

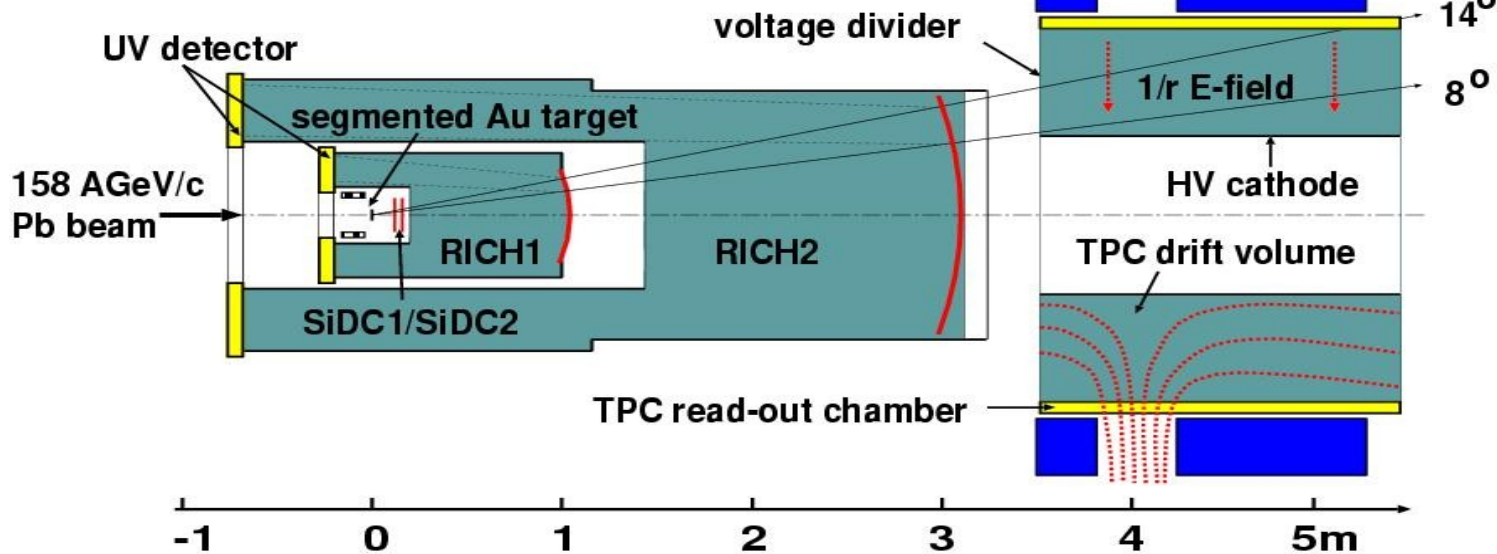
# Hydro, blast, and CERES

*Dariusz Miskowiec, GSI Darmstadt*

- 🌐 **hydro vs. CERES**
- 🌐 **blast vs. CERES**
- 🌐 **blast vs. hydro**

# CERES

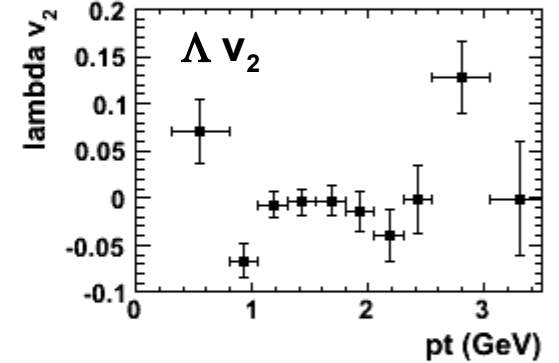
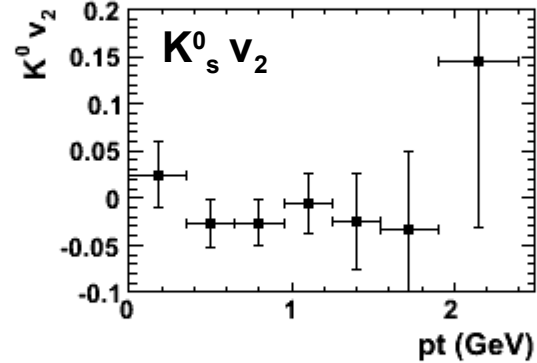
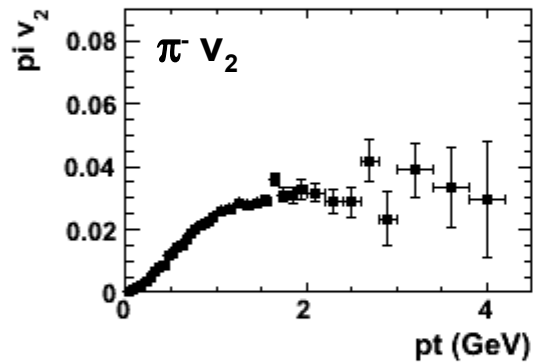
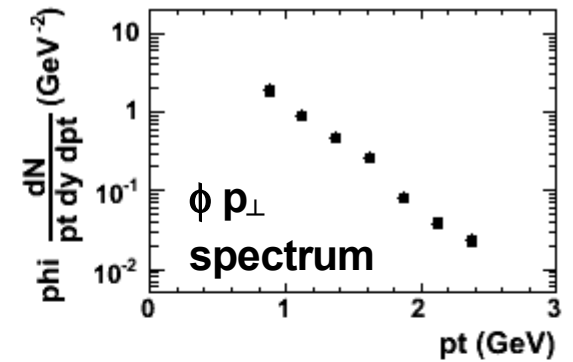
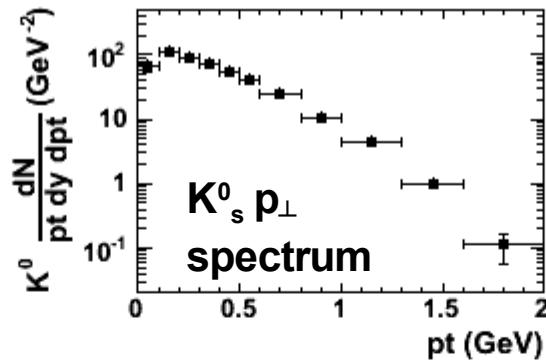
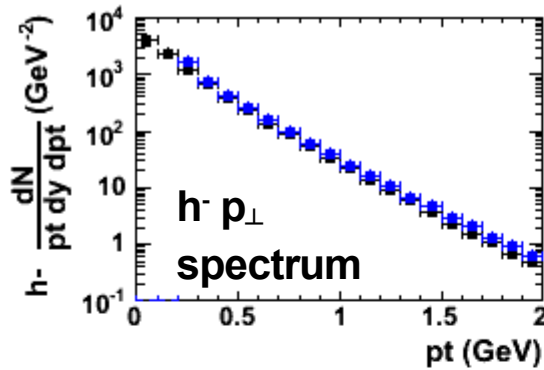
RUN2000:  $30 \cdot 10^6$  events, 8%  $\sigma/\sigma_{\text{geo}}$   
 $3 \cdot 10^6$  events, 20%  $\sigma/\sigma_{\text{geo}}$



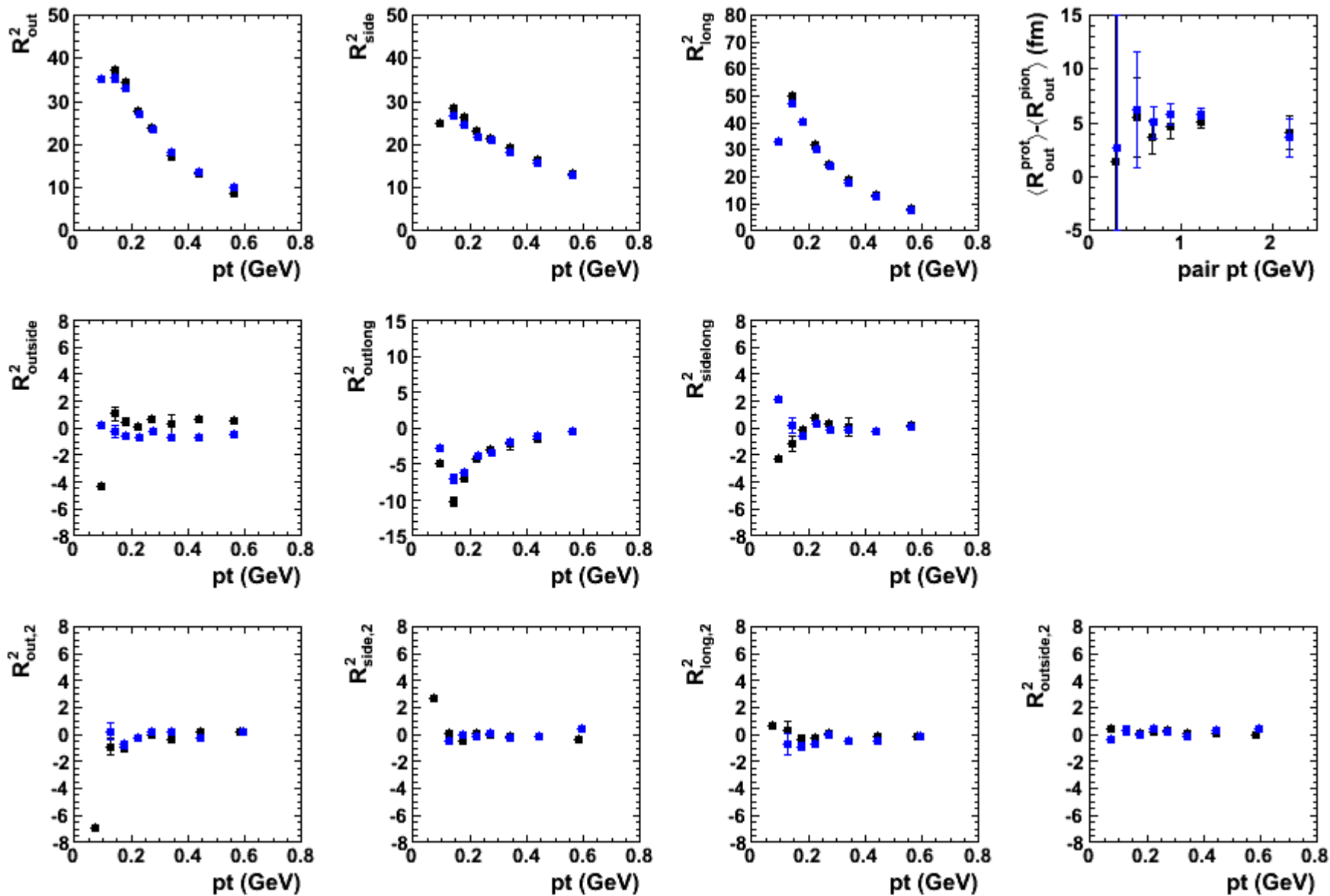
Pb+Au  
at 158 AGeV  
7% central

**CERES build and upgraded for leptons; but also good for...  
pt spectra, elliptic flow, two-particle correlations of hadrons**

# CERES pt spectra and elliptic flow



# CERES two-particle correlations



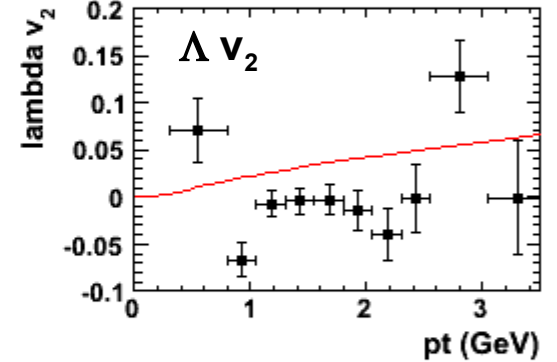
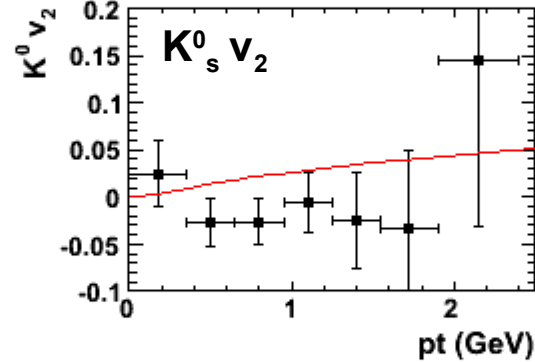
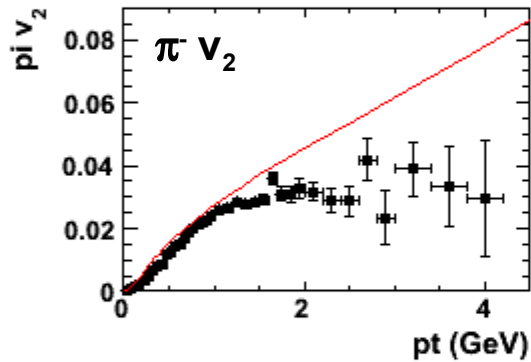
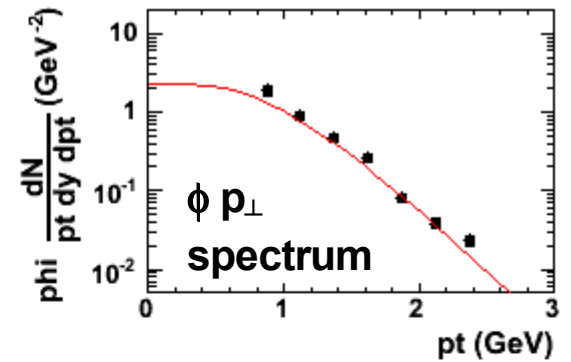
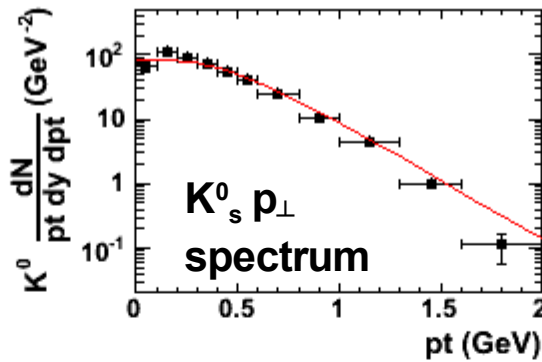
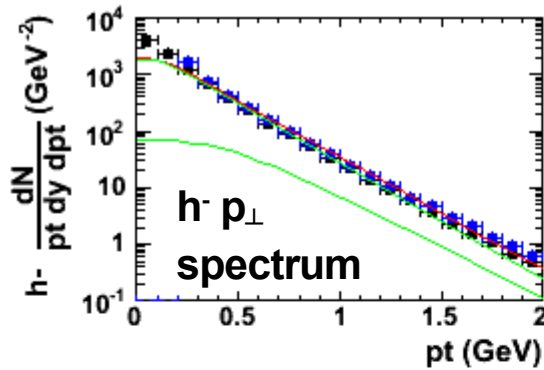
# Hydro

- 🌐 Pasi Huovinen, calculation of Au+Pb at 158 A GeV,  $b=2.6$  fm
- 🌐 hydrodynamical model, see e.g. nucl-th/0305064
- 🌐 freeze-out at a fixed energy density (similar to fixed temp)

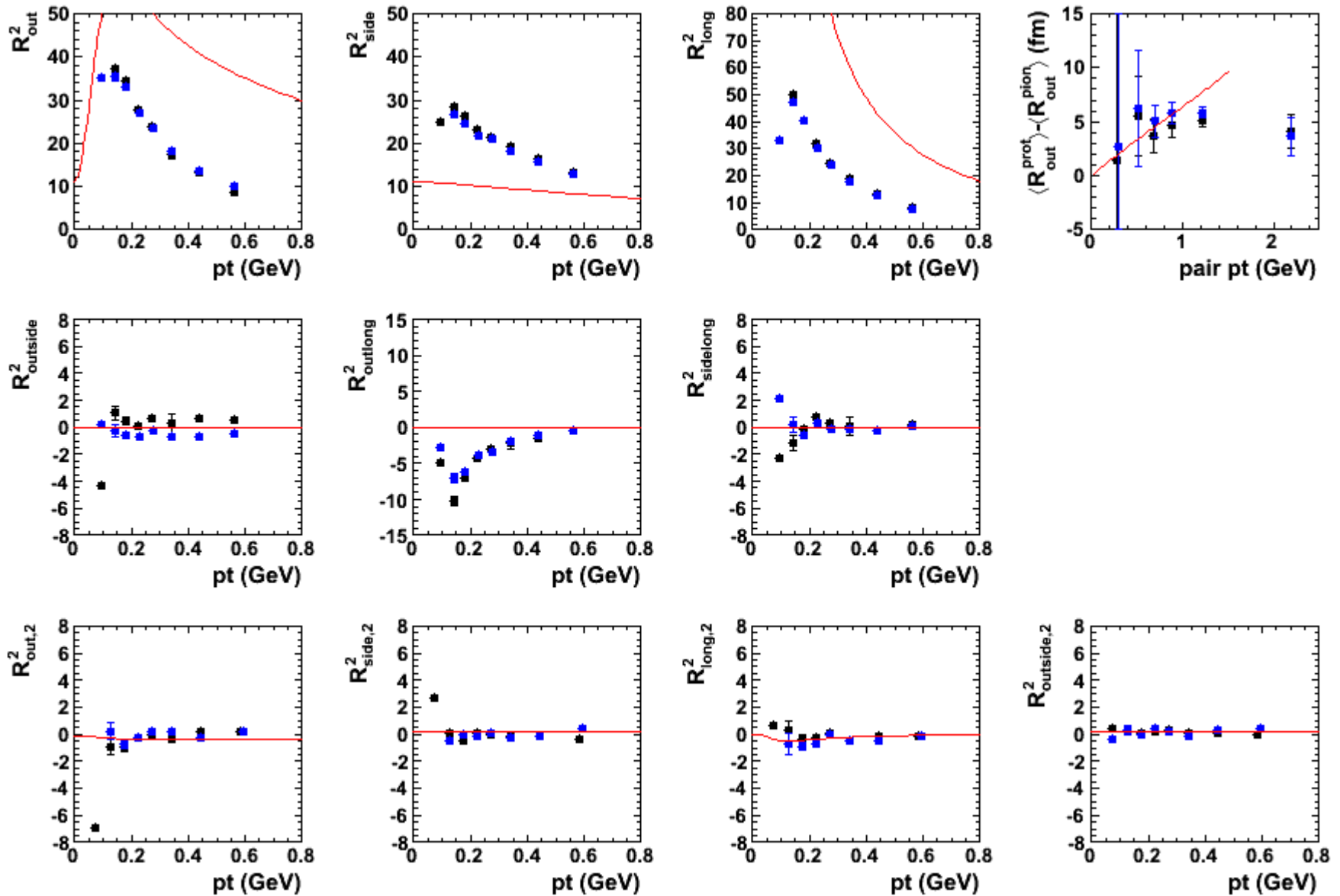
two sets of results:

- 🌐  $T=160$  MeV (like at chemical freeze-out)
- 🌐  $T=120$  MeV (like at kinetic freeze-out)

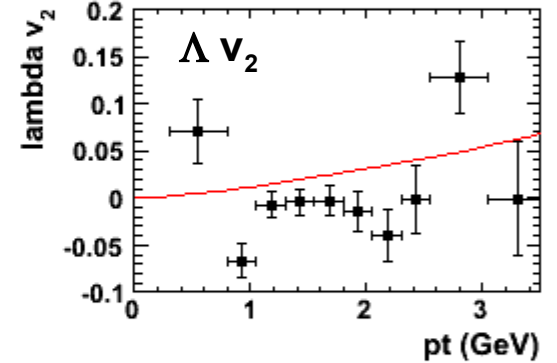
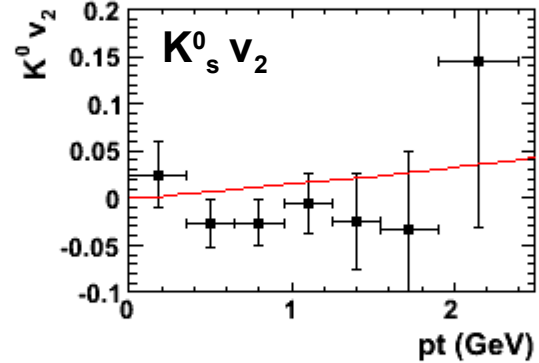
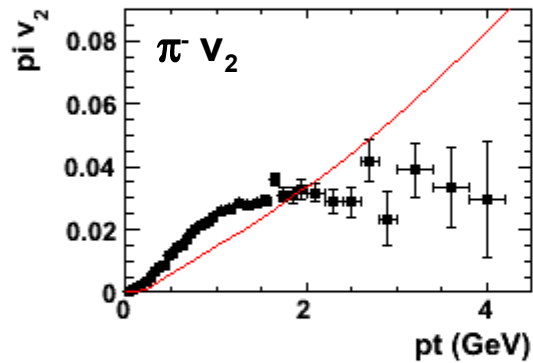
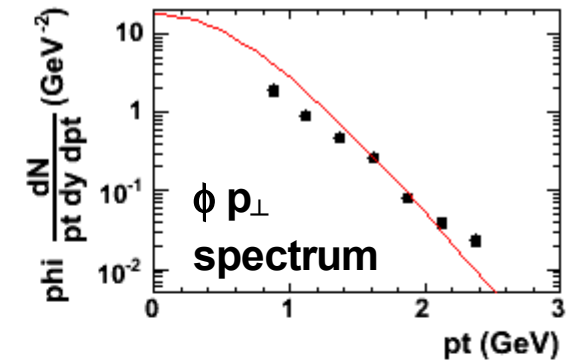
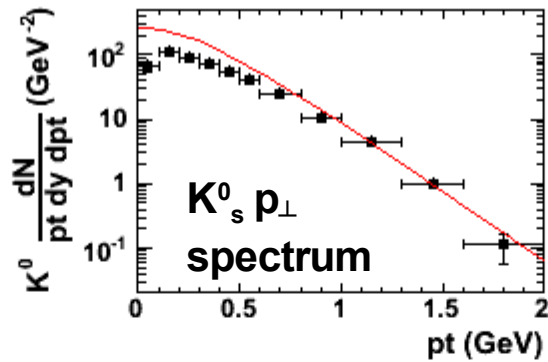
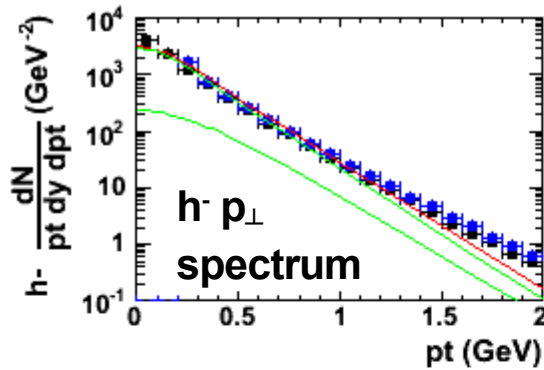
# hydro T=120 MeV (lines) and CERES (points)



# hydro T=120 MeV (lines) and CERES (points)

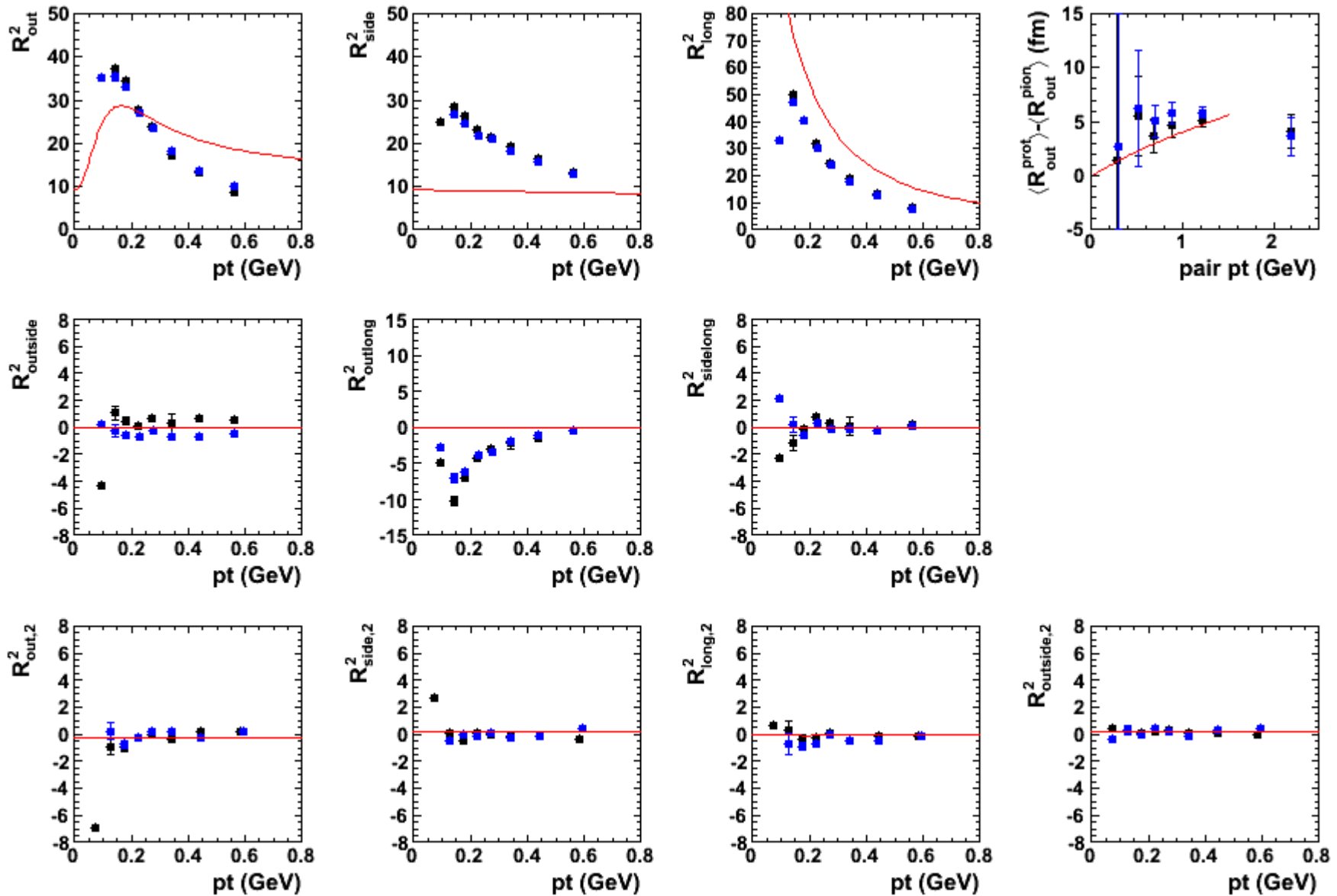


# hydro T=160 MeV (lines) and CERES (points)





# hydro T=160 MeV (lines) and CERES (points)



# puzzle

hydro

~~RHIC~~

HBT

puzzle

# Blast wave model

Retière, Lisa, PRC 70(2004)044907

analytic hydro-inspired 8-d emission function

$$S(x, K) = m_T \cosh(\eta - Y) \Omega(r, \phi_S) e^{\frac{-(\tau - \tau_0)^2}{2\Delta\tau^2}} \frac{1}{e^{K \cdot u/T} \pm 1}$$

with the space profile

$$\Omega(r, \phi_S) = \Omega(\tilde{r}) = \frac{1}{1 + e^{(\tilde{r}-1)/a}}$$

and the normalized elliptic radius

$$\tilde{r}(r, \phi_S) = \sqrt{\frac{(r \cos(\phi_S))^2}{R_x^2} + \frac{(r \sin(\phi_S))^2}{R_y^2}}$$

and the flow four-velocity

$$u = u_\mu(x, \rho_0, \rho_2)$$

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and the flow four-velocity

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space-time  
dependence

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and the flow four-velocity

$$u = u_\mu(x, \rho_0, \rho_2)$$

**four-momentum  
dependence**

# Blast wave model

Retière, Lisa, PRC 70(2004)044907

analytic hydro-inspired 8-d emission function

$$S(x, K) = m_T \cosh(\eta - Y) \Omega(r, \phi_S) e^{-\frac{(\tau - \tau_0)^2}{2\Delta\tau^2}} \frac{1}{e^{K \cdot u} T \pm 1}$$

with the space profile

$$\Omega(r, \phi_S) = \Omega(\tilde{r}) = \frac{1}{1 + e^{(\tilde{r}-1)/a}}$$

parameters

and the normalized elliptic radius

$$\tilde{r}(r, \phi_S) = \sqrt{\frac{(r \cos(\phi_S))^2}{R_x^2} + \frac{(r \sin(\phi_S))^2}{R_y^2}}$$

and the flow four-velocity

$$u = u_\mu(x, \rho_0, \rho_2)$$

# Blast wave model

Retière, Lisa, PRC 70(2004)044907

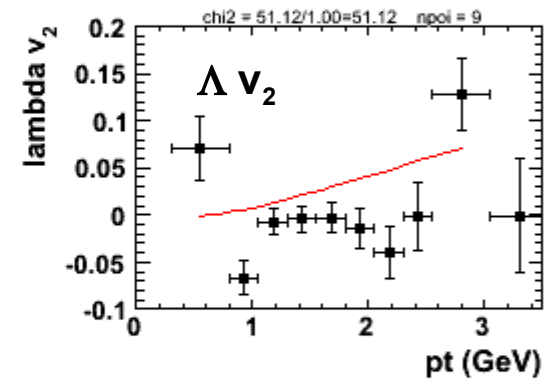
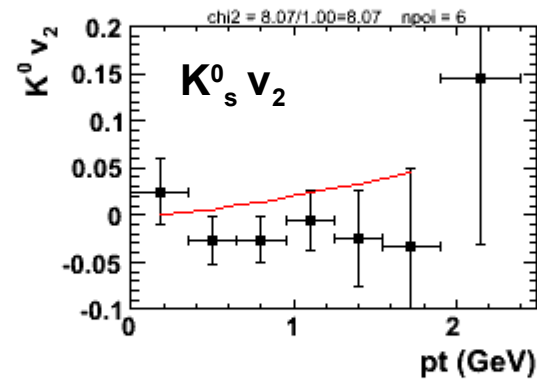
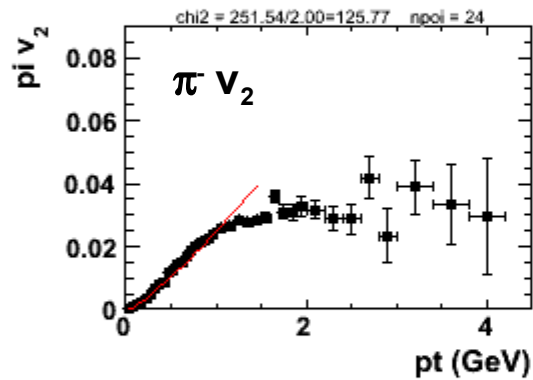
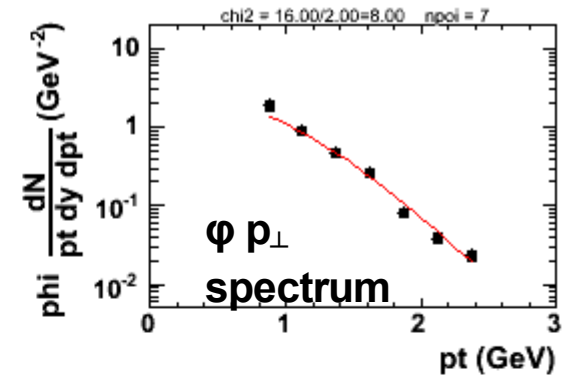
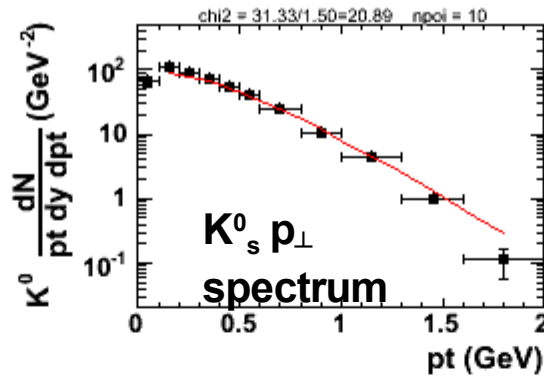
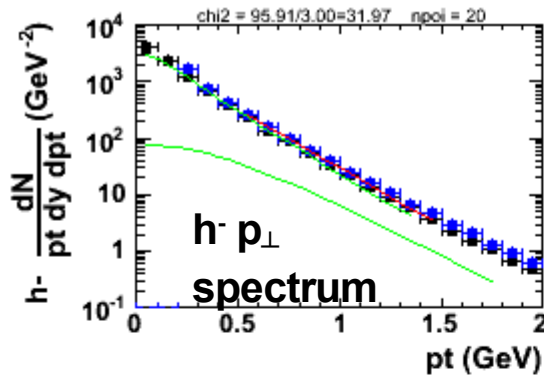
analytic hydro-inspired 8-d emission function

$$S(x, K) = m_T \cosh(\eta - Y) \Omega(r, \phi_S) e^{\frac{-(\tau - \tau_0)^2}{2\Delta\tau^2}} \frac{1}{e^{K \cdot u/T} \pm 1}$$

by semi-analytic integration gives

- 🌐 pt-spectra
- 🌐 elliptic flow
- 🌐 HBT radii (including their reaction-plane dependence)
- 🌐 non-identical particle correlations

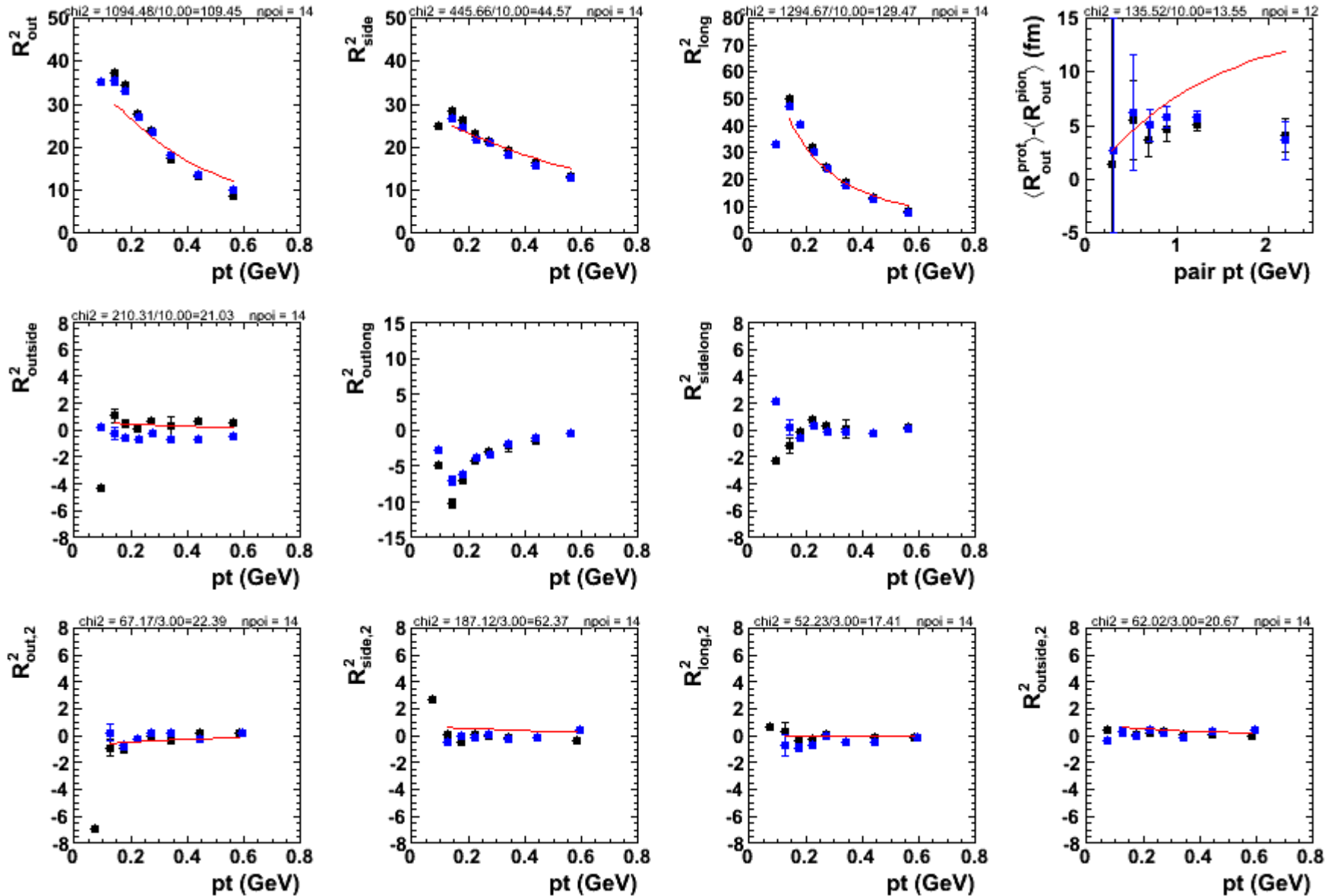
# blast T=100 MeV (lines) and CERES (points)



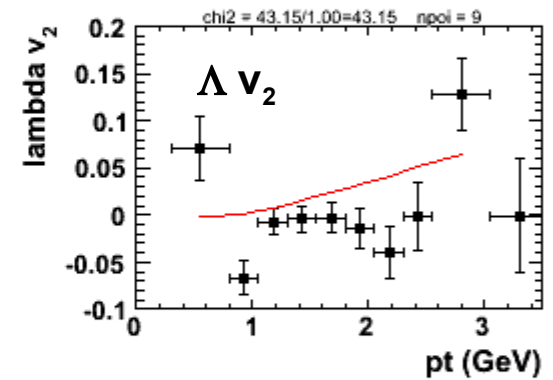
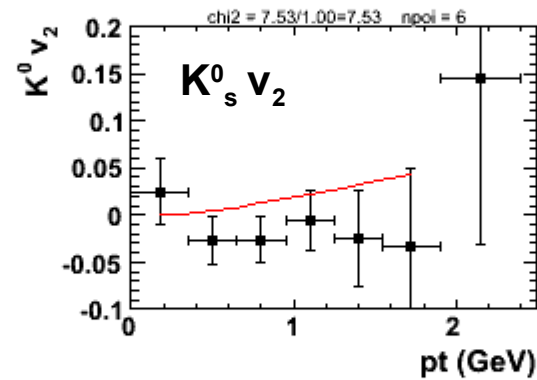
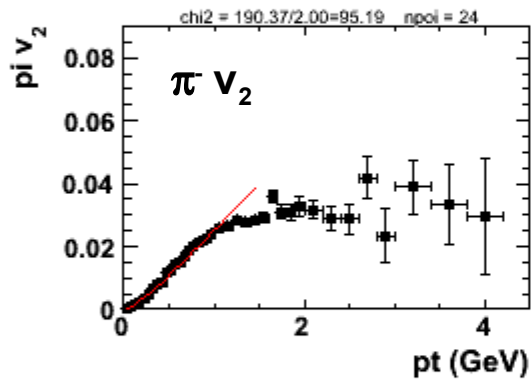
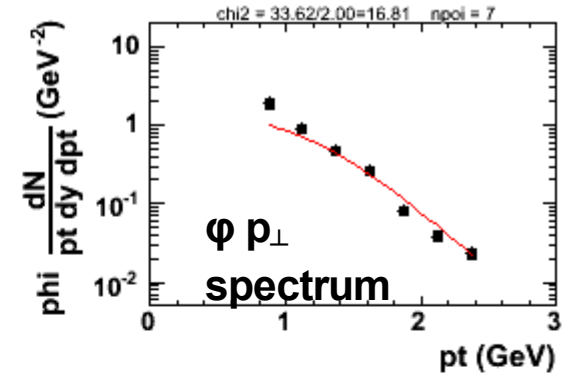
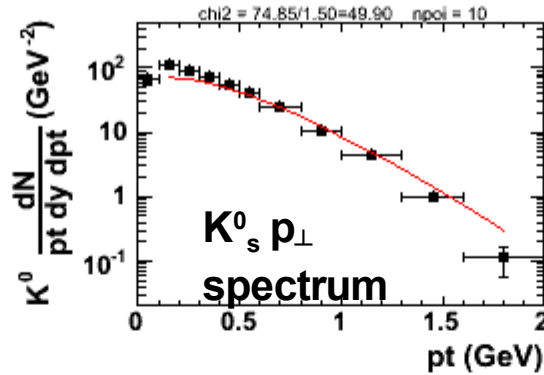
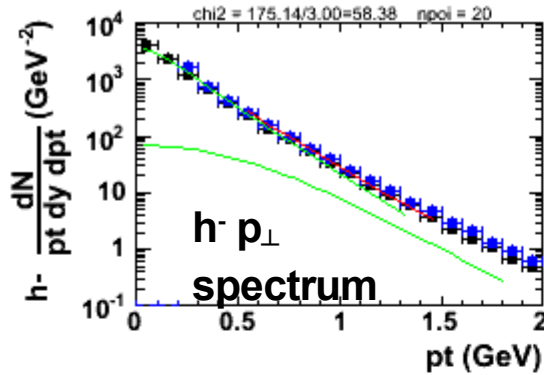
other->fPim = 152.7  
 other->fKa0 = 18.44  
 other->fPhi = 1.451  
 blast->fT = 0.100  
 blast->fRho0 = 0.87  
 blast->fRho2 = 0.016  
 blast->fRx = 11.26  
 blast->fRy = 11.42  
 blast->fAs = 0.010  
 blast->fTau0 = 7.37  
 blast->fDtau = 1.55



# blast T=100 MeV (lines) and CERES (points)

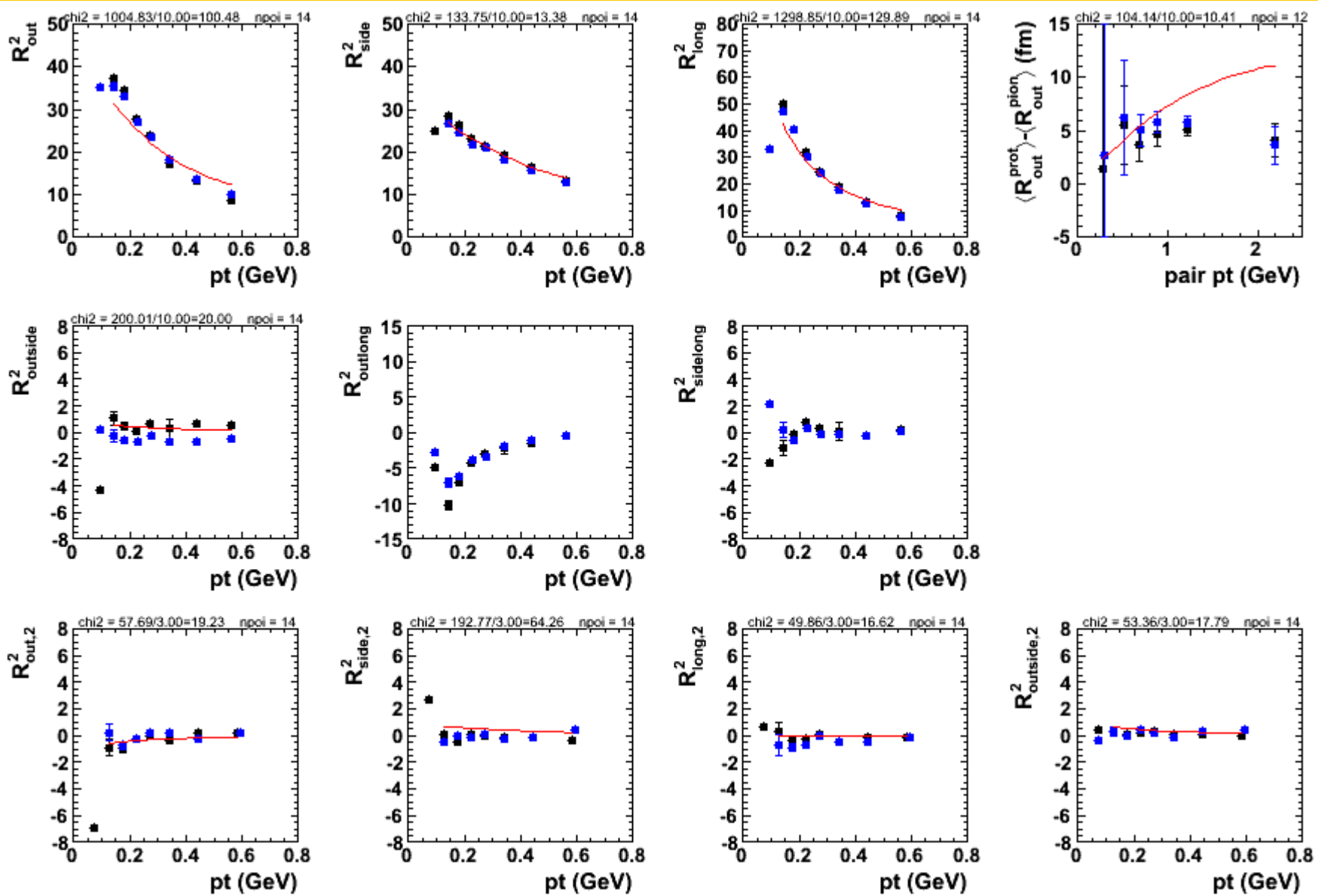


# blast T=80 MeV (lines) and CERES (points)

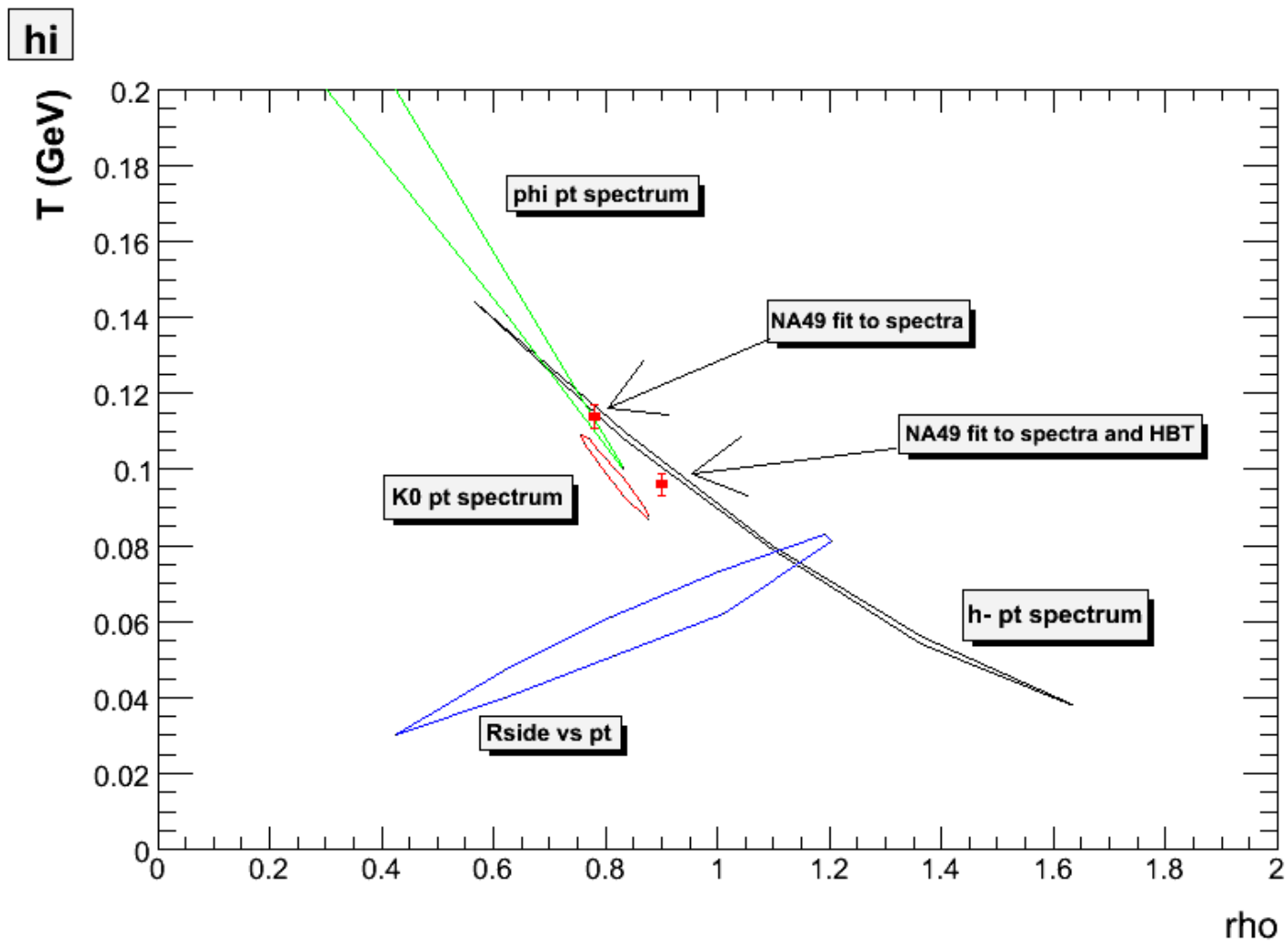


other->fPim = 165.0  
 other->fKa0 = 17.39  
 other->fPhi = 1.117  
 blast->fT = 0.080  
 blast->fRho0 = 1.02  
 blast->fRho2 = 0.014  
 blast->fRx = 12.62  
 blast->fRy = 12.79  
 blast->fAs = 0.010  
 blast->fTau0 = 8.69  
 blast->fDtau = 2.03

# blast T=80 MeV (lines) and CERES (points)



# T - $\rho$ contours



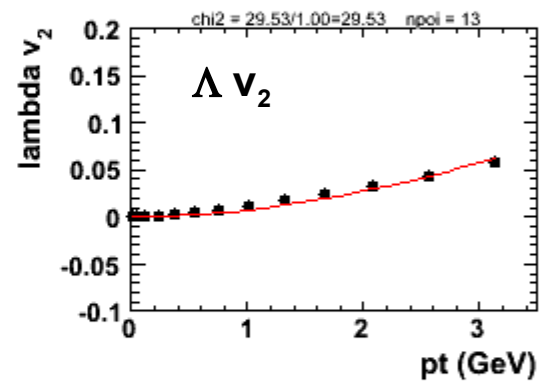
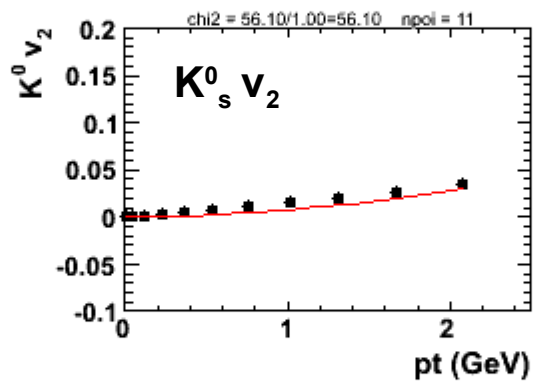
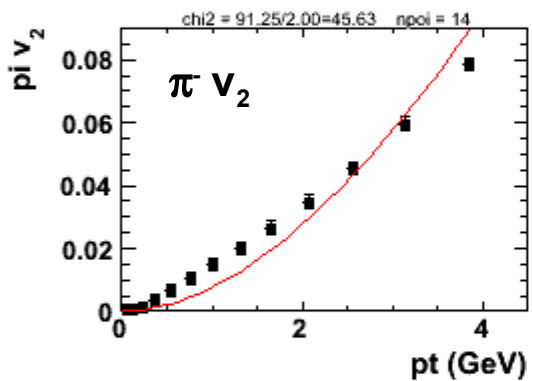
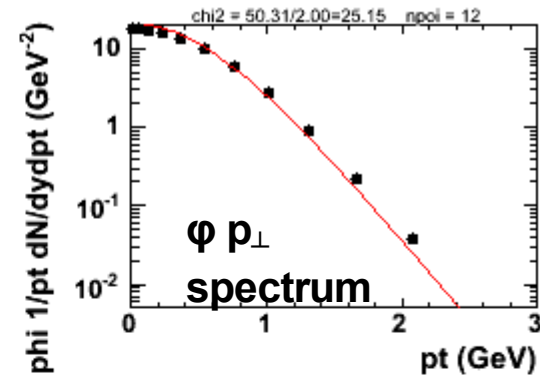
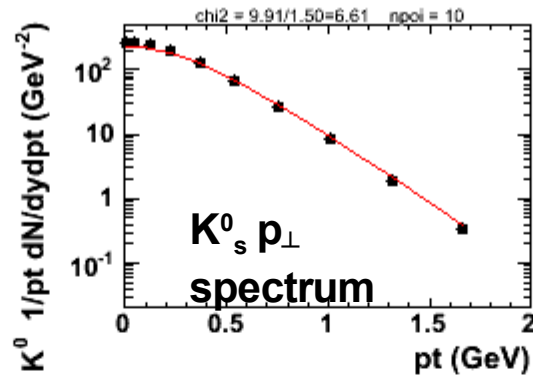
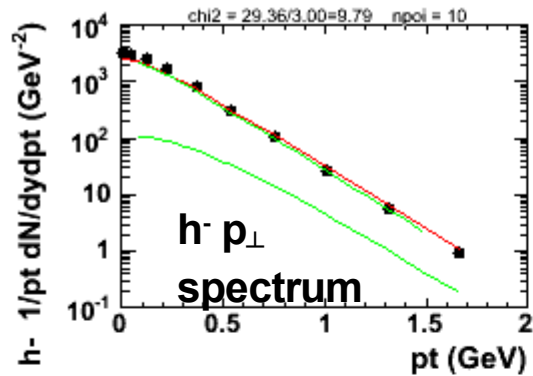
Thu Sep 7 20:23:17 2006

# blast vs. hydro

**Use blast to understand what is wrong in hydro:**

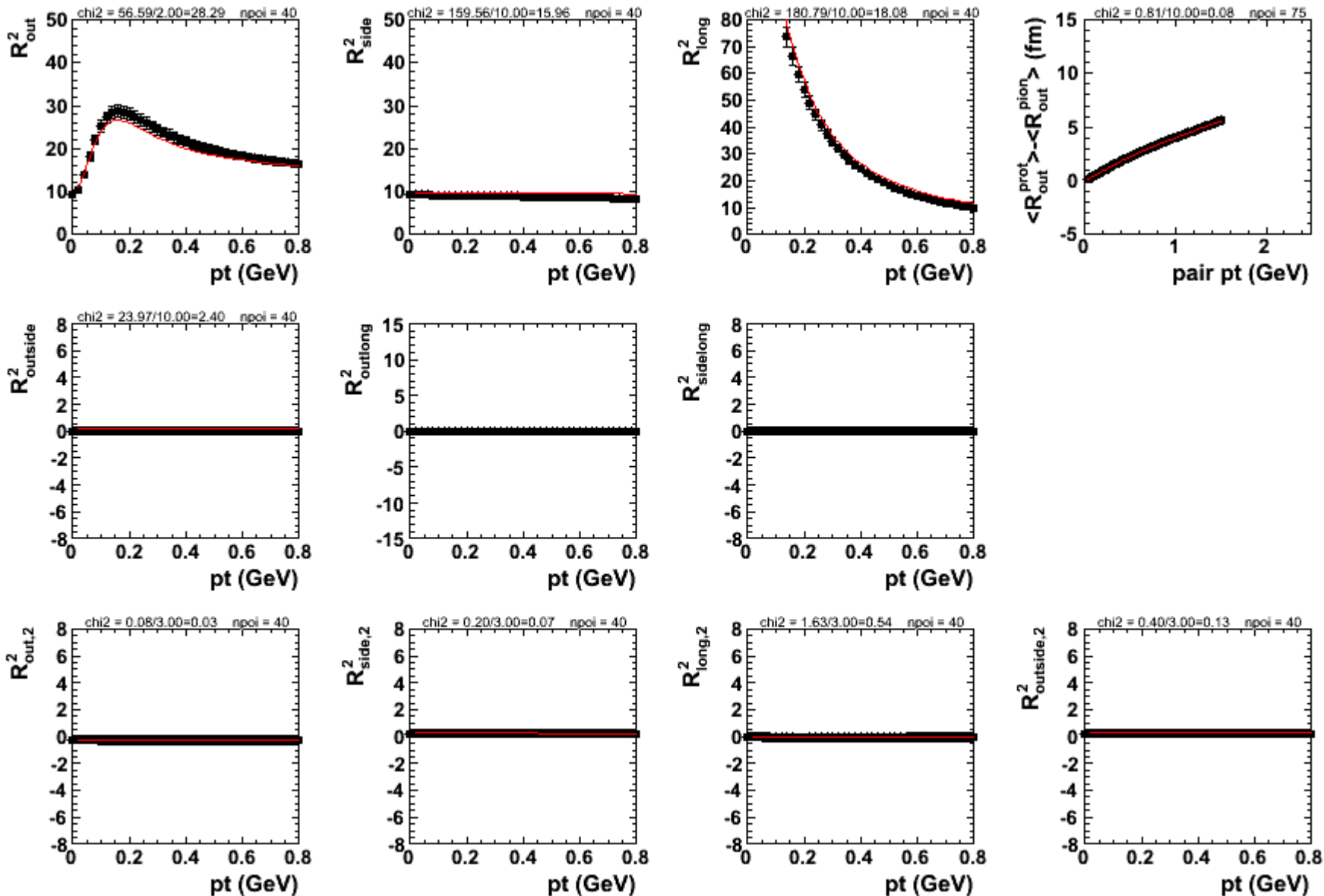
- 🌐 **blast is hydro inspired and has 8 free parameters**  
→ true hydro source must be a special case of blast source
- 🌐 **fit CERES by blast and fit hydro by blast and compare the resulting parameters**
- 🌐 **identify THE parameter which is different**  
→ this is what needs to be fixed in hydro

# blast (lines) and hydro 160 MeV (points)

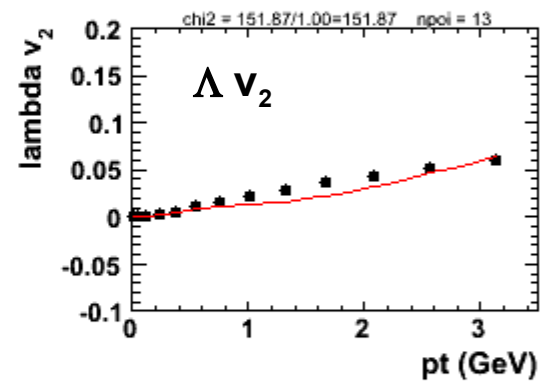
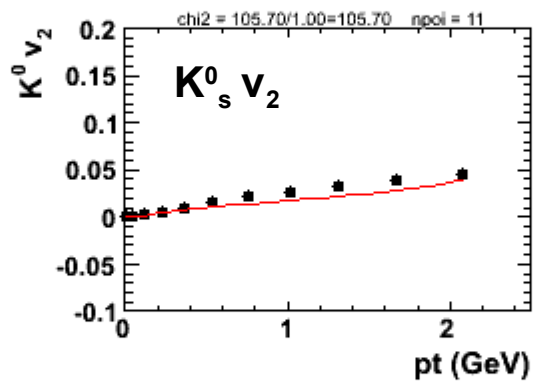
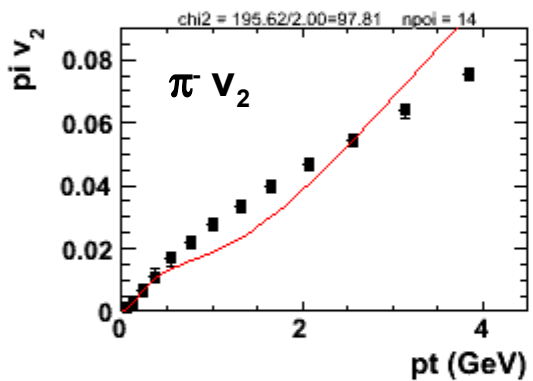
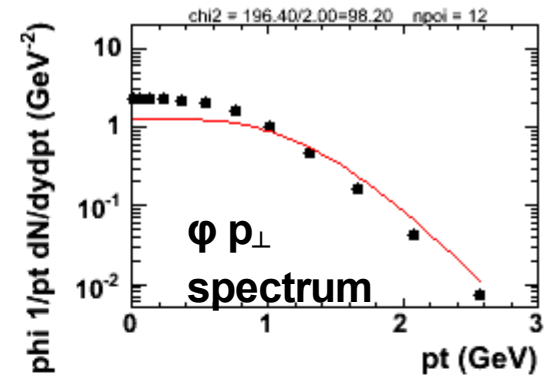
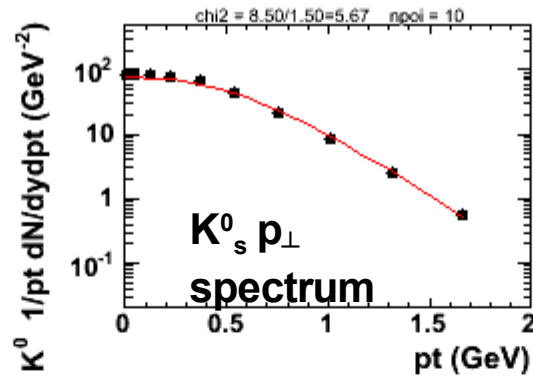
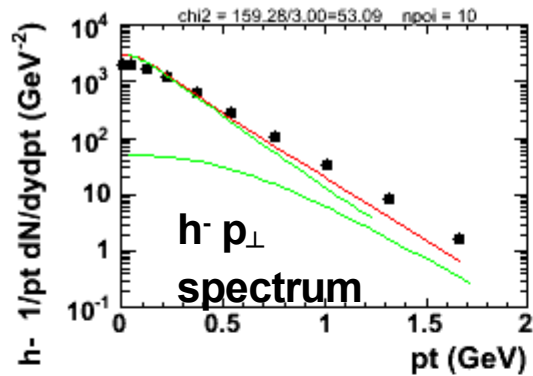


other->fPim = 155.5  
 other->fKa0 = 30.95  
 other->fPhi = 4.806  
 blast->fT = 0.174  
 blast->fRho0 = 0.15  
 blast->fRho2 = 0.026  
 blast->fRx = 6.22  
 blast->fRy = 6.30  
 blast->fAs = 0.010  
 blast->fTau0 = 4.57  
 blast->fDtau = 2.56

# blast (lines) and hydro 160 MeV (points)



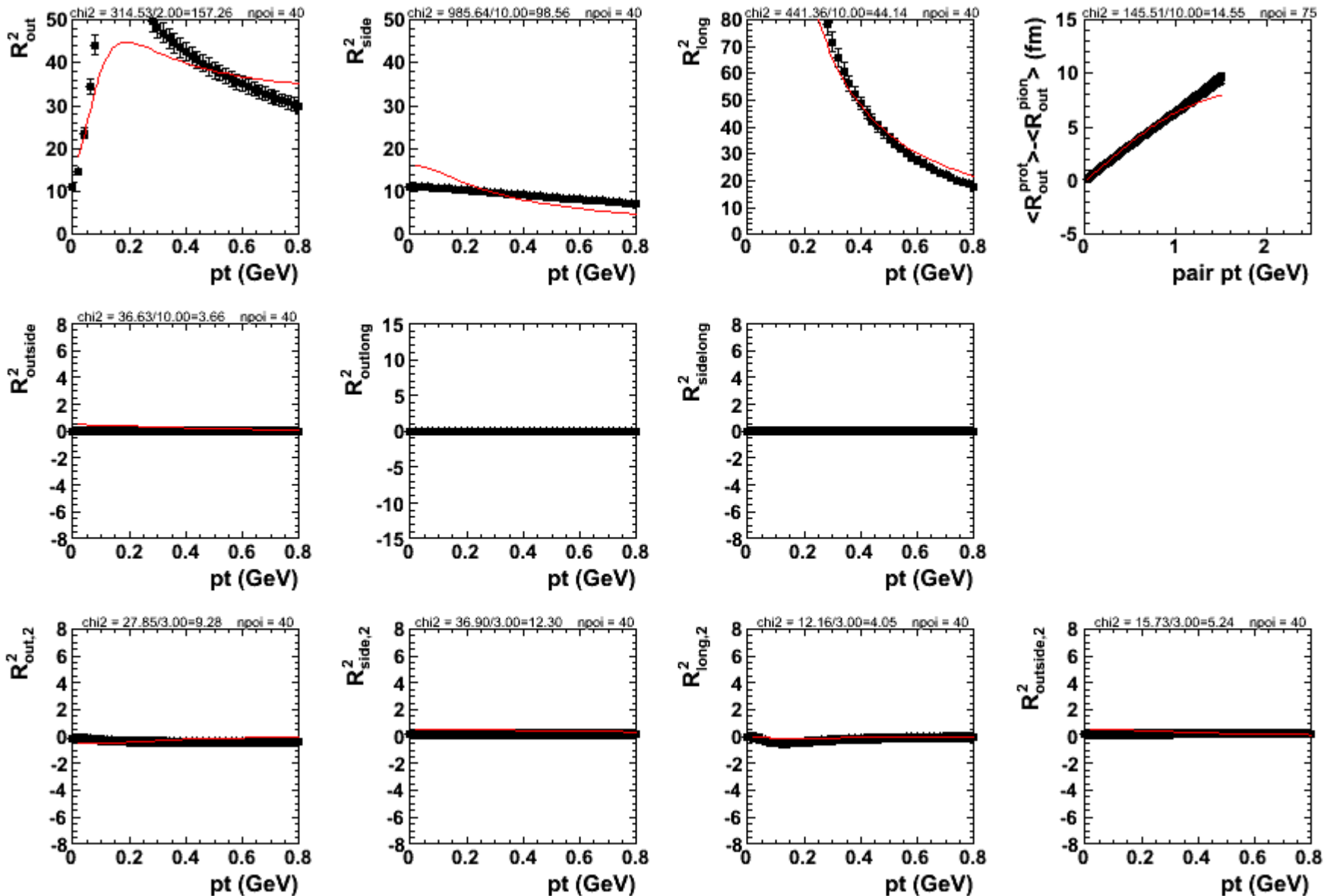
# blast (lines) and hydro 120 MeV (points)



other->fPim = 129.6  
 other->fKa0 = 19.10  
 other->fPhi = 1.164  
 blast->fT = 0.070  
 blast->fRho0 = 1.07  
 blast->fRho2 = 0.001  
 blast->fRx = 9.23  
 blast->fRy = 9.53  
 blast->fAs = 0.010  
 blast->fTau0 = 14.73  
 blast->fDtau = 6.13



# blast (lines) and hydro 120 MeV (points)

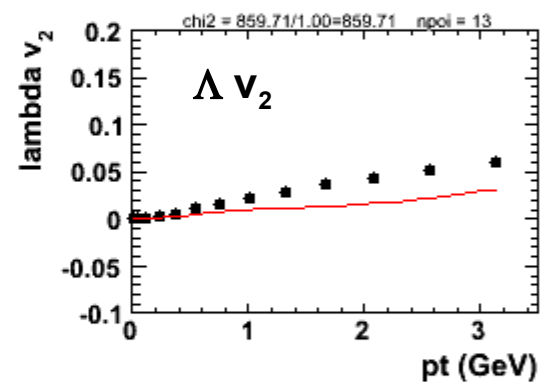
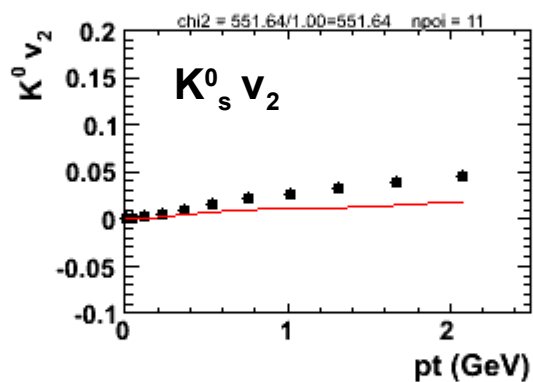
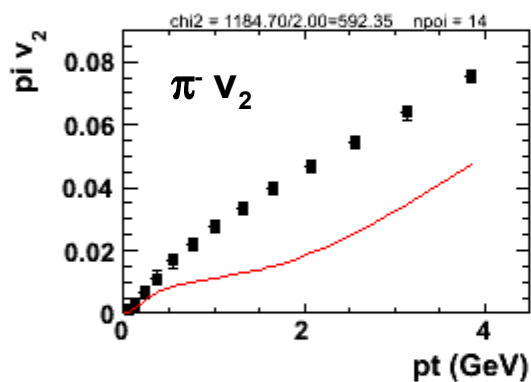
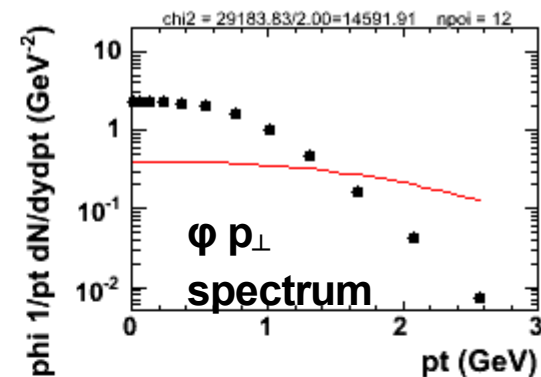
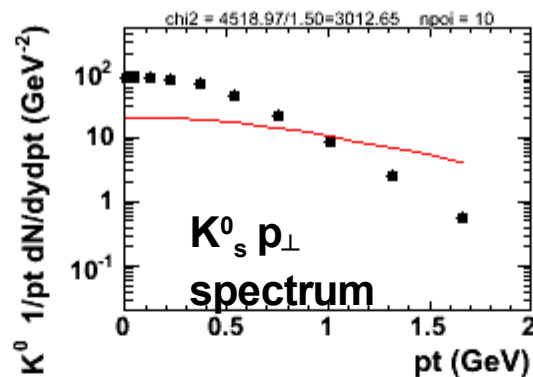
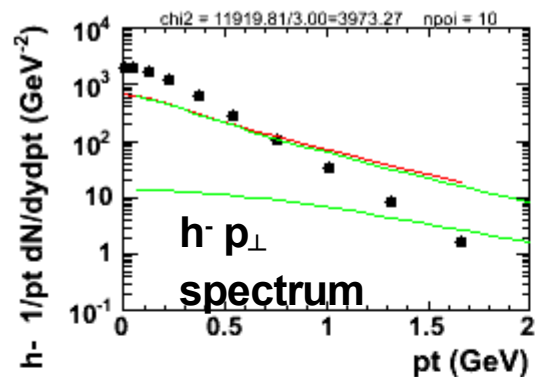


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Use blast to understand what is wrong in hydro:

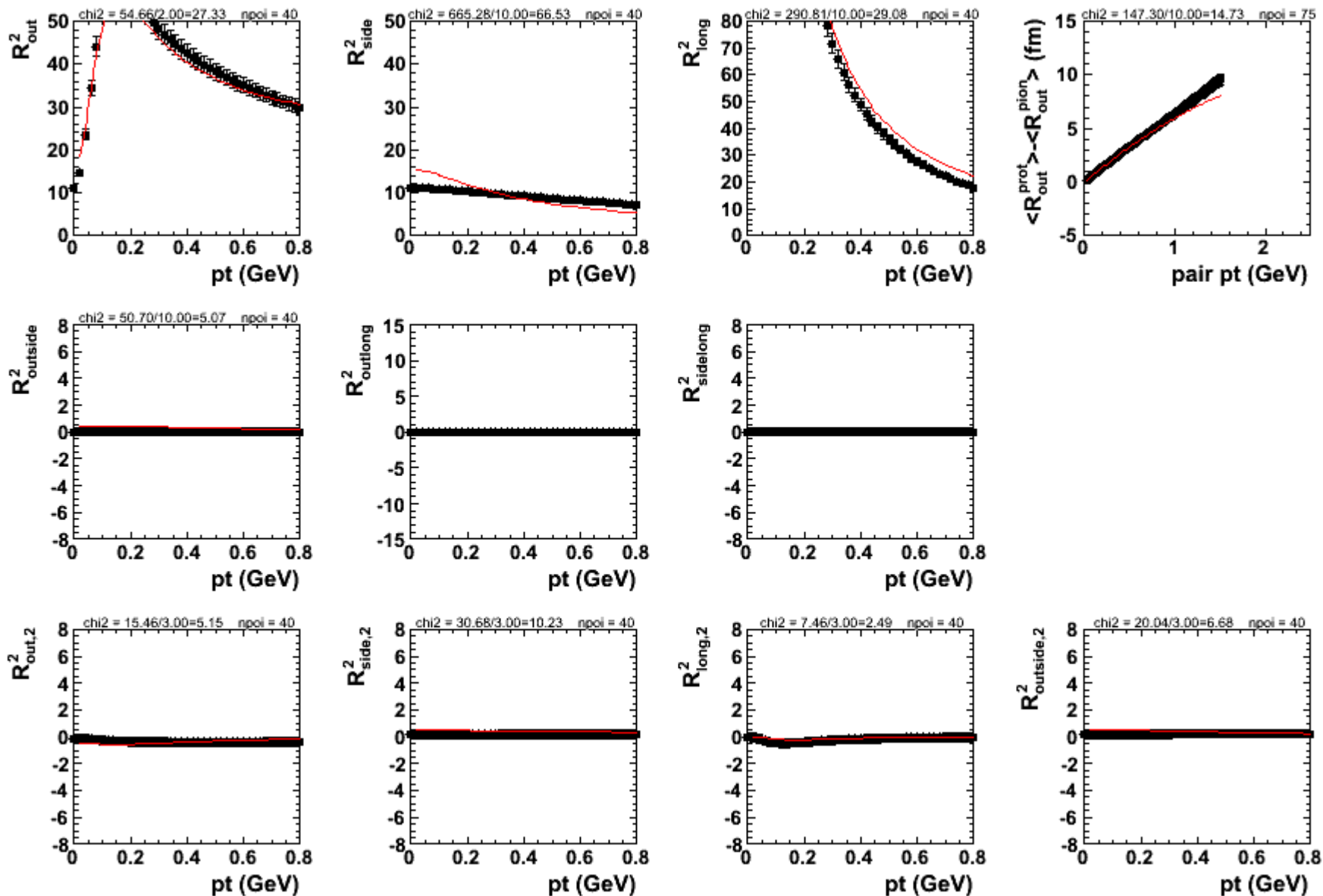
- 🌐 **blast is hydro inspired and has 8 free parameters**
  - true hydro source must be a special case of blast source
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  - this is what needs to be fixed in hydro

# blast only HBT (lines) and hydro 120 MeV (points)

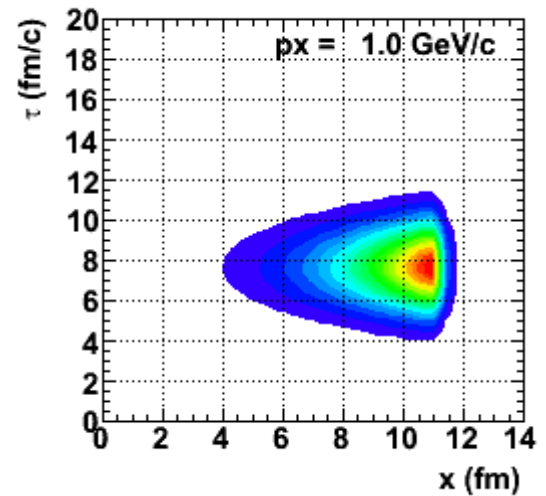
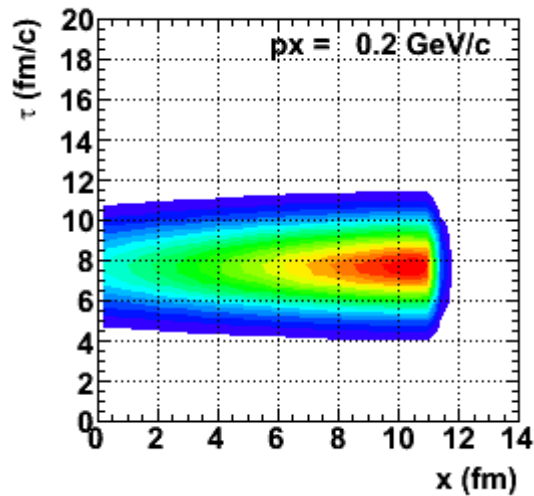
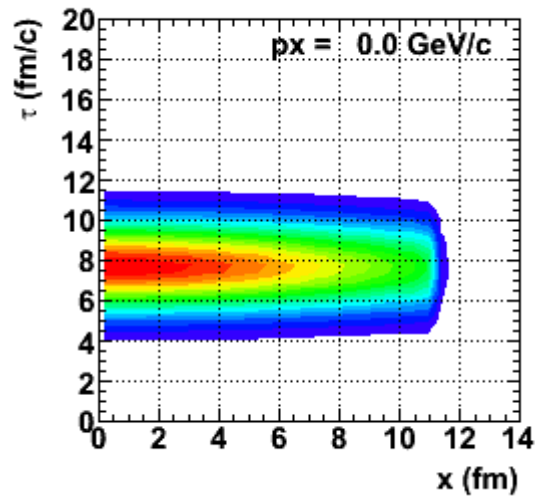
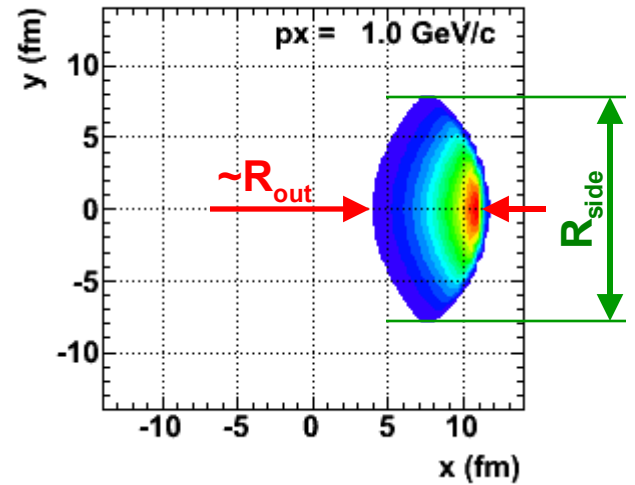
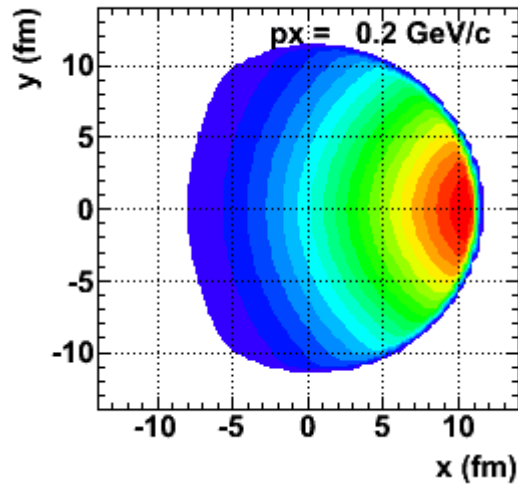
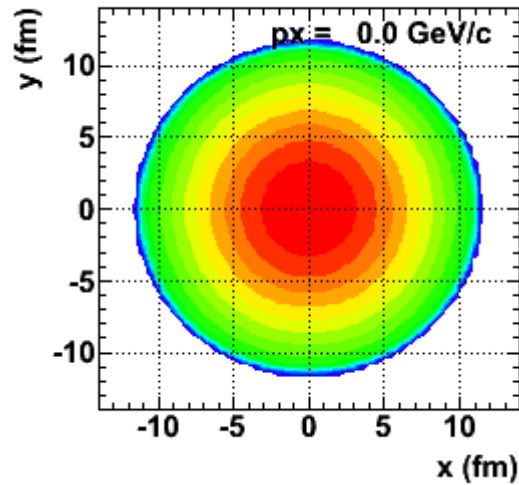


other->fPim = 129.6  
 other->fKa0 = 19.10  
 other->fPhi = 1.164  
 blast->fT = 0.139  
 blast->fRho0 = 1.59  
 blast->fRho2 = 0.001  
 blast->fRx = 9.68  
 blast->fRy = 9.98  
 blast->fAs = 0.010  
 blast->fTau0 = 10.11  
 blast->fDtau = 5.84

# blast only HBT (lines) and hydro 120 MeV (points)

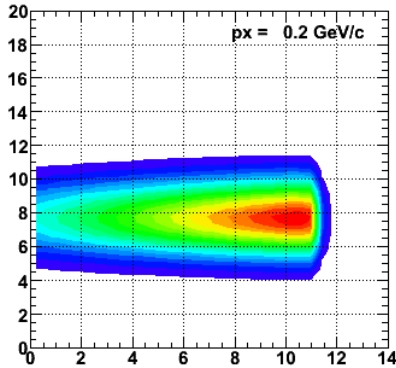


# blast - source shape

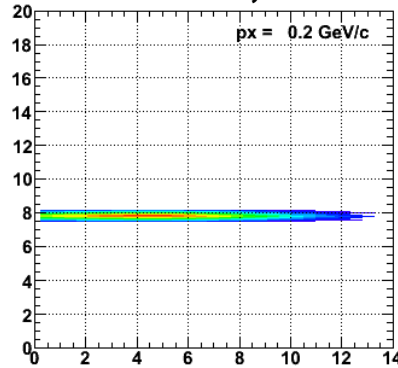


# fitted blast source shapes

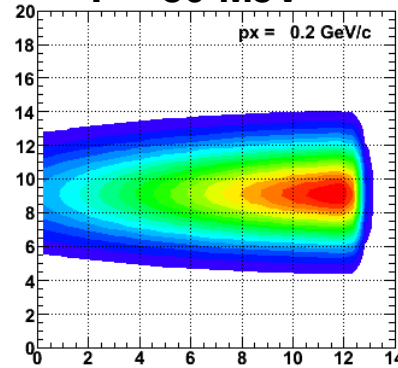
**T = 100 MeV**



**T=100 MeV, as=0.3**

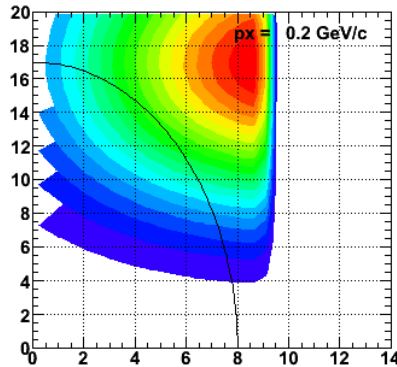


**T = 80 MeV**

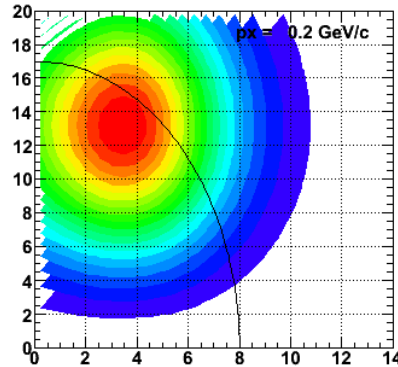


fit to CERES data

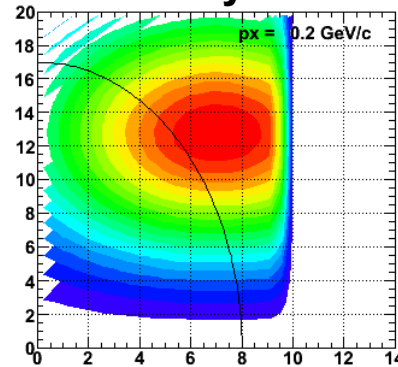
**standard**



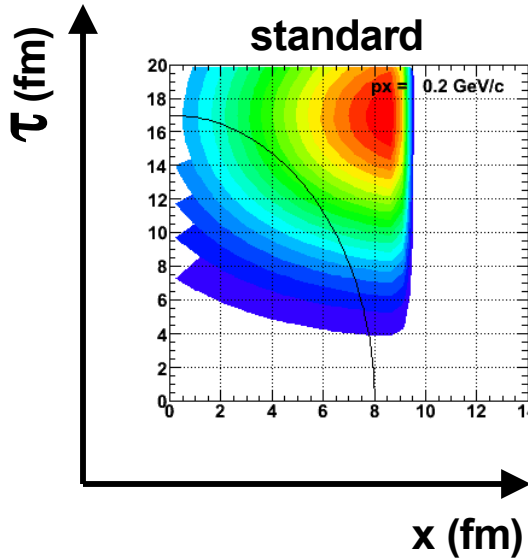
**as=0.3**



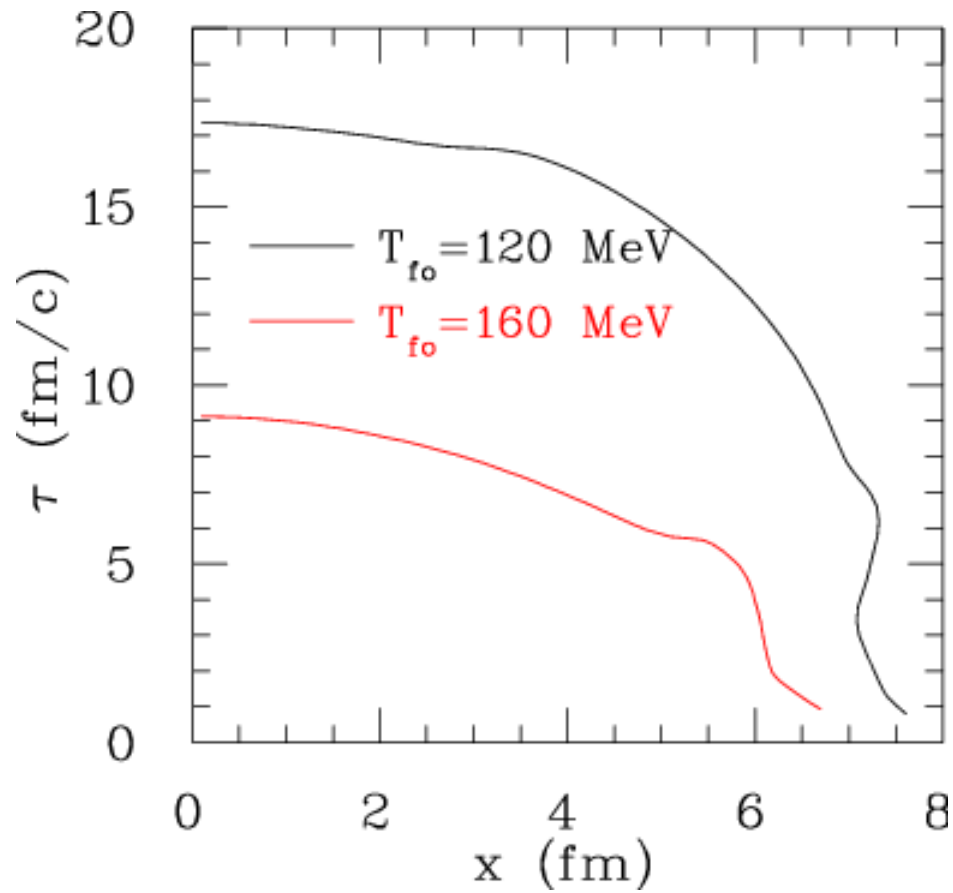
**fit only hbt**



"fit" to hydro  
120 MeV

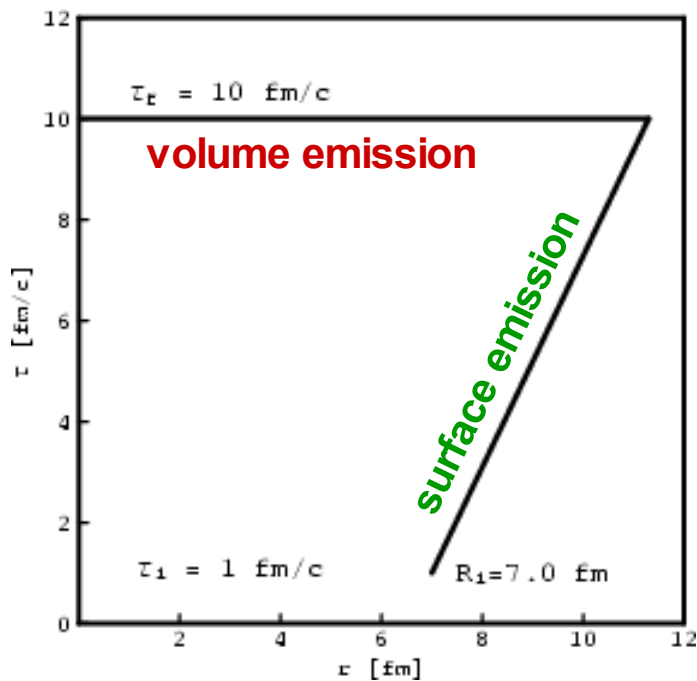


# hydro source shape

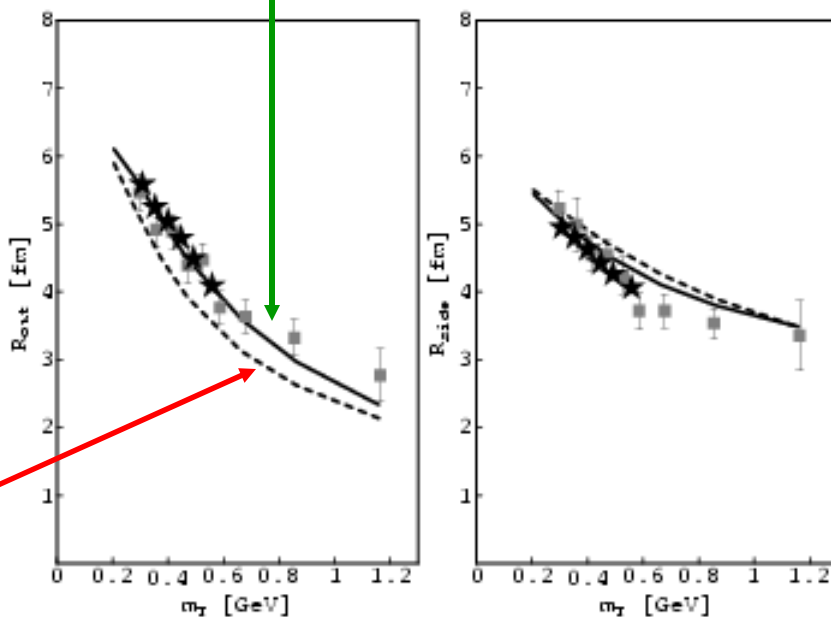


# Sinyukov's blast

Phys.Rev. C73 (2006) 024903  
pi- pi- from PHENIX and STAR



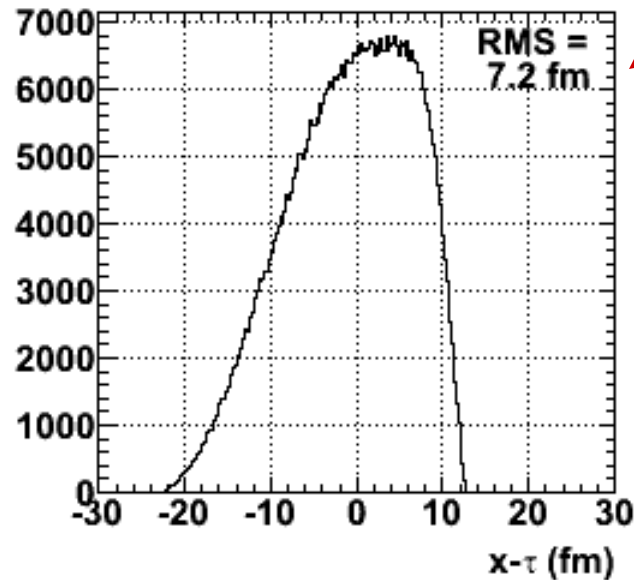
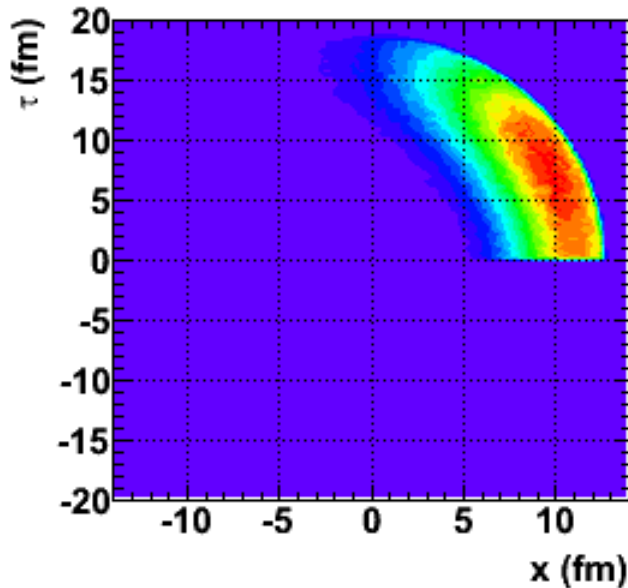
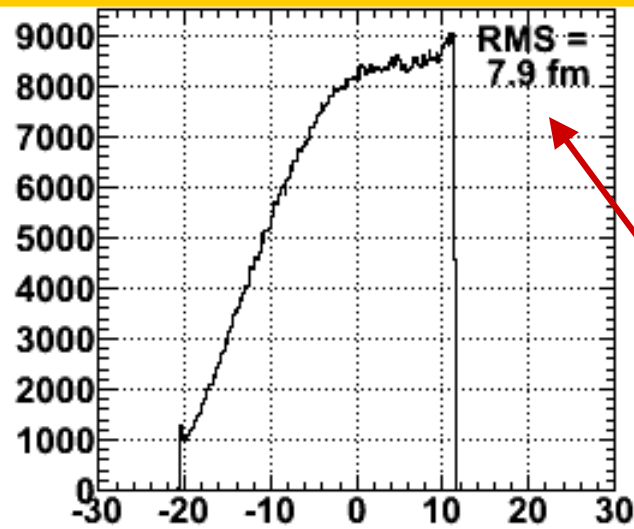
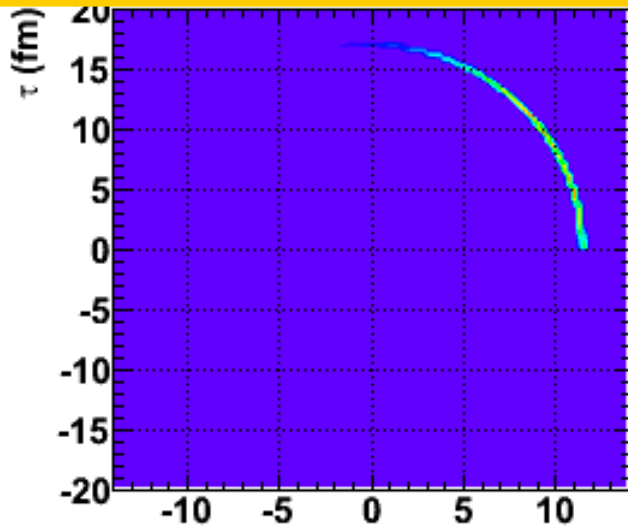
volume and surface



volume



# hydro, why is $R_{out}$ so large and $R_{side}$ so small: freeze-out surface too thin?



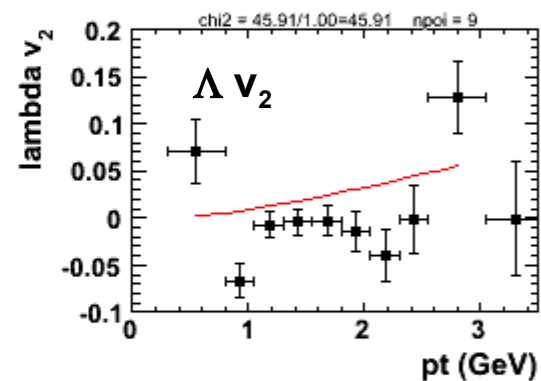
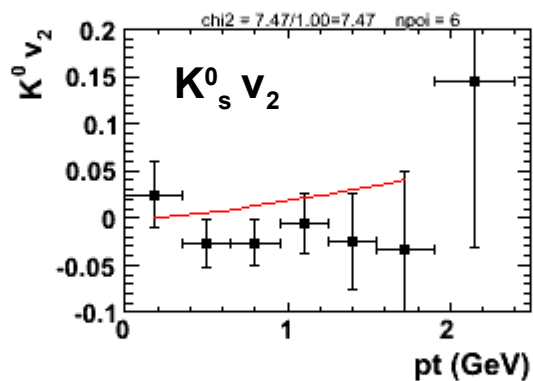
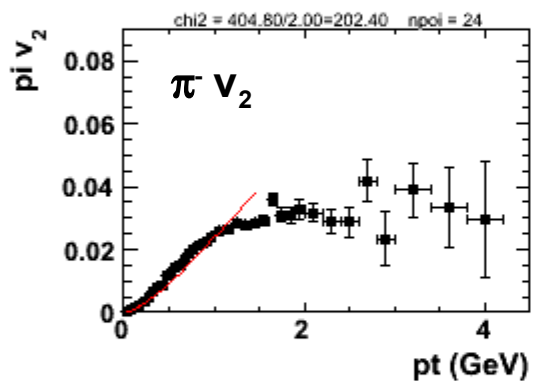
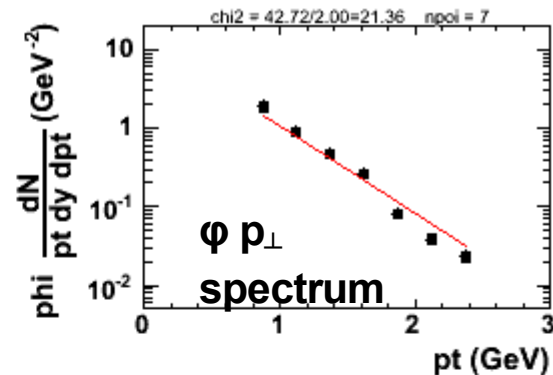
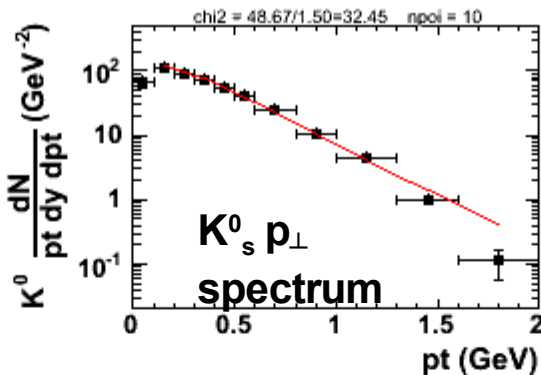
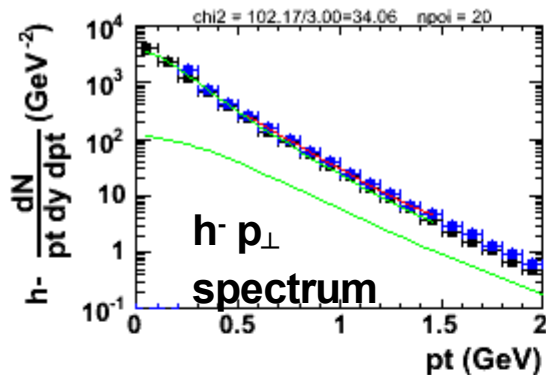
$\sim R_{out}$

# summary

- 🌐 blast fits CERES data reasonably well  
(in spite of the lacking resonances, lacking surface emission...)
- 🌐 hydro fits CERES spectra and flow but not HBT radii
- 🌐 blast is qualitatively different from hydro (even if "inspired" by it)
- 🌐 troubles with hydro may have to do with the freeze-out hypersurface moving inward (Pasi Huovinen)
- 🌐 ... combined with its unrealistic small thickness?

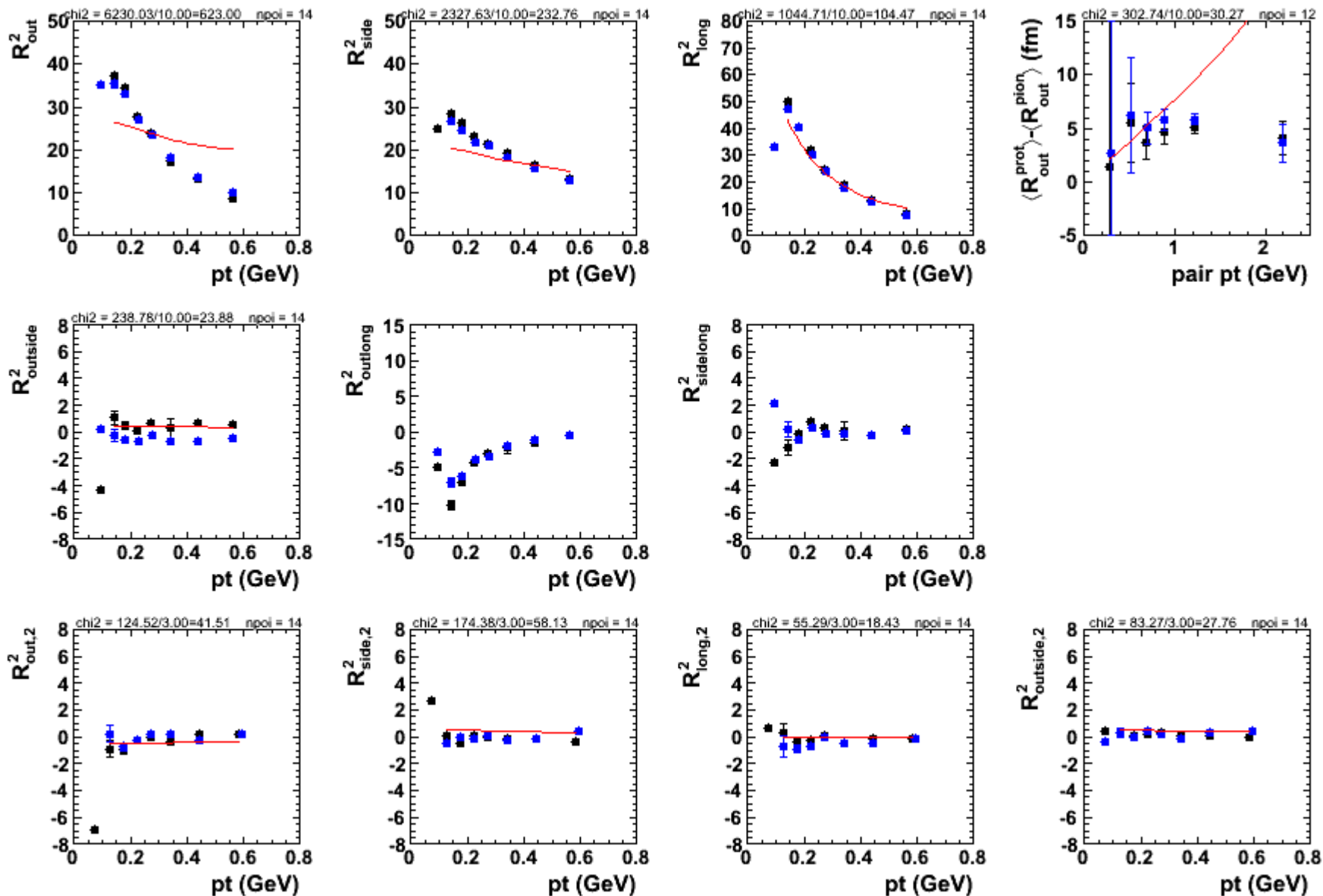
# backup slides

# blast T=100 MeV as=0.3 (lines) and CERES (points)

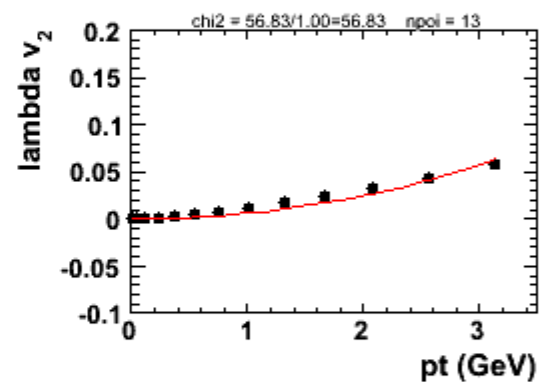
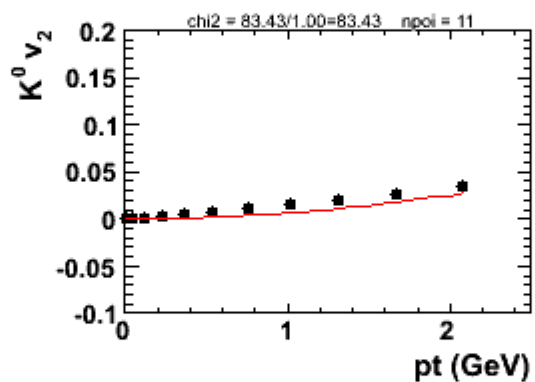
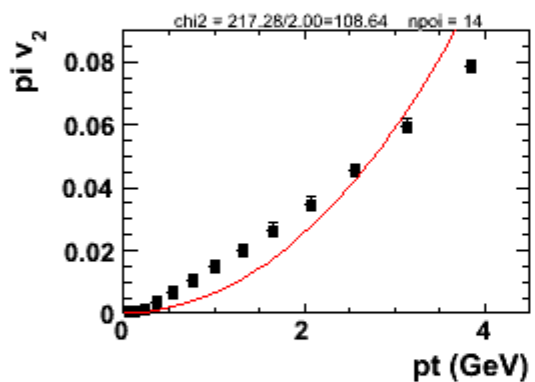
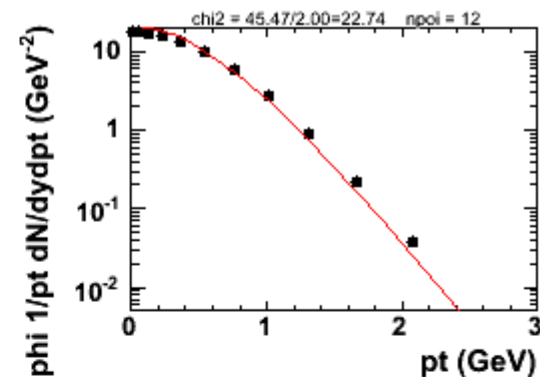
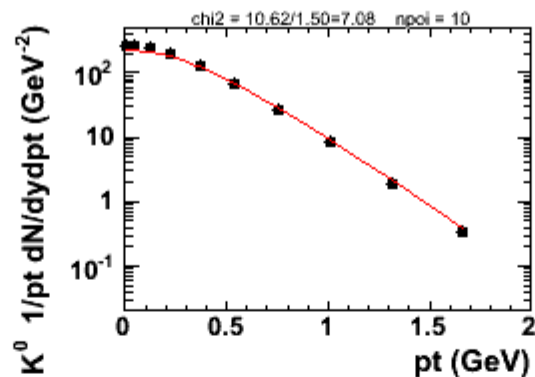
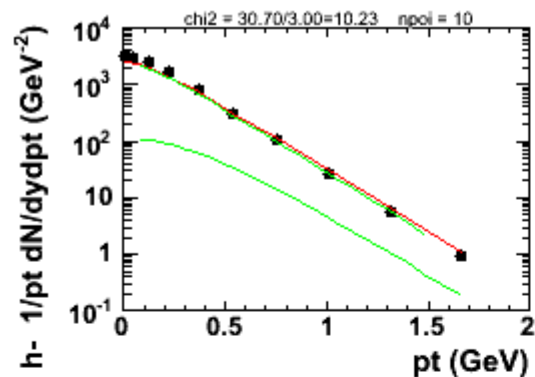


other->fPim = 169.6  
 other->fKa0 = 19.57  
 other->fPhi = 1.710  
 blast->fT = 0.100  
 blast->fRho0 = 0.52  
 blast->fRho2 = 0.009  
 blast->fRx = 6.96  
 blast->fRy = 7.07  
 blast->fAs = 0.300  
 blast->fTau0 = 7.65  
 blast->fDtau = 0.02

# blast T=100 MeV as=0.3 (lines) and CERES (points)

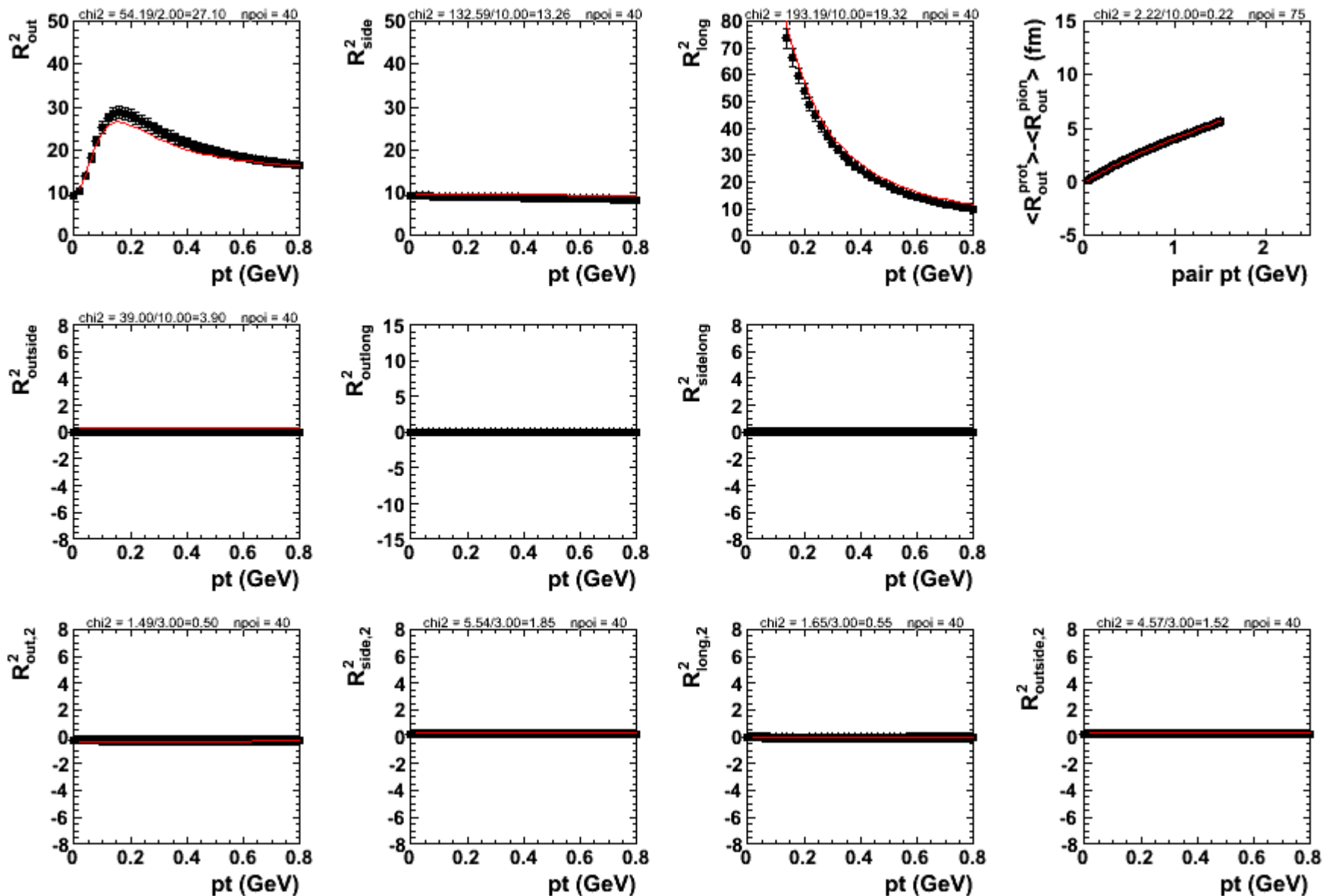


# blast as=0.3 (lines) and hydro 160 MeV (points)

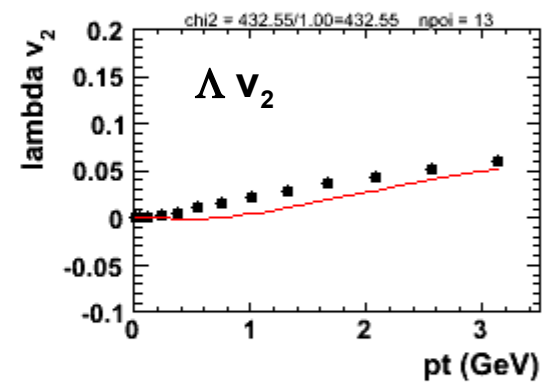
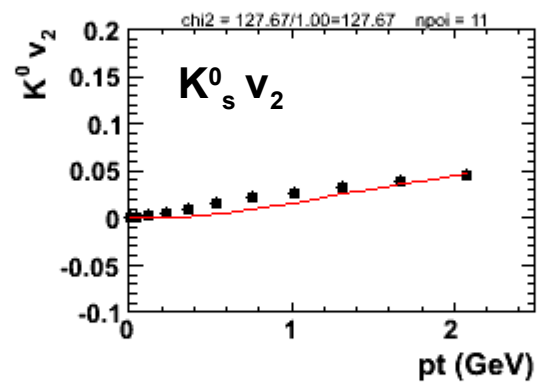
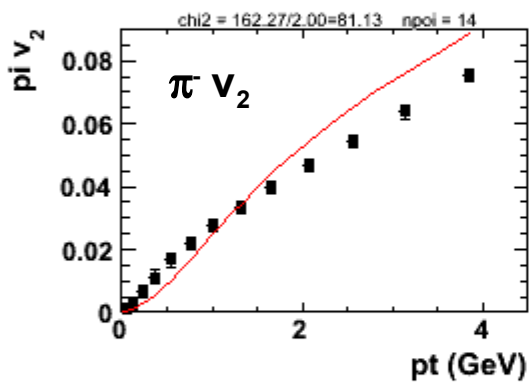
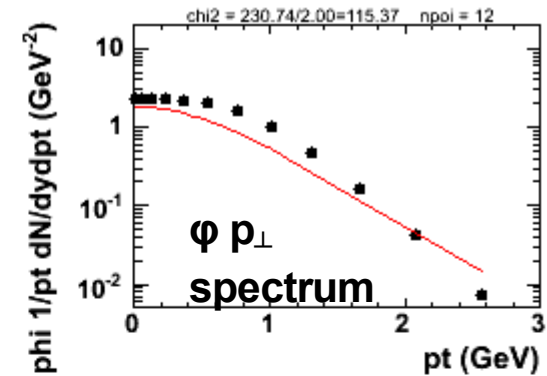
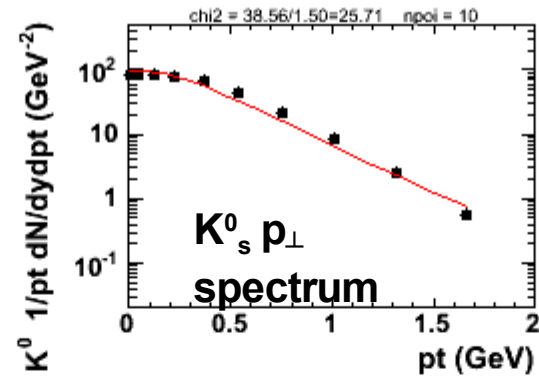
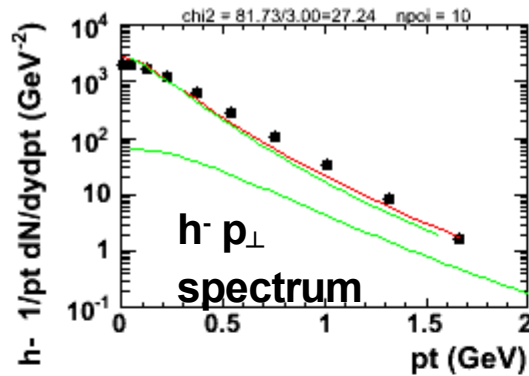


other->fPim = 156.0  
 other->fKa0 = 30.85  
 other->fPhi = 4.775  
 blast->fT = 0.174  
 blast->fRho0 = 0.10  
 blast->fRho2 = 0.012  
 blast->fRx = 3.97  
 blast->fRy = 4.10  
 blast->fAs = 0.300  
 blast->fTau0 = 4.78  
 blast->fDtau = 2.44

# blast as=0.3 (lines) and hydro 160 MeV (points)



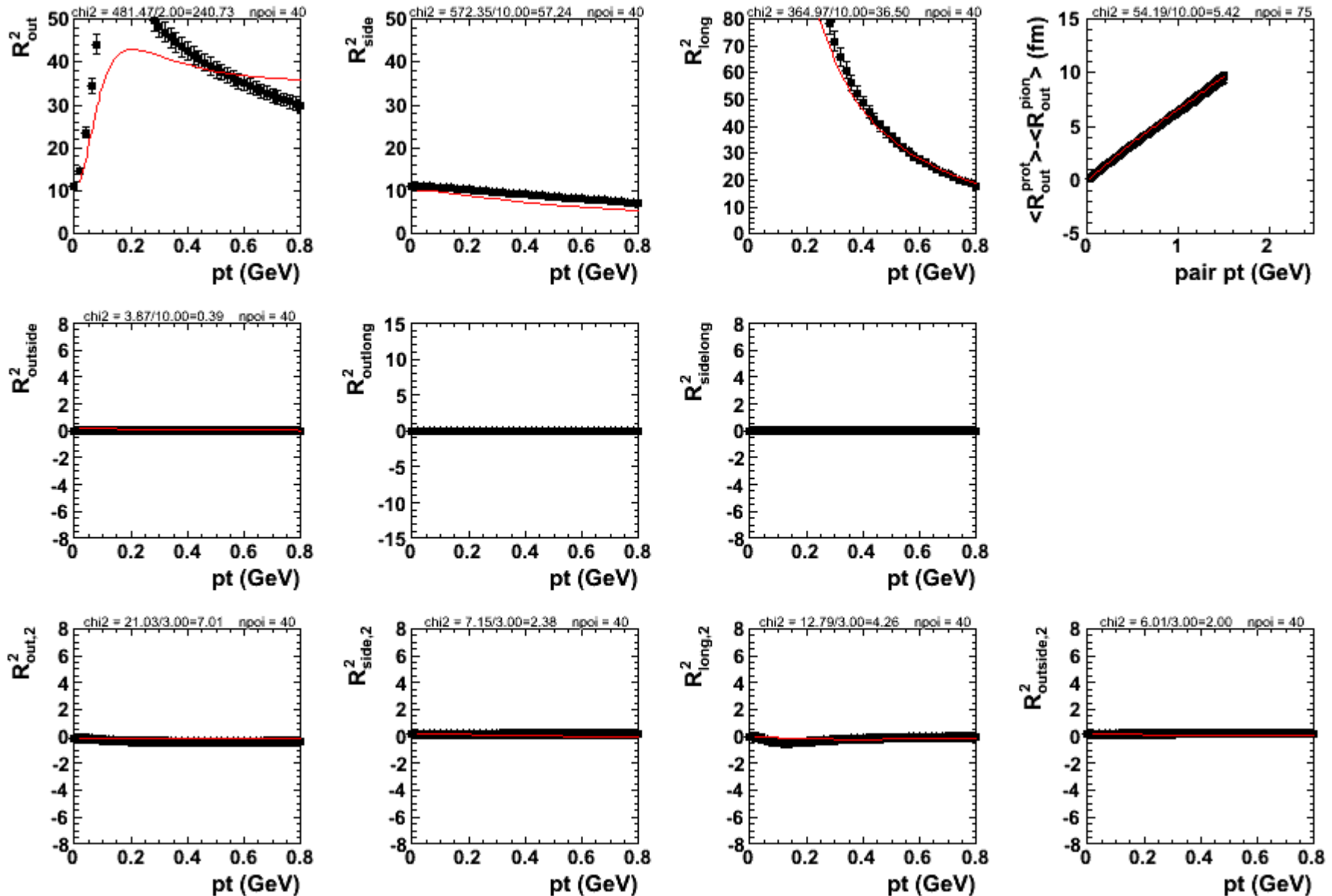
# blast as=0.3 (lines) and hydro 120 MeV (points)



other->fPim = 113.7  
 other->fKa0 = 16.43  
 other->fPhi = 0.842  
 blast->fT = 0.089  
 blast->fRho0 = 0.60  
 blast->fRho2 = 0.011  
 blast->fRx = 5.06  
 blast->fRy = 5.09  
 blast->fAs = 0.300  
 blast->fTau0 = 10.46  
 blast->fDtau = 5.98

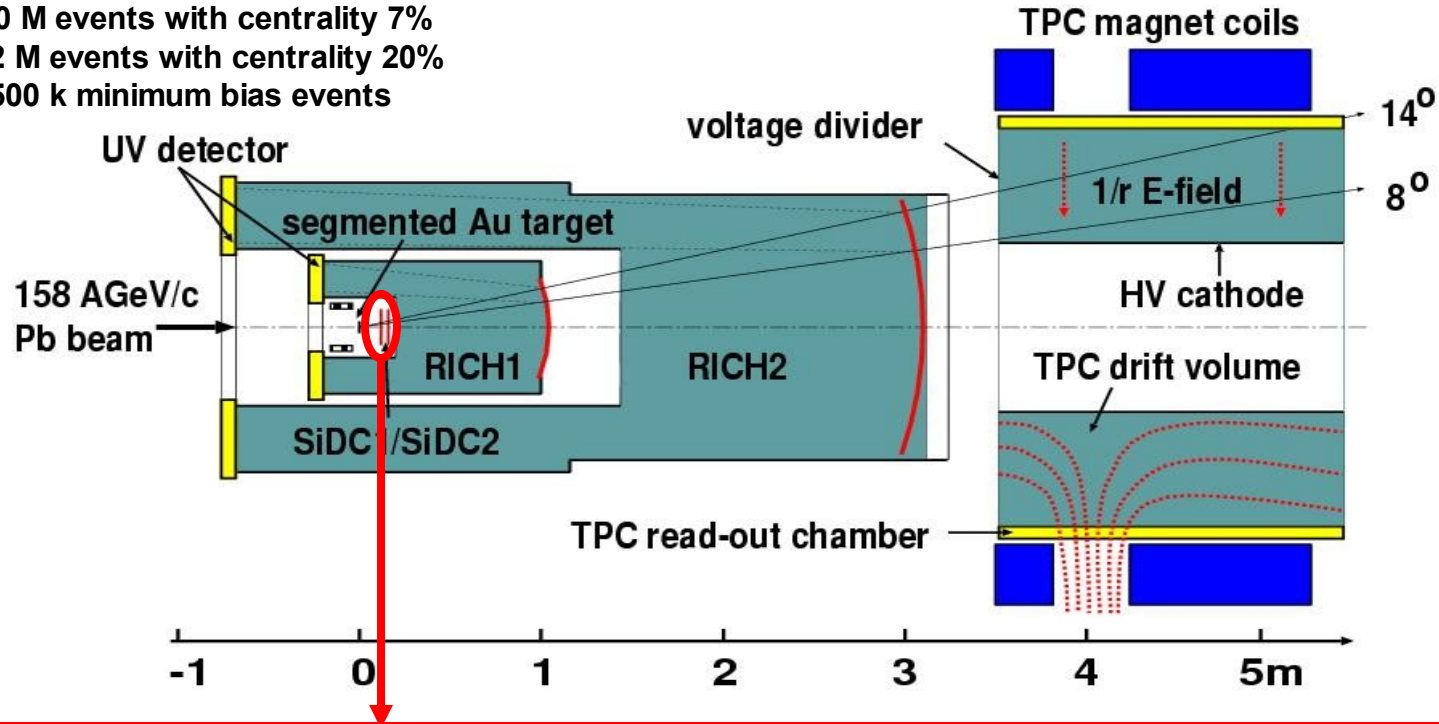


# blast as=0.3 (lines) and hydro 120 MeV (points)

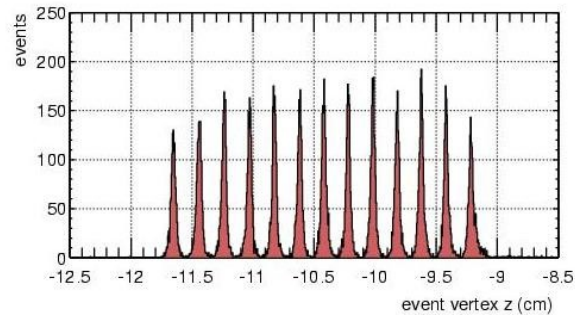
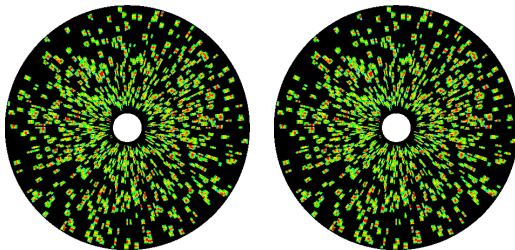


# setup with TPC: 1999 and 2000

run 2000: 30 M events with centrality 7%  
 2 M events with centrality 20%  
 500 k minimum bias events



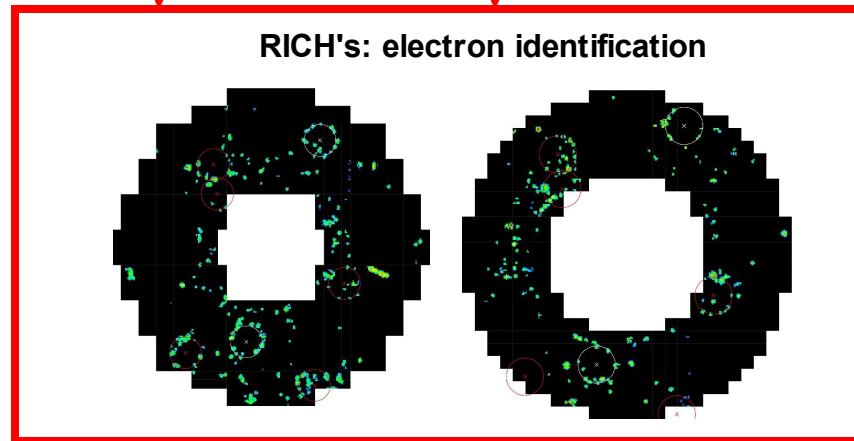
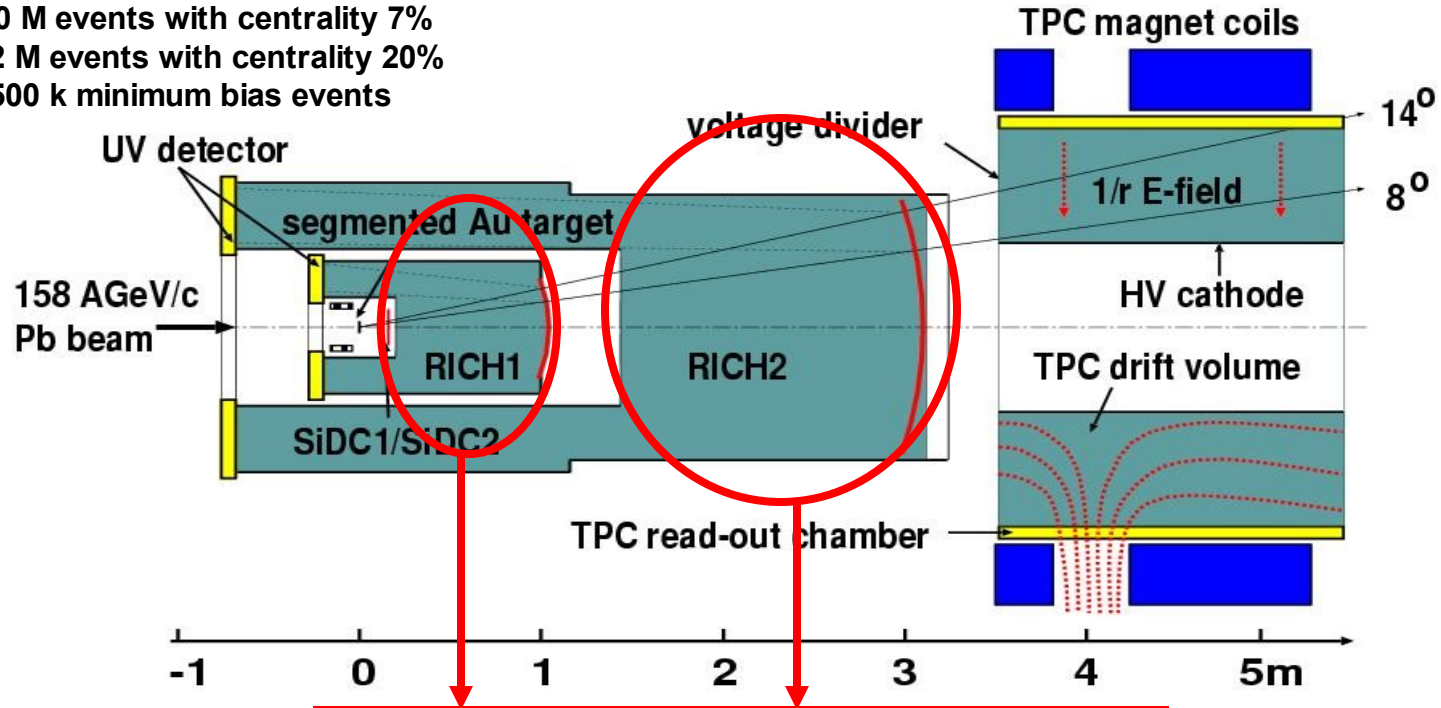
SD: event vertex, track vertex and angle



event  $\Delta z = 0.2$  mm  
 track  $\Delta\theta = 0.2$  mrad  
 $\Delta\phi = 2$  mrad

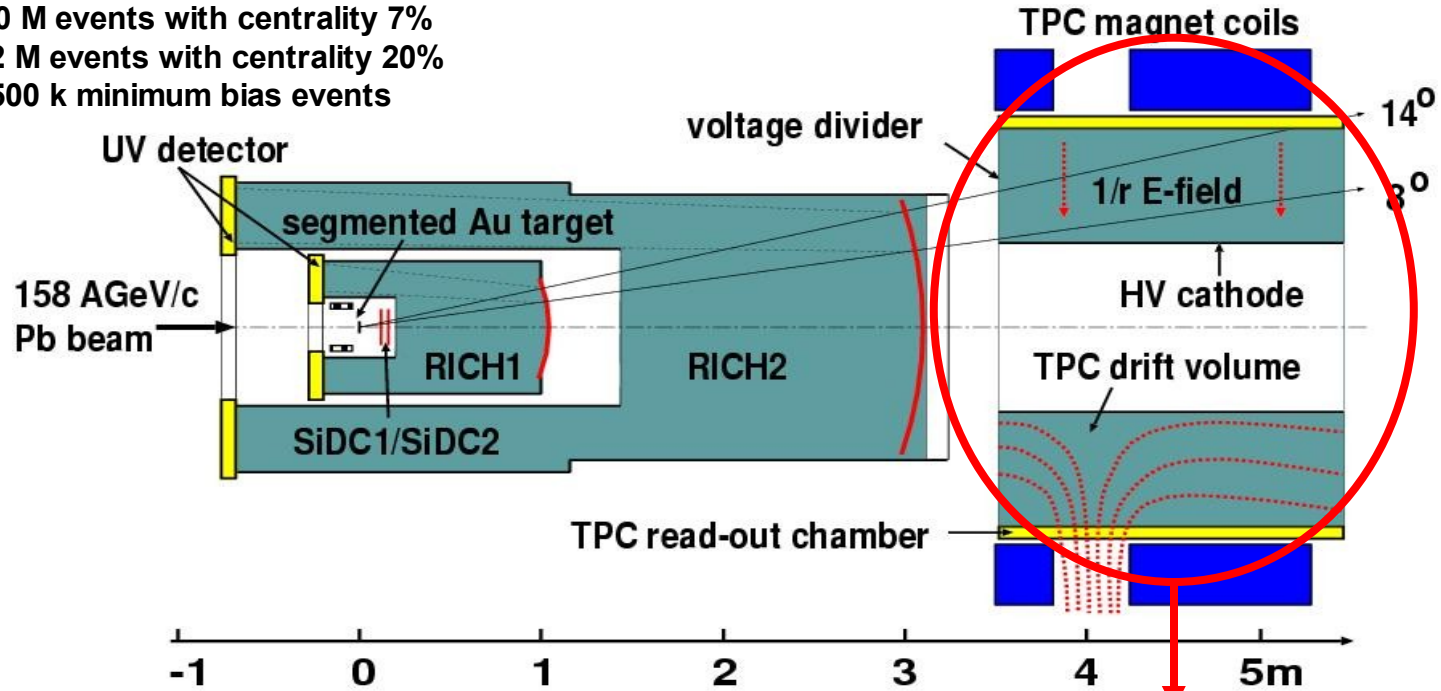
# setup with TPC: 1999 and 2000

run 2000: 30 M events with centrality 7%  
2 M events with centrality 20%  
500 k minimum bias events

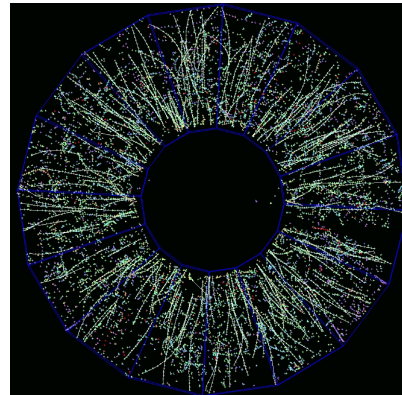


# setup with TPC: 1999 and 2000

run 2000: 30 M events with centrality 7%  
 2 M events with centrality 20%  
 500 k minimum bias events



radial drift TPC: momentum and energy loss

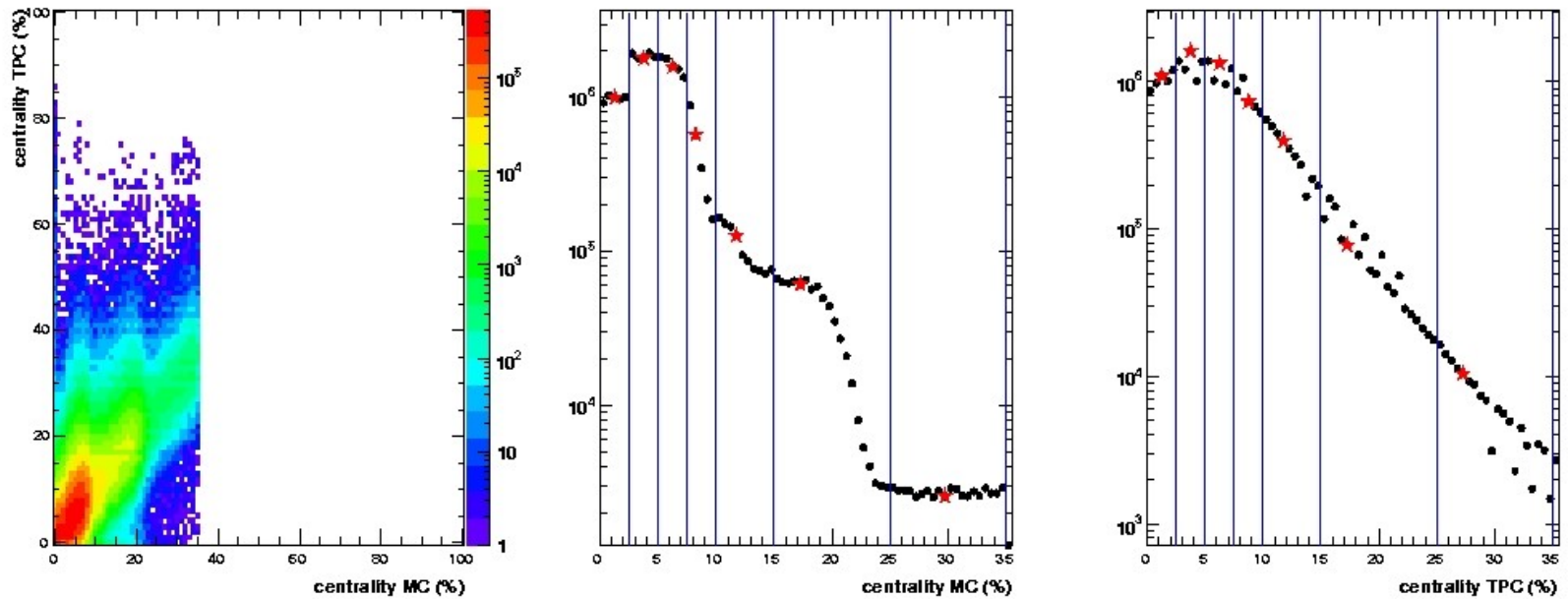


$$\Delta p/p = 2\% \oplus 1\% * p/\text{GeV}$$

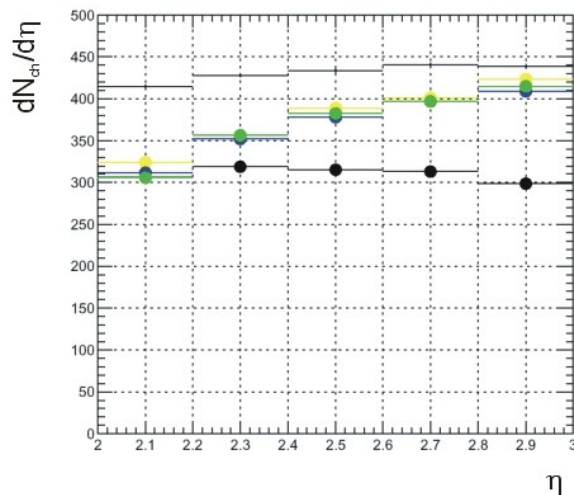
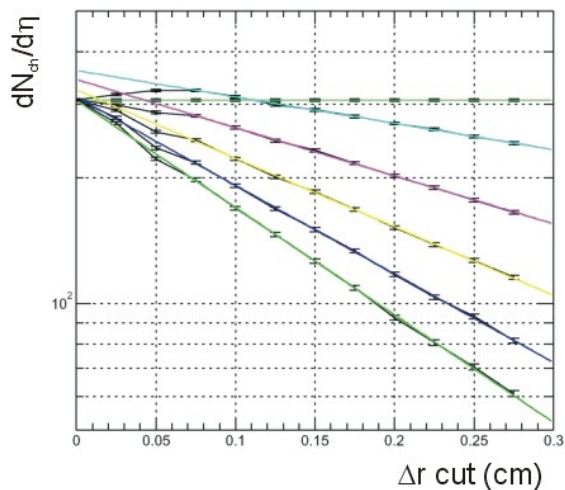
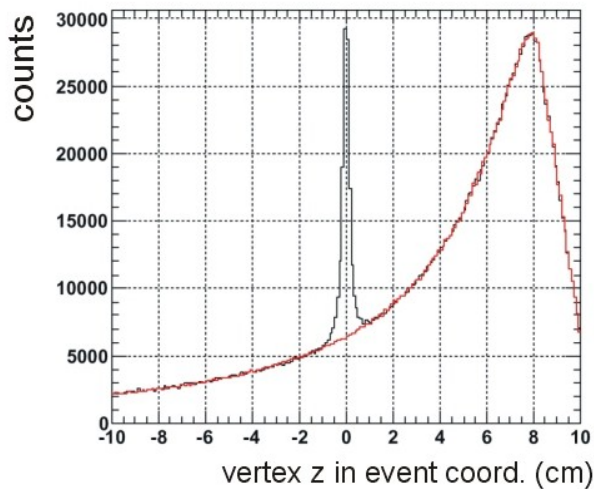
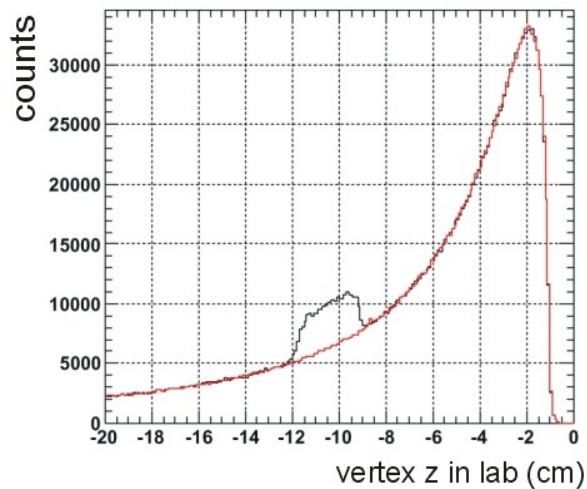
$$\Delta m/m = 3.8\% \text{ for } \phi$$

$$\Delta(dE/dx)/(dE/dx) = 10\%$$

# centrality of the analyzed data set

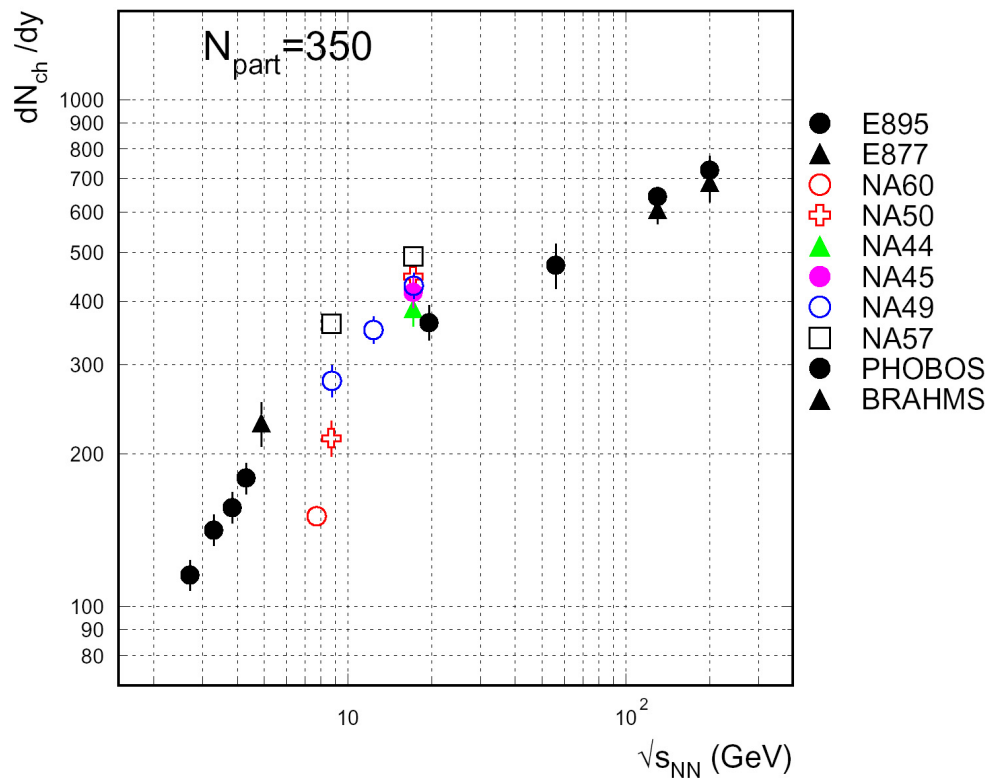
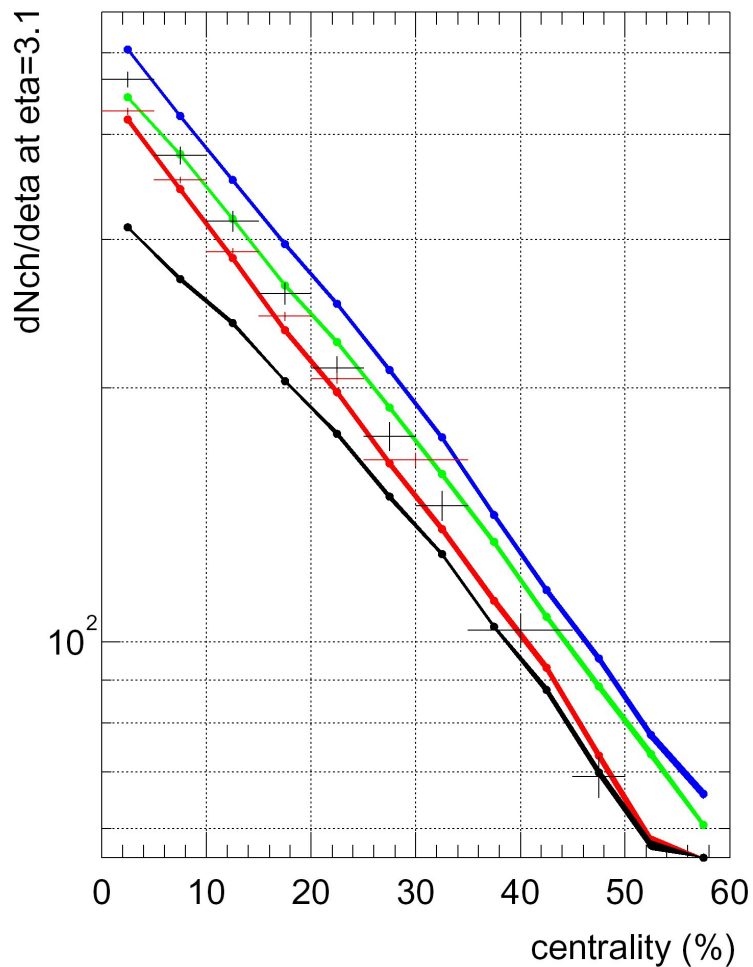


# Absolute multiplicity of charged particles





# Absolute multiplicity of charged particles



$dN_{ch}/dy = 1.025 dN_{ch}/d\eta$  applied at SPS  
 $dN_{ch}/dy = 1.1 dN_{ch}/d\eta$  applied at RHIC

# Fitting $R_{side}$ and $\Delta x$

$$R_{side}(p_{\perp}) = \frac{R_G}{\sqrt{1 + \frac{m_{\perp} \eta_f^2}{T}}}$$

$$m_{\perp} = \sqrt{m_{\pi} + \left(\frac{P_{\perp}}{2}\right)^2}$$

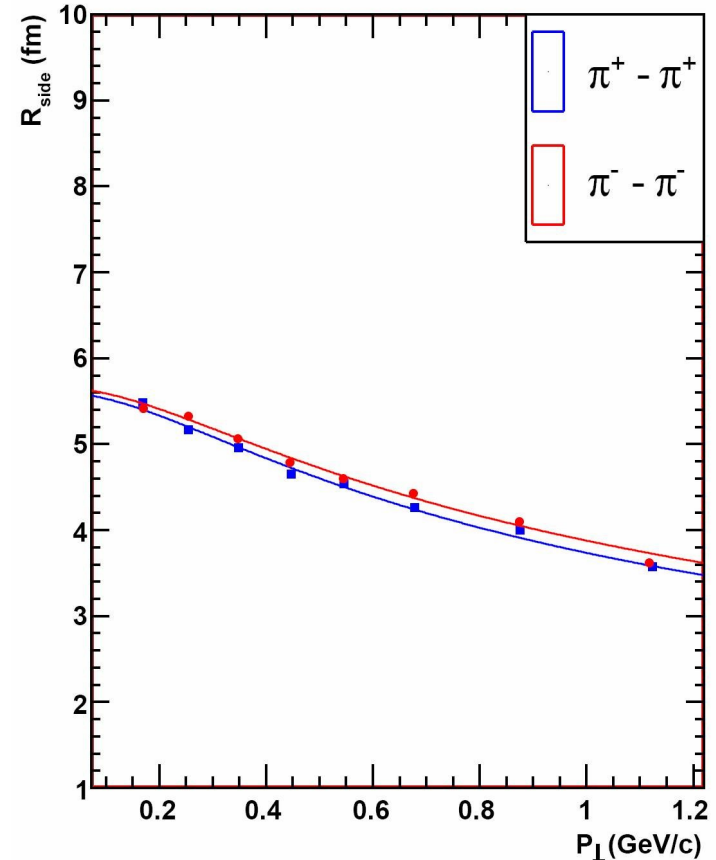
U. Heinz, many many papers

$$\langle \Delta x \rangle = \frac{R_G \beta_{\perp} \beta_0}{\beta_0^2 + \frac{T}{m_{\perp}}}$$

$$m_{\perp} = \sqrt{m_{\perp}^1 m_{\perp}^2}$$

$$\beta_{\perp} = \frac{1}{\sqrt{1 + \left(\frac{m_{\pi} + m_p}{P_{\perp}}\right)^2}}$$

$$\eta_f = \frac{1}{2} \log \frac{1 + \beta_0}{1 - \beta_0}$$



R. Lednicky, nucl-th/0305027, based on Akkelin, Sinyukov Z.Phys.C 72(1996)501

$R_{side}$  dominates the fit  
 $\Delta x$  agrees reasonably well  
 $\rightarrow$  all flow?