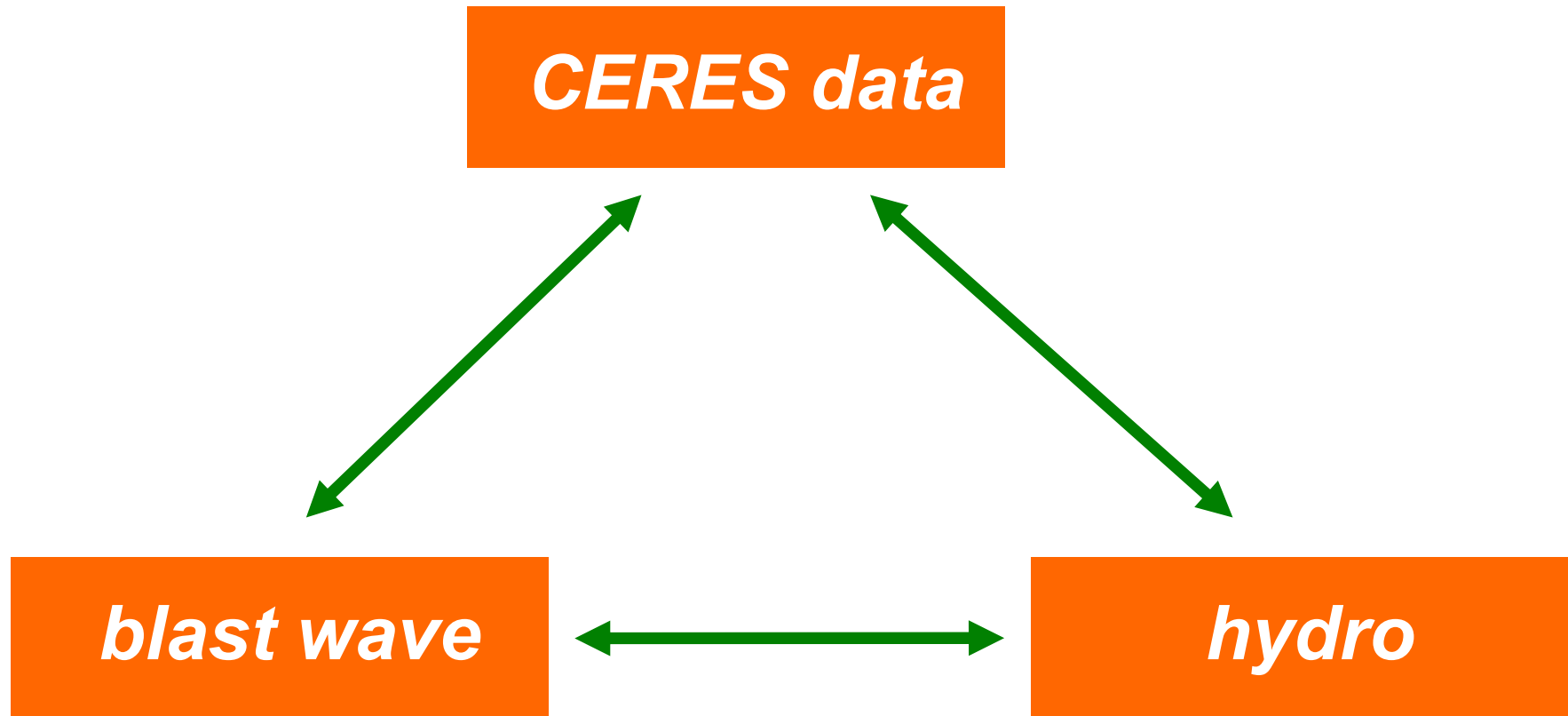


***Freeze-out characterization in  
Pb+Au collisions at 158 AGeVS***

***Dariusz Miśkowiec, GSI Darmstadt***



# CERES Collaboration

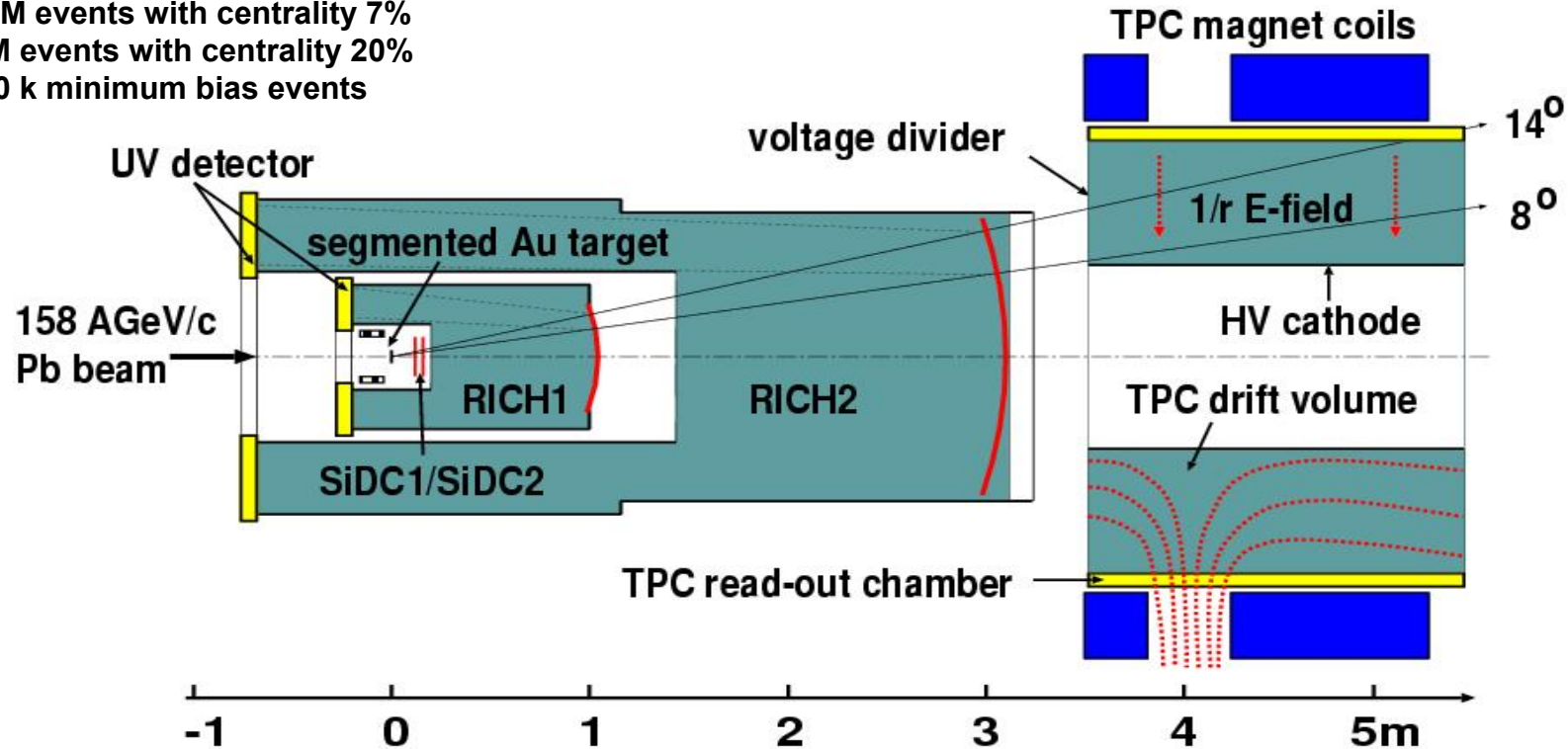
*D. Adamova, G. Agakichiev, **D. Antonczyk**, A. Andronic, H. Appelshäuser,  
V. Belaga, J. Bielcikova, P. Braun-Munzinger, O. Busch, A. Cherlin,  
S. Damjanovic, T. Dietel, L. Dietrich, A. Drees, S. Esumi, K. Filimonov,  
K. Fomenko, Z. Fraenkel, C. Garabatos, P. Glässel, G. Hering, J. Holeczek,  
M. Kalisky V. Kushpil, B. Lenkeit, W. Ludolphs, A. Maas, A. Marin,  
J. Milosevic, A. Milov, D. Miskowiec, R. Ortega, Yu. Panebrattsev,  
O. Petchenova, V. Petracek, A. Pfeiffer, M. Ploskon, S. Radomski, J. Rak,  
I. Ravinovich, P. Rehak, W. Schmitz, J. Schukraft, H. Sako, S. Shimansky,  
S. Sedykh, J. Stachel, M. Sumbera, H. Tilsner, I. Tserruya, G. Tsiledakis,  
T. Wienold, B. Windelband, J.P. Wessels, J.P. Wurm, W. Xie, S. Yurevich,  
V. Yurevich*

# CERES run history

1990	installation	
1991	completed	
1992	200 GeV S+Au	4M central 445 open pairs
1993	450 GeV p+Be 450 GeV p+Au	10M pairs 3M pairs
1995	160 GeV Pb+Au	10M central
1996	160 GeV Pb+Au	50M central 2700 open pairs
1997	upgrade	
1998	upgrade	
1999	40 GeV Pb+Au	10M central 185 open pairs
2000	80 GeV Pb+Au	1M central
	160 GeV Pb+Au	30M central

# CERES setup in 2000

run 2000: 30 M events with centrality 7%  
2 M events with centrality 20%  
500 k minimum bias events



**CERES built and upgraded for leptons; but also good for...  
pt spectra, elliptic flow, two-particle correlations of hadrons**

# blast wave model

Retière, Lisa, PRC 70(2004)044907

*analytic hydro-inspired 8-d emission function*

$$S(x, K) = m_T \cosh(\eta - Y) \Omega(r, \phi_S) e^{\frac{-(\tau - \tau_0)^2}{2\Delta\tau^2}} \frac{1}{e^{K \cdot u/T} \pm 1}$$

**with the space profile**

$$\Omega(r, \phi_S) = \Omega(\tilde{r}) = \frac{1}{1 + e^{(\tilde{r}-1)/a}}$$

**and the normalized elliptic radius**

$$\tilde{r}(r, \phi_S) = \sqrt{\frac{(r \cos(\phi_S))^2}{R_x^2} + \frac{(r \sin(\phi_S))^2}{R_y^2}}$$

**and the flow four-velocity**

$$u = u_\mu(x, \rho_0, \rho_2)$$

# blast wave model

analytic hydro-inspired 8-d emission function

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and the flow four-velocity

$$u = u_\mu(\mathbf{x}, \rho_0, \rho_2)$$

**function of four  
space-time  
coordinates**

# blast wave model

analytic hydro-inspired 8-d emission function

$$S(x, K) = m_T \cosh(\eta - Y) \Omega(r, \phi_S) e^{\frac{-(\tau - \tau_0)^2}{2\Delta\tau^2}} \frac{1}{e^{K \cdot u/T} \pm 1}$$

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and the flow four-velocity

$$u = u_\mu(x, \rho_0, \rho_2)$$

**function of four  
momentum  
components**



# blast wave model

analytic hydro-inspired 8-d emission function

$$S(x, K) = m_T \cosh(\eta - Y) \Omega(r, \phi_S) e^{-\frac{(\tau - \tau_0)^2}{2\Delta\tau^2}} \frac{1}{e^{K \cdot u} T \pm 1}$$

with the space profile

$$\Omega(r, \phi_S) = \Omega(\tilde{r}) = \frac{1}{1 + e^{(\tilde{r}-1)/a}}$$

and the normalized elliptic radius

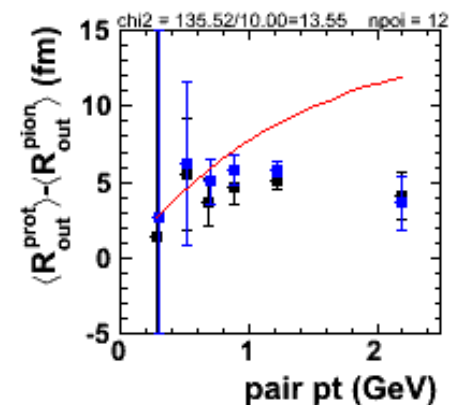
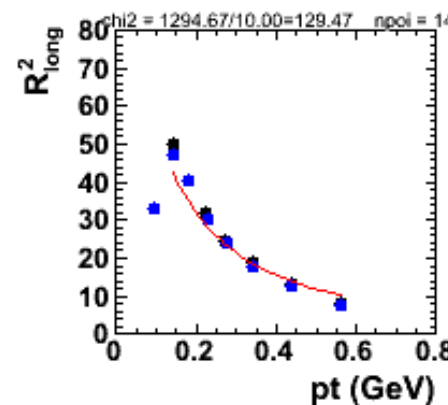
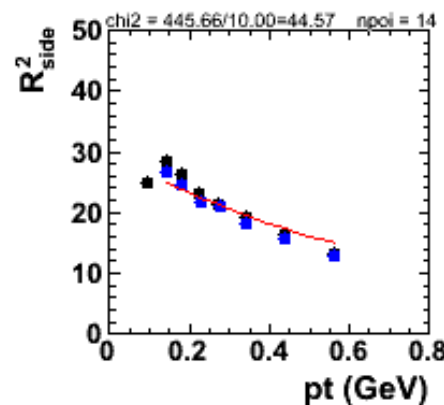
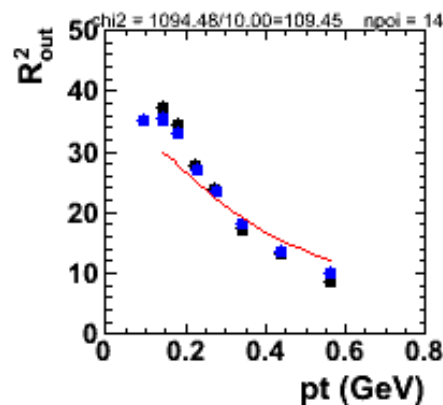
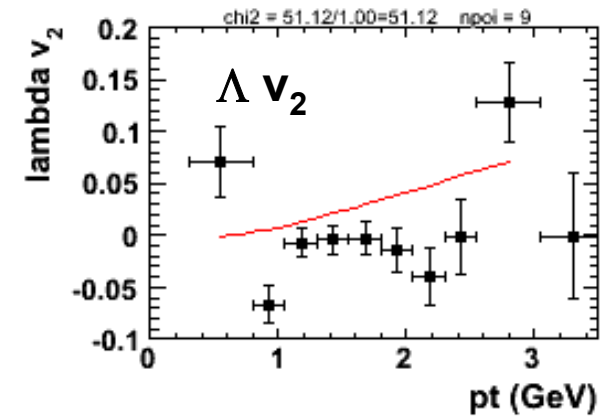
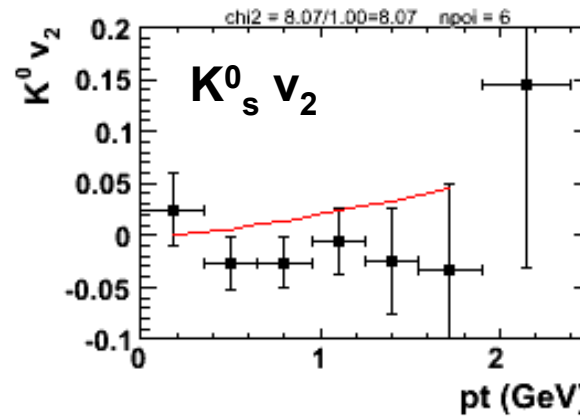
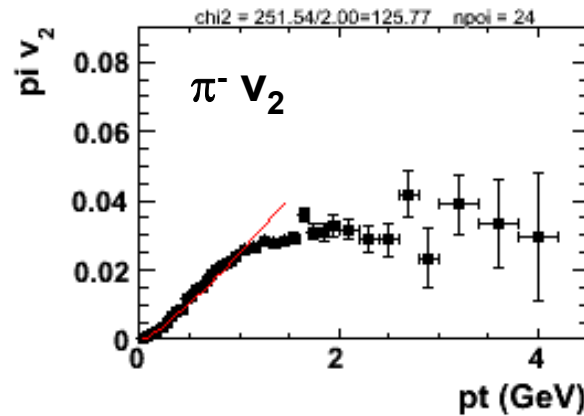
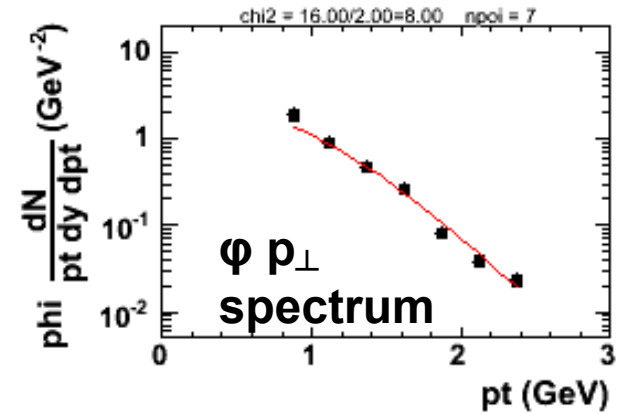
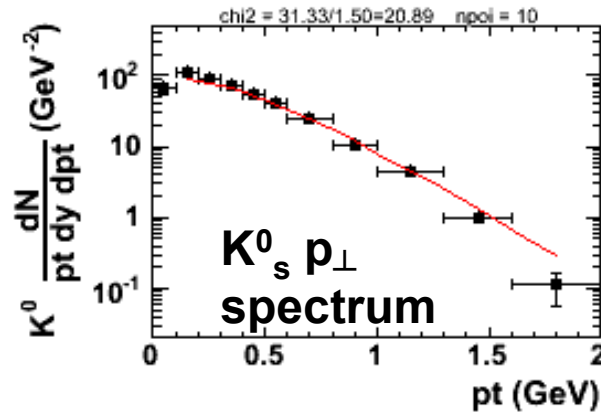
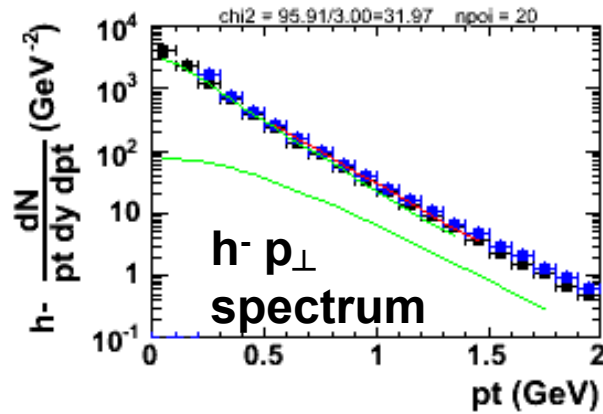
$$\tilde{r}(r, \phi_S) = \sqrt{\frac{(r \cos(\phi_S))^2}{R_x^2} + \frac{(r \sin(\phi_S))^2}{R_y^2}}$$

and the flow four-velocity

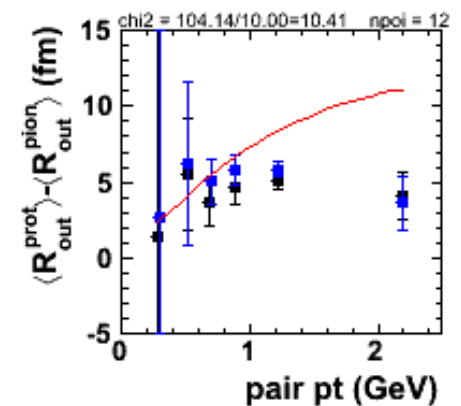
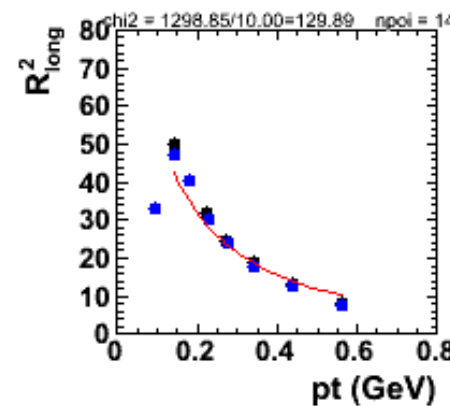
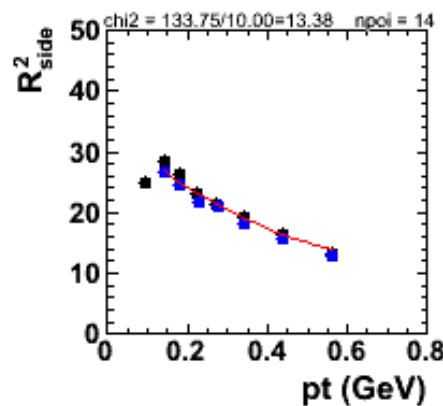
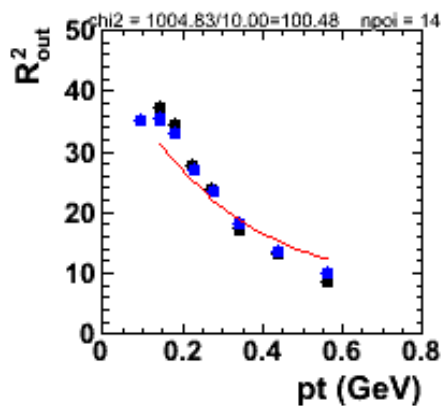
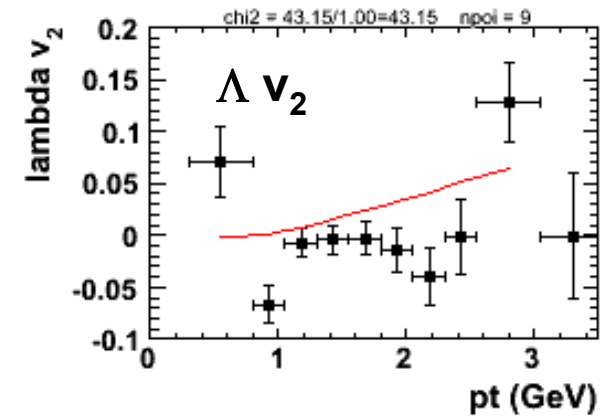
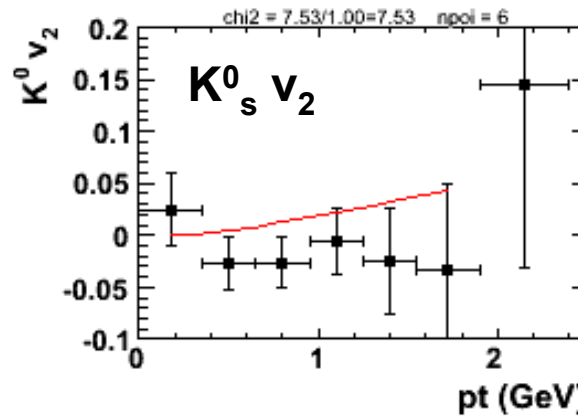
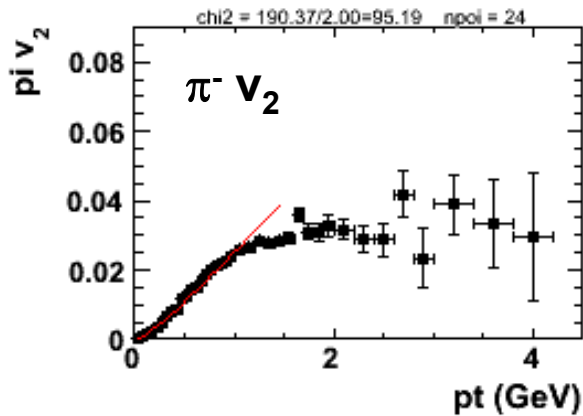
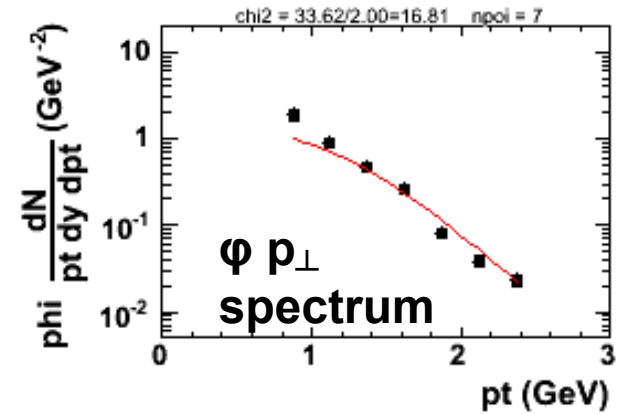
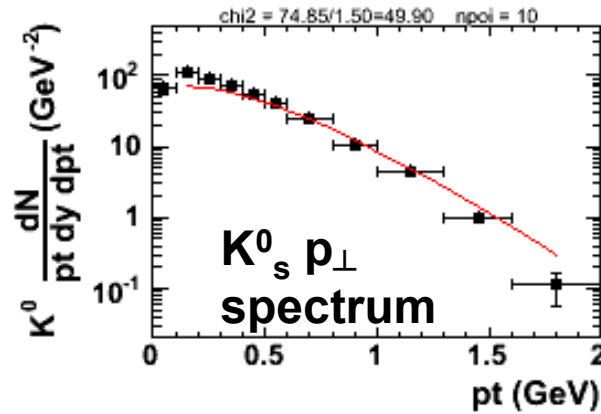
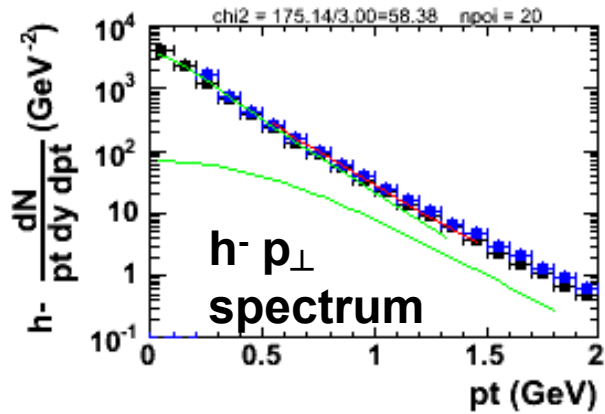
$$u = u_\mu(x, \rho_0, \rho_2)$$

with eight  
parameters

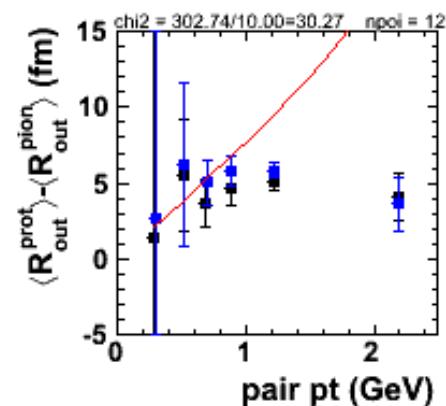
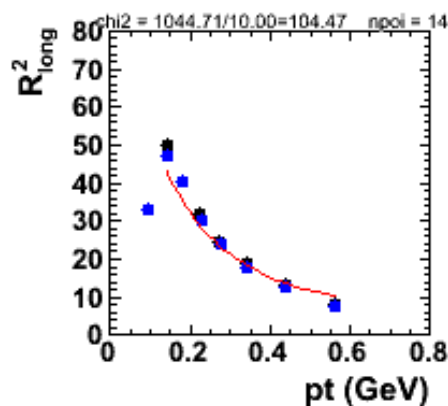
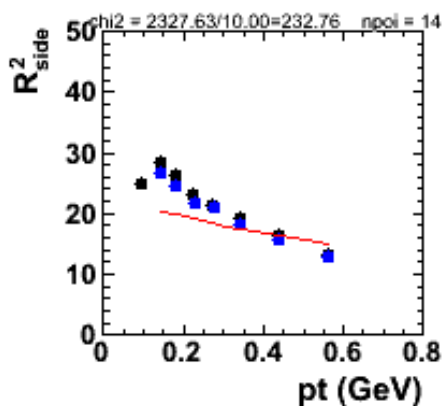
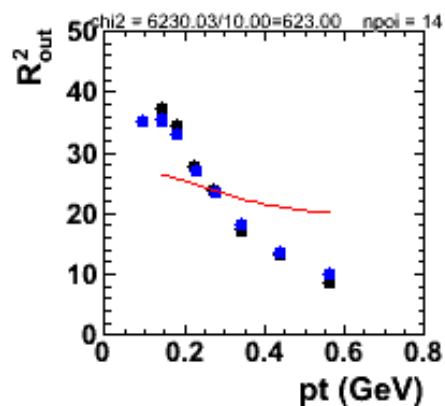
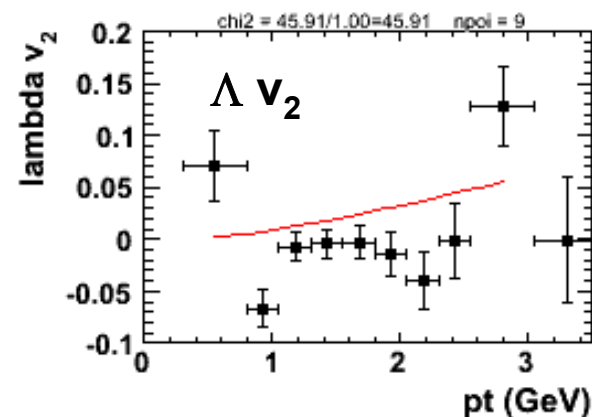
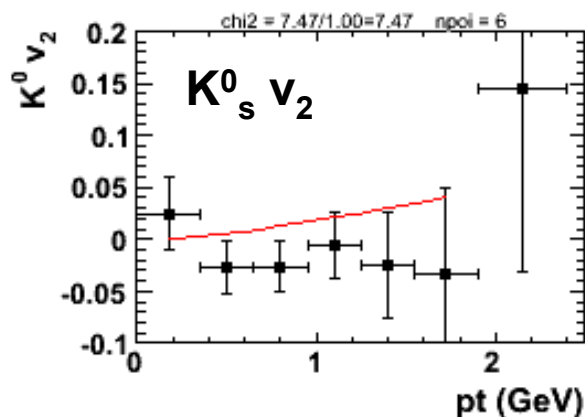
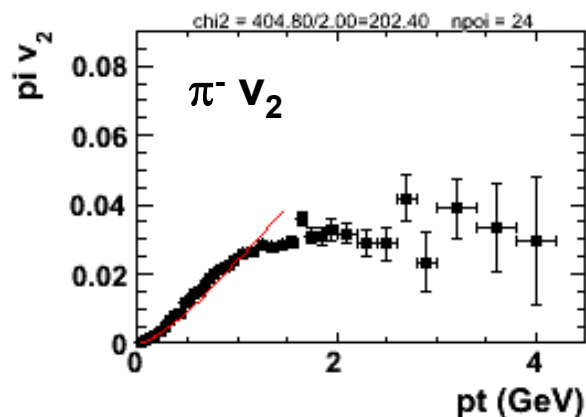
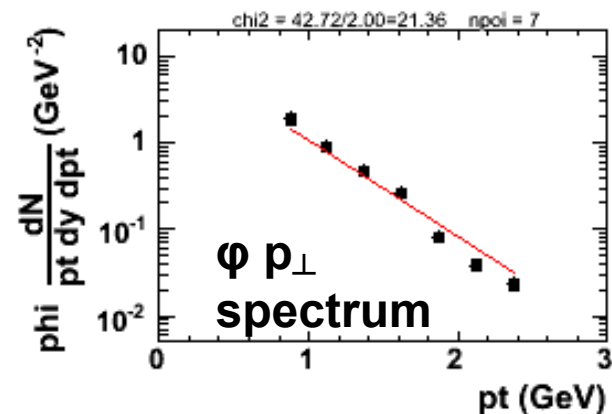
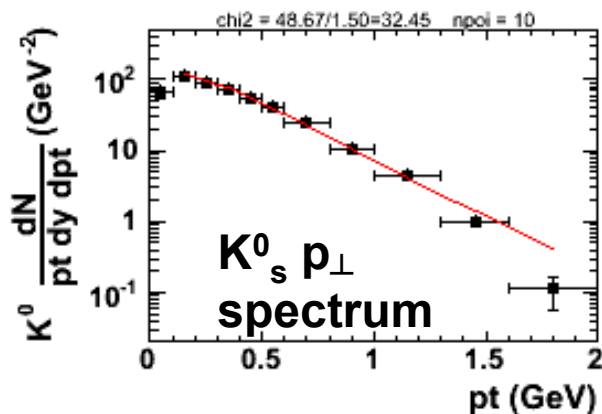
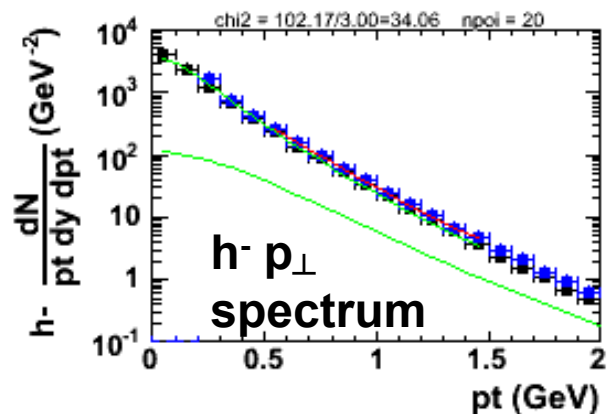
# CERES (points) and blast $T=100$ MeV (lines)



# CERES (points) and blast $T=80$ MeV (lines)



# CERES (points) and blast $T=100$ MeV $as=0.3$ (lines)



# hydro

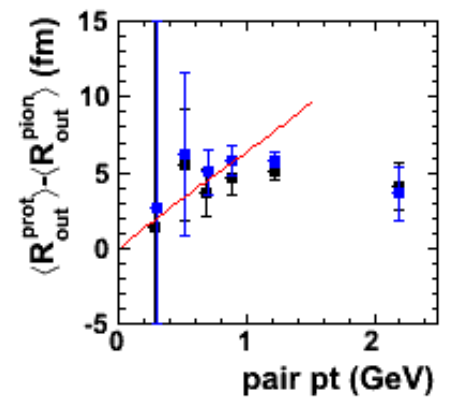
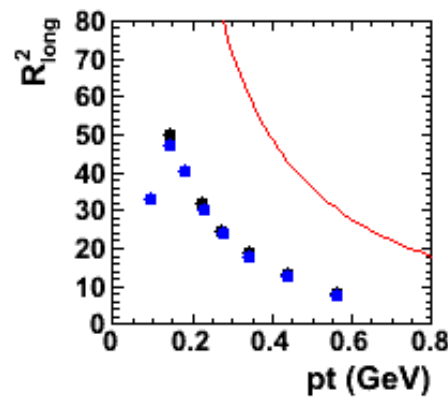
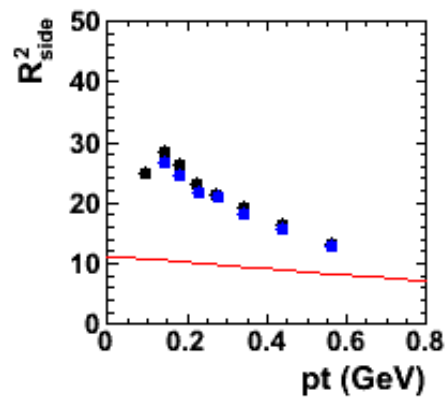
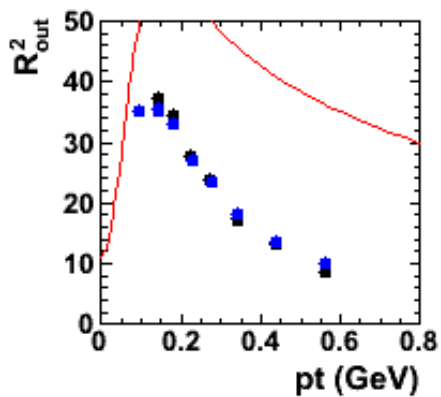
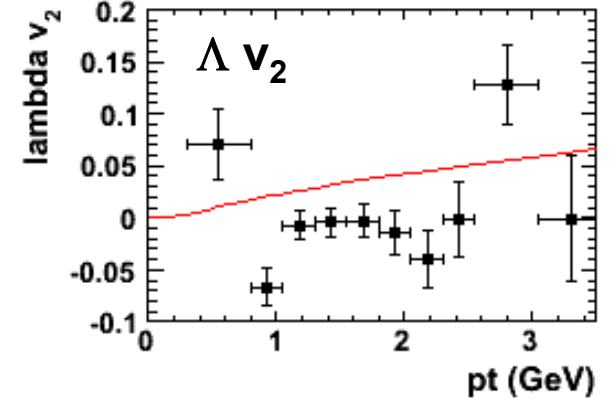
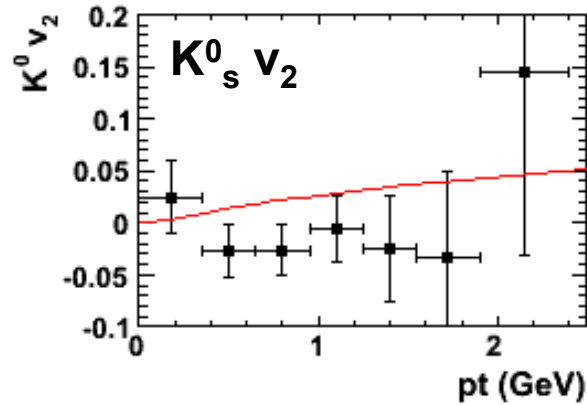
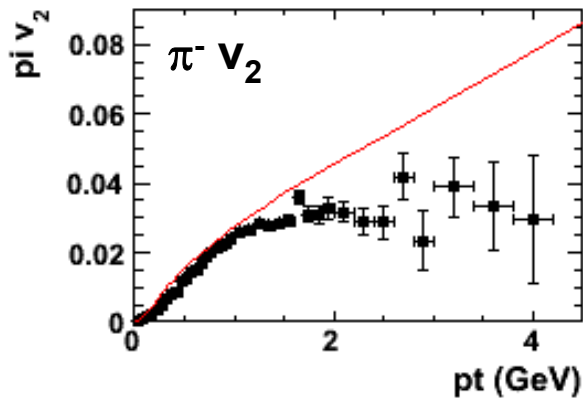
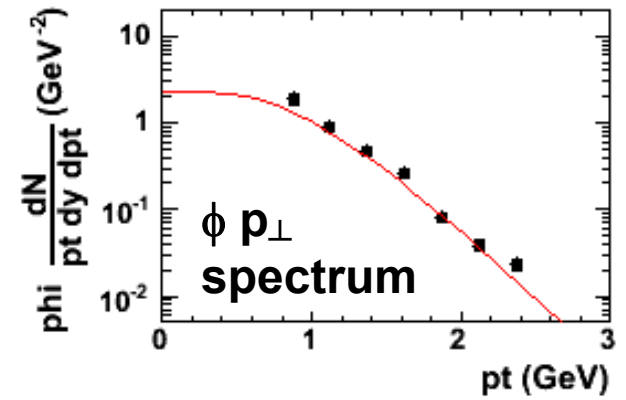
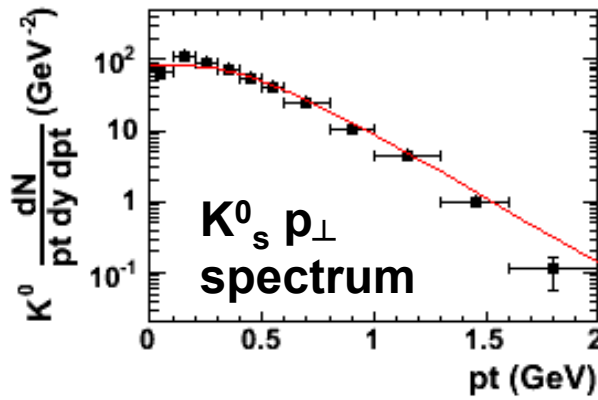
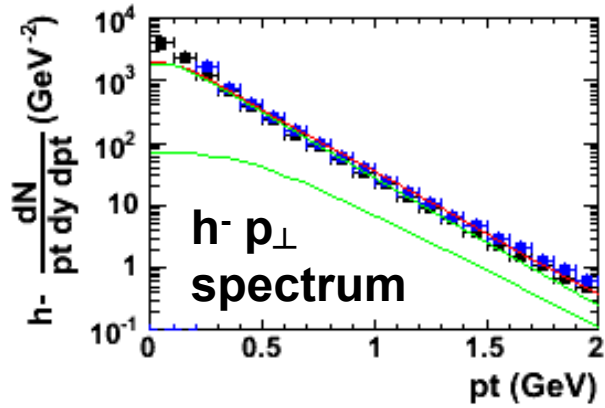
Pasi Huovinen

- 🌐 **hydrodynamical model, see e.g. nucl-th/0305064**
- 🌐 **freeze-out at a fixed energy density (similar to fixed temp)**
- 🌐 **dedicated calculation of Au+Pb at 158 A GeV,  $b=2.6$  fm**

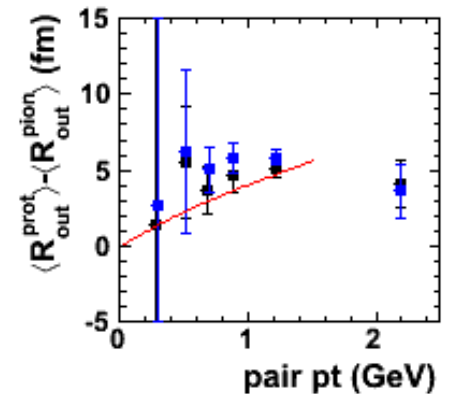
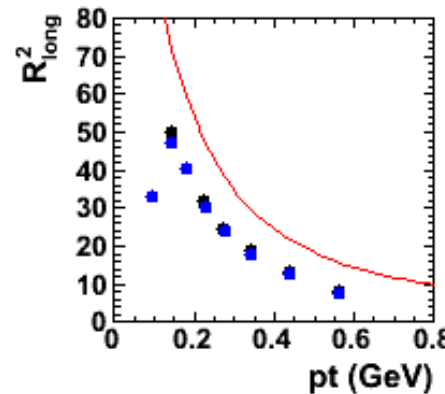
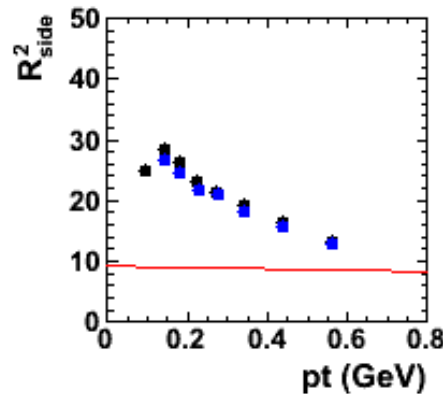
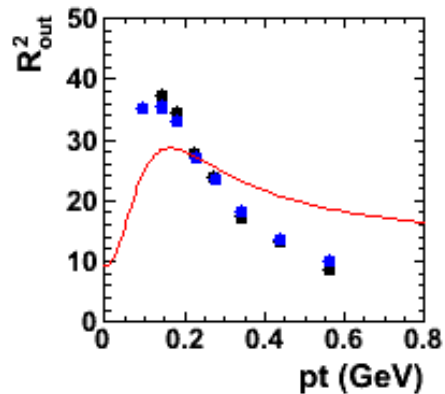
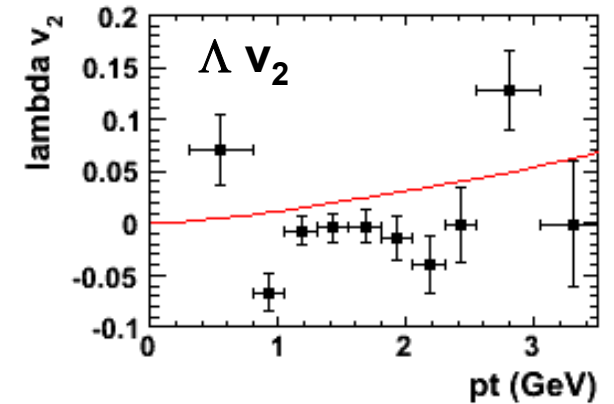
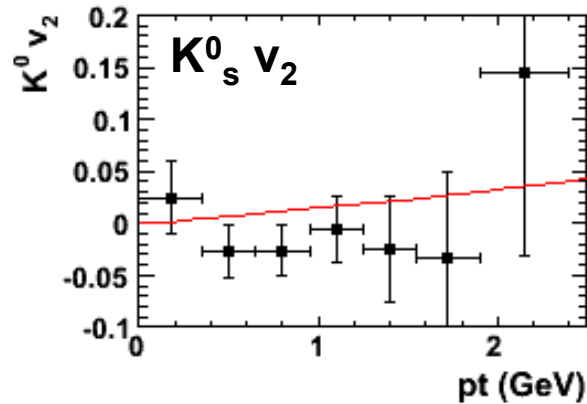
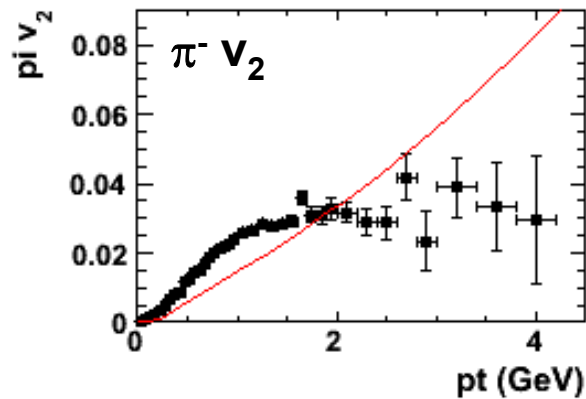
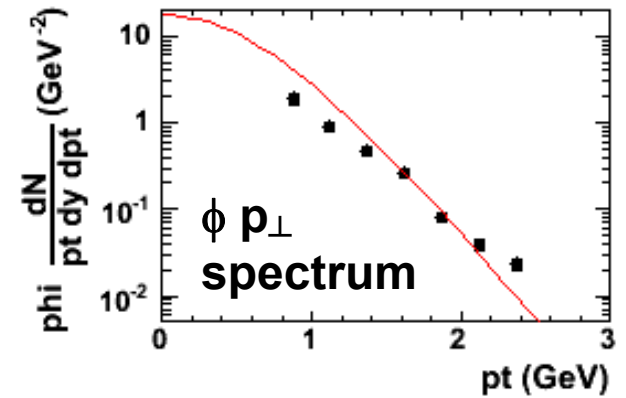
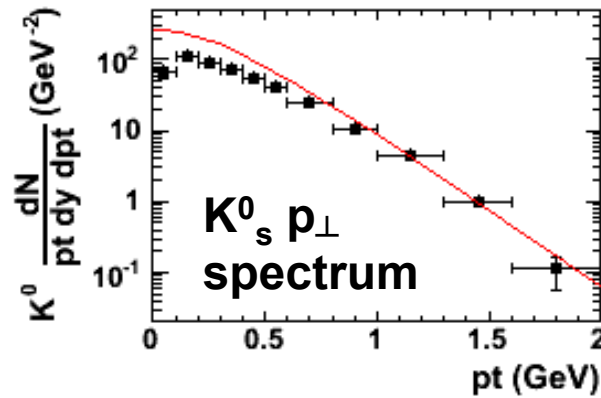
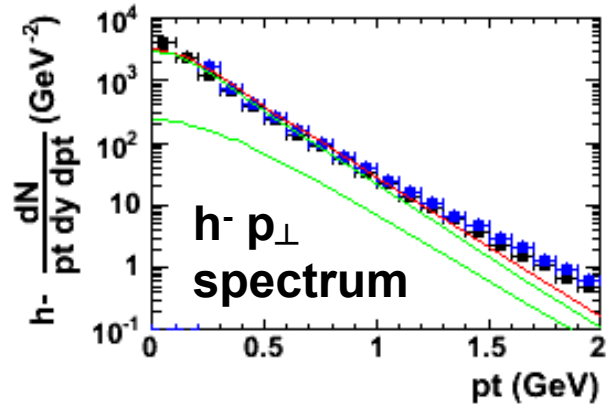
**two sets of results:**

- 🌐  **$T=160$  MeV (like at chemical freeze-out)**
- 🌐  **$T=120$  MeV (like at kinetic freeze-out)**

# CERES (points) and hydro $T=120$ MeV (lines)



# CERES (points) and hydro $T=160$ MeV (lines)



# *puzzle*

hydro

~~RHIC~~

HBT

puzzle

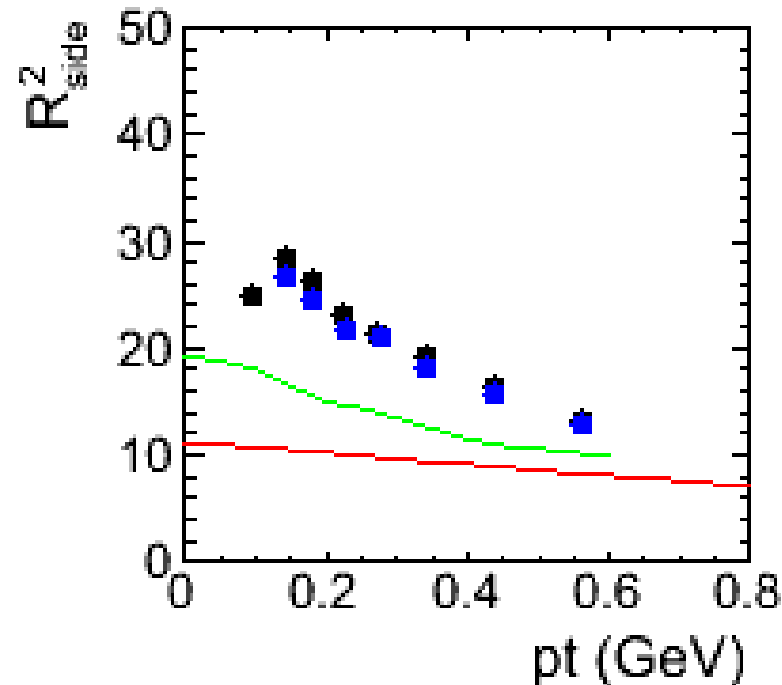
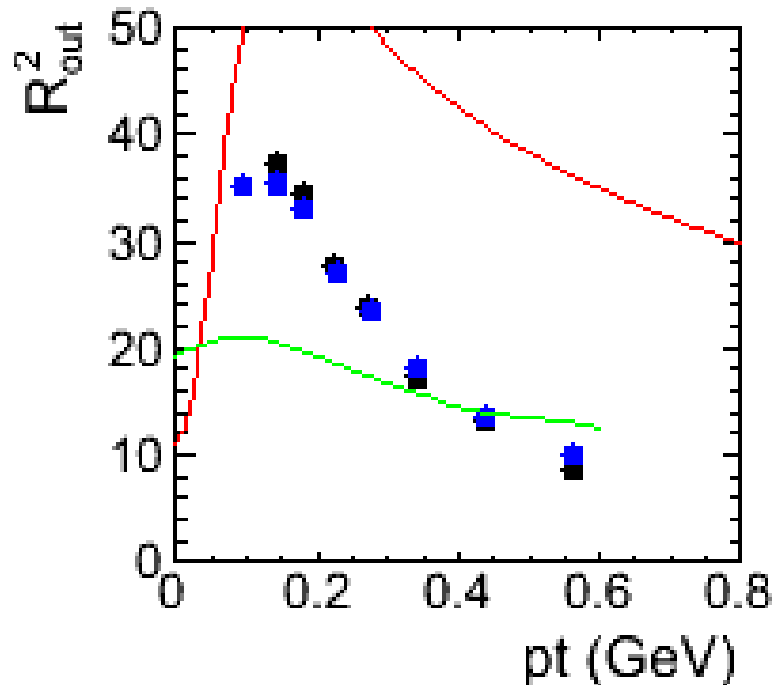


# try another flavour of hydro

black and blue points: CERES data

red line: present day hydro (Pasi Huovinen)

green line: old days hydro (Bernd Schlei)



*Ornik, Plümer, Schlei, Strottman, Weiner PRC 54(1996)1381, Pb+Pb at 160A GeV; rapidity and centrality not matched to CERES data so detailed comparison not possible; but, in any case...*

***R<sub>out</sub>/R<sub>side</sub> totally different from the present hydro***

*part of the puzzle?*

**hydro** **≠** **hydro**

# *room for improvement in the present hydro?*

***Use blast to understand what is "wrong" in hydro:***

🌐 ***blast is "hydro inspired" and has 8 free parameters***

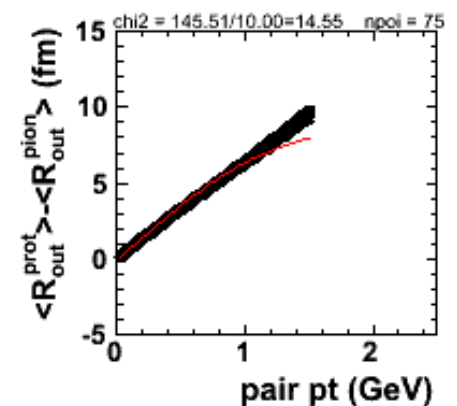
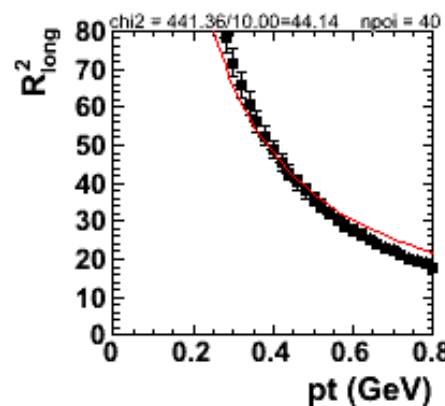
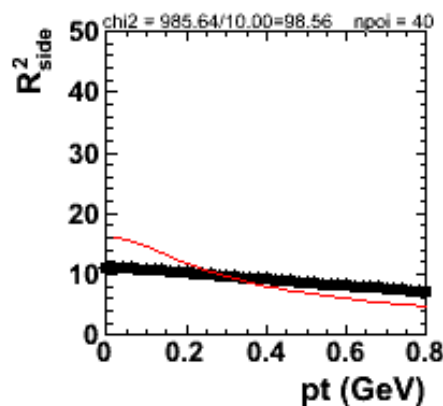
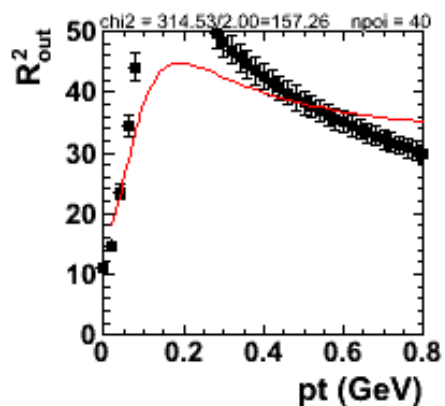
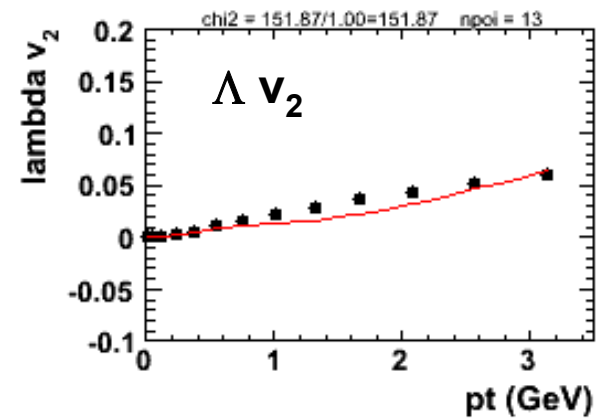
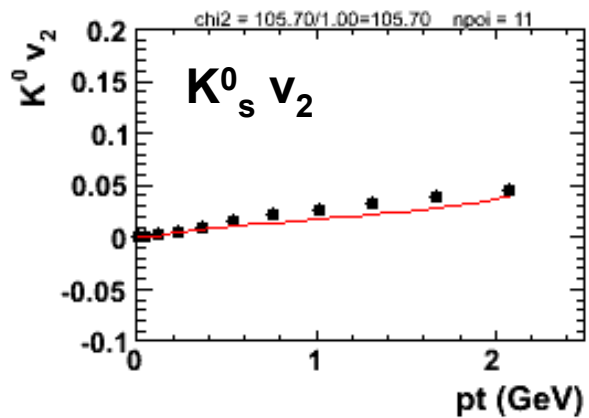
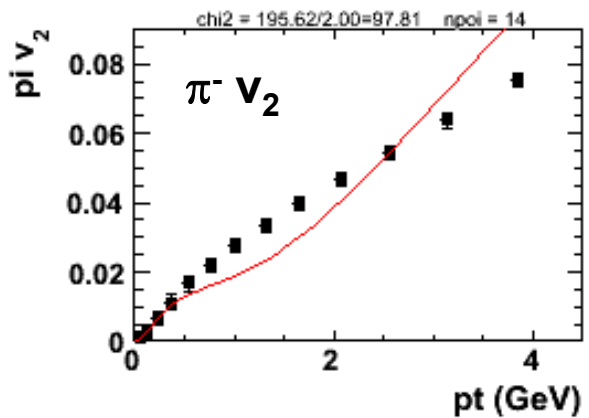
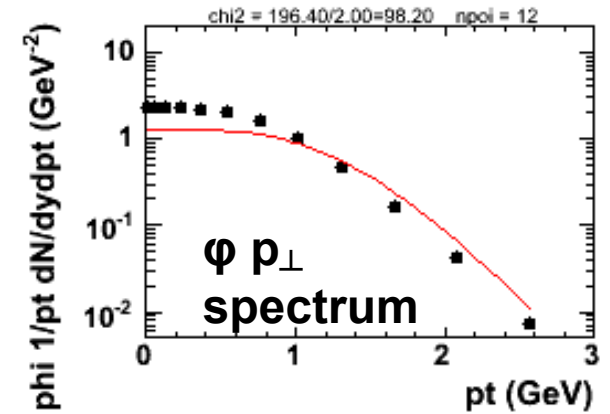
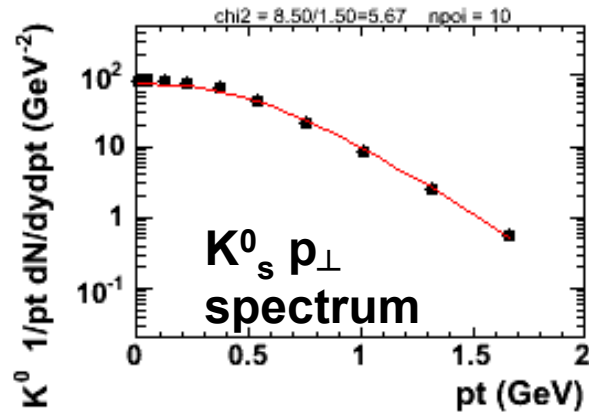
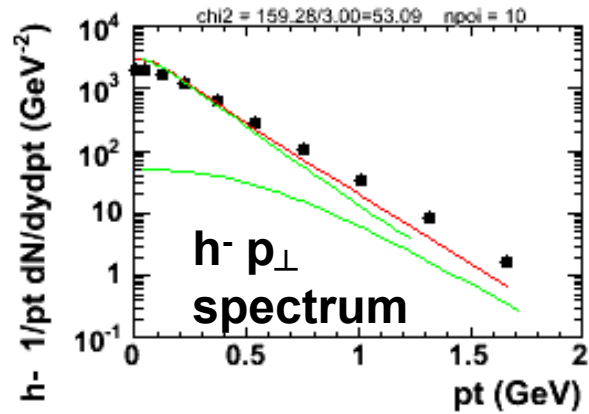
***→ hydro source must be a special case of blast source***

🌐 ***fit CERES by blast and fit hydro by blast and compare the resulting parameters***

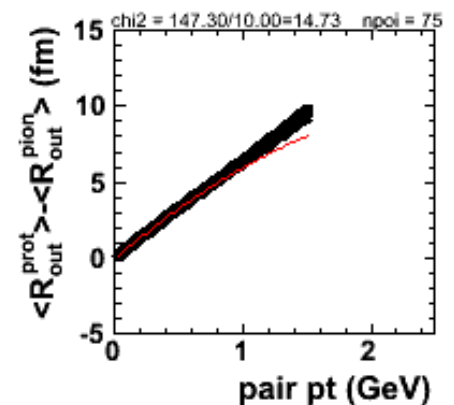
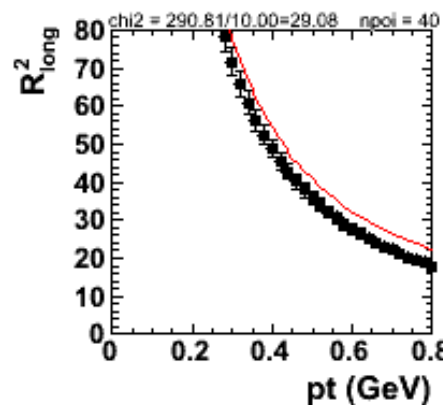
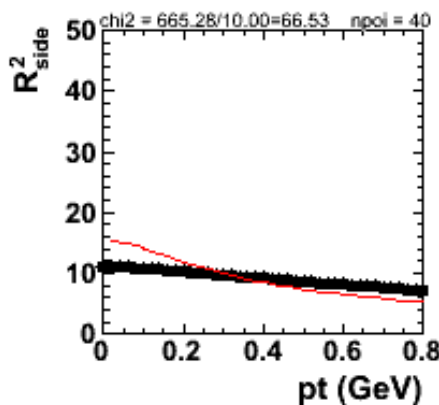
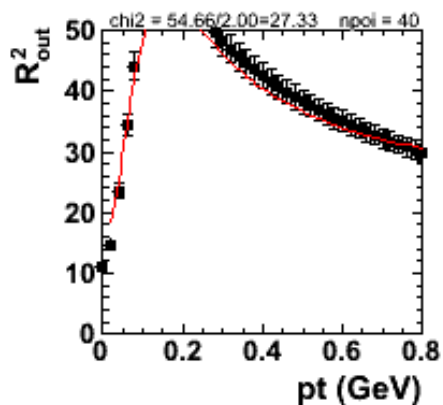
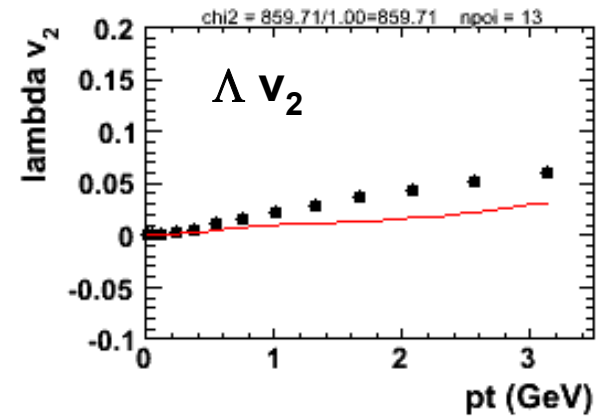
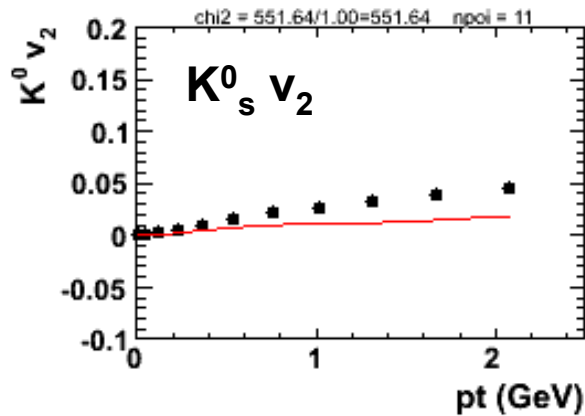
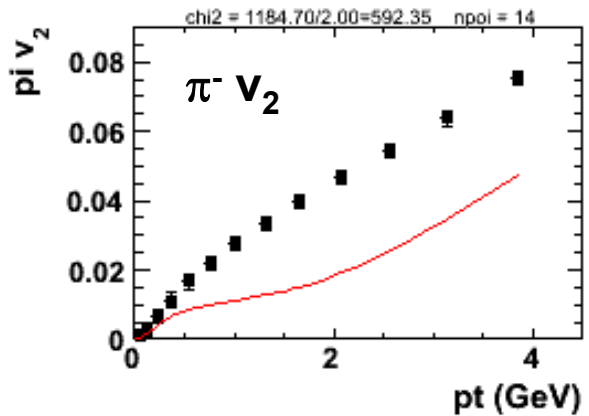
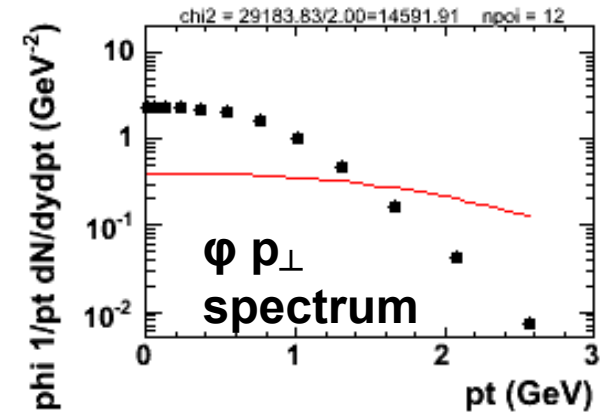
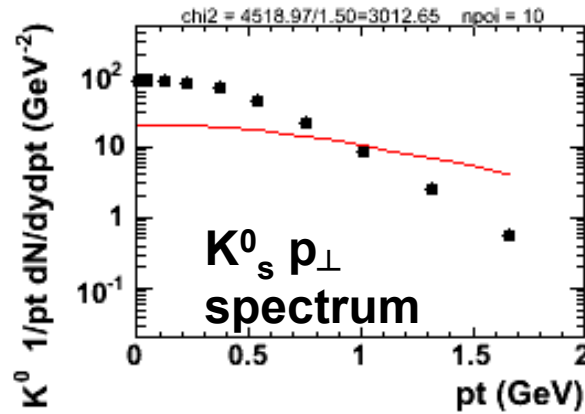
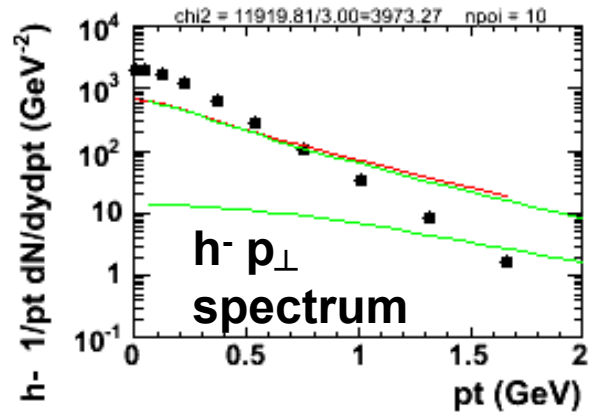
🌐 ***identify THE parameter which is different***

***→ this is what needs to be fixed in hydro***

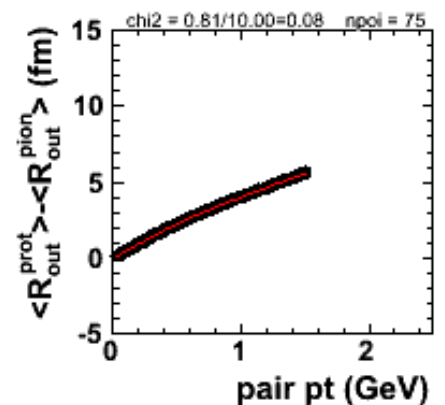
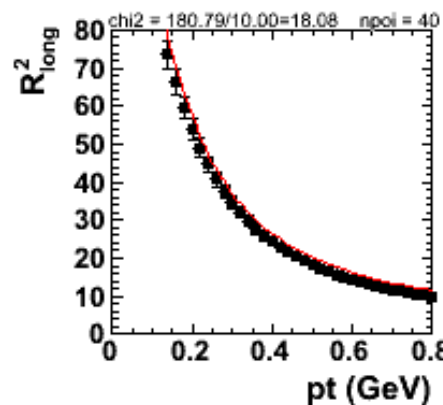
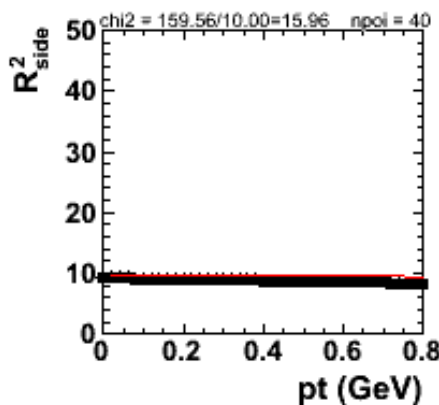
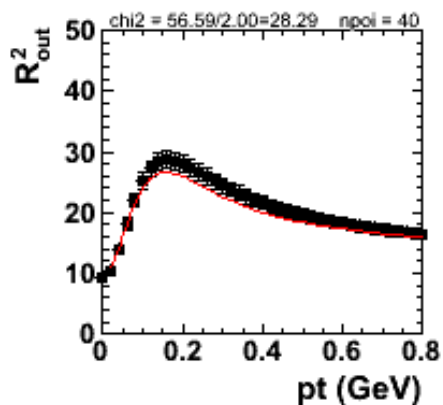
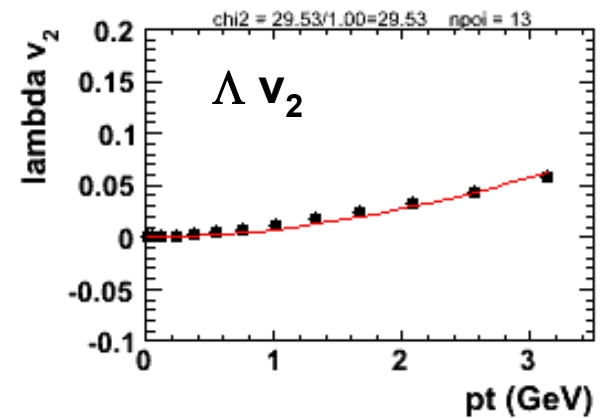
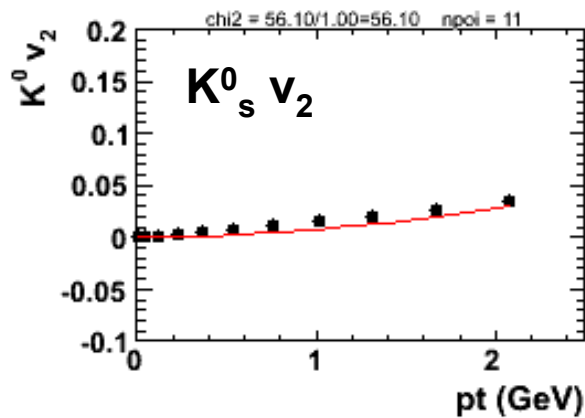
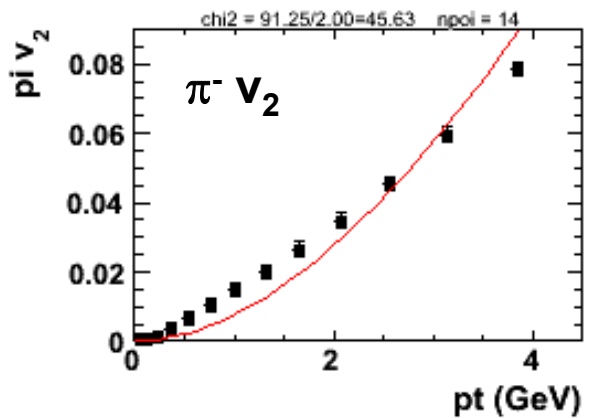
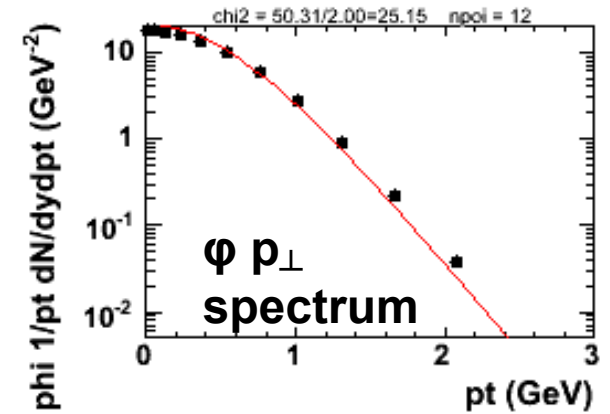
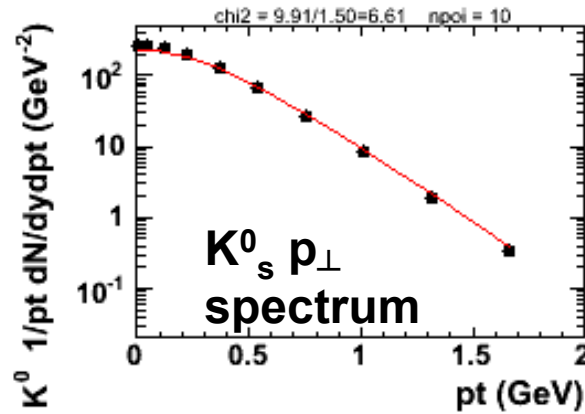
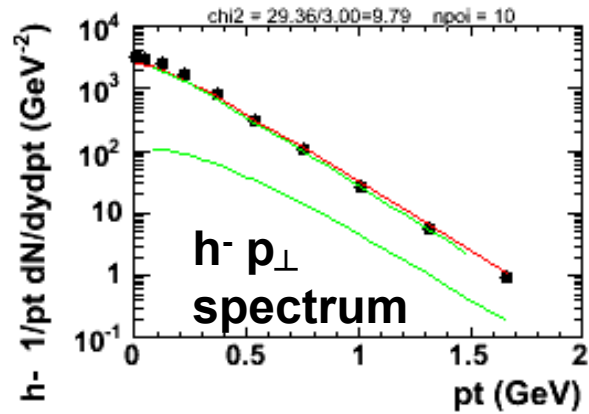
# hydro 120 MeV (points) and blast (lines)



# hydro 120 MeV (points) and blast, fit only HBT!



# hydro 160 MeV (points) and blast (lines)



# *blast vs. hydro*

*Use blast to understand what is wrong in hydro:*

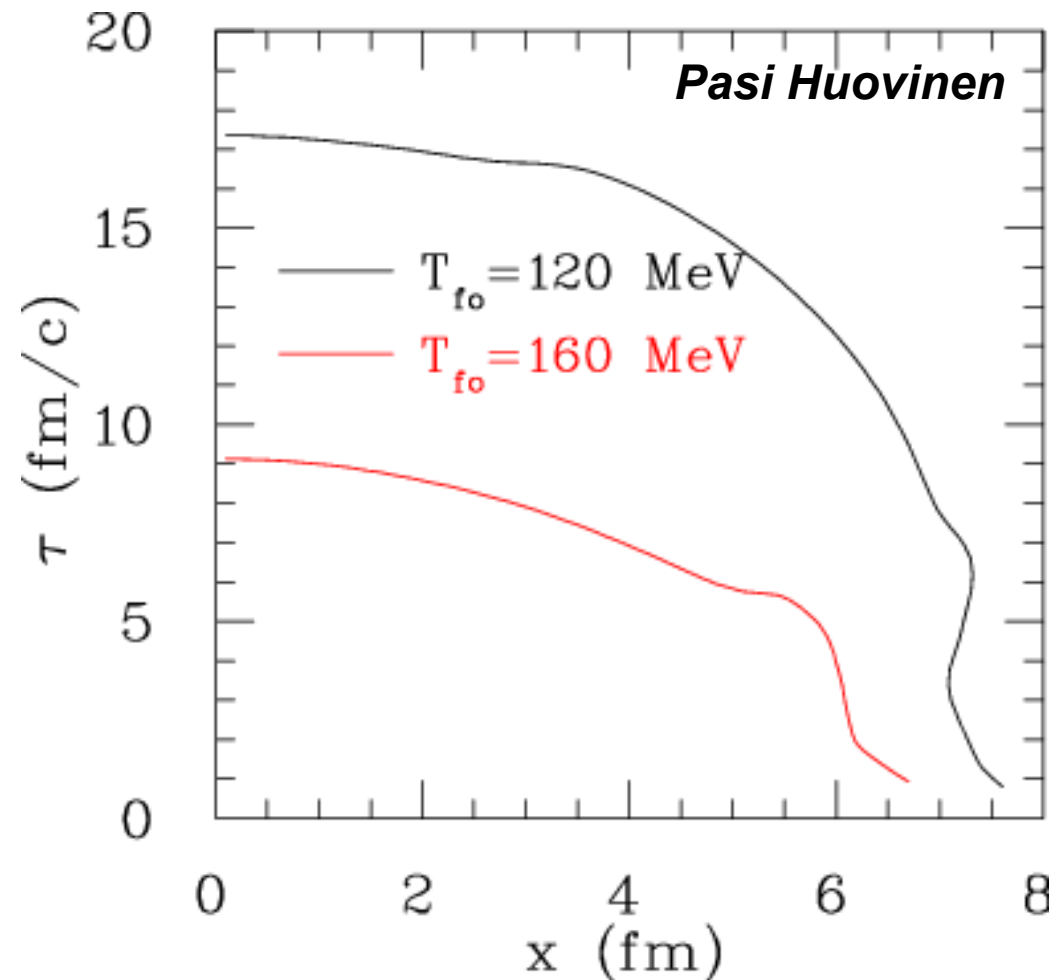
- 🌍 blast is "hydro inspired" and has 8 free parameters  
→ hydro source must be a special case of blast source*
- 🌍 fit CERES by blast and fit hydro by blast and compare the resulting parameters*
- 🌍 identify THE parameter which is different  
→ this is what needs to be fixed in hydro*

**no way to fit  
blast to hydro**

# hydro freeze-out profile

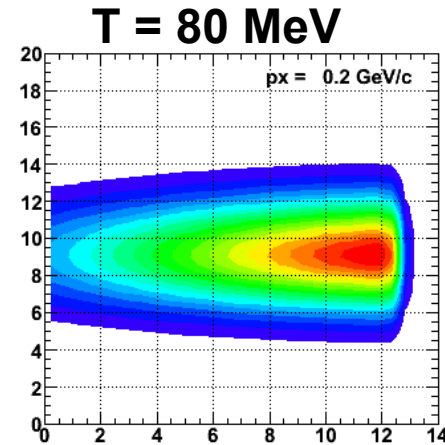
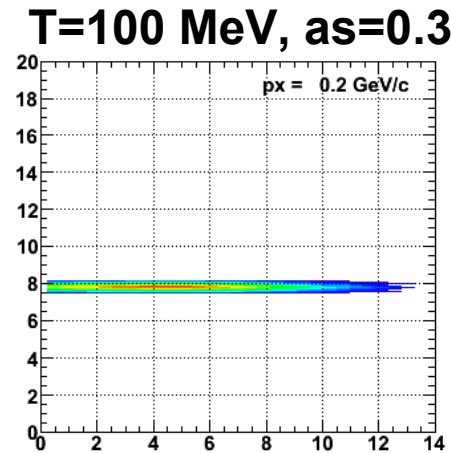
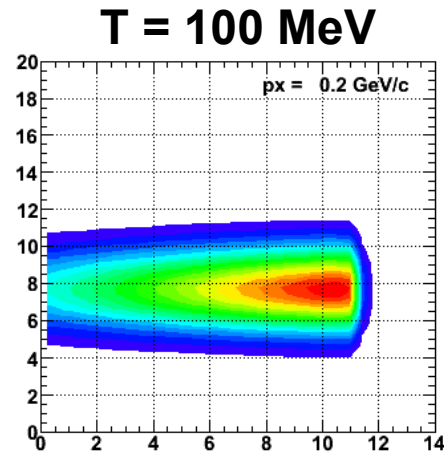
**Why is  $R_{out}$  so large  
and  $R_{side}$  so small in  
hydro ?**

**Hint by Pasi Huovinen:  
freeze-out profile**

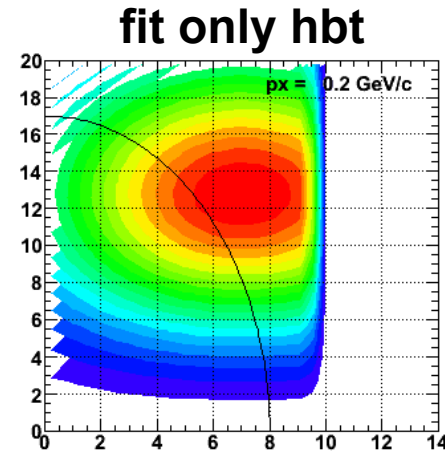
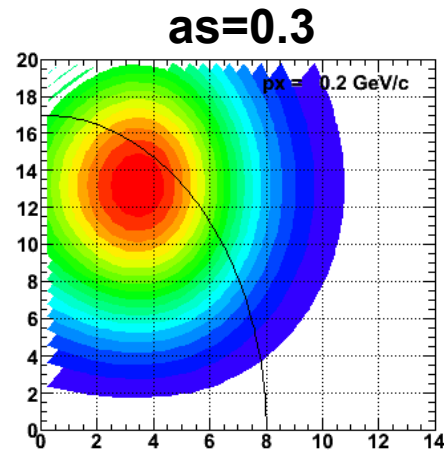
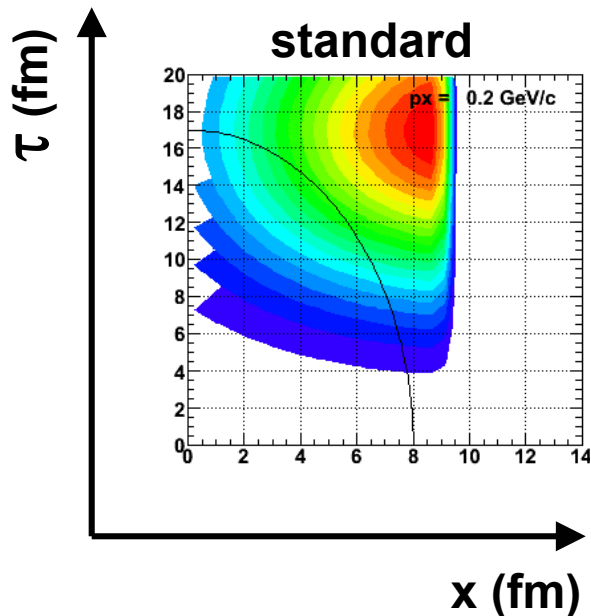




# blast wave freeze-out profile



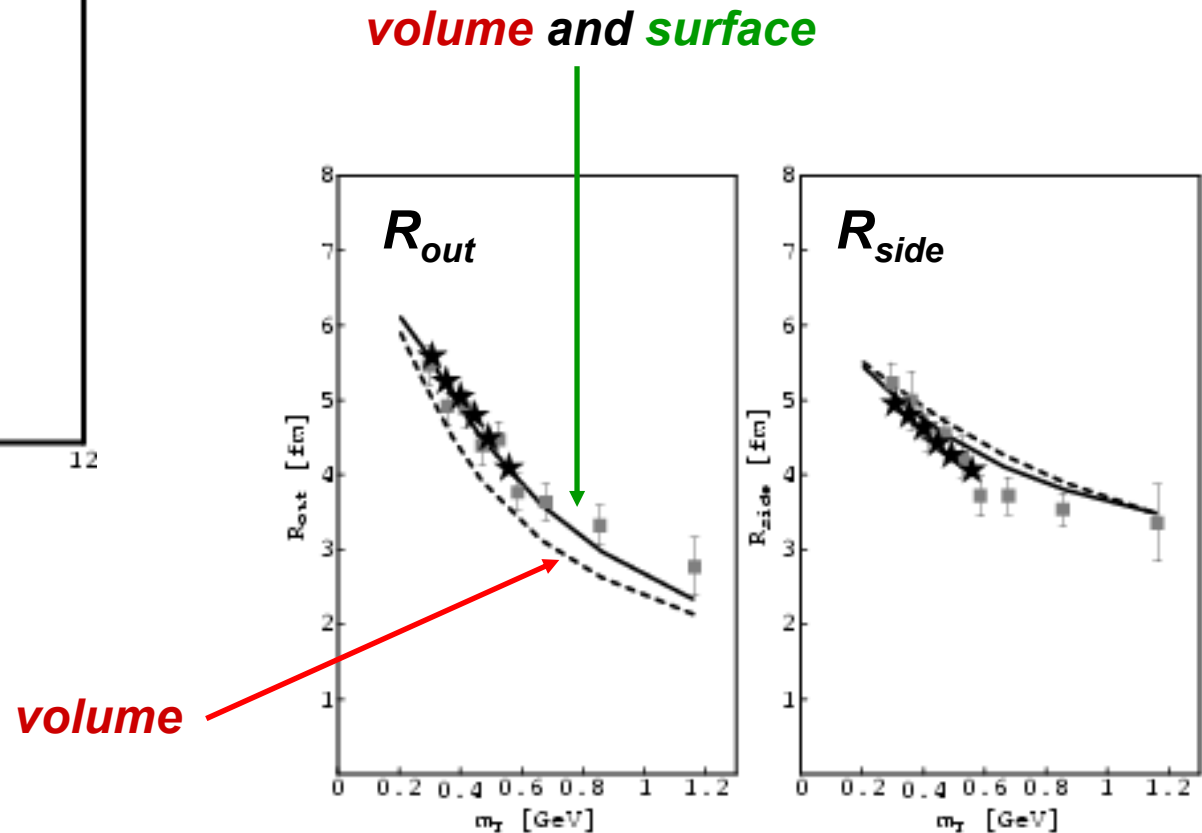
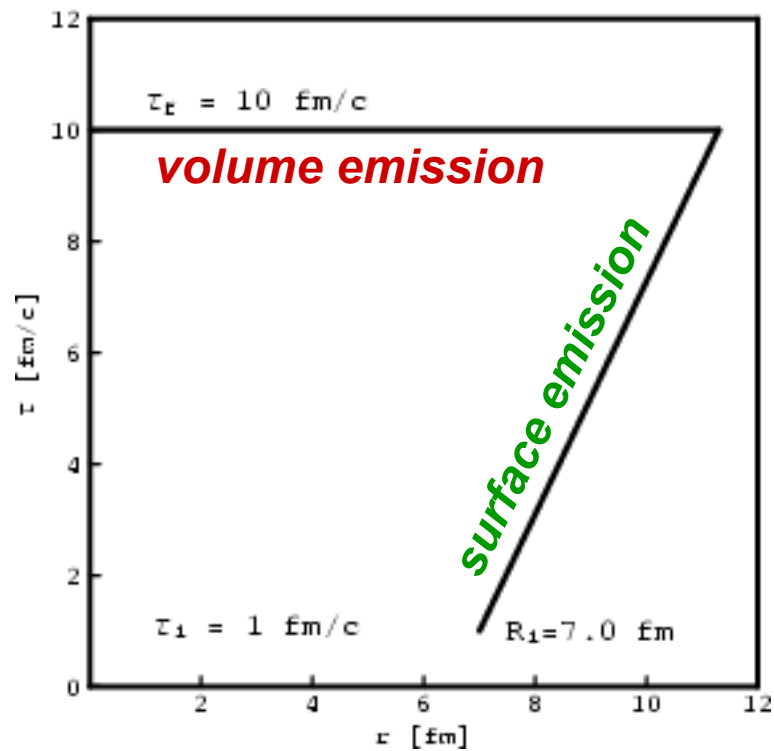
fit to CERES data



"fit" to hydro  
120 MeV

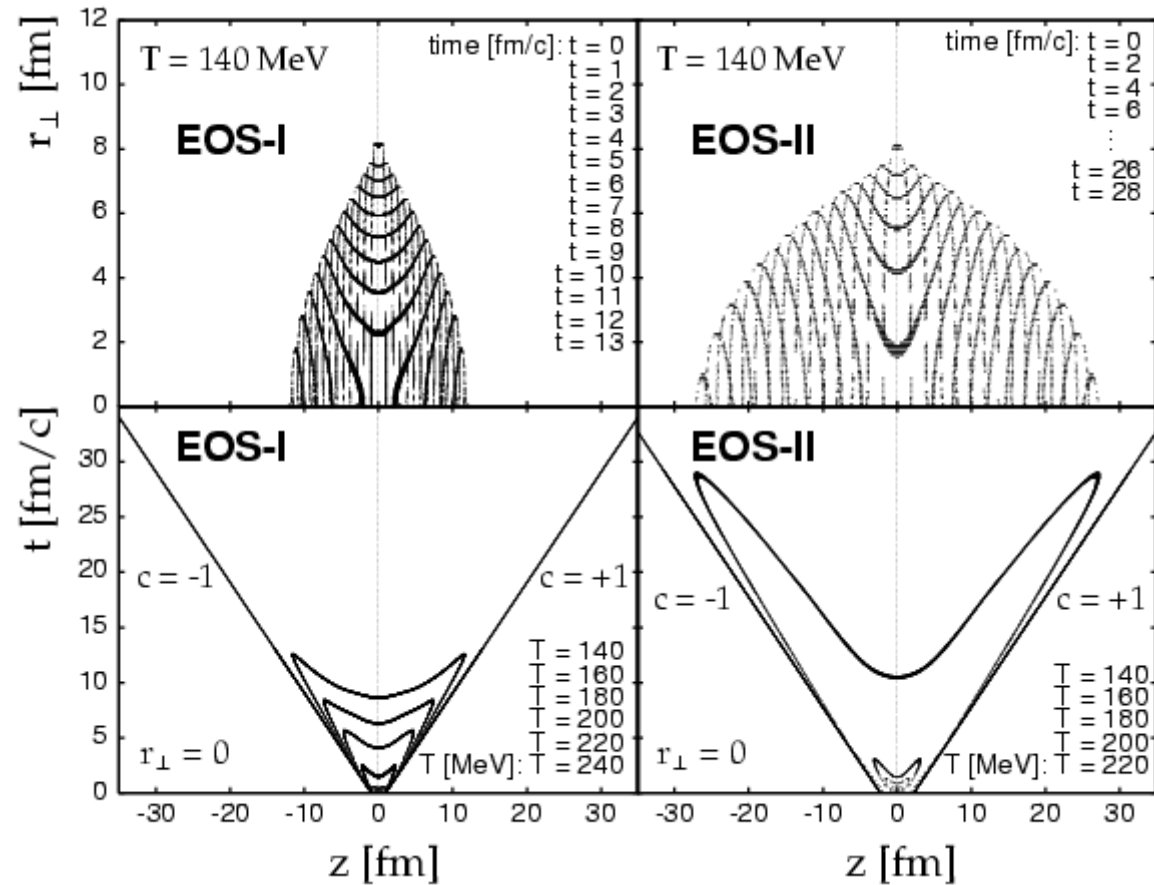
# Yuri Sinyukov's blast wave freeze-out profile

Phys.Rev. C73 (2006) 024903  
*pi- pi-* from PHENIX and STAR

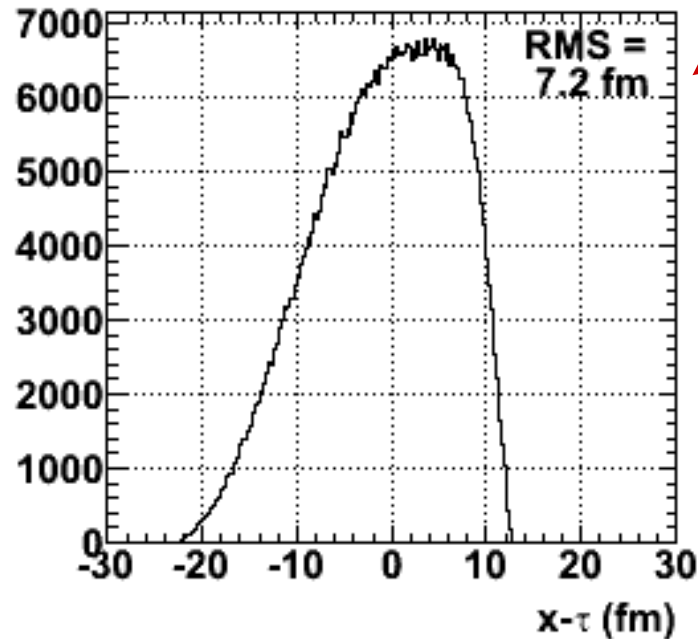
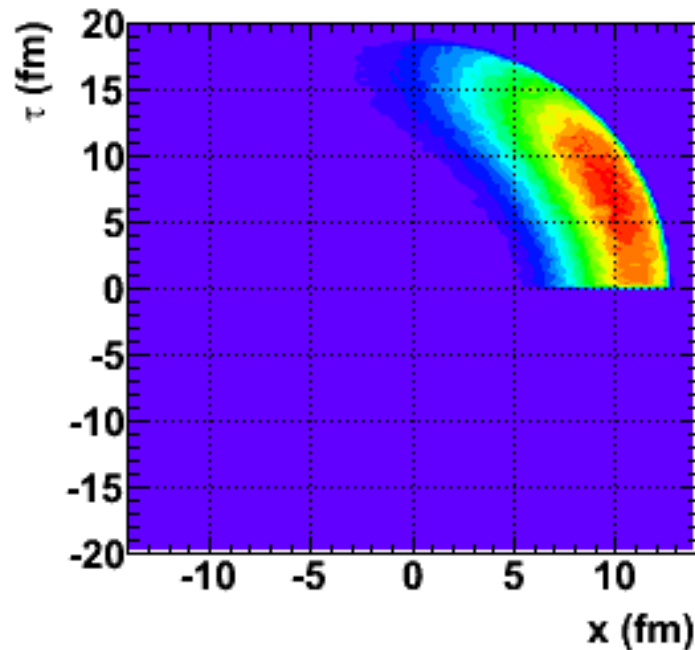
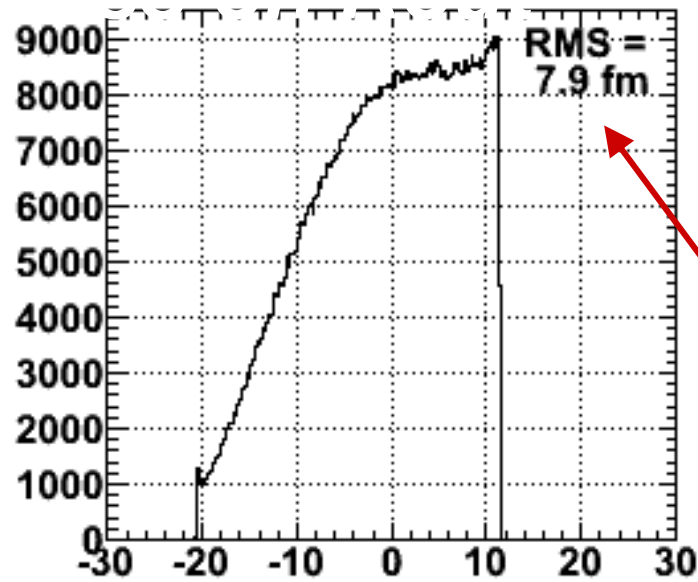
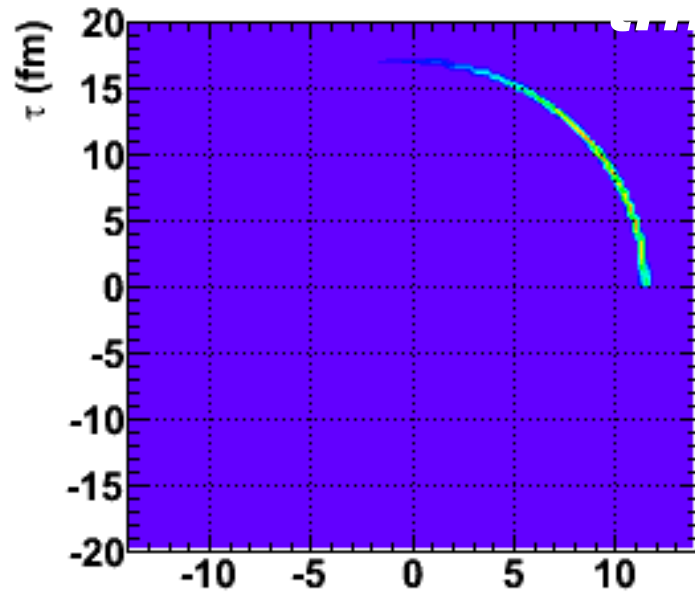


# Bernd Schlei's hydro freeze-out profile

nucl-th/9706037



# influence of the freeze-out surface



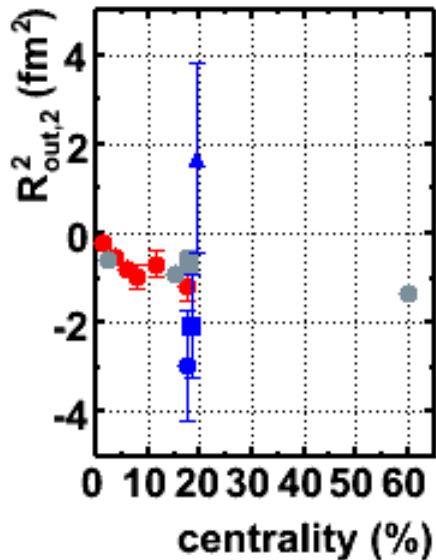
$\sim R_{\text{out}}$

# summary

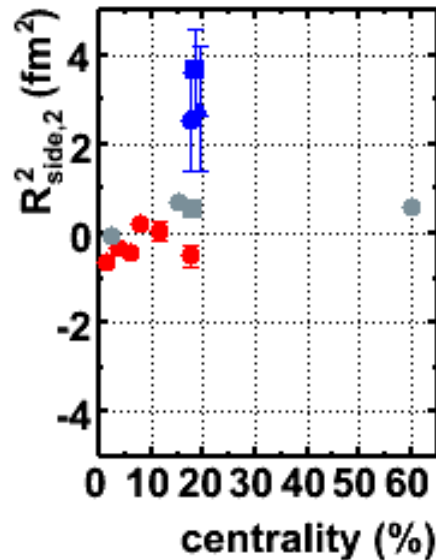
- 🌐 **blast fits reasonably well CERES spectra, flow, and HBT**
- 🌐 **hydro fits CERES spectra and flow but not HBT radii**
- 🌐 **blast is qualitatively different from hydro (even if "inspired" by it)**
- 🌐 **troubles with hydro may be caused by:**
  - freeze-out surface moving inward? probably not...**
  - its unrealistically small thickness? probably not...**
  - with the two hydro versions giving so different results**
  - one should be able to nail it down!**

# azimuthal HBT from CERES: appetizer

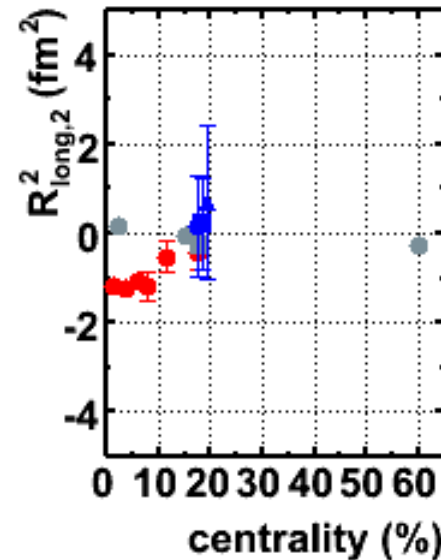
Pb+Au at 158 AGeV  
preliminary



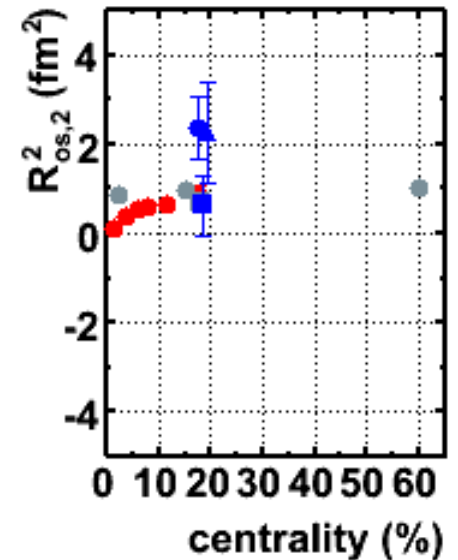
*suggests an out-of-plane elongation*



*no effect -- inconsistent with  $R_{out}$*



*significant -- against expectation and symmetry*



*consistent with  $R_{out}$*

***more about this subject in the talk of D. Antończyk on Friday morning***

# *azimuthal dependence of pion HBT radii*

*more about this subject in the talk of  
D. Antończyk on Friday morning*

# pion-pion correlation function

## correlation function

= pair distribution,  
normalized to event mixing

$$C_2(\mathbf{P}, \mathbf{q}) = \frac{n(\mathbf{p}_1, \mathbf{p}_2)}{n(\mathbf{p}_1) n(\mathbf{p}_2)}$$

with mean momentum

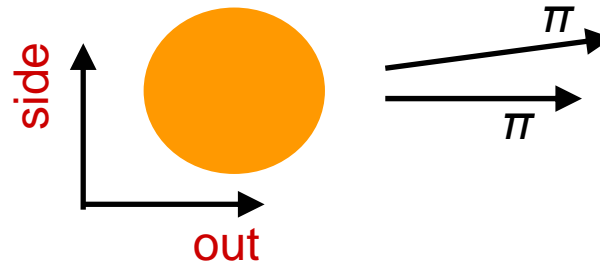
$$\mathbf{P} = (\mathbf{p}_1 + \mathbf{p}_2) / 2$$

and momentum difference

$$\mathbf{q} = \mathbf{p}_2 - \mathbf{p}_1$$

Bertsch-Pratt coordinates  
LCMS frame

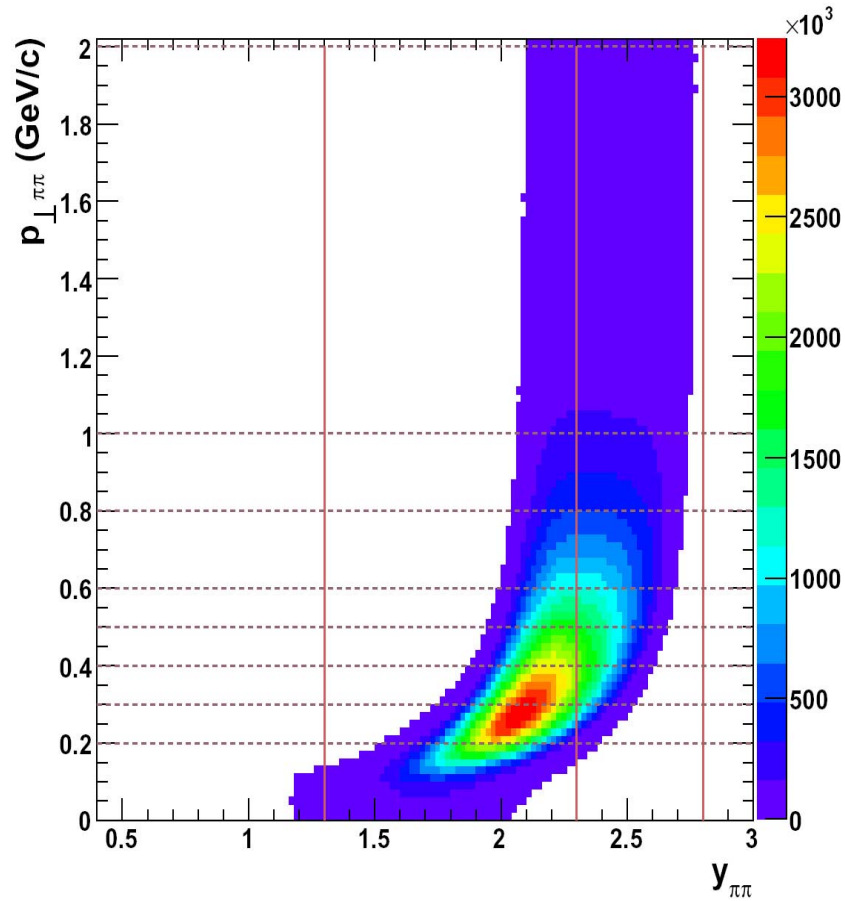
$$\mathbf{q} = (q_{out}, q_{side}, q_{long})$$



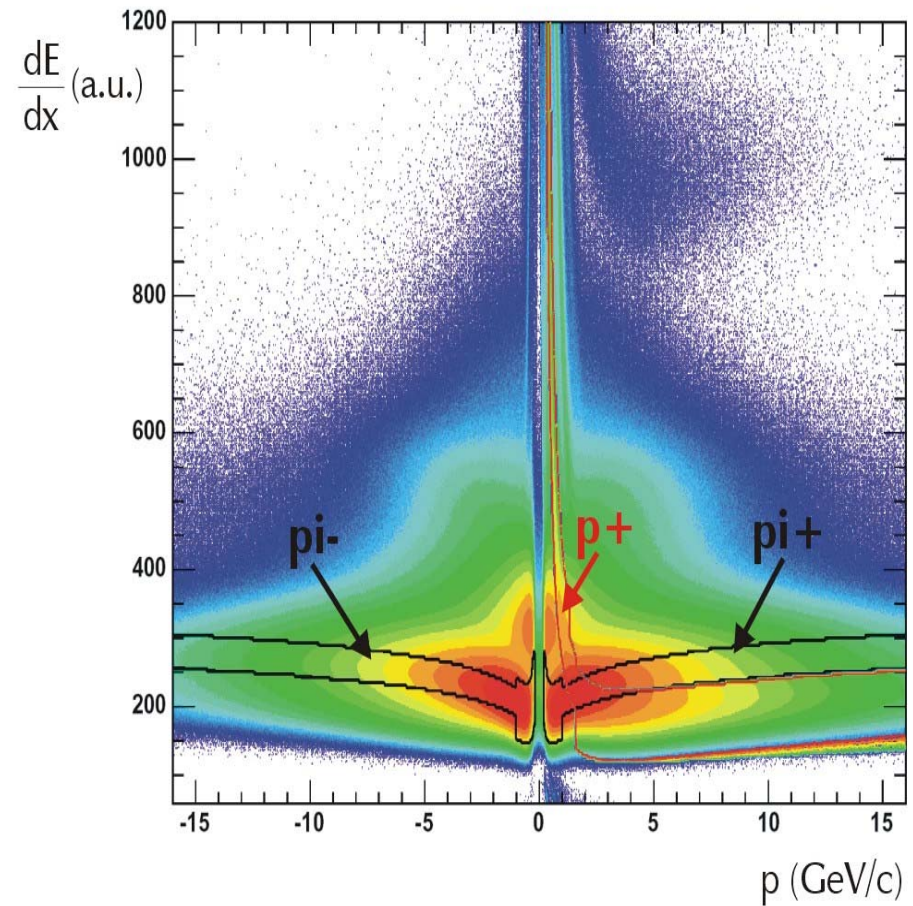


# acceptance and particle id

Pb+Au at 158 AGeV



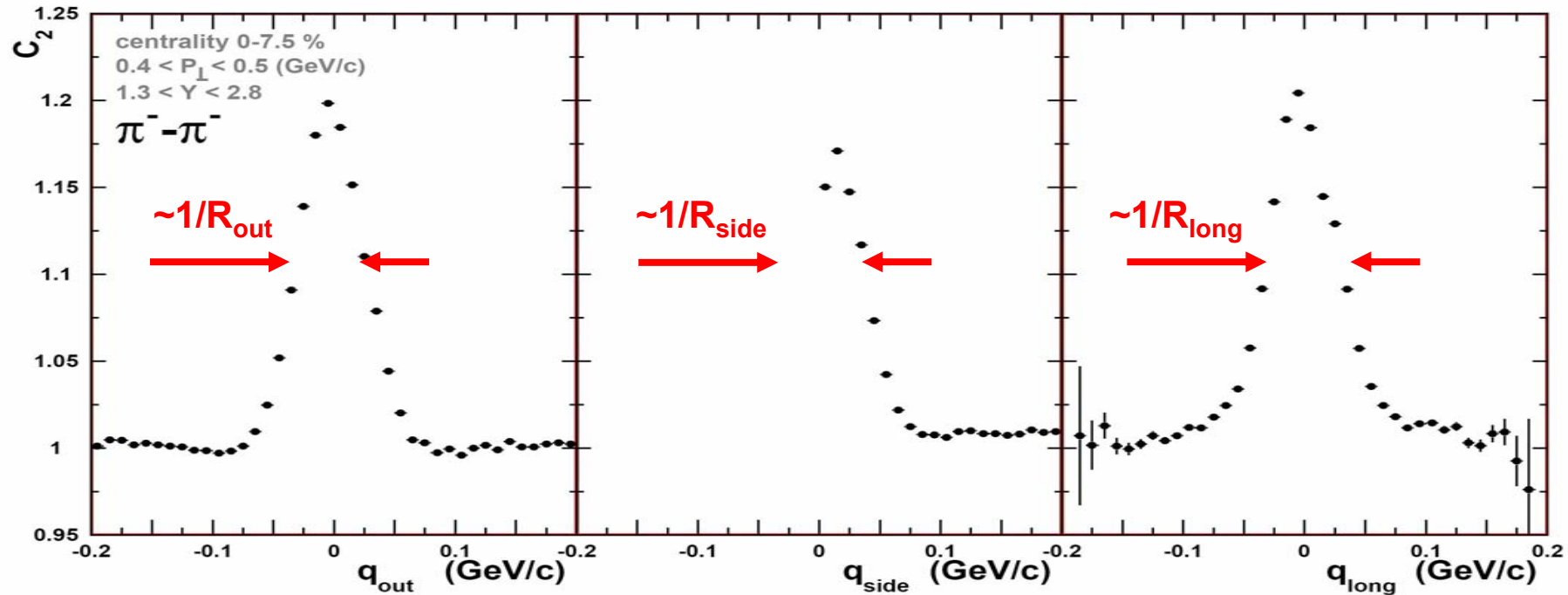
↑  
midrapidity:  $y=2.91$



# two-pion correlation function

Pb+Au at 158 AGeV

D. Antonczyk



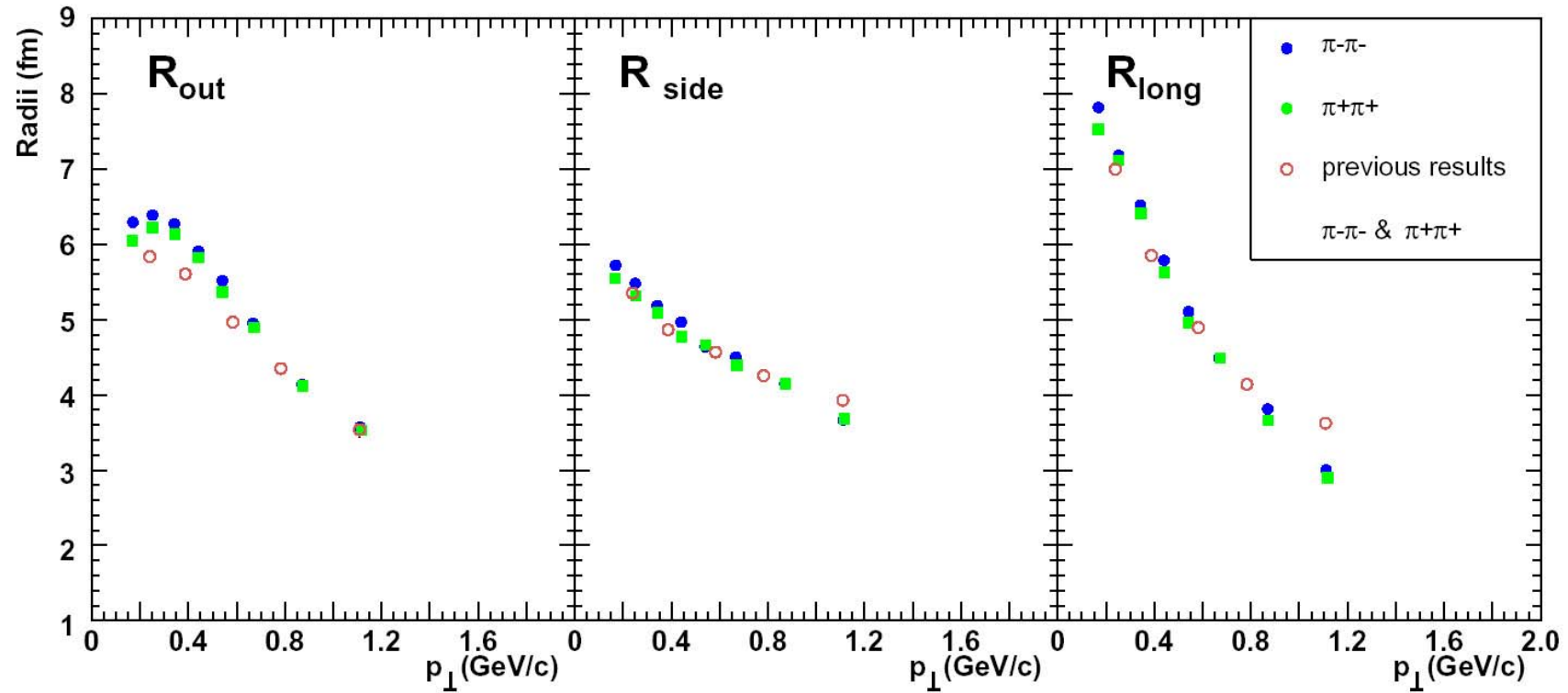
fit with 
$$C_2(q) = 1 + \lambda \exp \left\{ - \sum_{i,j} R_{i,j}^2 q_i q_j \right\} \quad \text{with } i,j = \text{out, side, long}$$

correct for Coulomb and finite momentum resolution

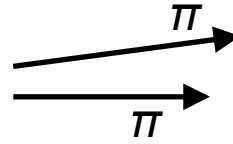
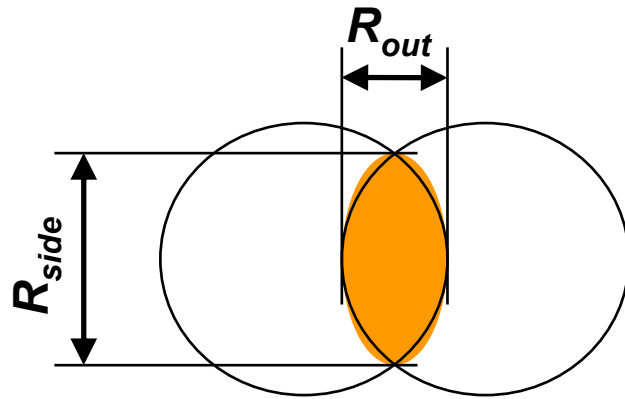
# HBT radii: $p_t$ dependence

Pb+Au at 158 AGeV  
centrality 5%

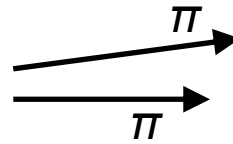
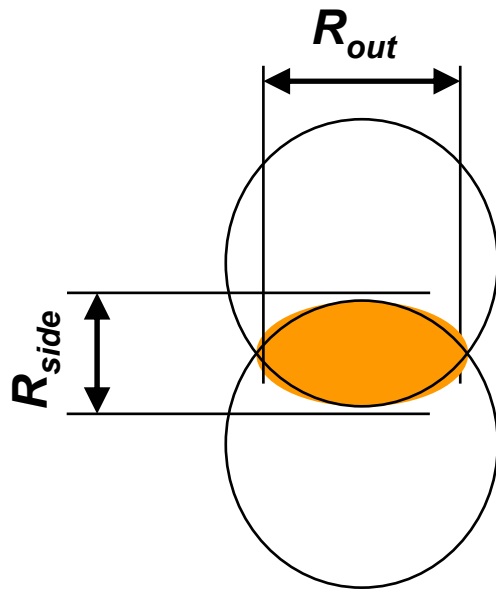
D. Antonczyk



# HBT radii vs azimuthal pion angle - expectation

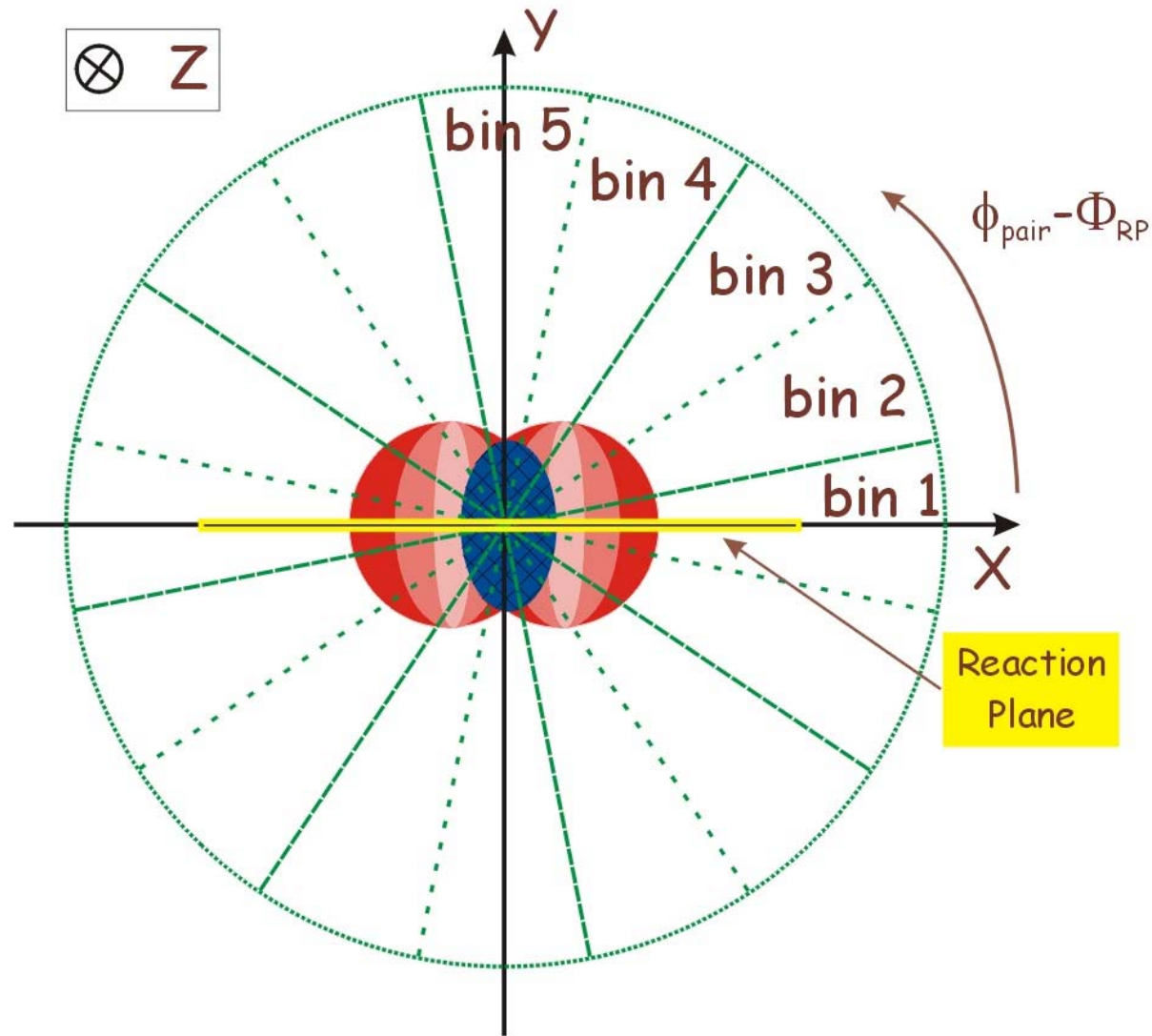


*in-plane*

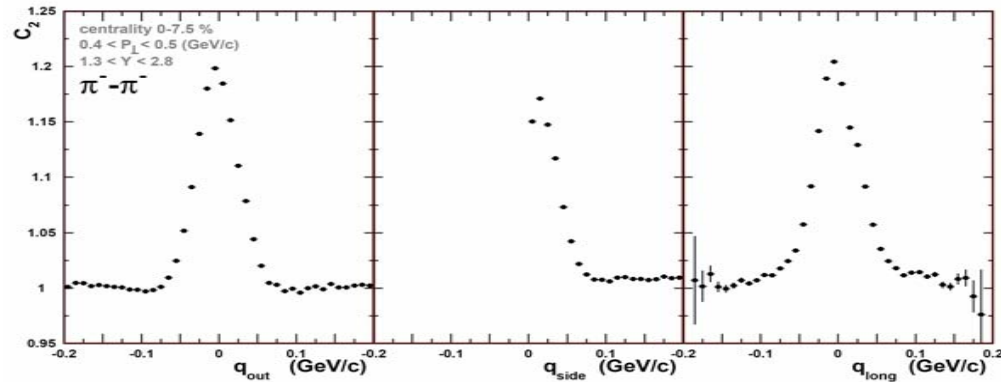


*out-of-plane*

# HBT radii in bins of the azimuthal pair angle



# *pion-pion correlation function*



3-dimensional fit to  $C_2$  performed  
 $R_{out}$ ,  $R_{side}$ ,  $R_{long}$ ,  $R_{ol}$ ,  $R_{os}$ ,  $R_{sl}$  extracted

separately in  
 each  $\phi$ -bin

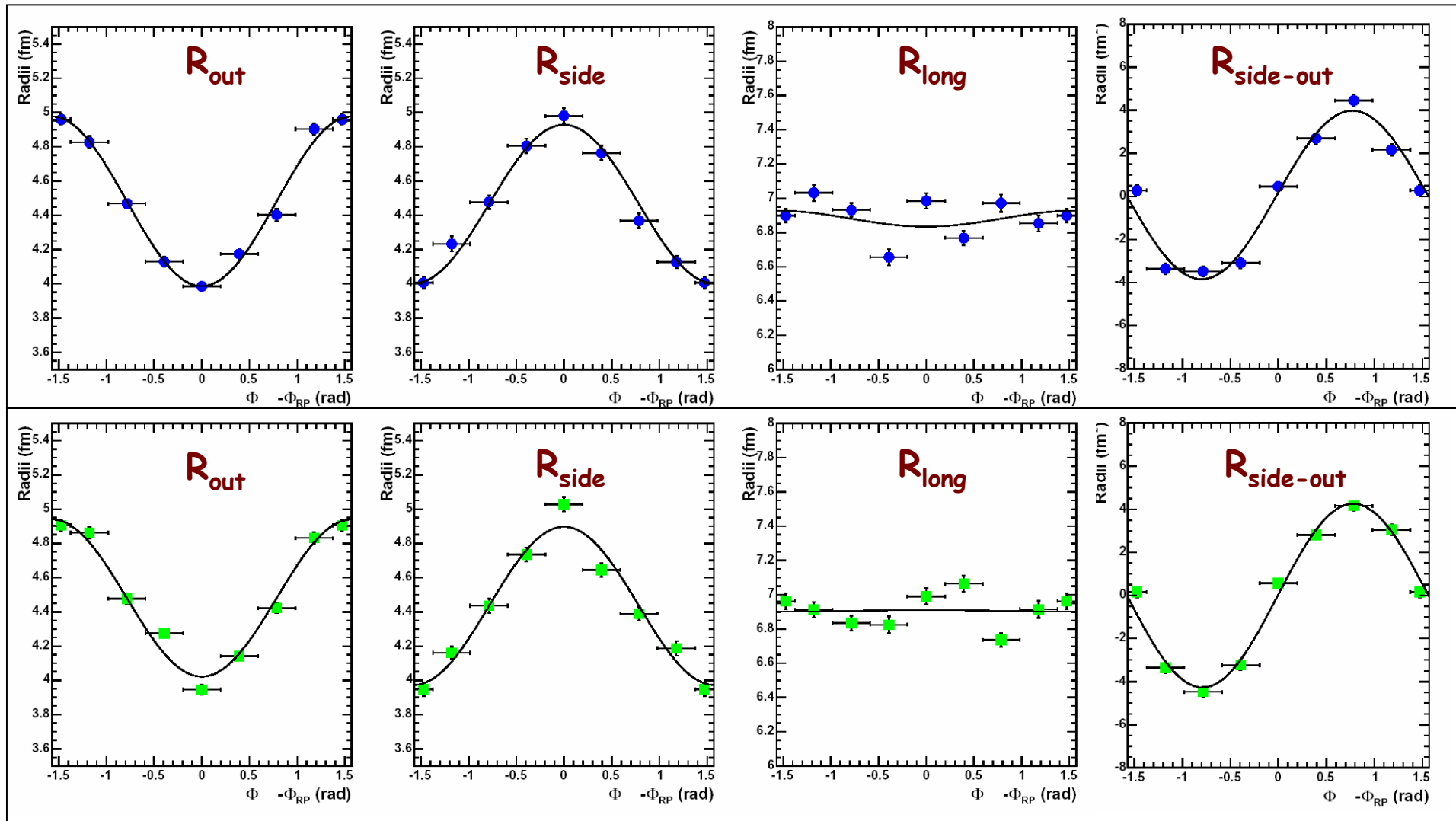
$\phi = \phi_{\pi\pi} - \phi_{RP}$   
 azimuthal pair angle  
 with respect to the RP

# azimuthal angle dependence of the HBT radii - simulation

D. Antonczyk

- $\pi^-\pi^-$
- $\pi^+\pi^+$

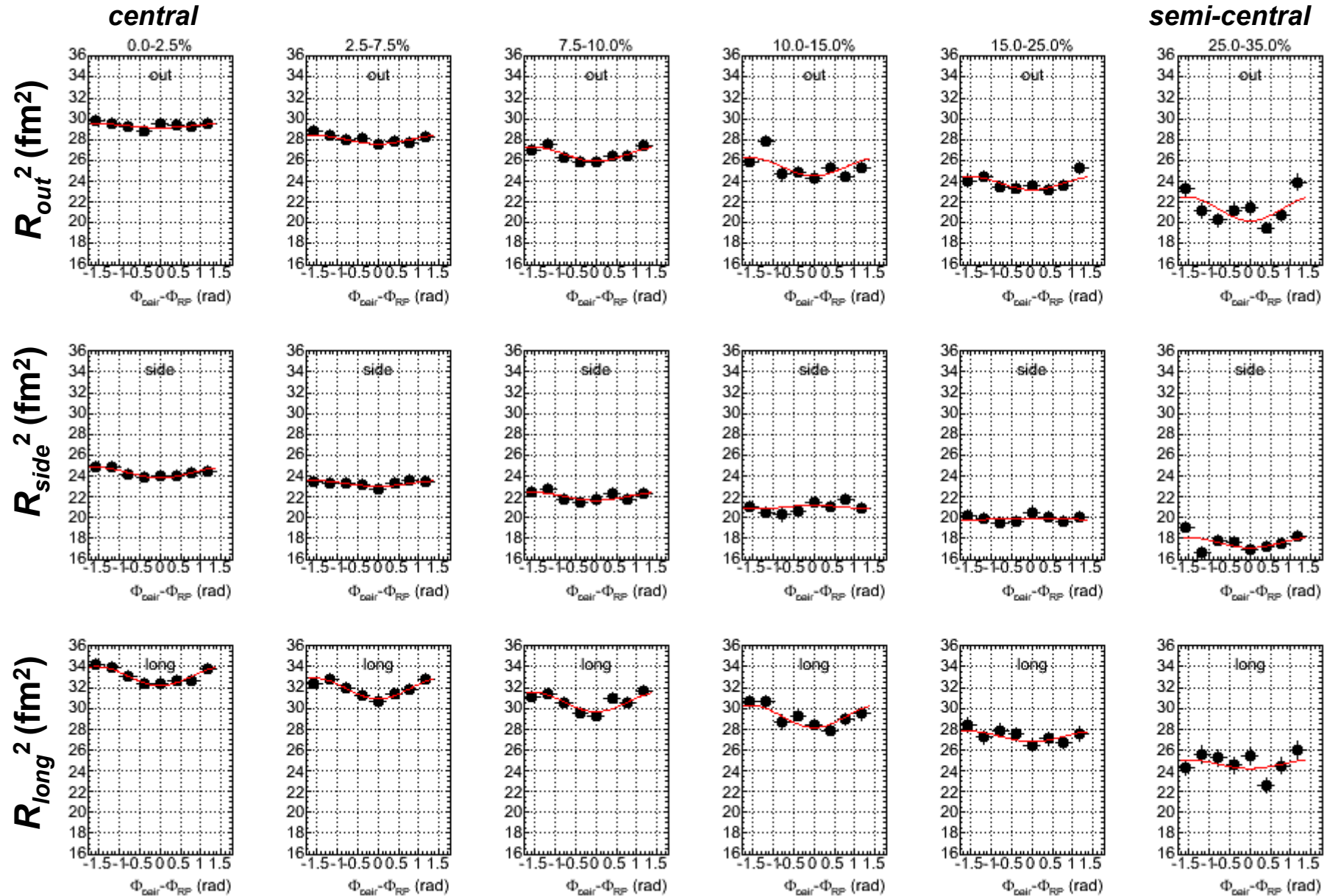
Gaussian source parameterization with  $R_x = 4$  (fm),  $R_y = 5$  (fm),  $R_z = 7$  (fm)



# azimuthal angle dependence of HBT radii

Pb+Au at 158 AGeV

D. Antonczyk

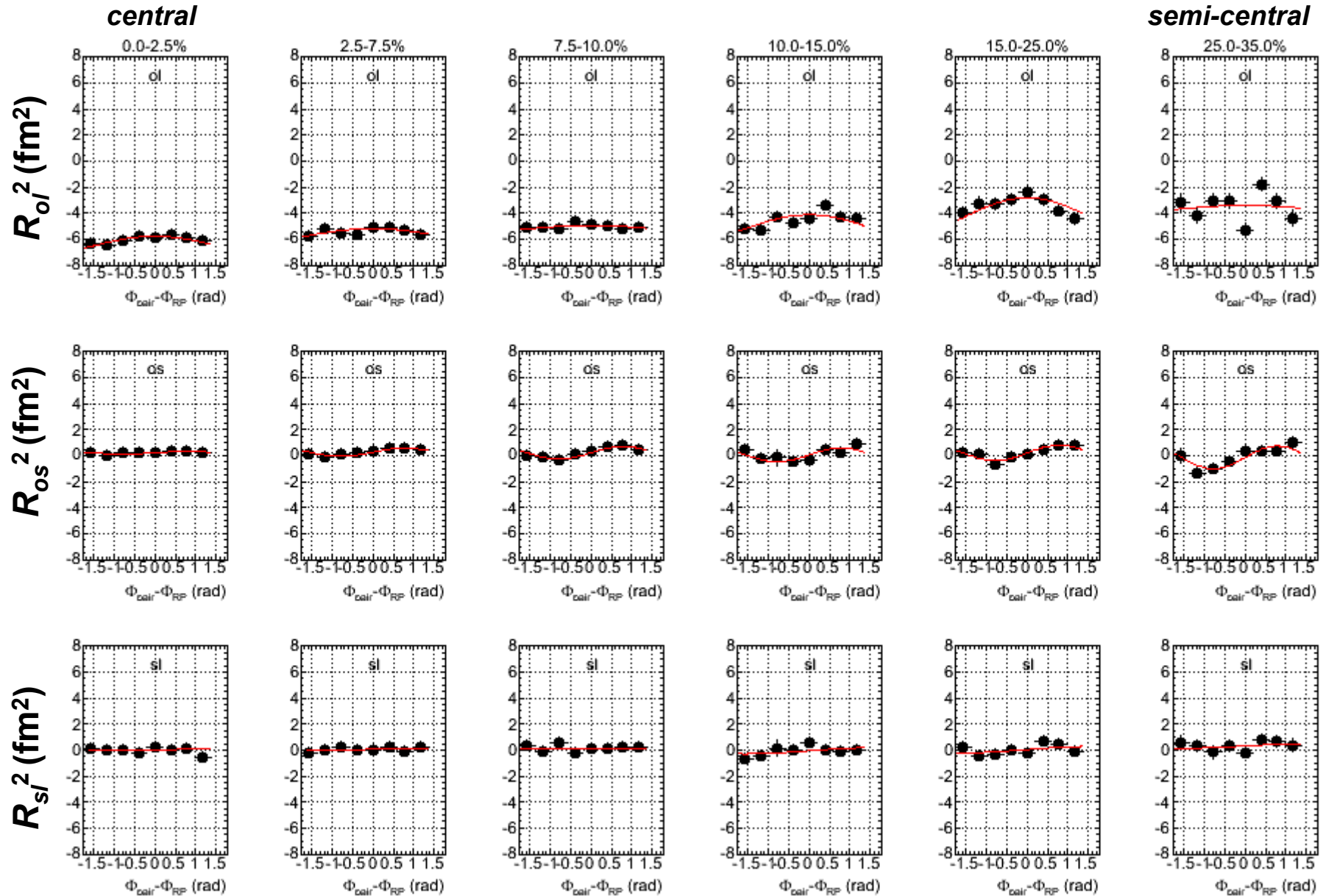




# azimuthal angle dependence of HBT radii

Pb+Au at 158 AGeV

D. Antonczyk

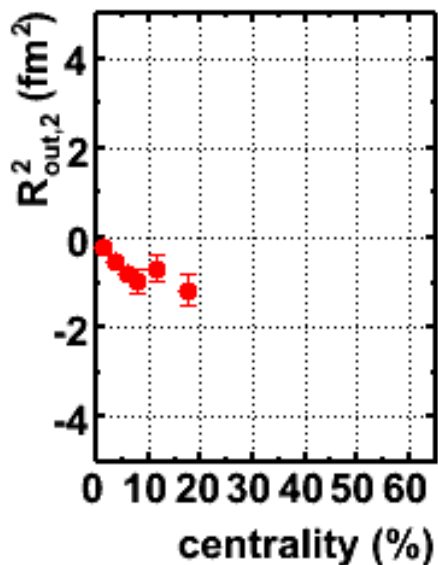


# *pion source size anisotropy*

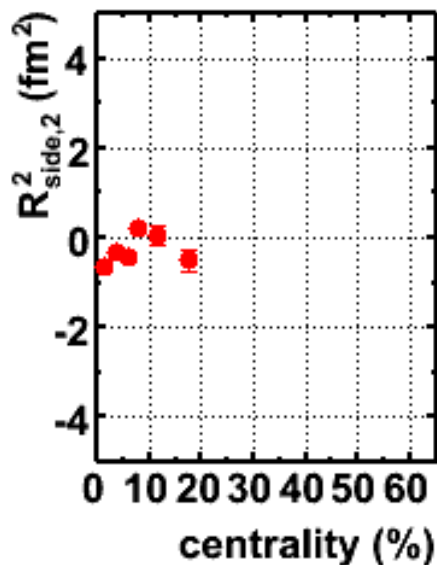
Pb+Au at 158 AGeV  
preliminary

D. Antonczyk

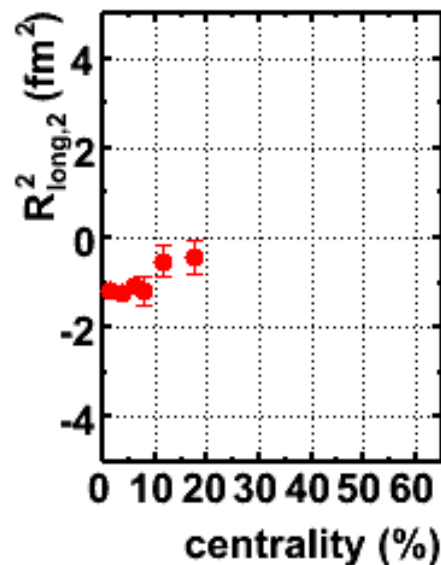
parametrize the oscillation with  $R_i^2 = R_{i,0}^2 + 2 R_{i,2}^2 \cos [2(\Phi_{\pi\pi} - \Phi_{RP})] \rightarrow$



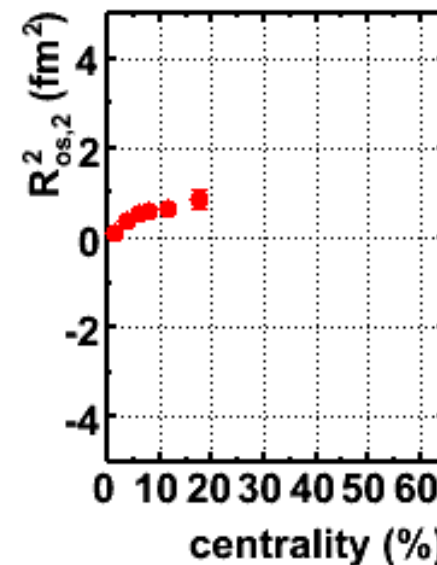
↑  
*suggests an  
out-of-plane  
elongation*



↑  
*no effect --  
inconsistent  
with  $R_{out}$*

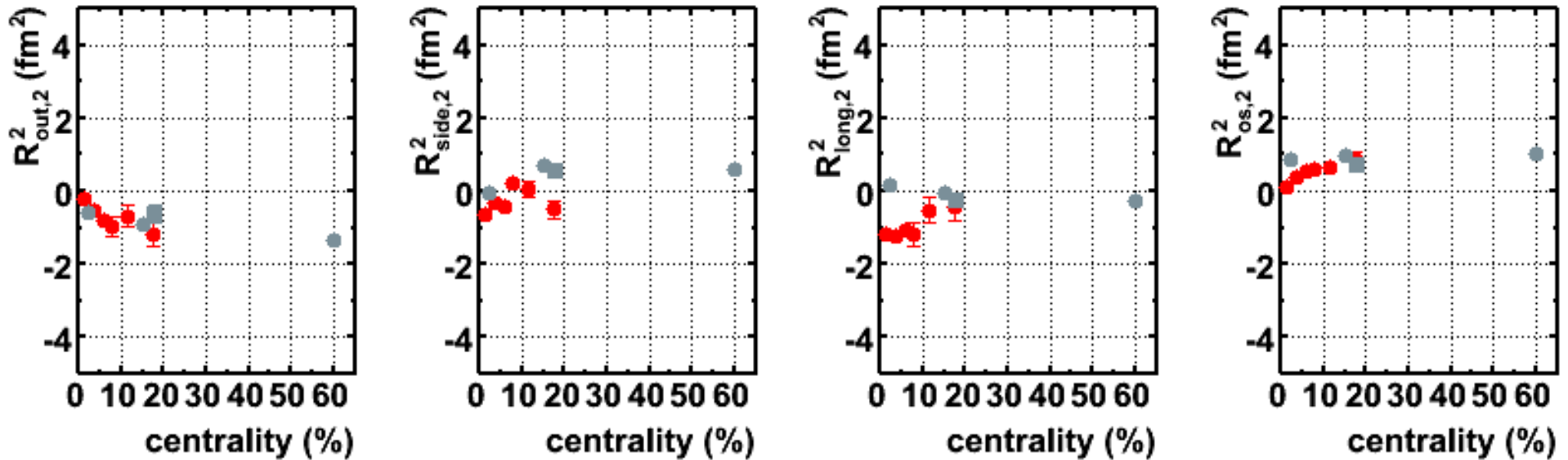


↑  
*significant --  
against  
expectation  
and symmetry*



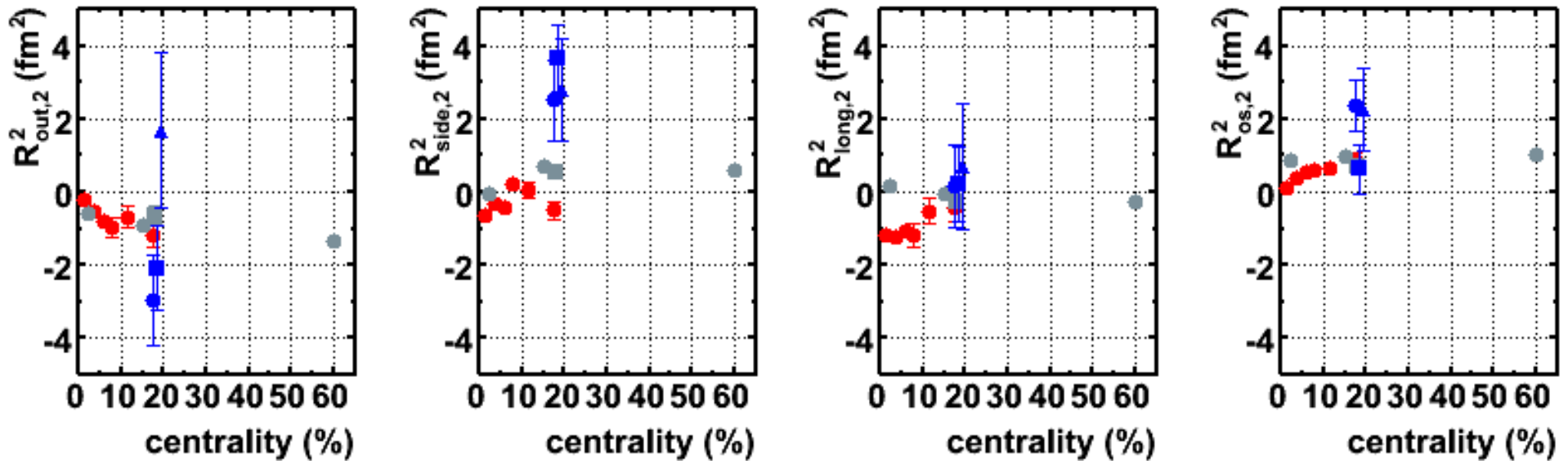
↑  
*consistent  
with  $R_{out}$*

# ...compared to RHIC



- CERES      158 AGeV       $\langle pt \rangle = 0.47$  GeV/c      D. Antonczyk, Ph.D.
- STAR       $\sqrt{s} = 130$  GeV       $0.125 < pt < 0.45$  GeV/c
- STAR       $\sqrt{s} = 200$  GeV       $0.15 < pt < 0.6$  GeV/c      PRL 93 (2004) 012301

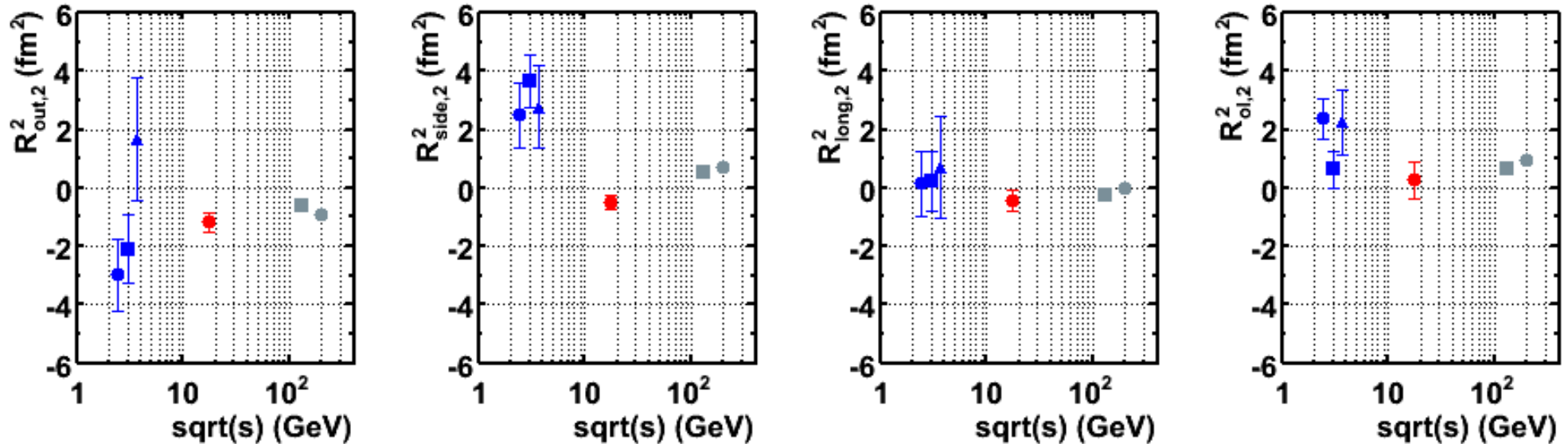
# ... and AGS



<b>E895</b>	● 2, ■ 4, ▲ 6 AGeV	$\langle pt \rangle = 0.11 \text{ GeV}/c$	<i>Phys. Lett. B 496 (2000) 1</i>
● CERES	158 AGeV	$\langle pt \rangle = 0.47 \text{ GeV}/c$	<i>D. Antonczyk, Ph.D.</i>
■ STAR	$\sqrt{s} = 130 \text{ GeV}$	$0.125 < pt < 0.45 \text{ GeV}/c$	
● STAR	$\sqrt{s} = 200 \text{ GeV}$	$0.15 < pt < 0.6 \text{ GeV}/c$	<i>PRL 93 (2004) 012301</i>

# source anisotropy vs sqrt(s)

Pb+Au, Au+Au  
centrality 15-20%



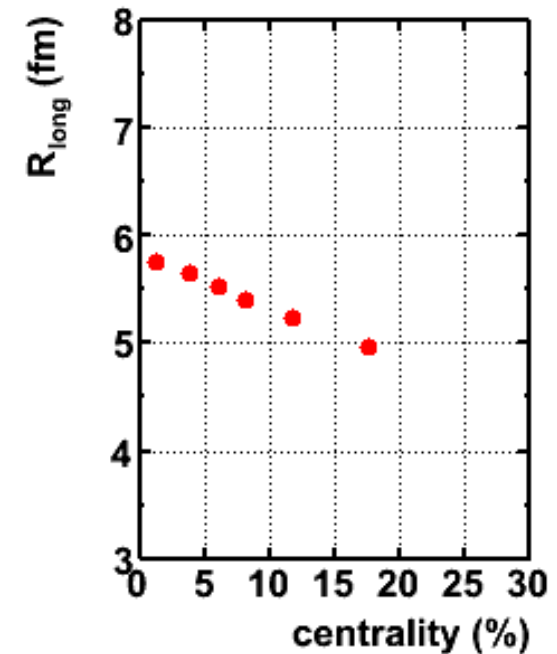
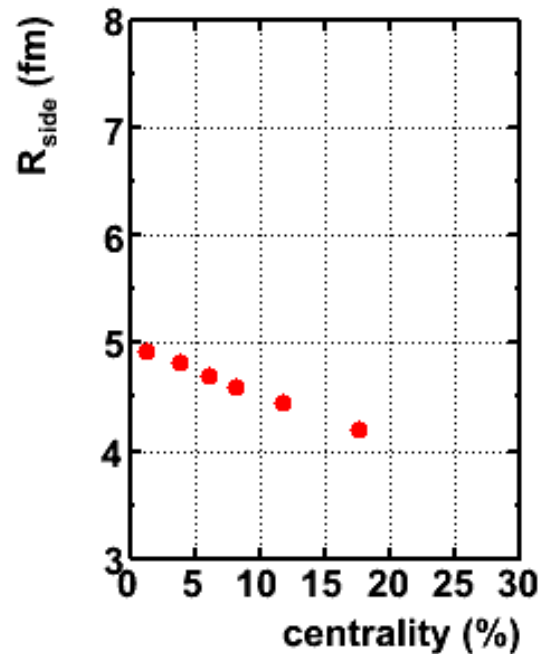
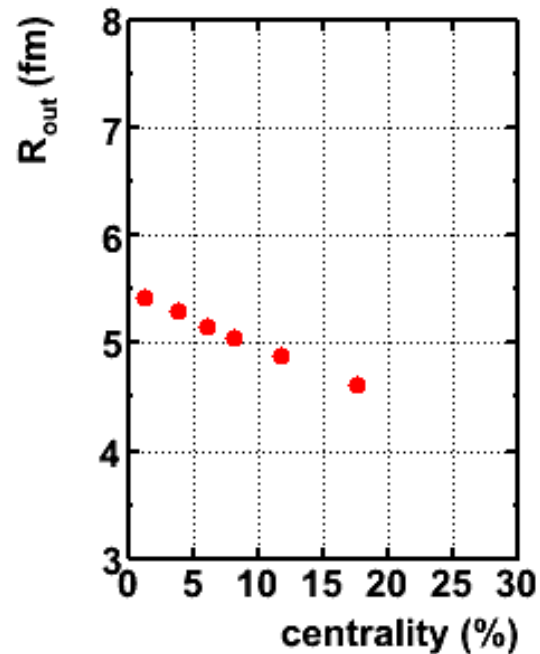
- ⊗ *non-monotonic behavior of  $R_{\text{side}}$*
- ⊗  *$R_{\text{side}}$  inconsistent with  $R_{\text{out}}$  → different freeze-out times in-plane and out-of-plane?*

*backup slides*

# HBT radii: centrality dependence

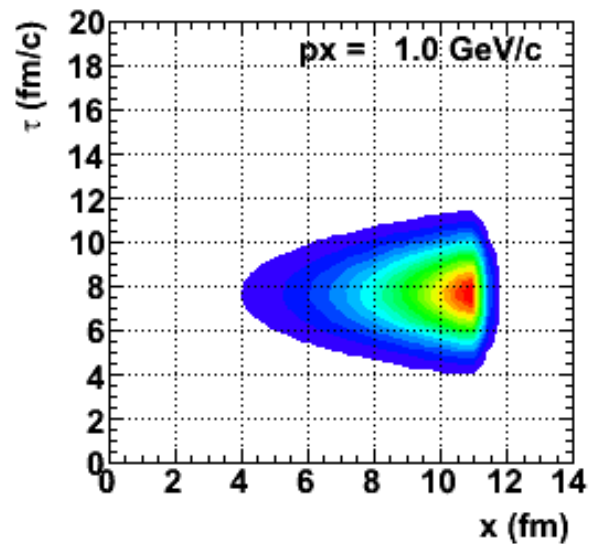
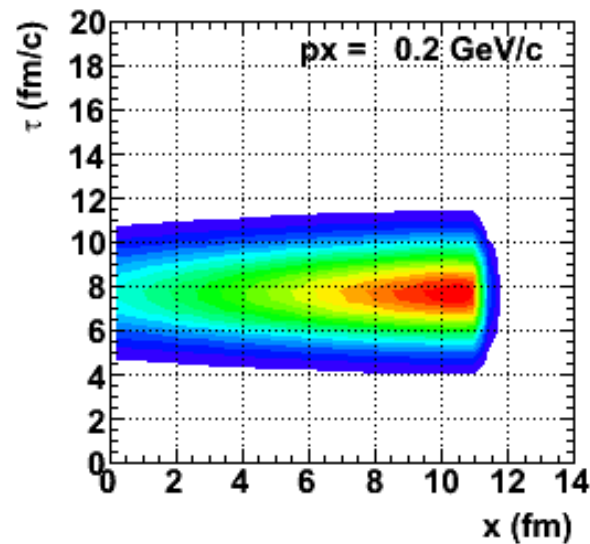
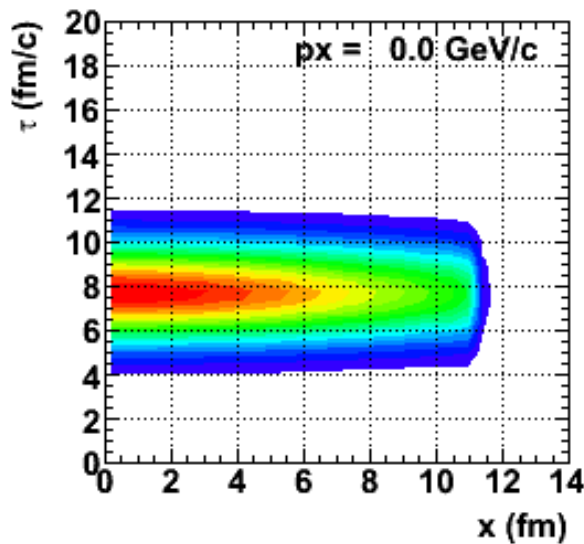
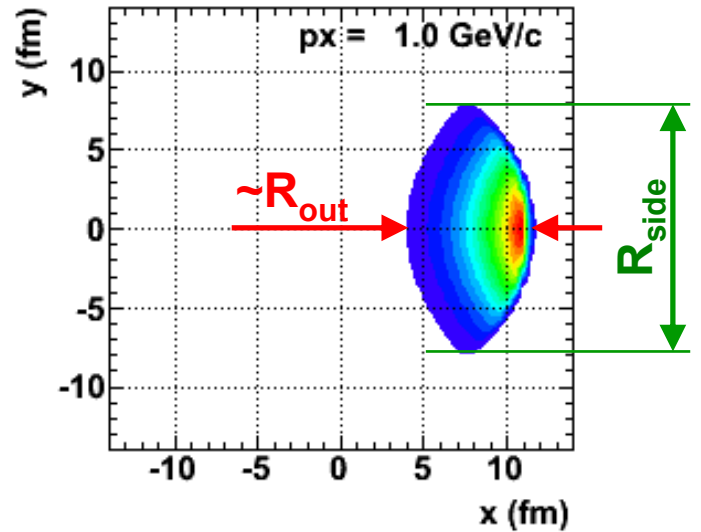
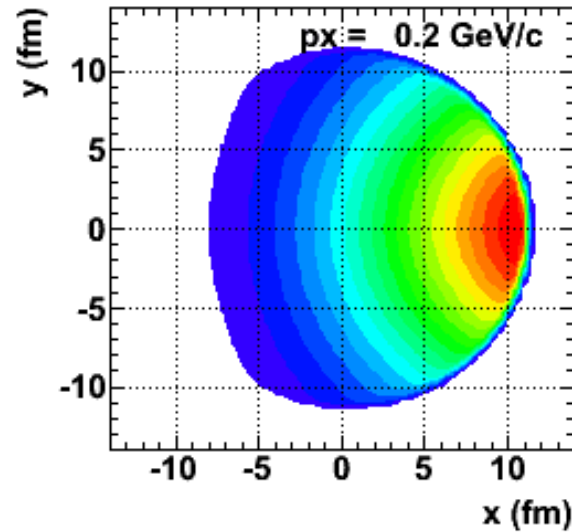
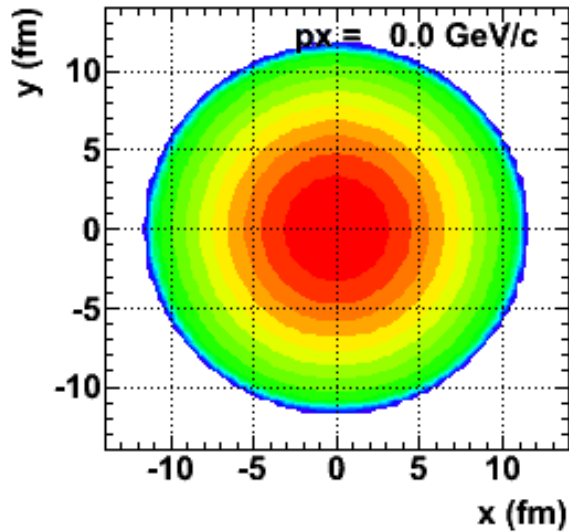
Pb+Au at 158 AGeV  
 $\langle p_t \rangle = 0.47$  GeV/c

D. Antonczyk



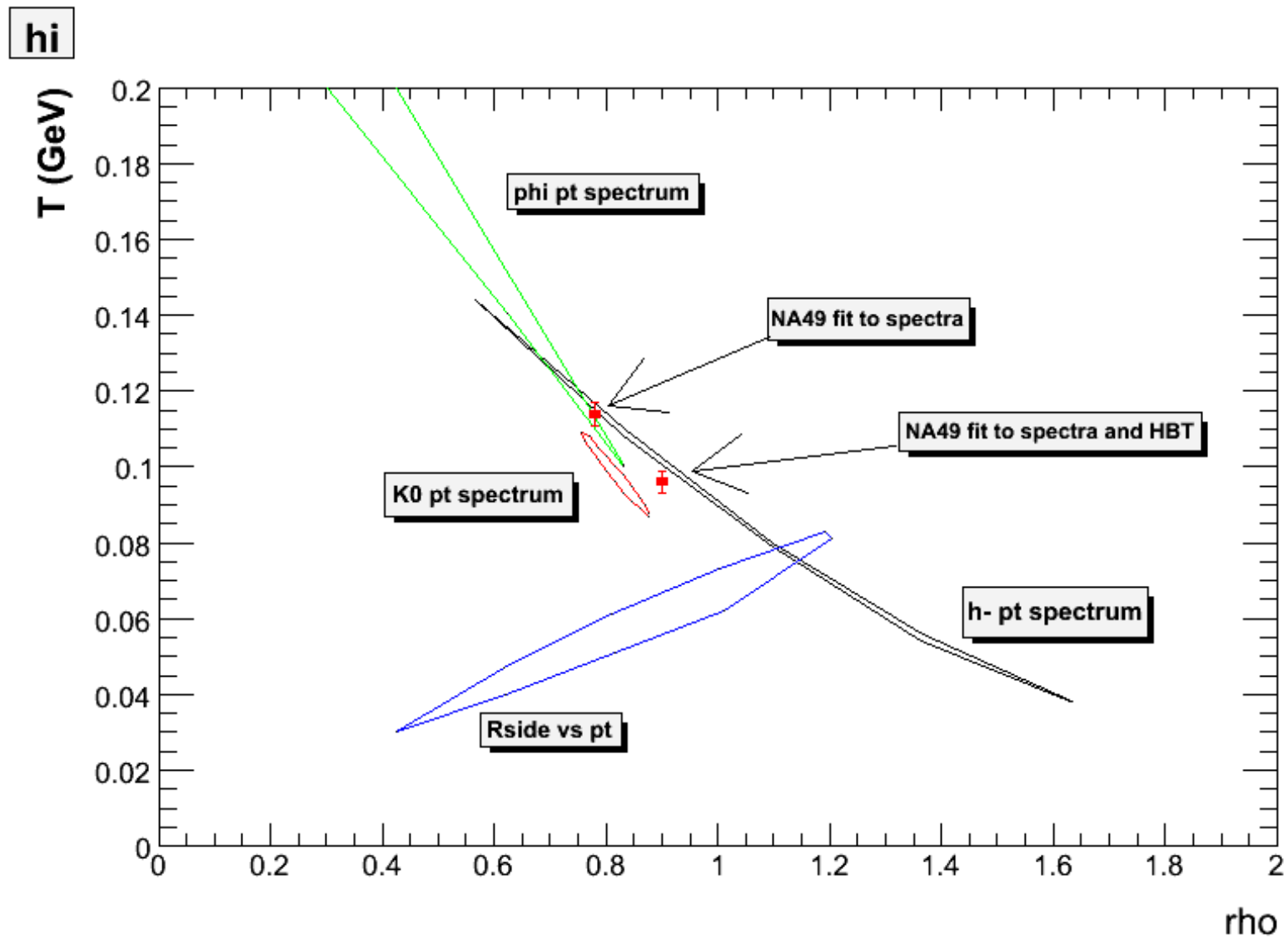
centrality is defined as  $\sigma/\sigma_{GEOM}$   
with  $\sigma_{GEOM} = 6.94$  b

# blast - source shape



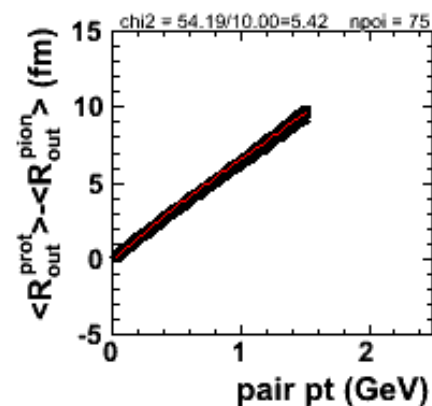
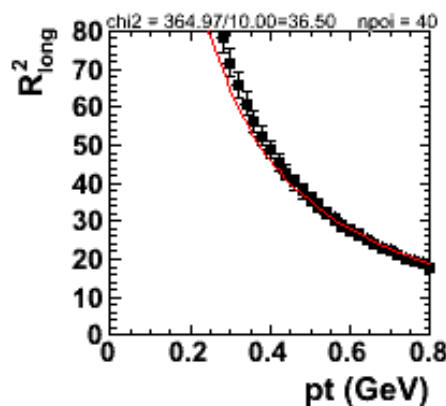
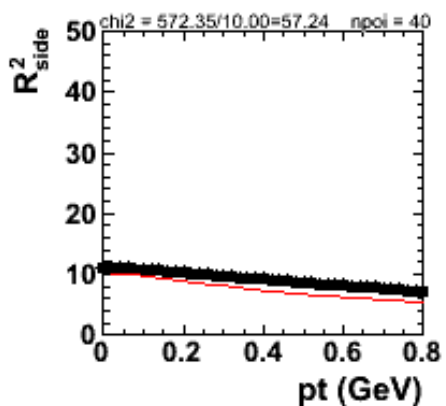
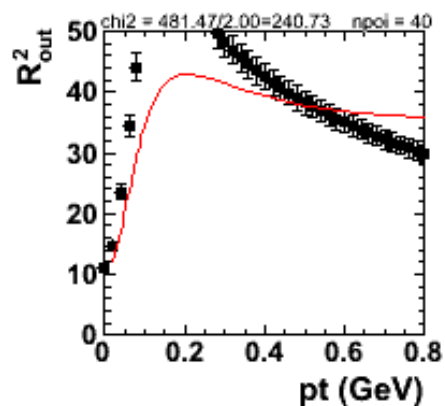
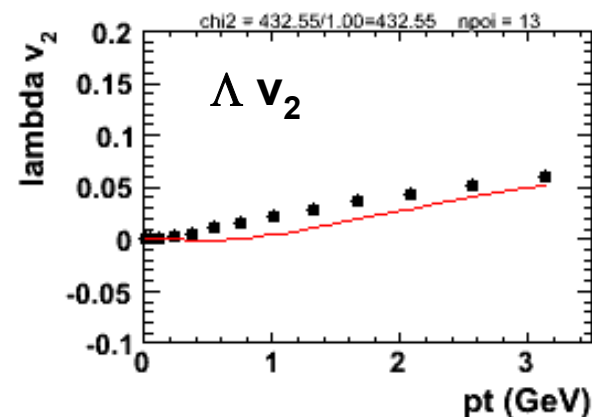
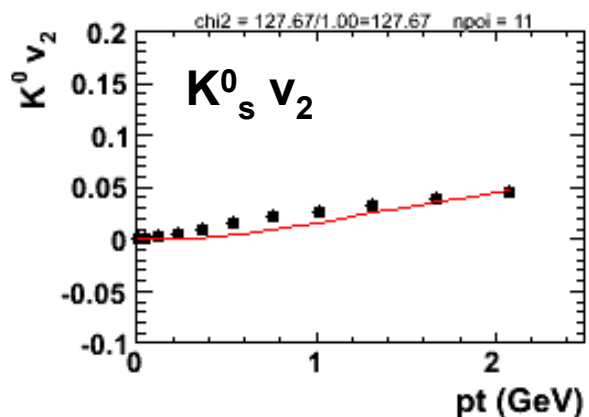
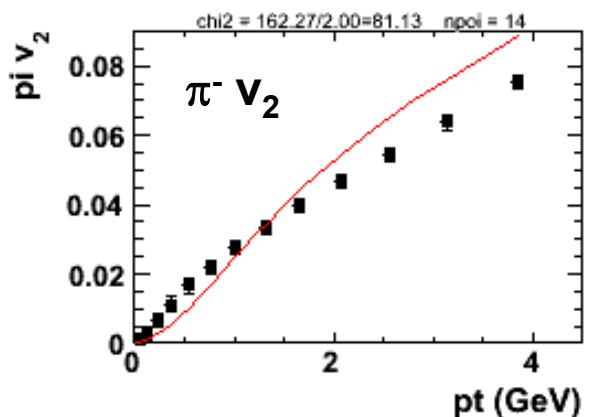
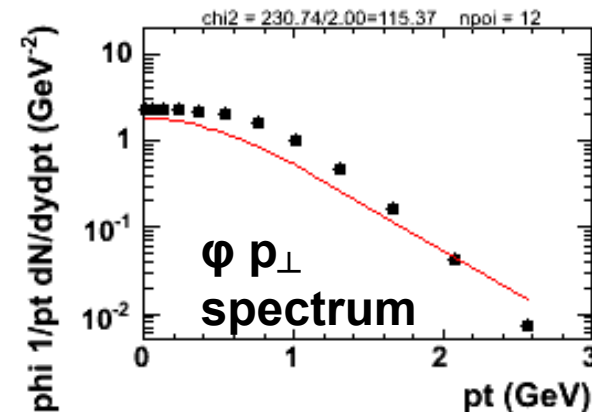
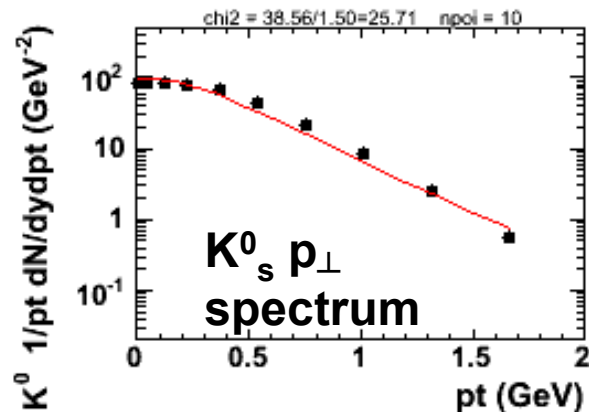
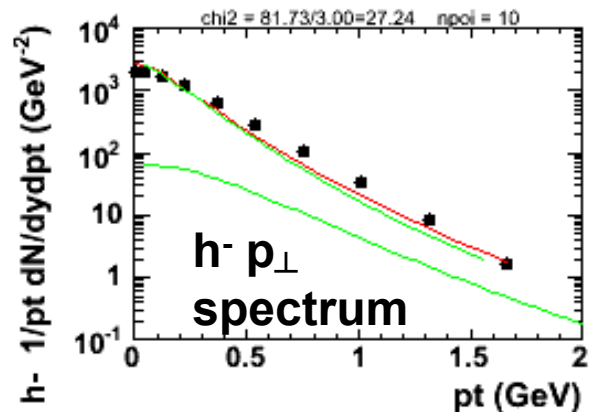


# $T - \rho$ contours

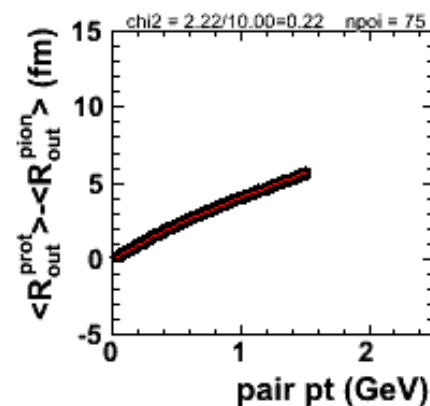
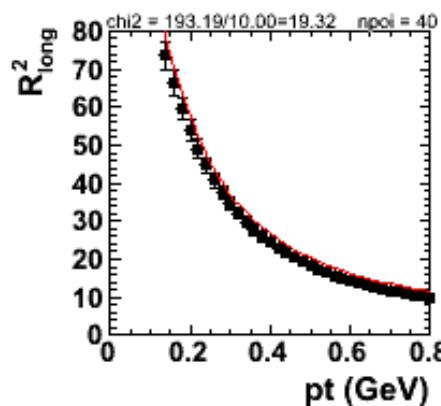
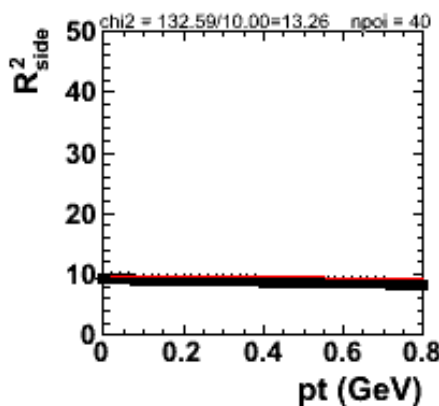
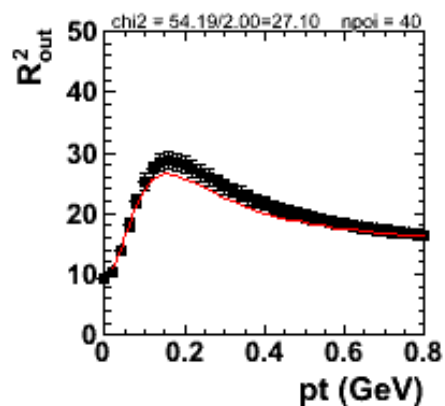
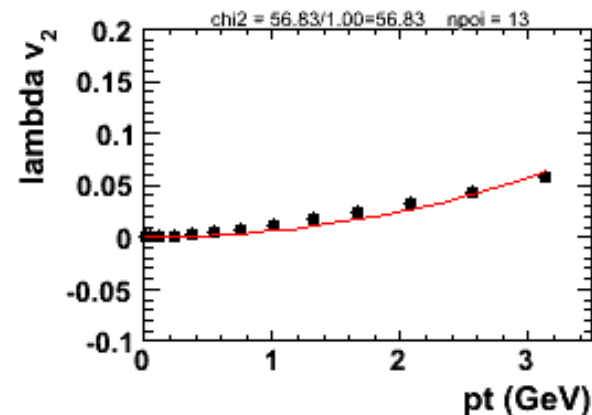
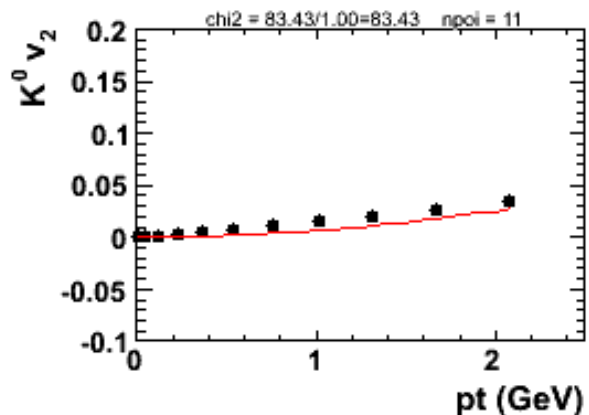
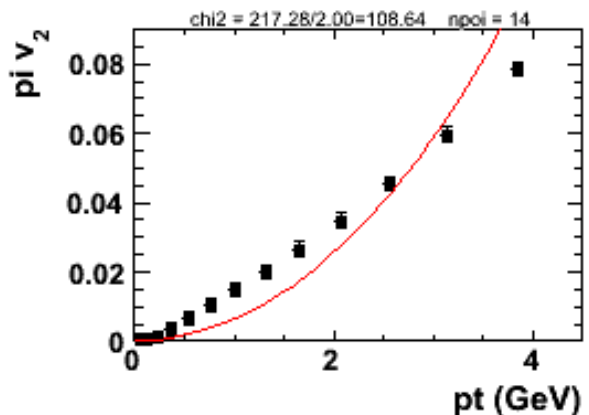
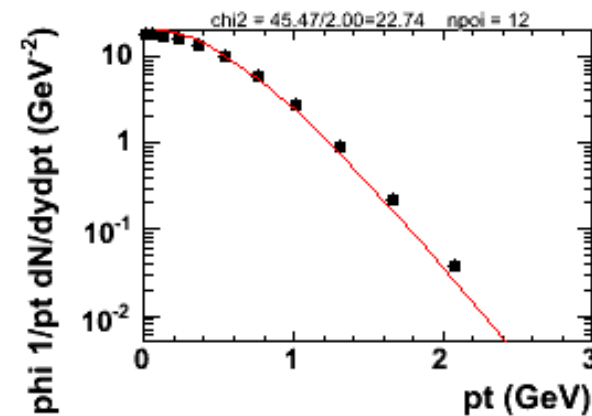
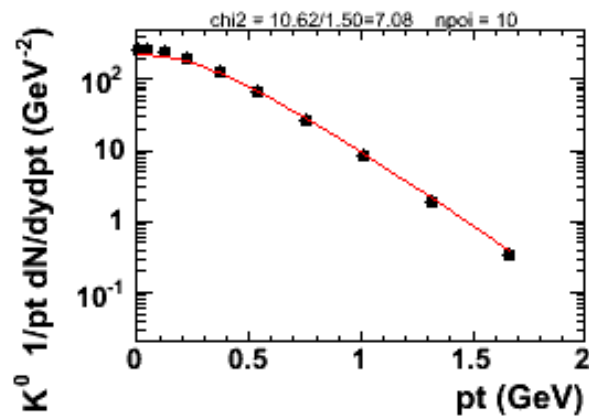
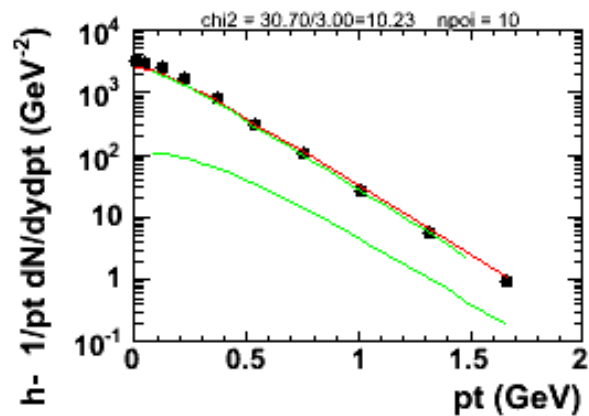


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# hydro 120 MeV (points) and blast as=0.3 (lines)

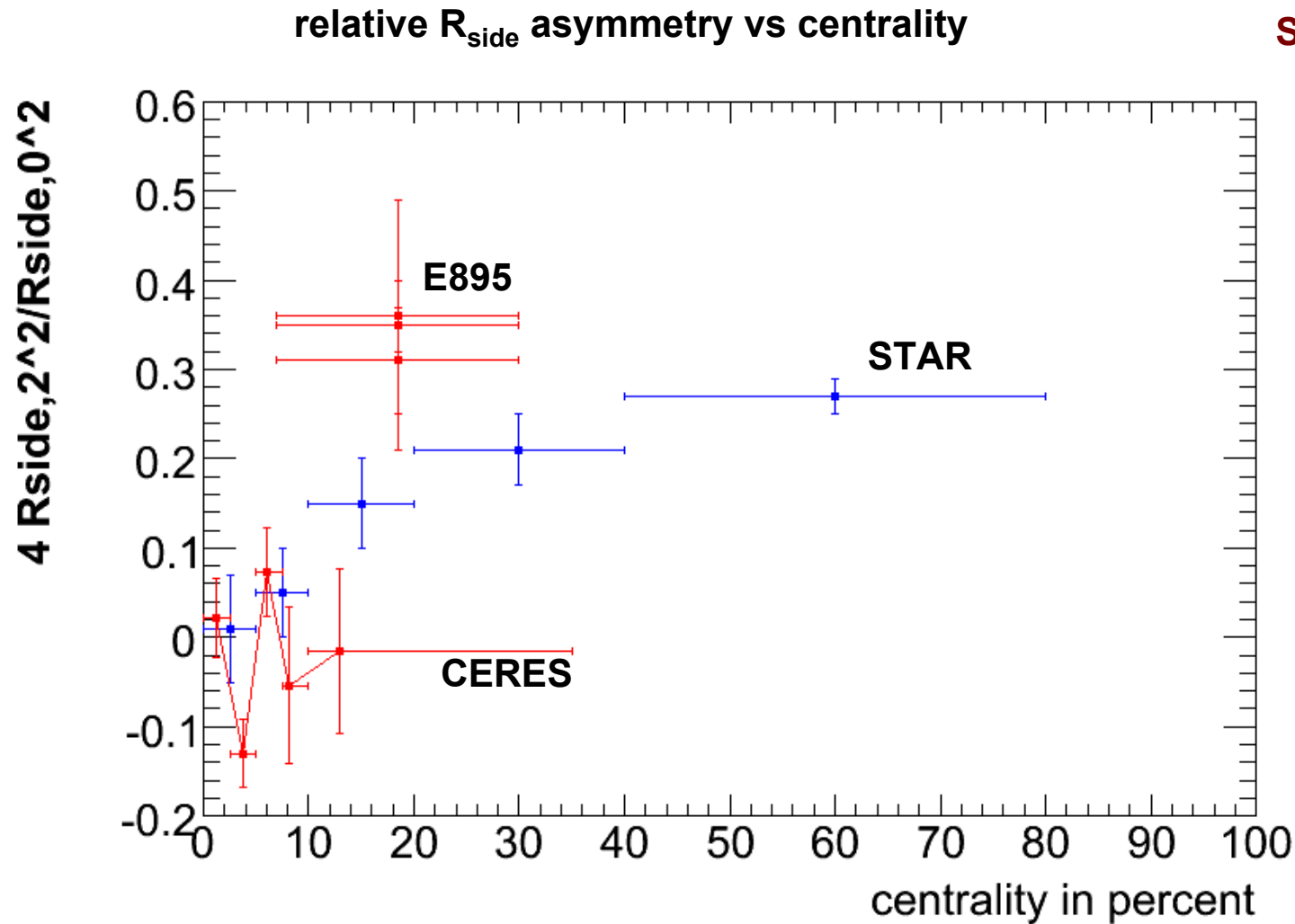


# hydro 160 MeV (points) and blast as=0.3 (lines)



# Source anisotropy from HBT

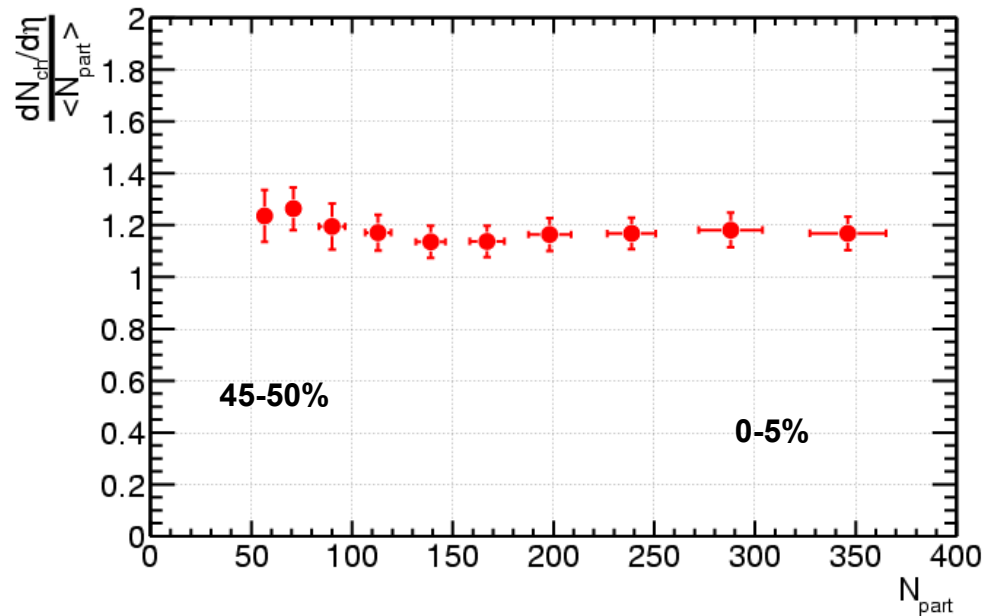
E895 PLB 496 (2000) 1  
STAR nucl-ex/0312009



# charged particle multiplicity

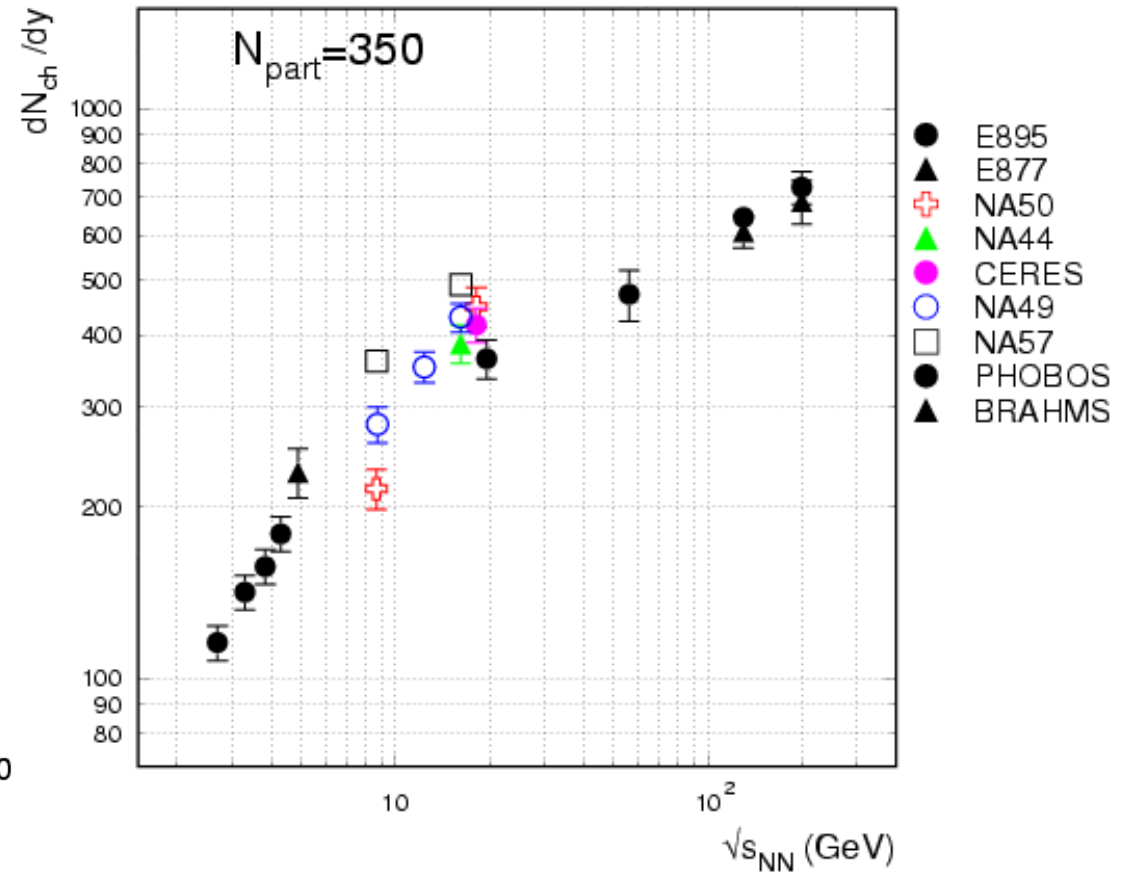
Pb+Au at 158 GeV per nucleon

charged particle multiplicity determined from hits in the two silicon detectors



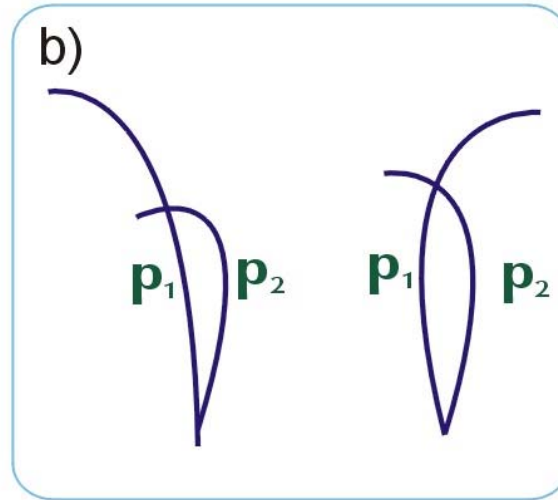
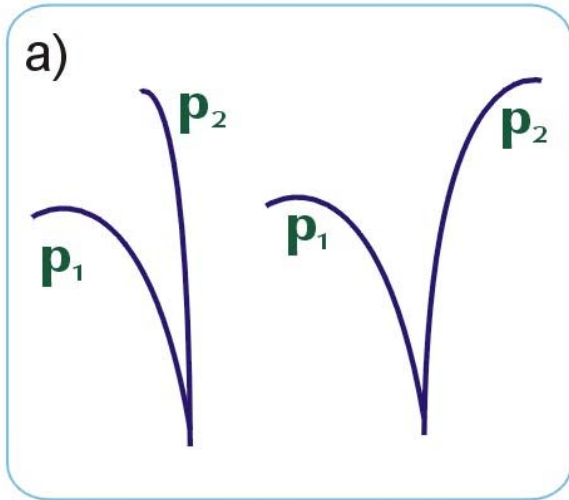
flat  $N_{ch}$  per participant

$dN_{ch}/d\eta$  in central collisions of Au or Pb  
compilation by A. Andronic

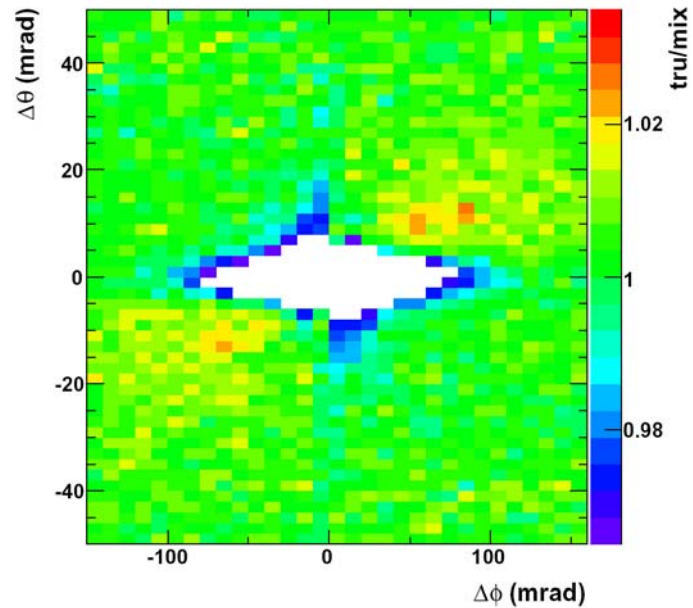
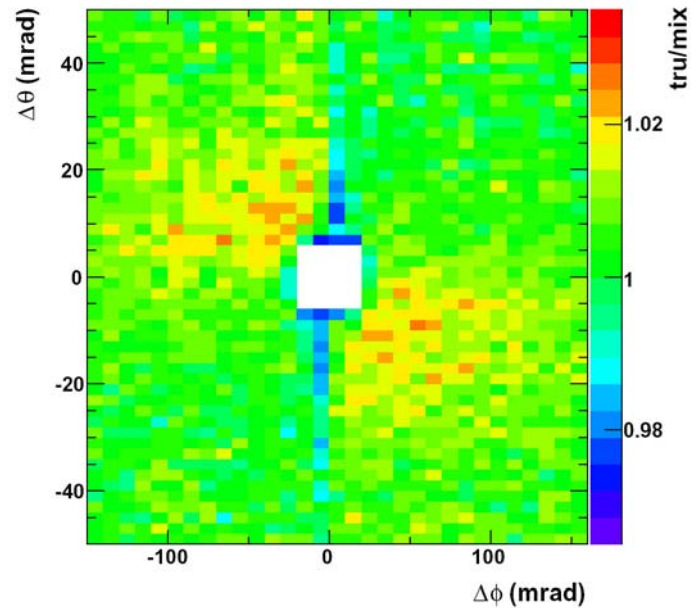


good agreement in  $dN_{ch}/d\eta$  between CERES, NA49, NA50, and NA44

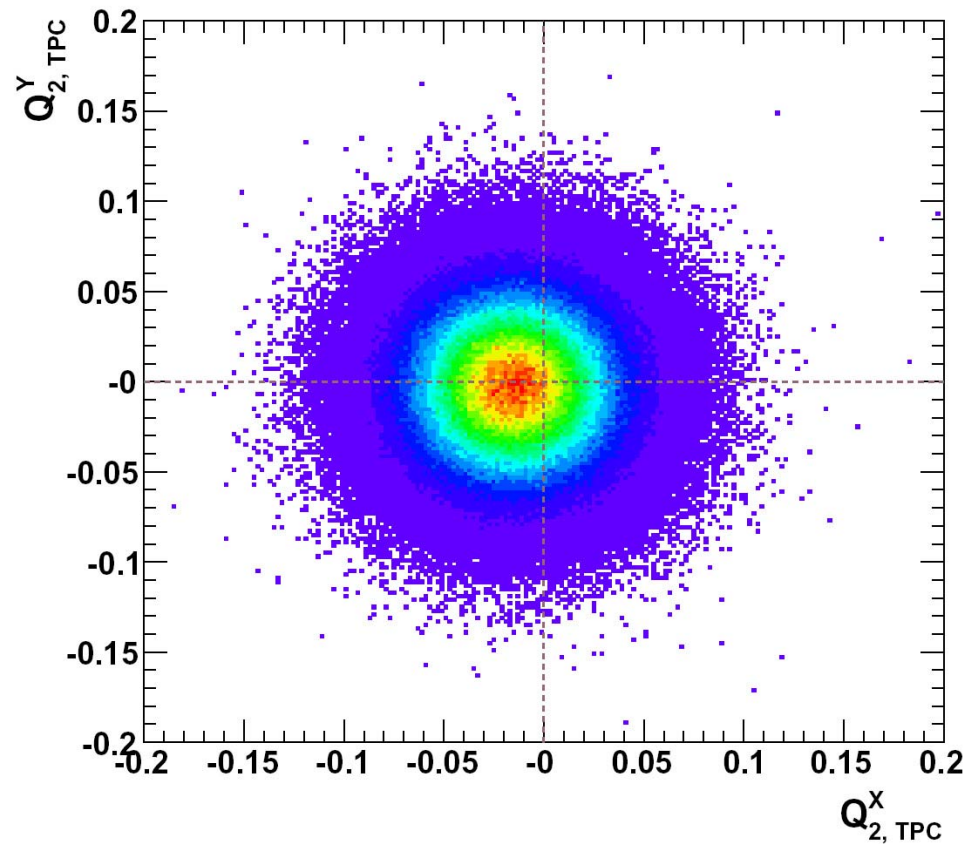
# two-track cut



Different cuts needed for the two topologies: sailor and cowboy



# determination of the reaction plane



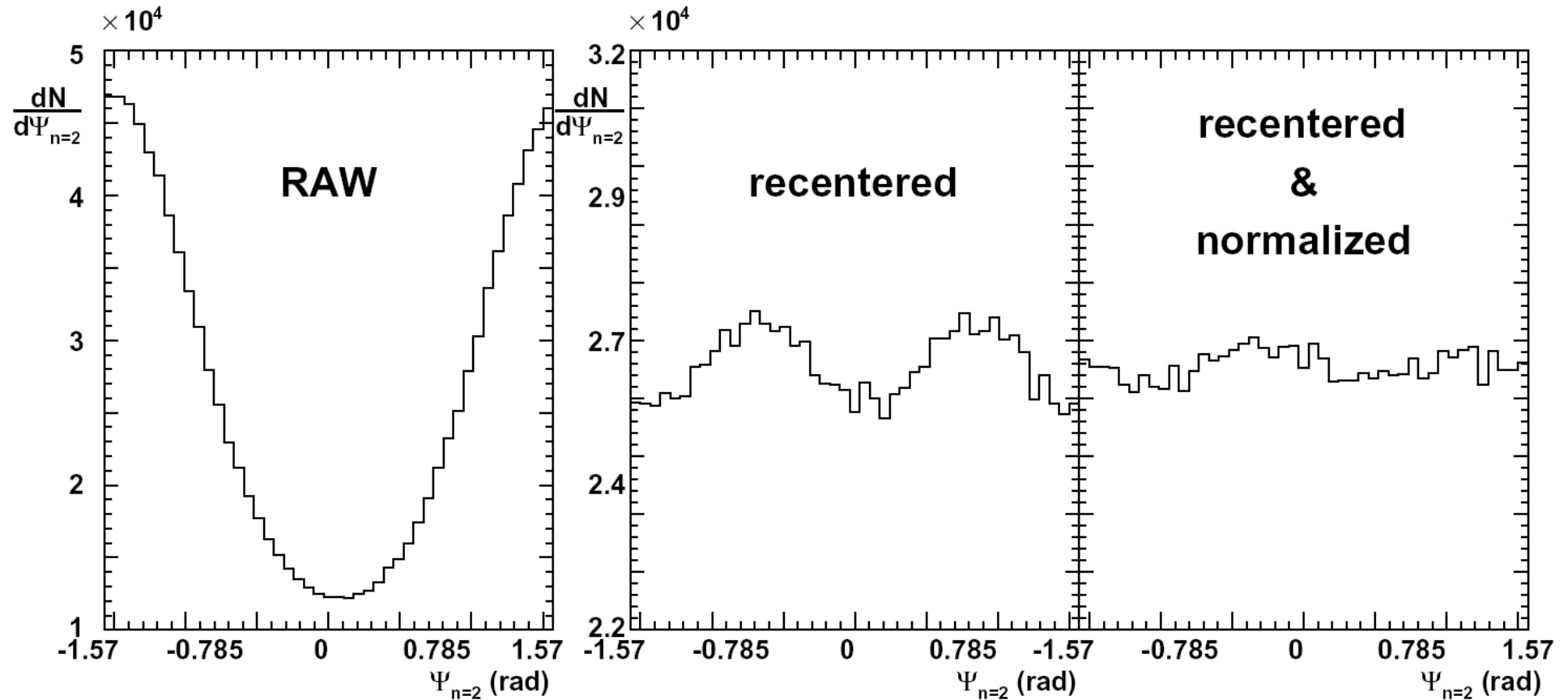
$$Q_2^X = \sum_i p_t \cdot \cos(2\varphi_i)$$

$$Q_2^Y = \sum_i p_t \cdot \sin(2\varphi_i)$$

$$\Phi_{RP} = \frac{1}{2} \arctan\left(\frac{Y_2}{X_2}\right)$$

# distribution of the reaction plane angle

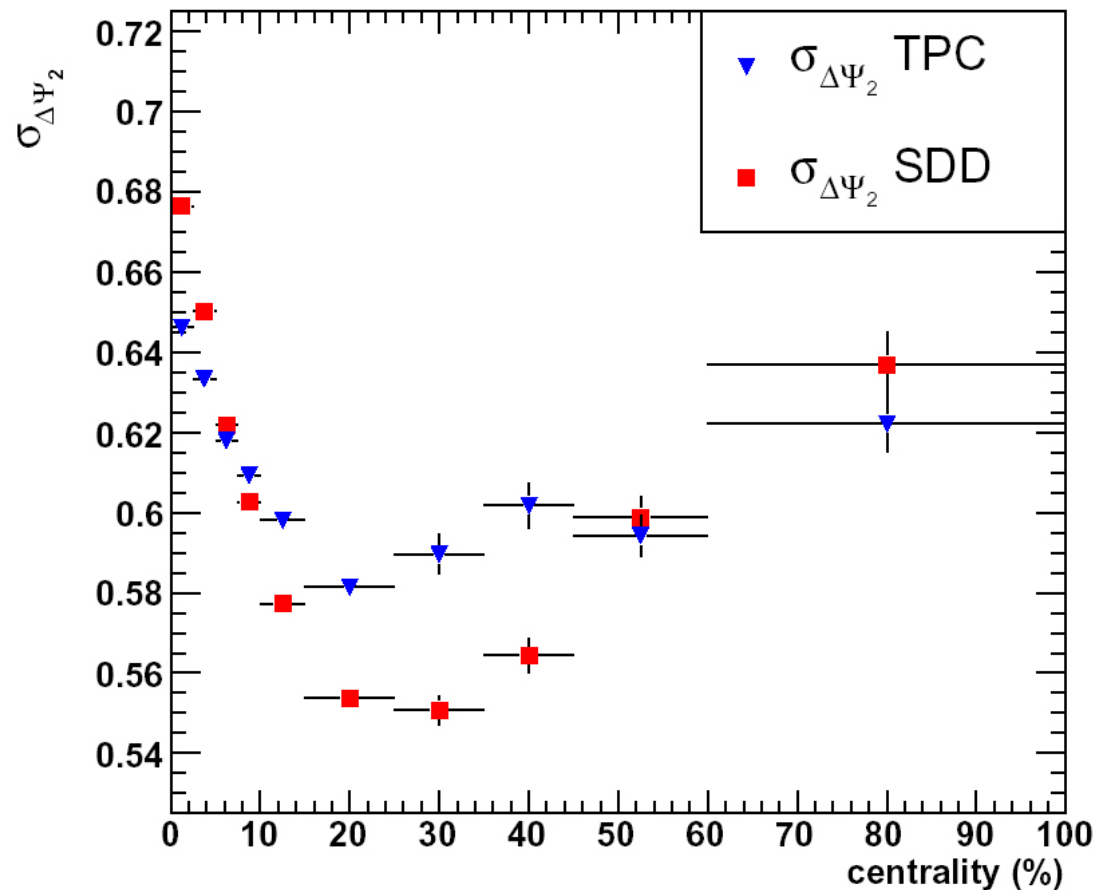
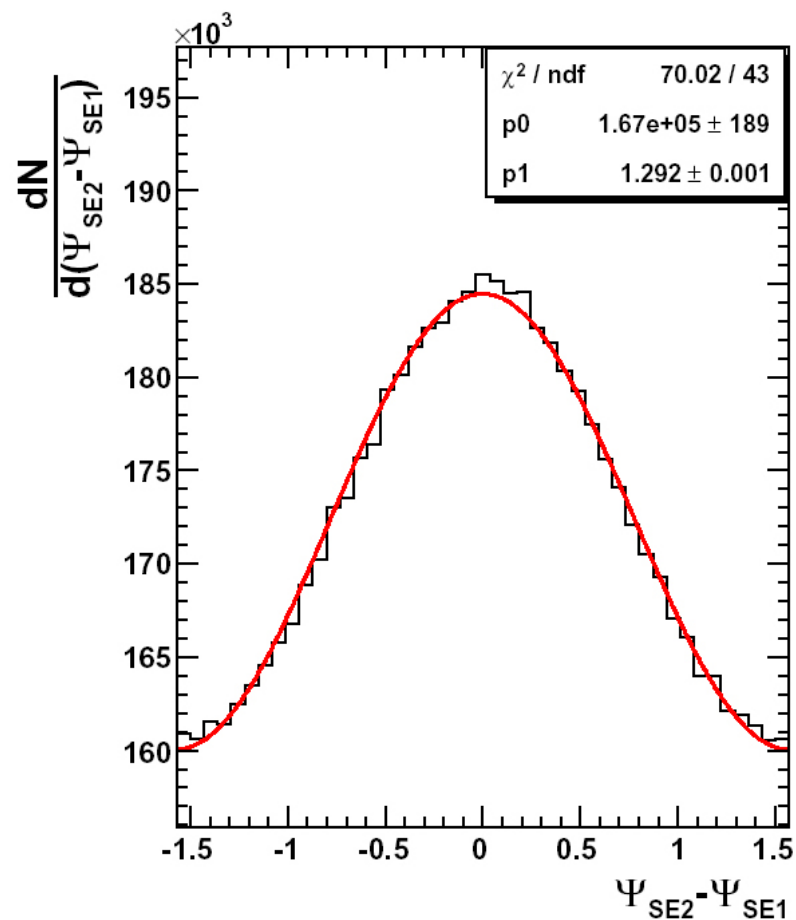
D. Antonczyk





# resolution of the reaction plane

D. Antonczyk



resolution  $31^\circ - 38^\circ$  (depending on centrality)