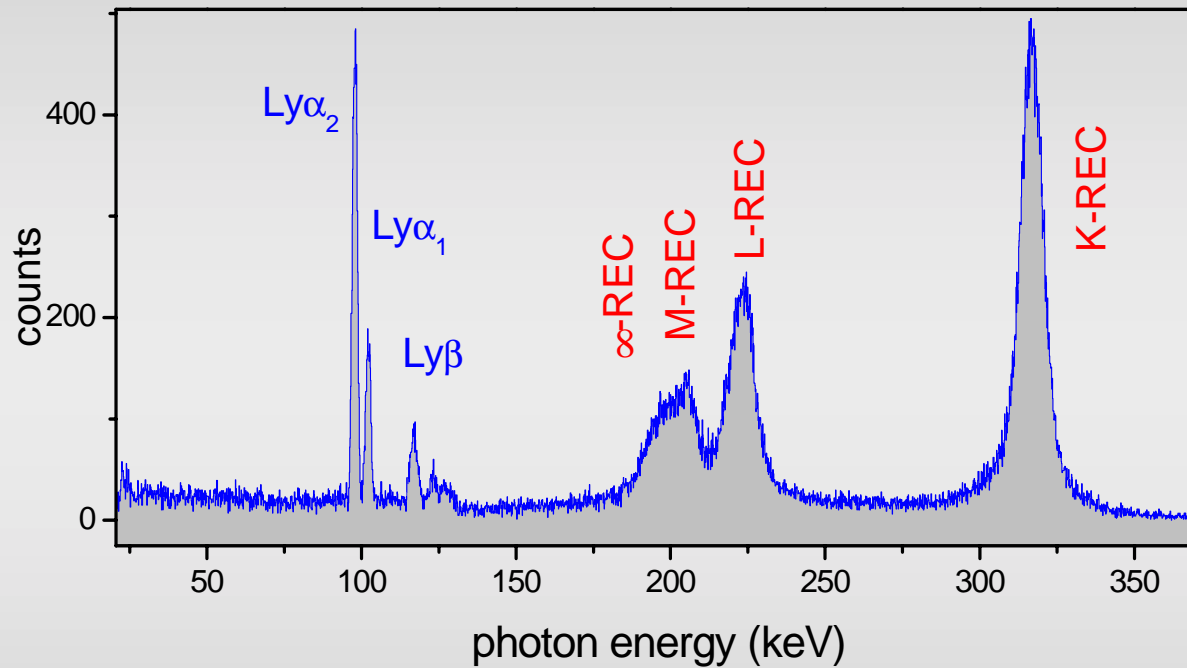
# Experiments at the Jet-Target





# Radiative Electron Capture of Quasifree Targetelectrons

$U^{92+} \Rightarrow N_2, 358 \text{ MeV/u}$



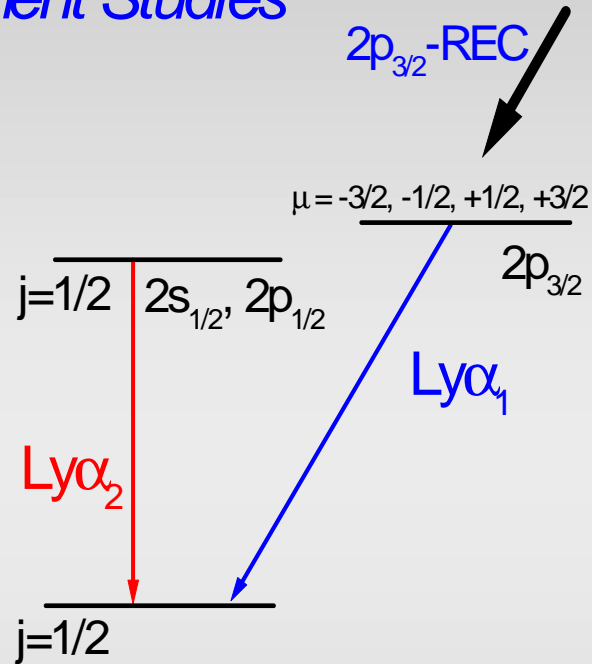
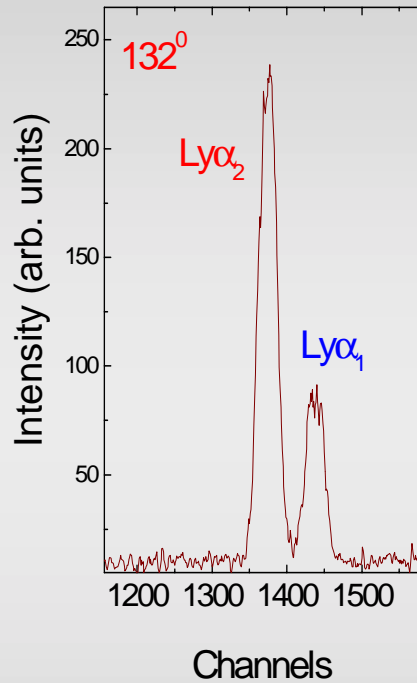
REC photon energy

$$\hbar\omega_{REC} = E_B + m_e c^2 (\gamma - 1) + \gamma (v_i p_z - E_T)$$

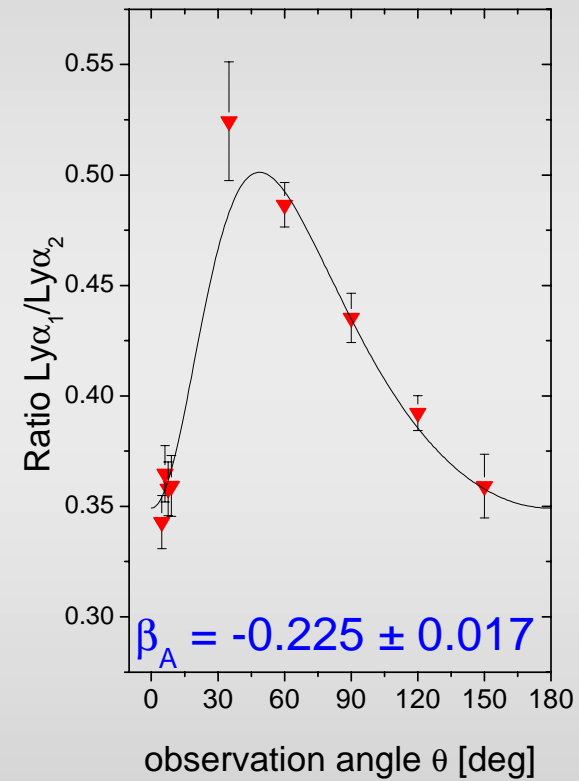
Shape and width of REC lines are determined by the **momentum distribution** of the target electrons

# 2p<sub>3/2</sub> transitions in high-Z ions produced by REC

## Alignment Studies



## Lyα<sub>1</sub> transitions at 310 MeV/u



**1st photon: resonant excitation to the 2p<sub>3/2</sub> state**  
+  
**2nd photon: ionization**

**Δt ≈ 10<sup>-17</sup> s**

$$W(\theta) \propto 1 + \beta_A \cdot \left[ 1 - \frac{3}{2} \sin^2 \theta \right]$$

# Alignment Studies

non-statistical population of the magnetic sublevels of the  $2p_{3/2}$  state leads to an anisotropic photon emission

$$W(\theta) \propto 1 + \beta_A \cdot \left[ 1 - \frac{3}{2} \sin^2 \theta \right]$$

alignment parameter

$$\beta_A < 0$$

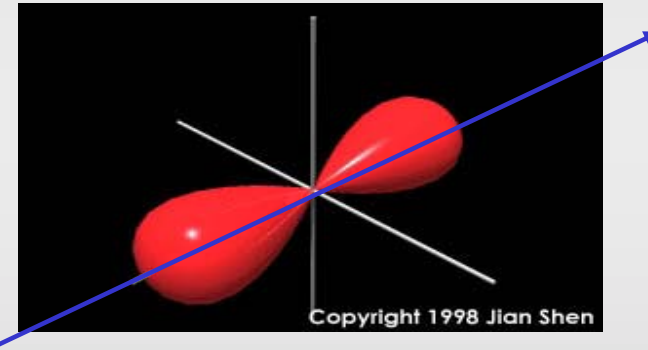
preferred population of  $m_j = \pm 1/2$

alignment parameter

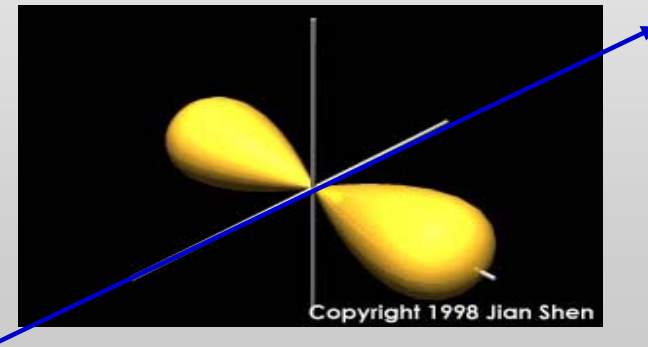
$$\beta_A > 0$$

preferred population of  $m_j = \pm 3/2$

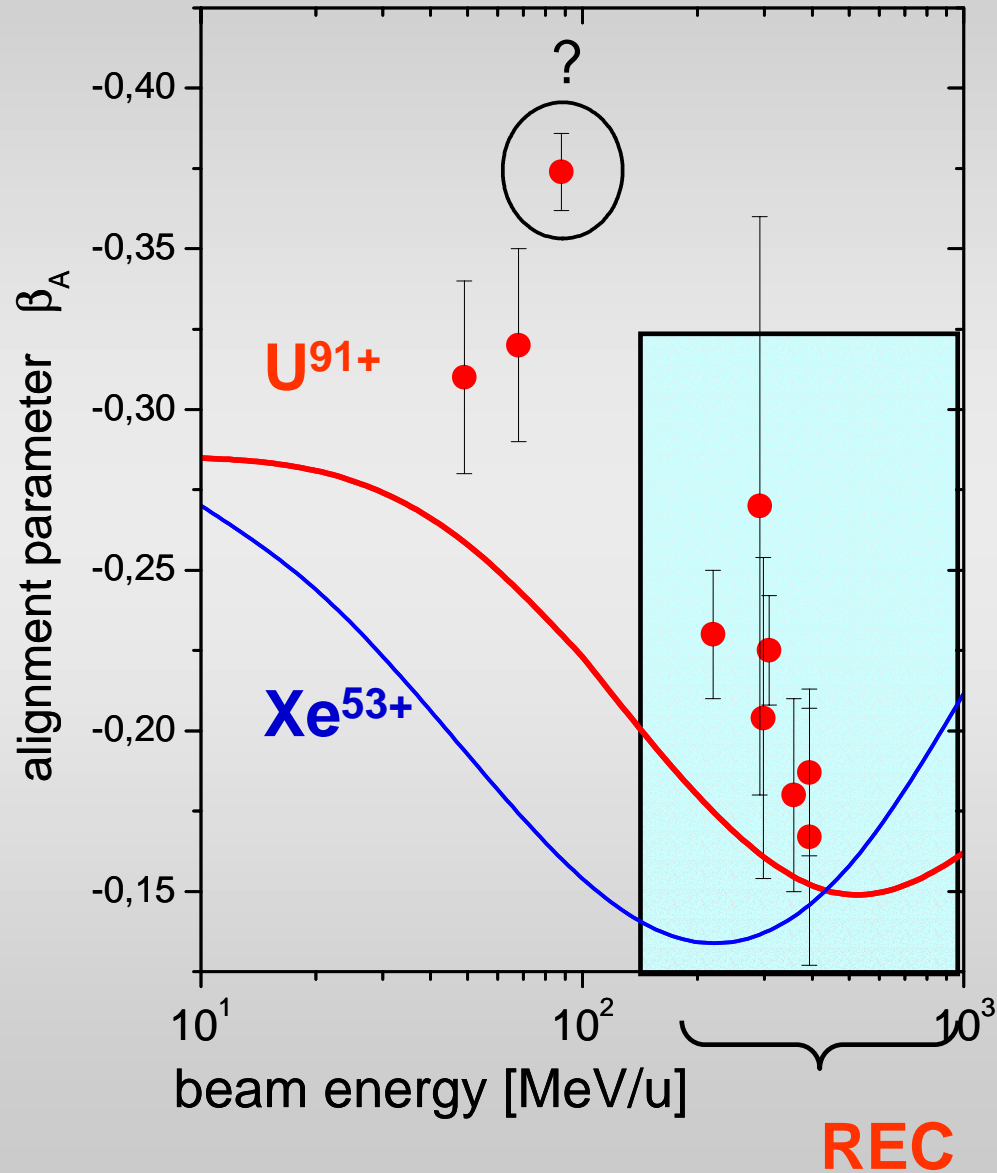
collision axis



collision axis



# Strong Alignment Observed for REC into the $2p_{3/2}$ State



Theory by J. Eichler et al.

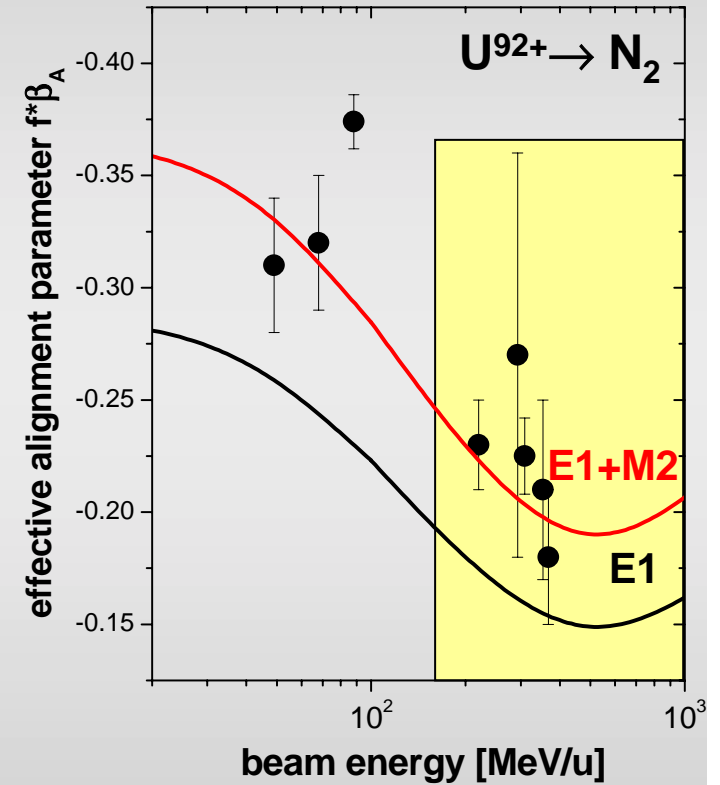
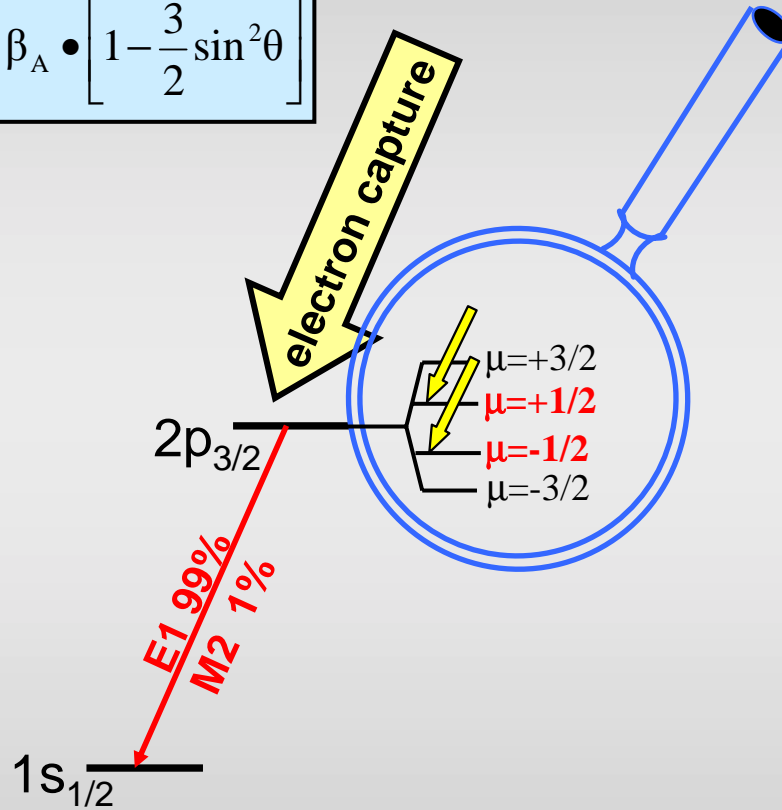
Disagreement  
with theory ?

PRL 79, 3270 (1997)

# Multipolmixing (E1/M2) observed for atomic transitions

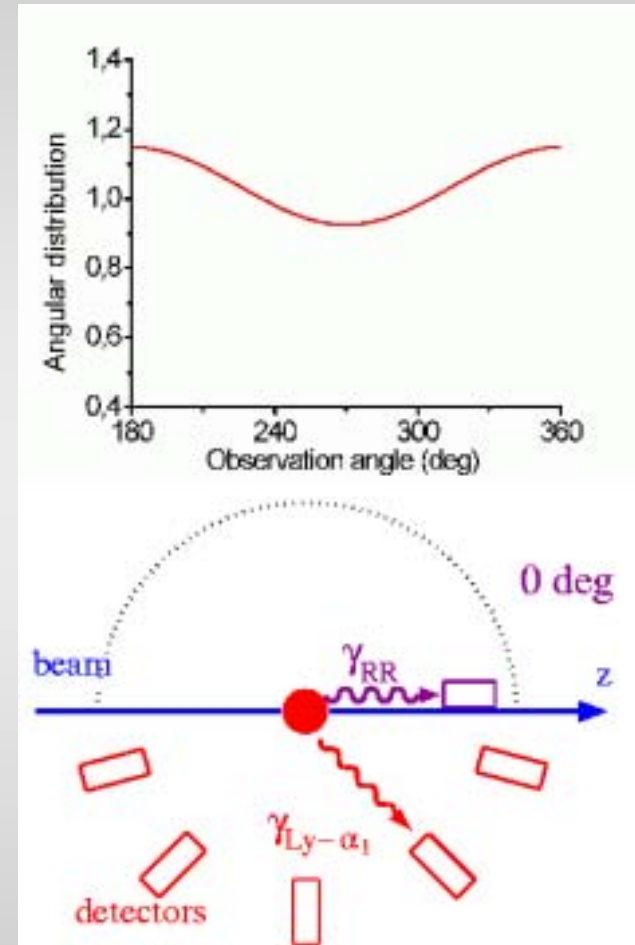
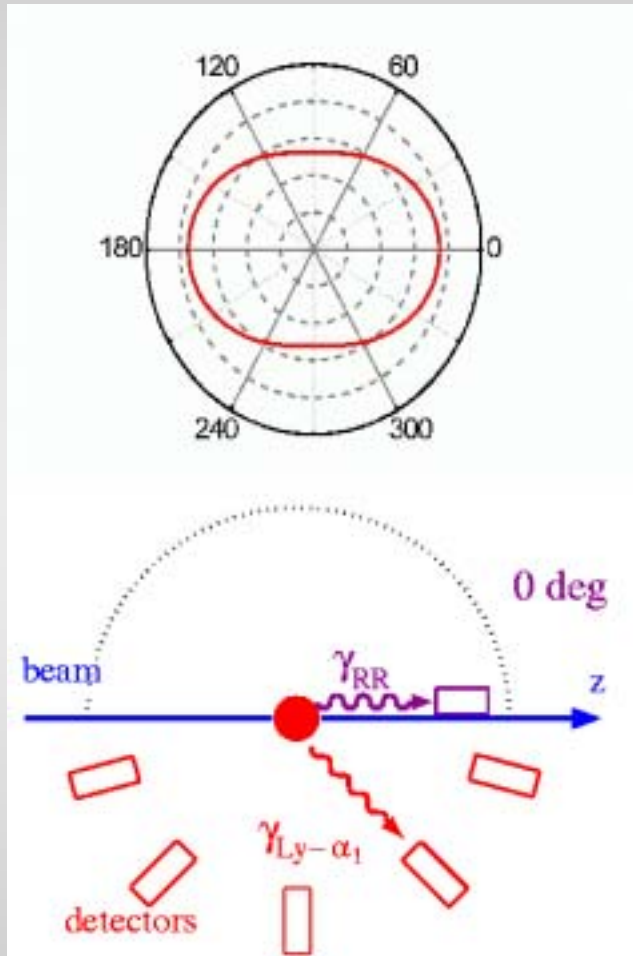
[2p<sub>3/2</sub> → 1s<sub>1/2</sub> Transition in High-Z H-Like Ions]

$$W(\theta) \propto 1 + f \left( \frac{a_{M2}}{a_{E1}} \right) \cdot \beta_A \cdot \left[ 1 - \frac{3}{2} \sin^2 \theta \right]$$



$$f \left( \frac{a_{M2}}{a_{E1}} \right) = 1.38 \pm 0.07 \Rightarrow \frac{\langle \|M2\| \rangle}{\langle \|E1\| \rangle} = 0.11 \pm 0.02 \Rightarrow \frac{\Gamma_{M2}}{\Gamma_{E1}} = 0.012 \pm 0.004$$

# Differential Alignment Distribution



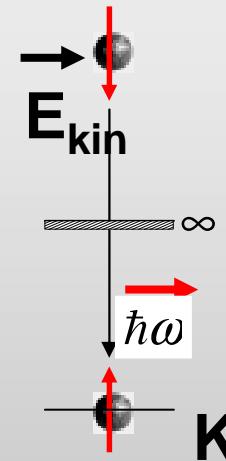
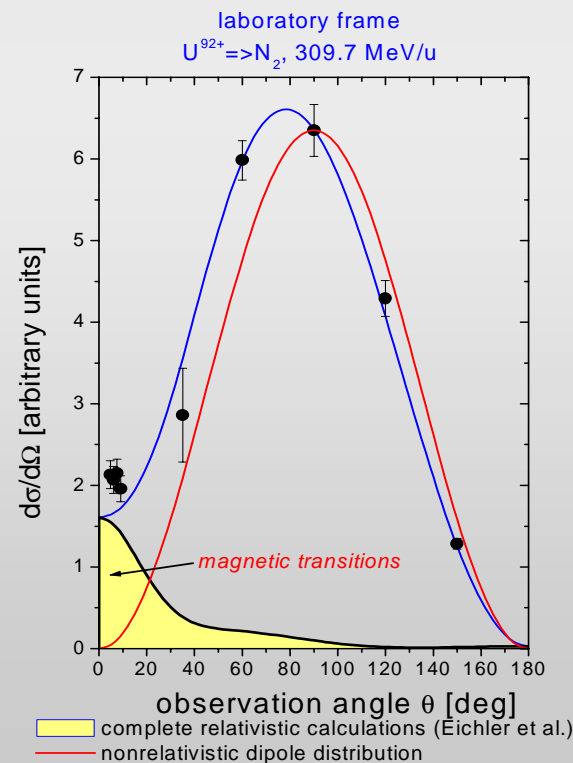
## X-X angular correlations

# Experimental REC studies performed up to now

total REC cross sections for bare ions up to uranium  
(20 MeV/u – 170 GeV/u) ✓

photon angular distribution studies for REC into the  
ground and excited states ✓

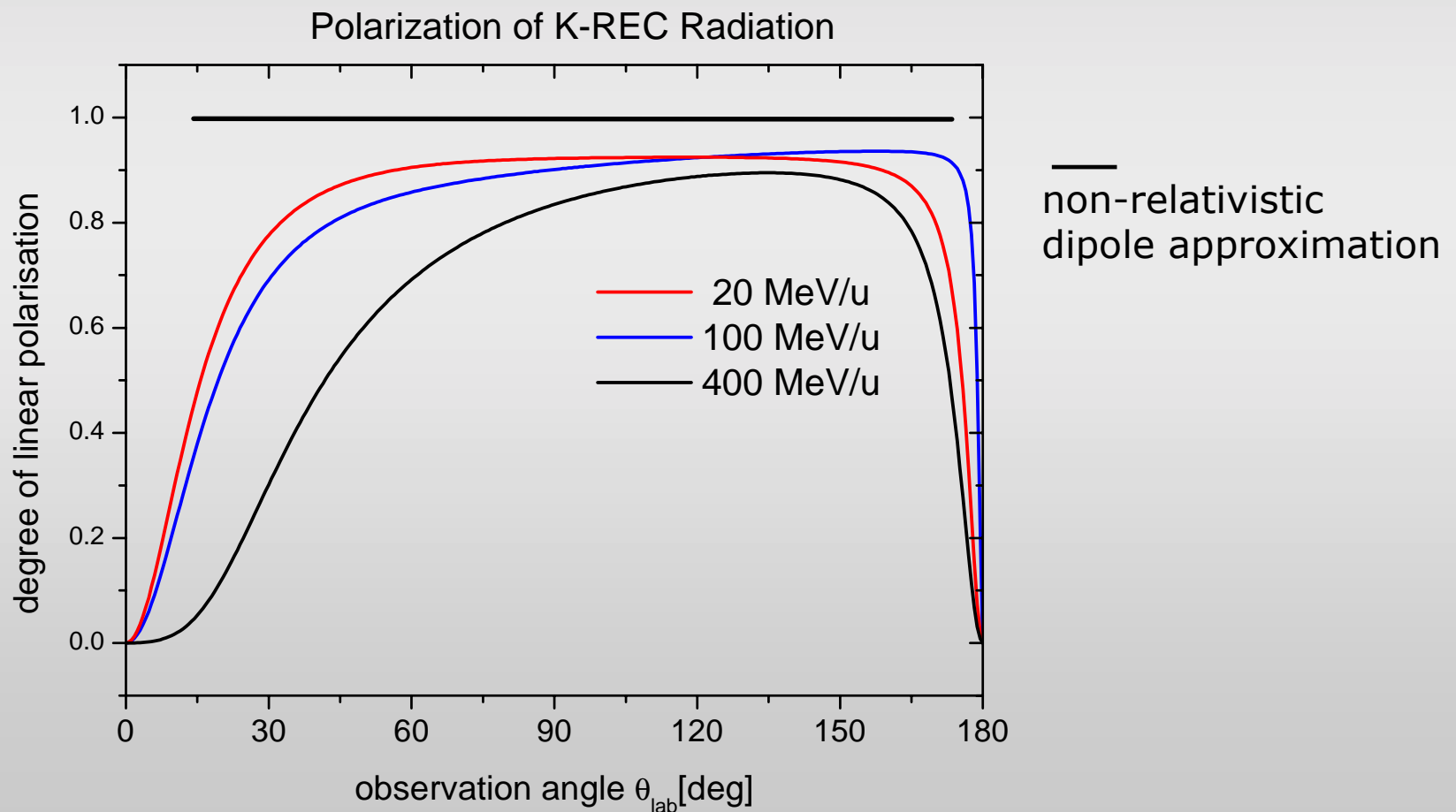
**Kinematical  
Identification of  
Spin-Flip  
Transitions  
from Continuum  
States into the 1s-  
Ground State**



# Open Questions

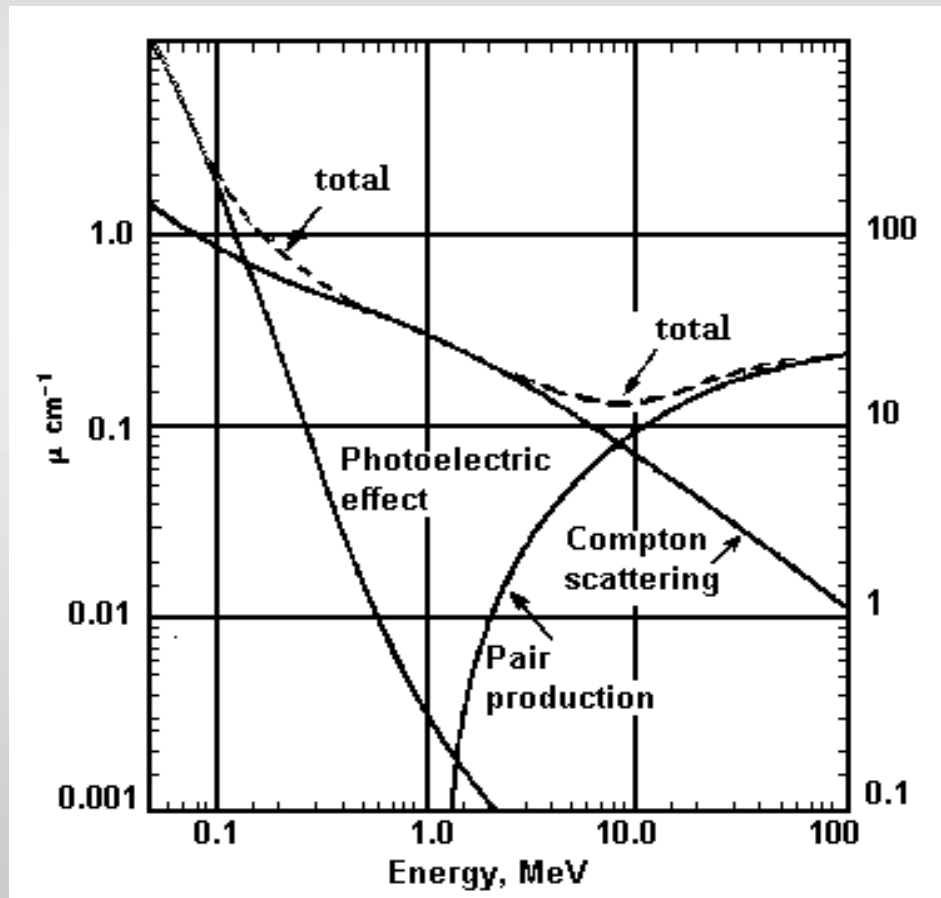
Angular distributions for few-electron ions close to the threshold (decelerated ions) (no appropriate theories available)

Polarization of the emitted photons (no experimental information available)



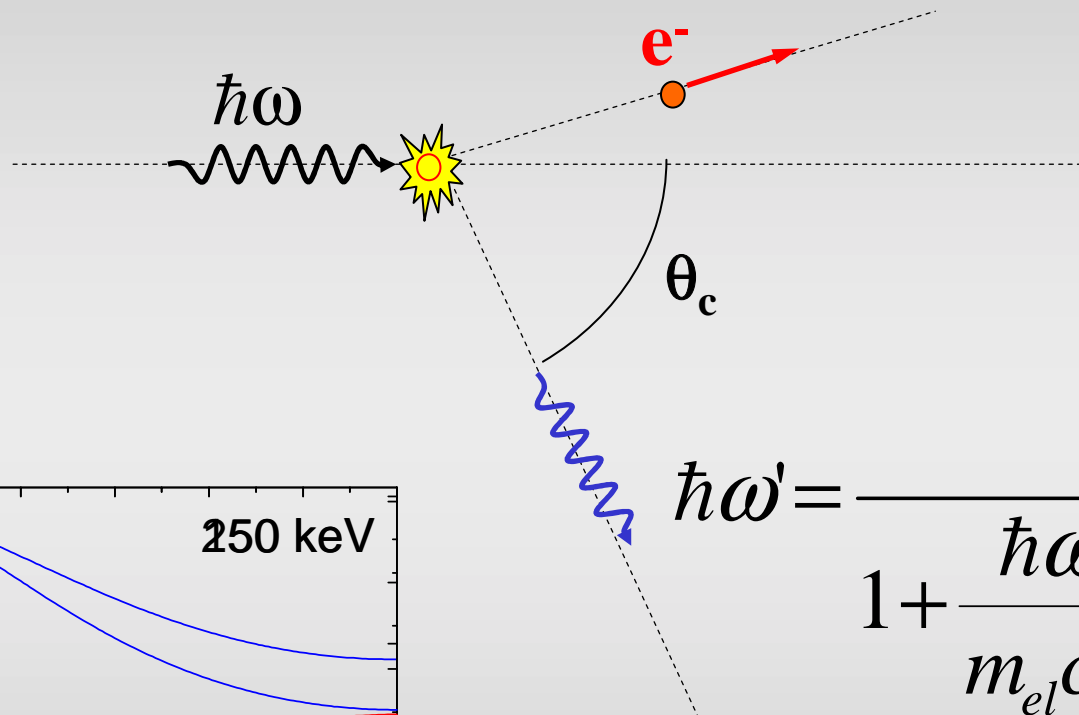


# Interaction of electro-magnetic radiation with matter

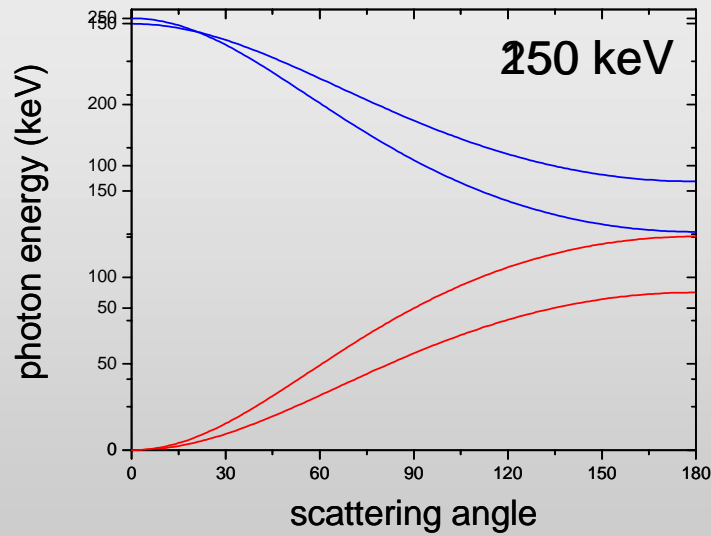


- photoelectric effect
- **Compton scattering**
- pair production

# Compton scattering



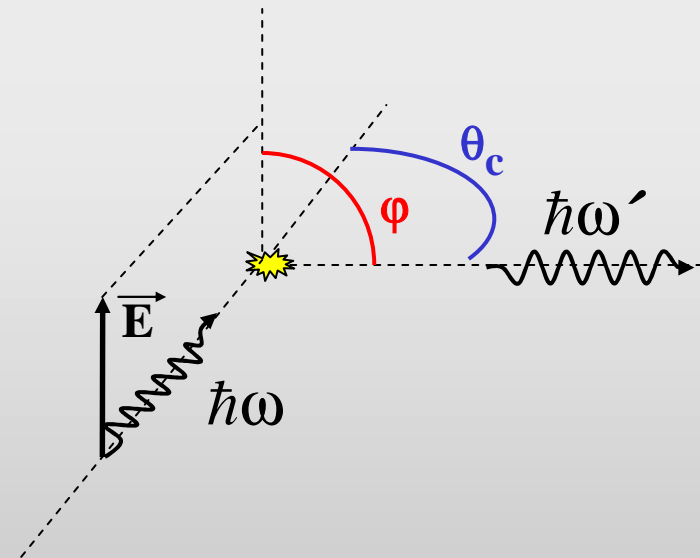
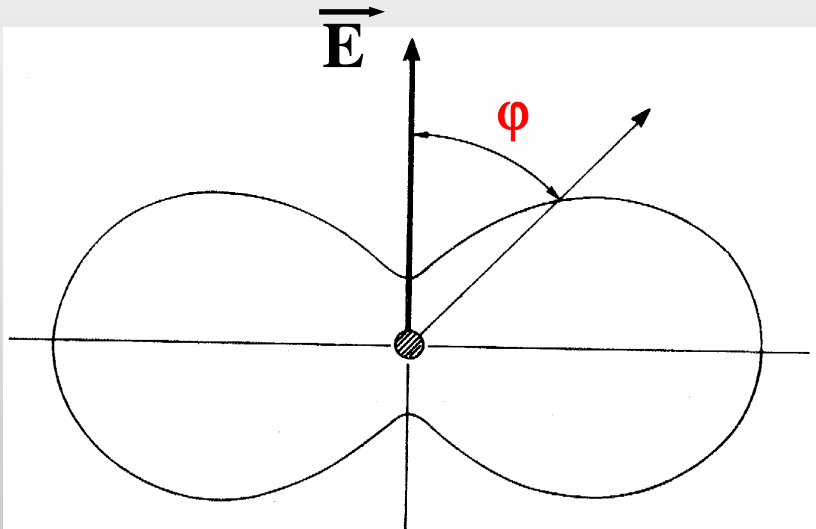
$$\hbar\omega' = \frac{\hbar\omega}{1 + \frac{\hbar\omega}{m_{el}c^2} (1 - \cos\theta_c)}$$



# Polarization Measurements by Means of Compton Scattering

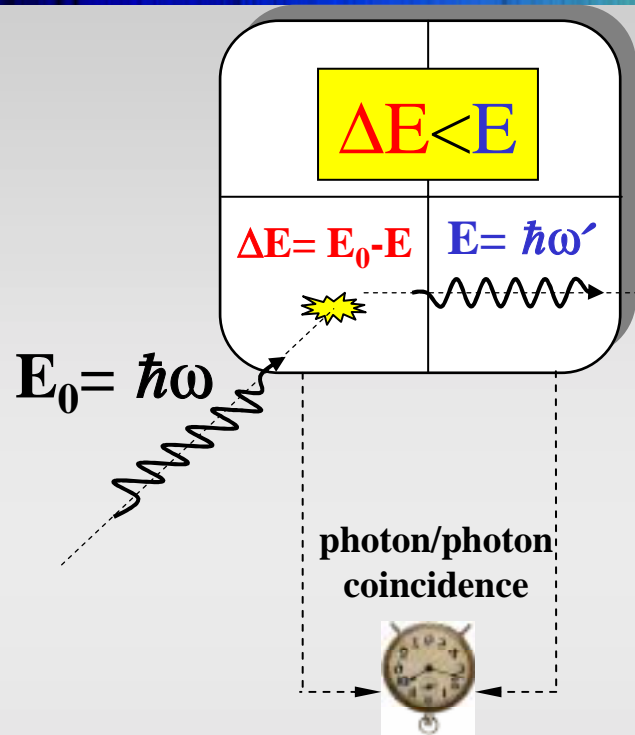
## Klein-Nishina formula

$$\frac{d\sigma}{d\Omega} = \frac{1}{2} r_0^2 \left(\frac{\hbar\omega'}{\hbar\omega}\right)^2 \left(\frac{\hbar\omega'}{\hbar\omega} + \frac{\hbar\omega}{\hbar\omega'} - 2 \sin^2 \theta_c \cos^2 \varphi\right)$$



angular distribution of scattered photons

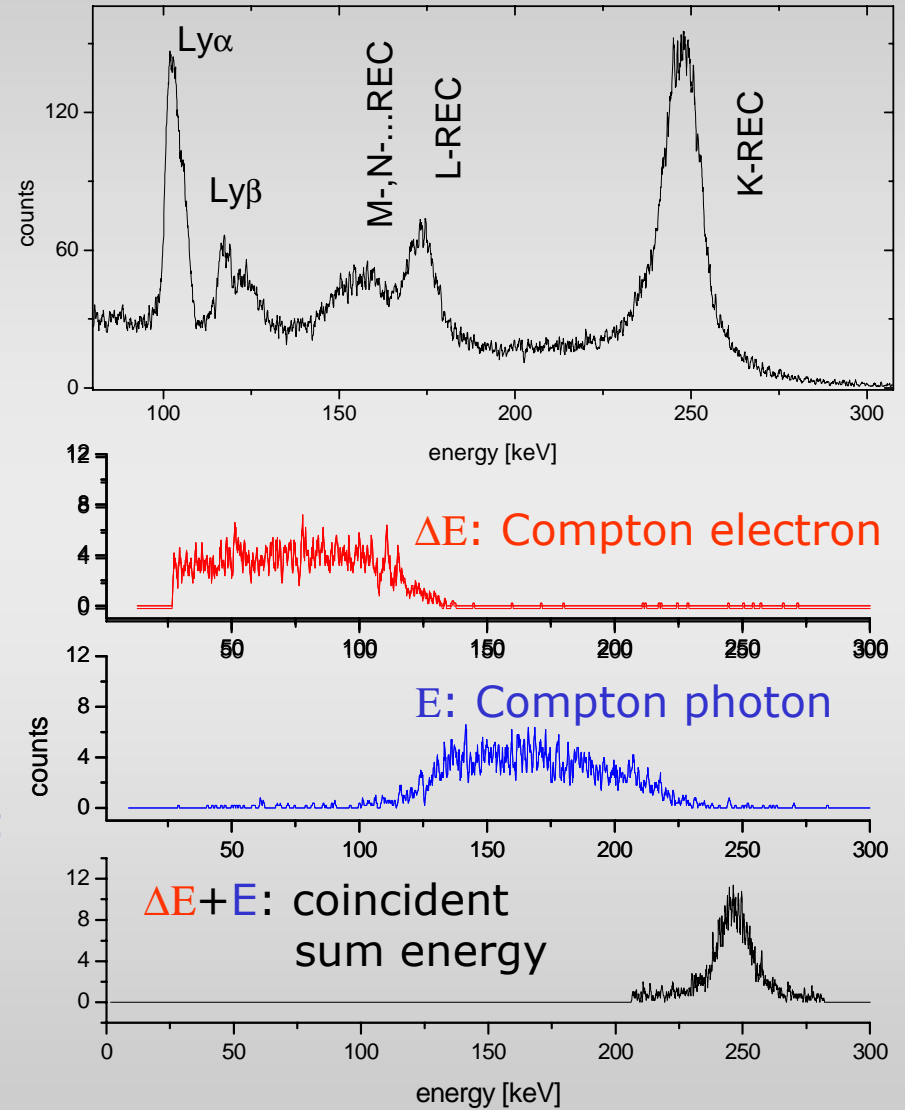
# Compton scattered photons



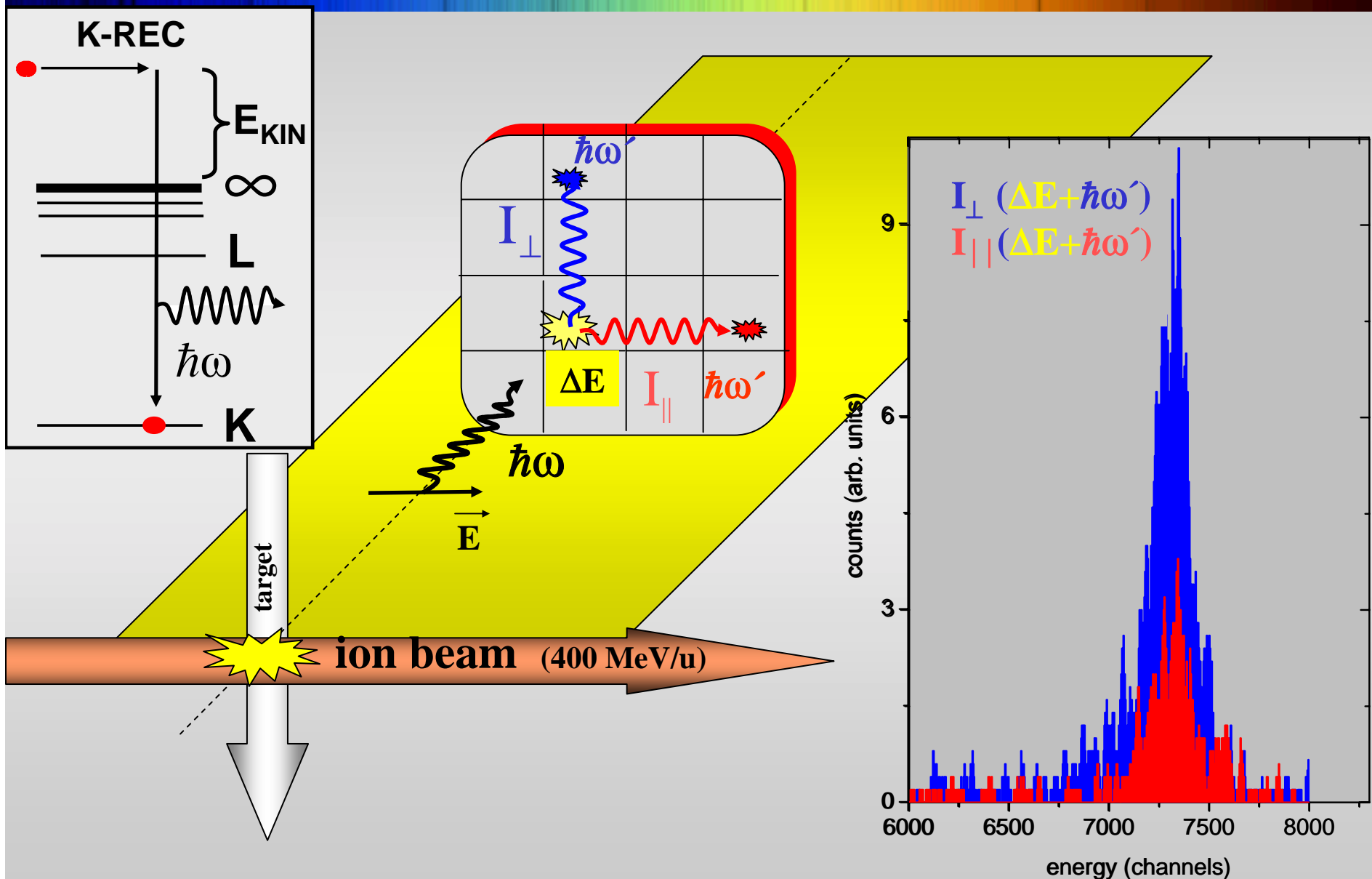
energy deposition in two independent parts of the detector



reconstruction of compton events



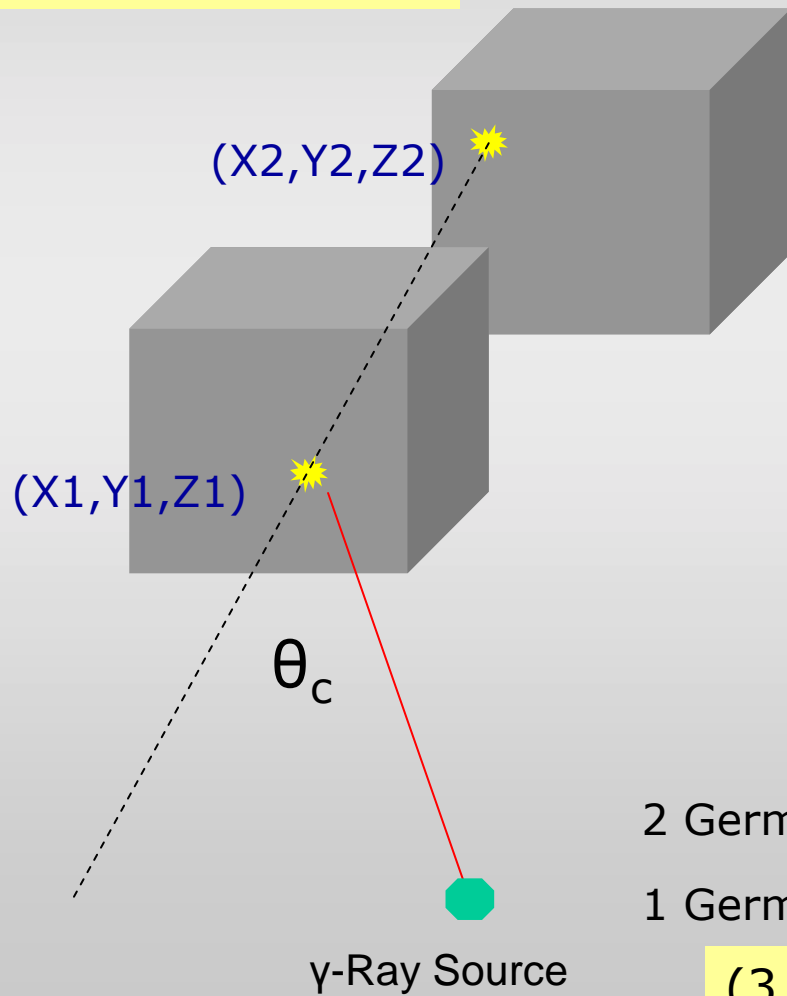
# First Polarization Measurement for Radiative Recombination Transitions ( $U^{92+} + e^- \Rightarrow U^{91+} + \hbar\omega$ )



preliminary data from the ESR beam time May 2002

# Compton/Gamma Camera

$$\hbar\omega' = \frac{\hbar\omega}{1 + \frac{\hbar\omega}{m_{el}c^2}(1 - \cos\theta_c)}$$



Imaging Quality depends on

- energy resolution
- spatial resolution
- Compton profile

(LBL, Burke et al. NRL; Kroeger et al.)

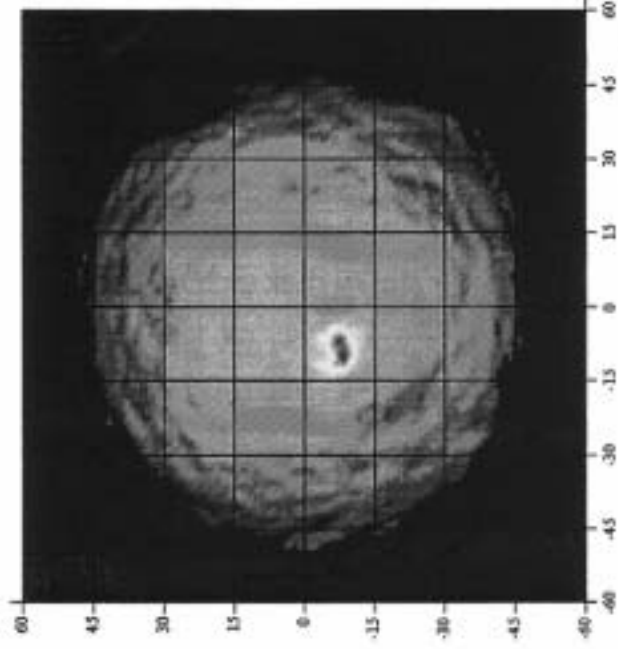
2 Germanium Detectors for  $\hbar\omega > 1 \text{ MeV}$

1 Germanium Detector for  $\hbar\omega \approx 300 \text{ keV}$

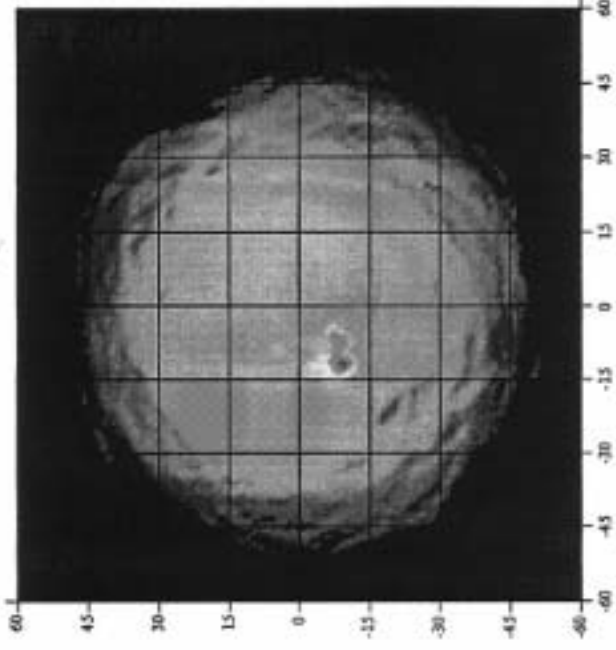
(3 D position sensitive)

## Compton Telescope

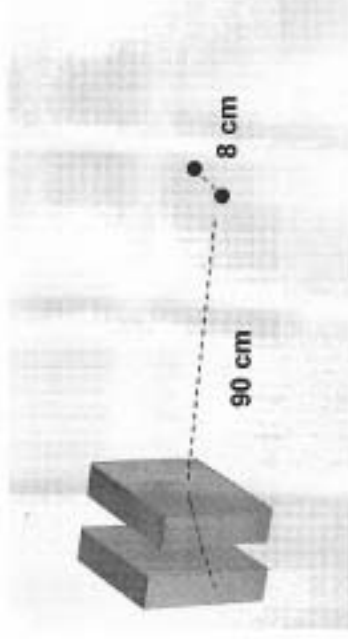
Resolving between two point sources (each 662 keV)



**3.8° separation**

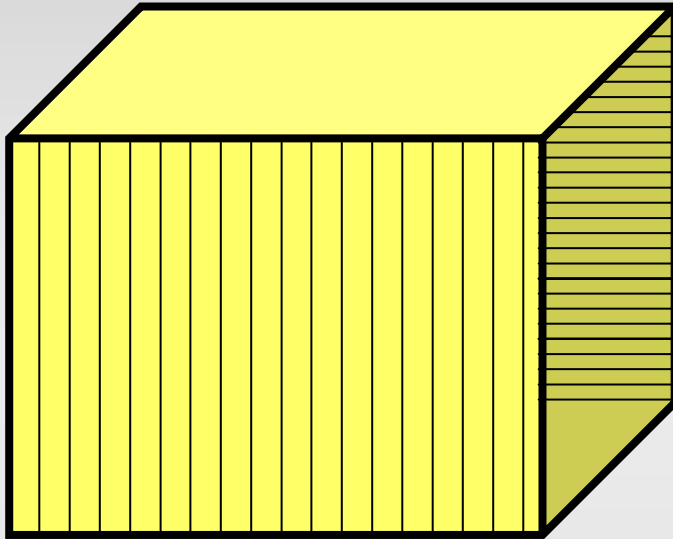


**5° separation**



**Source size ~1.3°**

## Compton/Gamma Camera



double sided Ge(i)  
strip detector  
(3D position sensitive)

128 x 320  $\mu\text{m}$   
24 x 1.3 mm

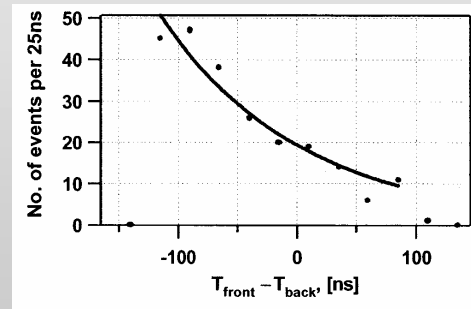
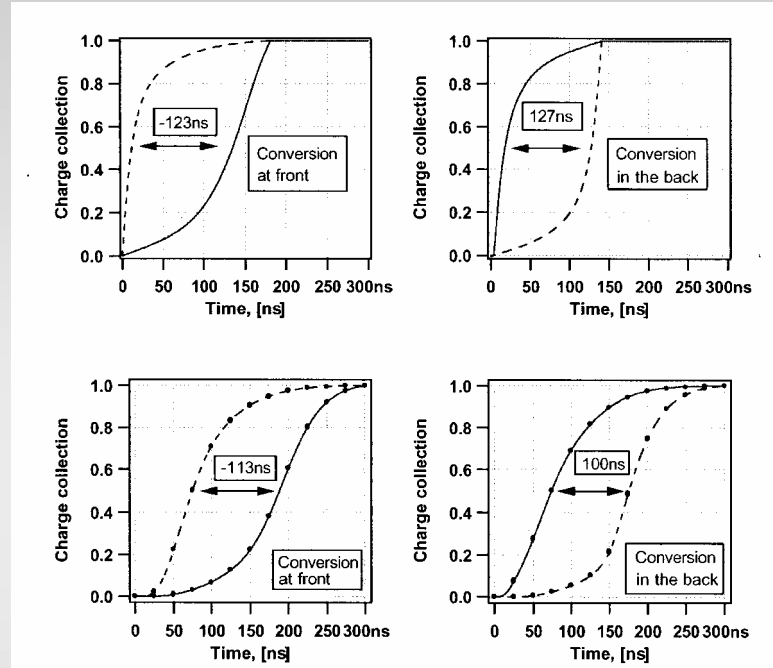
Thickness: 2 cm

D. Protic, FZ-Jülich



# 3D read out: z direction

M. Momayezi et al. 1999



## Summary

Storing and cooling of highly charged ions delivers brilliant beams for experiments

The ESR provides ideal conditions for accurate atomic structure studies

1s-LS experiments at the ESR allowed to improve the experimental accuracy by an order of magnitude

Study of 2eQED provides a test of QED in the strong field limit which is not blended by nuclear effects

The study of elementary atomic processes for highly- charged heavy ions via their time-reversal

## Outlook

Implementation of new spectroscopic tools and techniques which are currently in preparation may provide a further gain of accuracy towards the 1 eV limit

Expansion of collision studies to few-electron ions

Polarisation and x-x correlation studies

Development of 3D x-ray detectors

Experiments with polarized targets and ions

Combined photon, electron and recoil ion momentum spectroscopy

Structure and Collision Studies at High- $\gamma$