

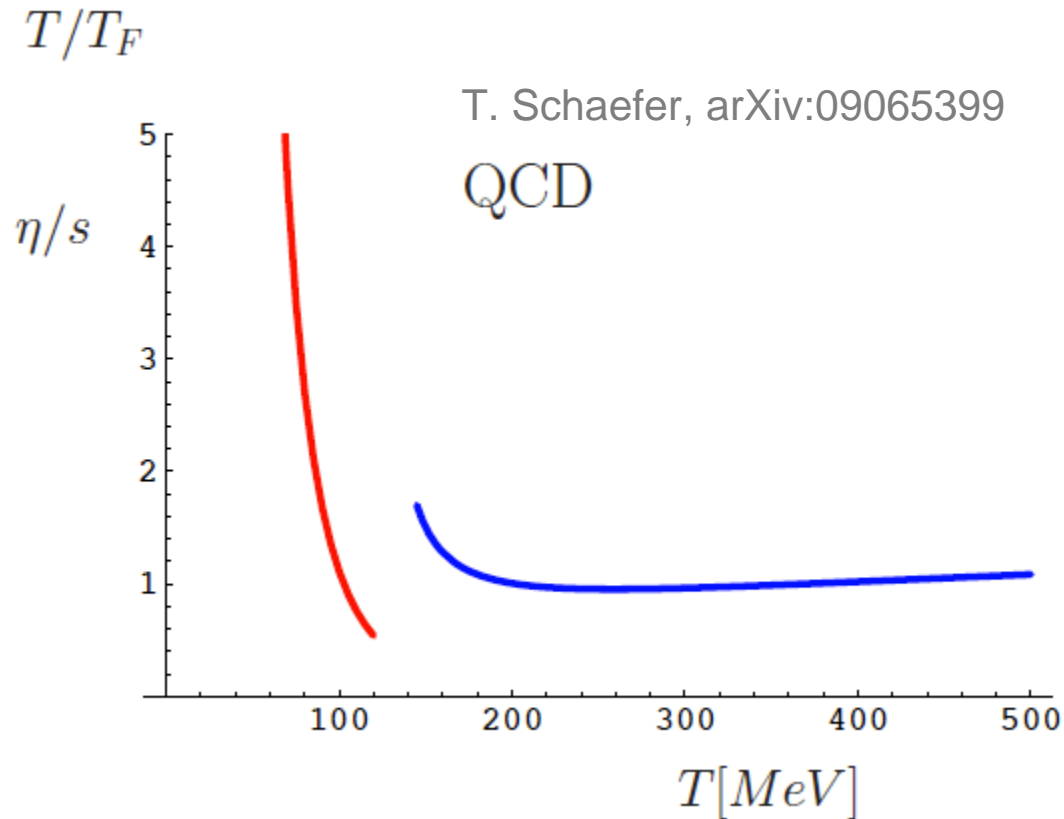
Viscosity and HBT

*Dariusz Miśkowiec, GSI Darmstadt
WPCF2009, CERN, 15-Oct-2009*

- ⊗ attempt of CERES to extract η/s from $R_{\text{long}}(\mathbf{k}_t)$
- ⊗ problems with this approach
- ⊗ other approaches?

prerequisites: R_{out} , R_{side} , R_{long} , η/s , v_2 , m_t

Viscosity in nuclear collisions – what to expect



- ☼ η/s reaches minimum near the critical point
- ☼ at the critical point it diverges
- ☼ high viscosity at low energies

Viscosity in nuclear collisions - observables

finite viscosity reduces velocity gradients



less in-plane, more out-of-plane expansion

⊗ reduced v_2

less longitudinal, more transverse expansion

⊗ narrower dN/dy distributions

⊗ harder p_t spectra

⊗ reduced R_{long}

⊗ reduced R_{out}

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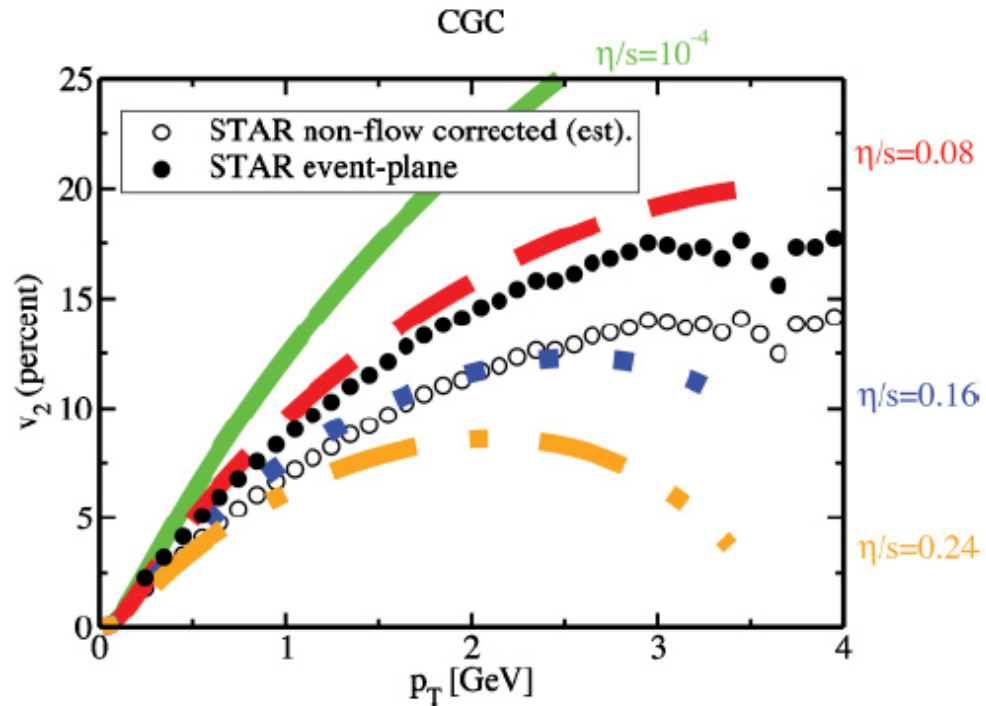
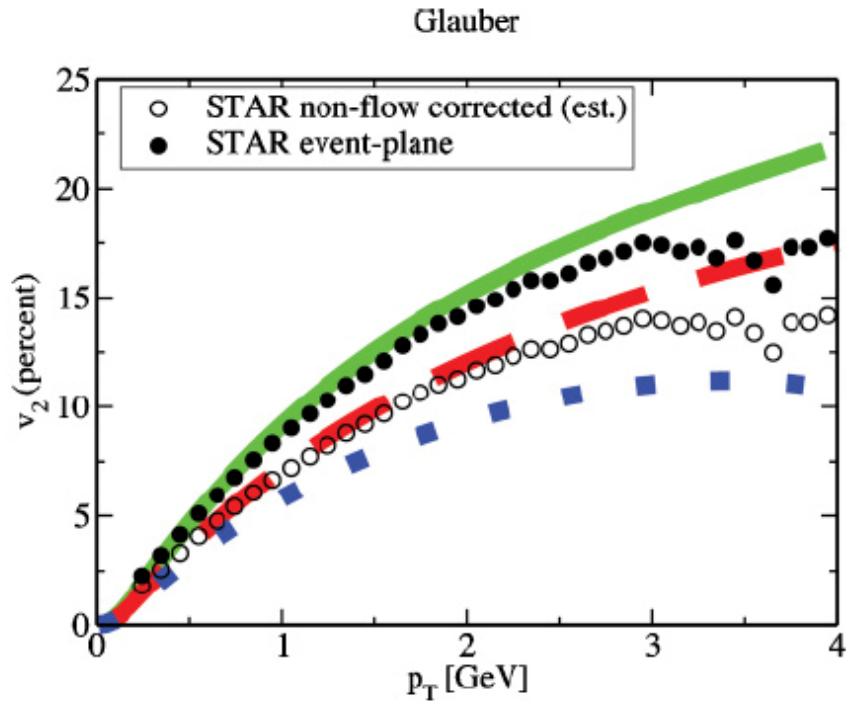
Viscosity via v_2

| | η/s |
|------------------------|-----------------|
| 🌐 PRL 99 (2007) 172301 | 0.03, 0.08 |
| 🌐 PRC 78 (2008) 034915 | 0.10 ± 0.13 |
| 🌐 PRL 98 (2007) 092301 | 0.1 |
| 🌐 PRC 76 (2007) 024905 | 0.19, 0.11 |
| 🌐 arXiv:0901.0460 | 0.15 ± 0.6 |

result close to the lower limit of $\eta/s = 0.08$

Viscosity via v_2

Luzum and Romatschke, PRC 79, 039903 (2009)



result depends on the assumed initial conditions

Viscosity in nuclear collisions - observables

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R_{long} basics

Makhlin-Sinyukov

$$R_{long} = \tau_f \sqrt{\frac{T}{m_t}}$$

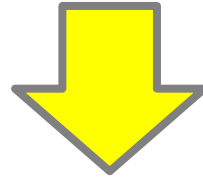
Herrmann-Bertsch

$$R_{long} = \tau_f \sqrt{\frac{T}{m_t} \frac{K_2(m_t/T)}{K_1(m_t/T)}}$$

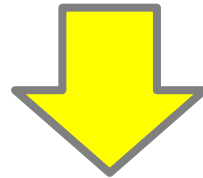
$\tau_f \sim$ inverse of the longitudinal Hubble constant

How finite viscosity affects R_{long}

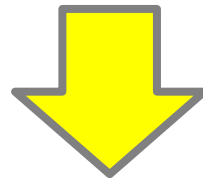
enhanced transverse expansion



reduced lifetime



reduced longitudinal length at freeze-out



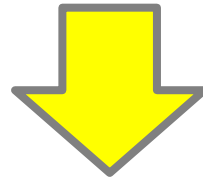
smaller R_{long}

How finite viscosity affects R_{long}

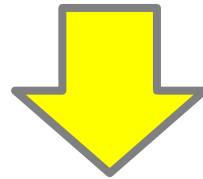
enhanced transverse expansion



reduced lifetime



~~reduced longitudinal length~~ at freeze-out
larger Hubble constant



smaller R_{long}

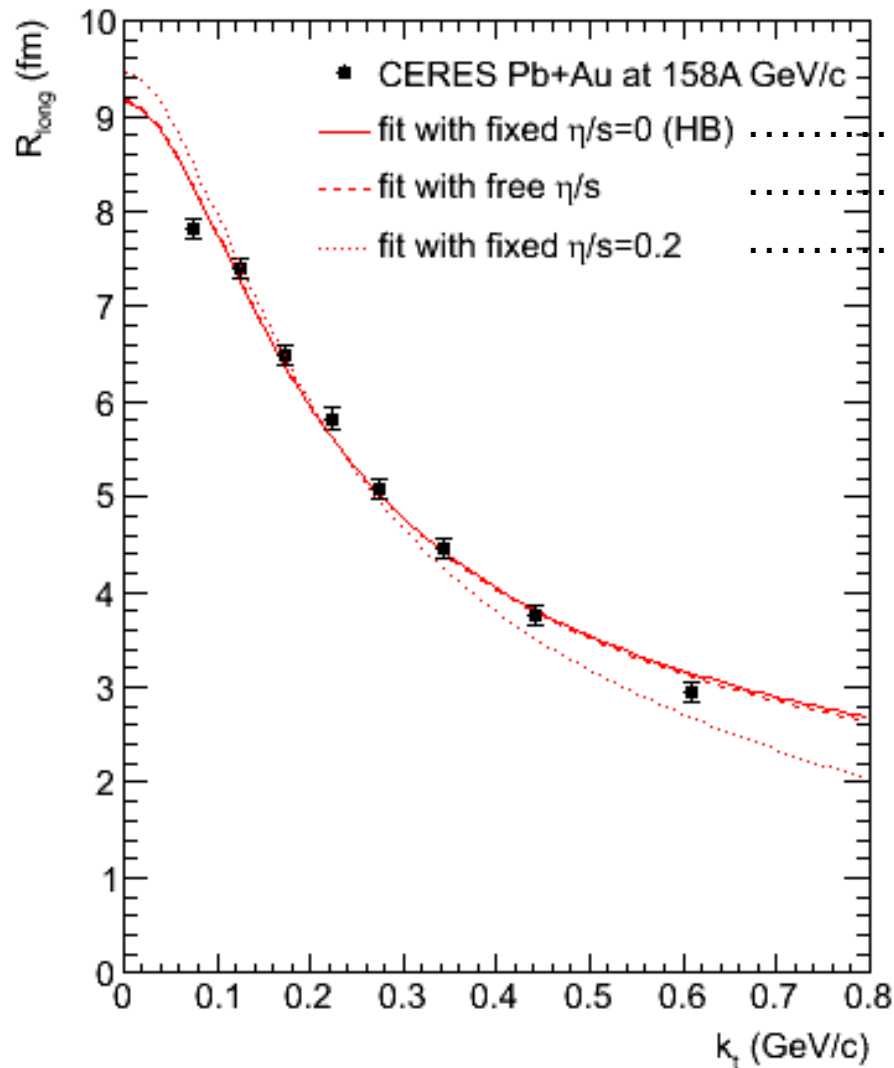
Effect of viscosity on R_{long} quantitatively

viscous correction, D. Teaney, PRC 68, 034913 (2003)

$$\frac{\delta R_L^2}{(R_L^2)^{(0)}} = -\frac{\Gamma_s}{\tau} \left[\frac{6}{4} \frac{x K_3(x)}{K_2(x)} - x^2 \frac{1}{8} \left(\frac{K_3(x)}{K_2(x)} - 1 \right) \right], \quad \Gamma_s \equiv \frac{4}{3} \frac{\eta}{sT}$$

$$x \equiv \sqrt{m^2 + K_T^2} / T$$

Viscosity via R_{long} – fit to CERES data



$\tau_f = 6.3$ fm
 $\tau_f = 6.5$ fm $\eta/s = 0.02$
 $\tau_f = 8.0$ fm

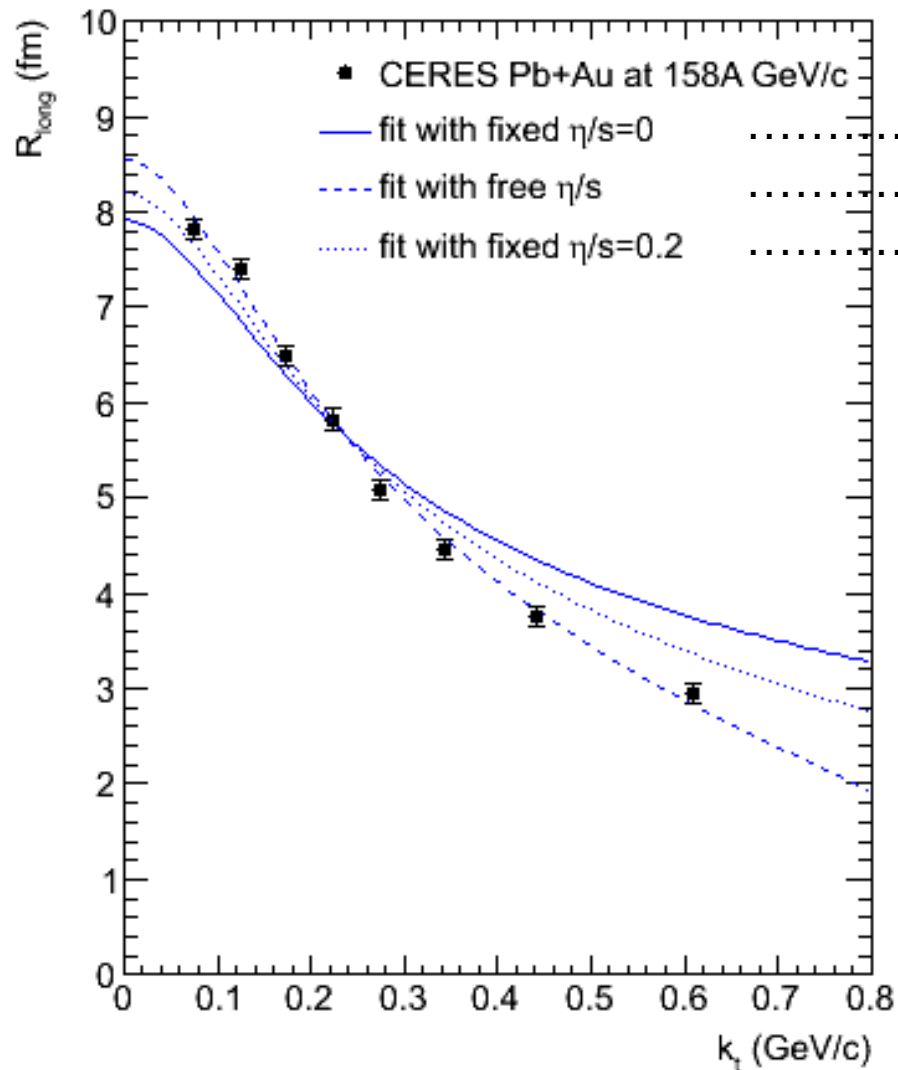
$T = 120$ MeV (fixed)

fit function:
Herrmann-Bertsch with viscous correction

$$\frac{\delta R_L^2}{(R_L^2)^{(0)}} = -\frac{\Gamma_s}{\tau} \left[\frac{6}{4} \frac{x K_3(x)}{K_2(x)} - x^2 \frac{1}{8} \left(\frac{K_3(x)}{K_2(x)} - 1 \right) \right]$$

**result: η/s below 0.1
(recall lower bound 0.08)**

Viscosity via R_{long} – fit to CERES data



..... $\tau_f = 8.5$ fm
 $\tau_f = 9.9$ fm $\eta/s = 0.42$
 $\tau_f = 9.2$ fm

$T = 120$ MeV (fixed)

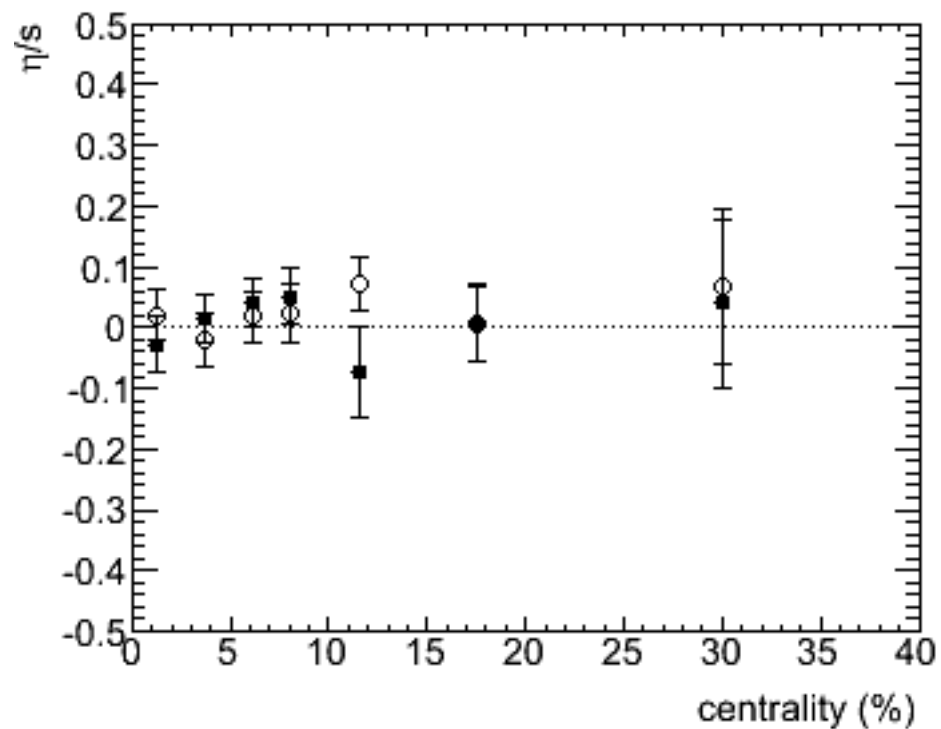
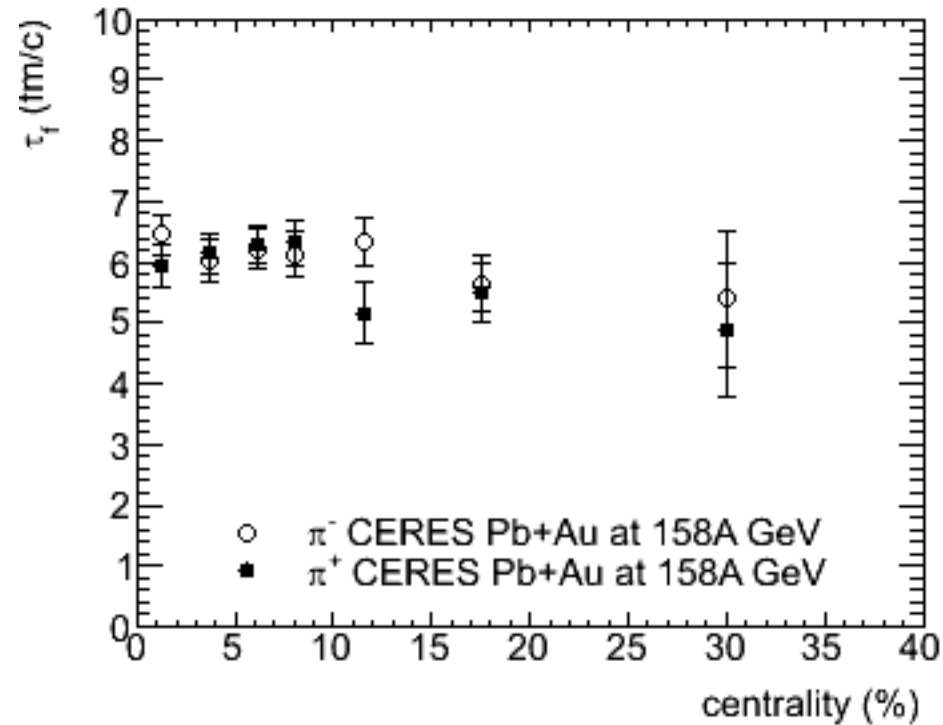
fit function:

Makhlin-Sinyukov with appr. visc. cor.

$$(R_L^2)^{(0)} + \delta R_L^2 = \tau_o^2 \left(\frac{T}{m_T} - \frac{19}{16} \frac{\Gamma_s}{\tau_o} \right)$$

**very different result,
beware!**

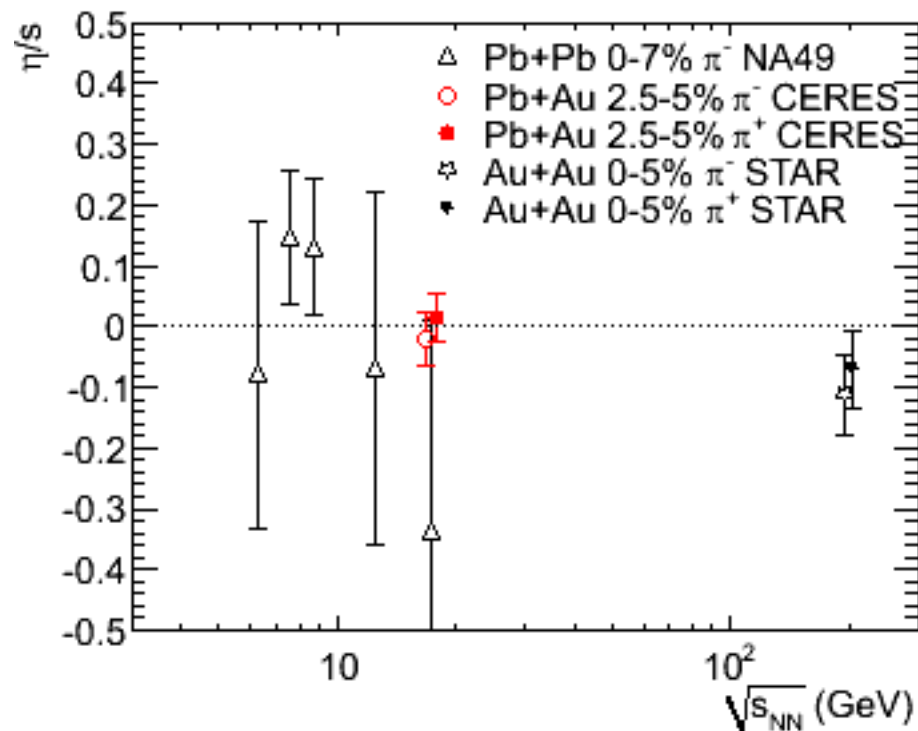
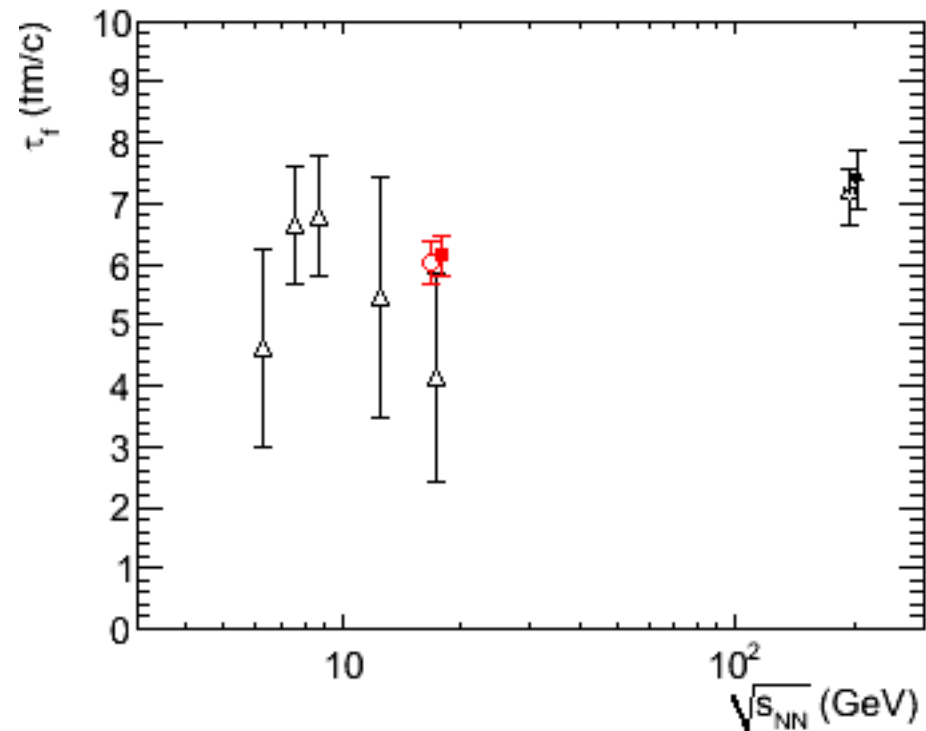
Viscosity via R_{long} – fit to CERES data



η/s is small for both charges and all centralities

Viscosity via R_{long} – fit to NA49, CERES, STAR data

CERES Collaboration, arXiv:0907.2799



η/s is small for all energies

Viscosity low at all energies? Why not!

N. Auerbach and S. Shlomo

“The η/s ratio in finite nuclei”

arXiv:0908.4441v1 [nucl-th], 31-Aug-2009

- 🌐 **giant resonance width** $\rightarrow \eta \approx 0.5-2.5 \times 10^{-23} \text{ MeV fm}^{-3} \text{ s}$
- 🌐 **fission** $\rightarrow \eta \approx 0.9-1.9 \times 10^{-23} \text{ MeV fm}^{-3} \text{ s}$
- 🌐 **Fermi gas of nucleons in Woods-Saxon well** $\rightarrow s$

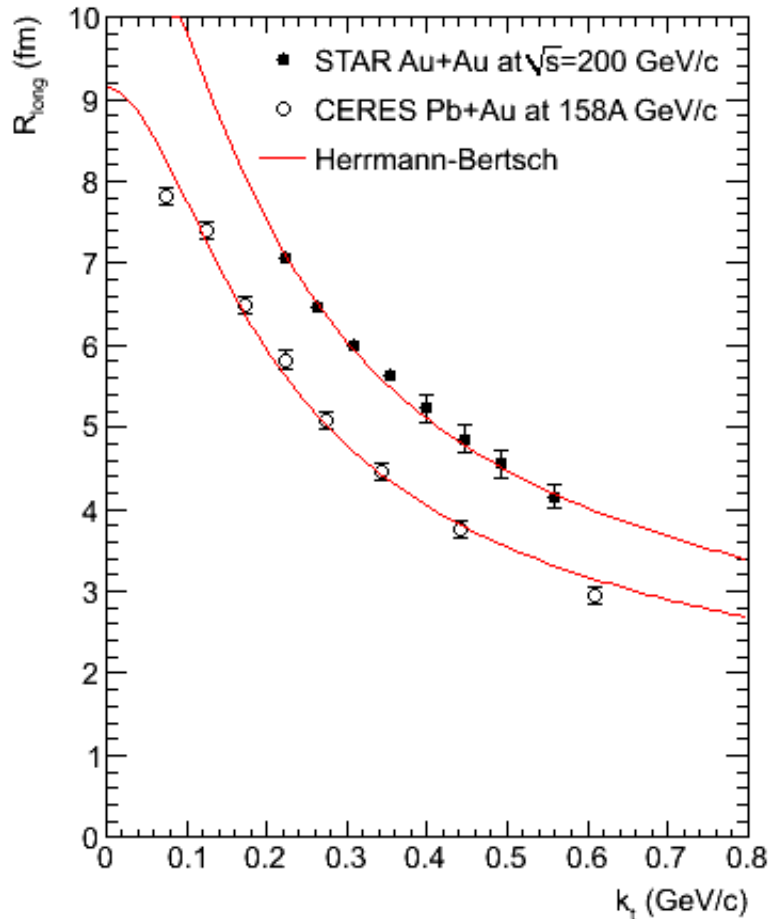
$\rightarrow \eta/s \sim 0.3-1.5$ for large nuclei
 $\eta/s \sim 0.2-1.0$ for small nuclei

However, serious problems in our analysis:

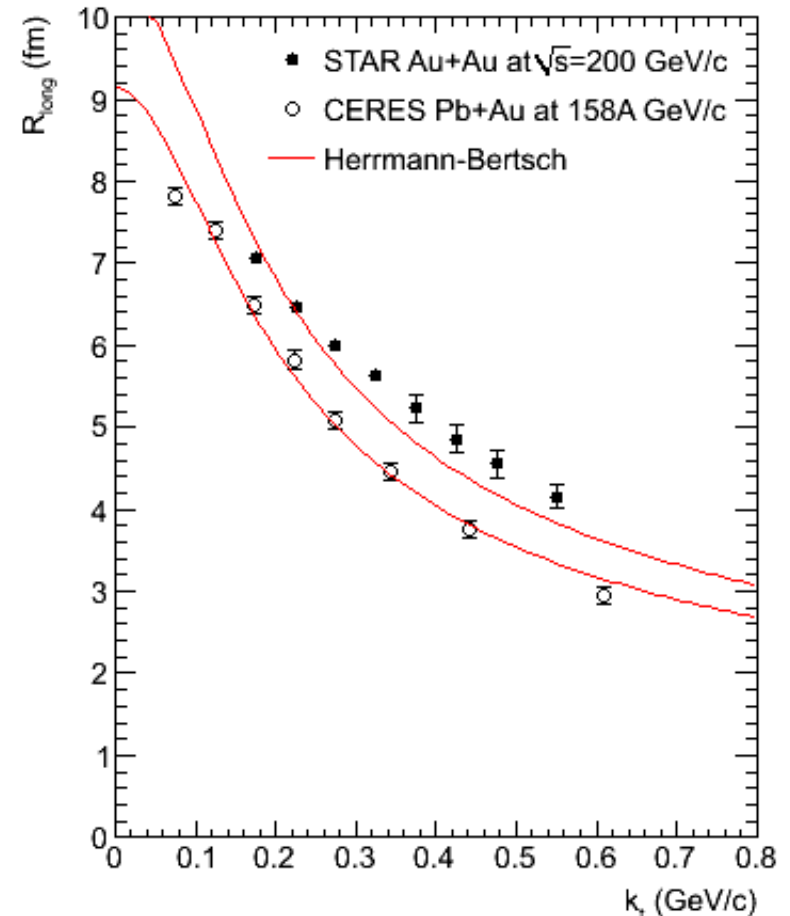
- ⊛ neglected transverse expansion
- ⊛ Teaney's formula accounts for the modified distribution at freeze-out but not for flow! (M. Lisa, U. Heinz)
- ⊛ even the freeze-out part is not clear:
 - Bożek/Wyskiel see no effect on HBT radii when using the same method with $\eta/s=0.16$
 - Song/Heinz get opposite modification of p_t spectra
- ⊛ last but not least:
my mistake when interpreting STAR data (m_t vs k_t)

mistake when interpreting STAR data (m_t vs k_t)

STAR points misplaced



STAR points placed correctly

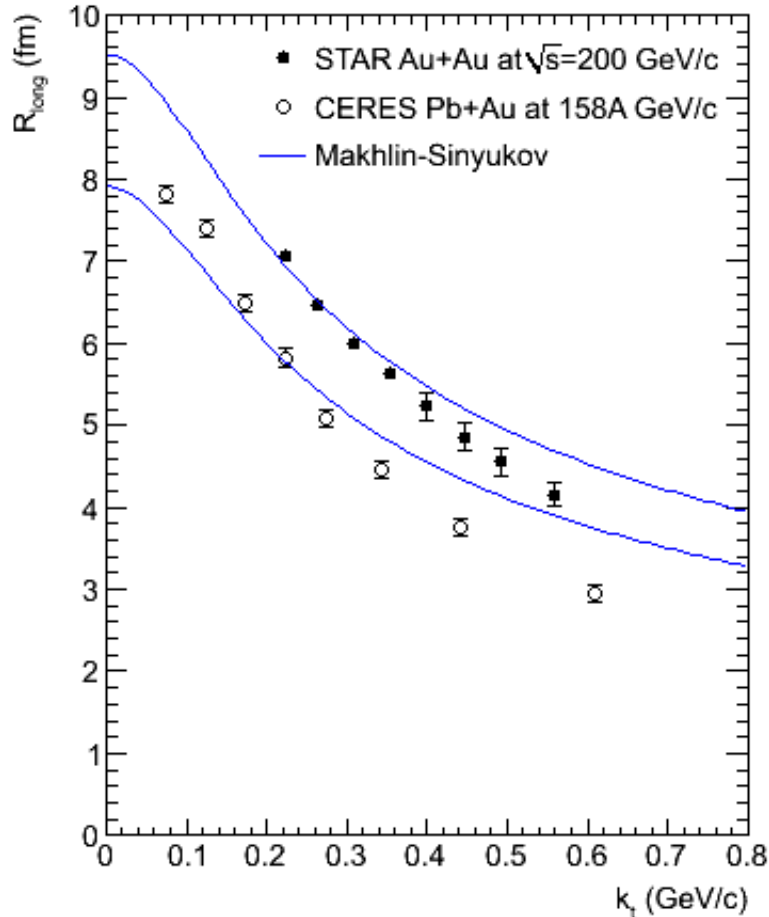


$$R_{long} = \tau_f \sqrt{\frac{T K_2(m_t/T)}{m_t K_1(m_t/T)}}$$

no room for viscosity, even the pure Herrmann-Bertsch curve is steeper than the data

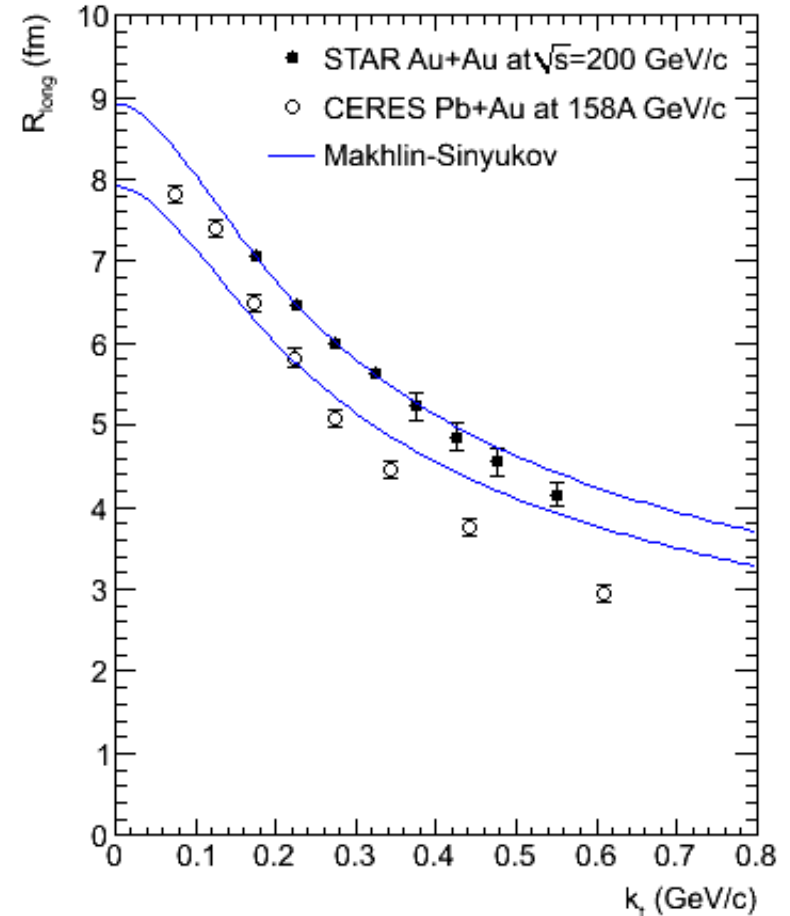
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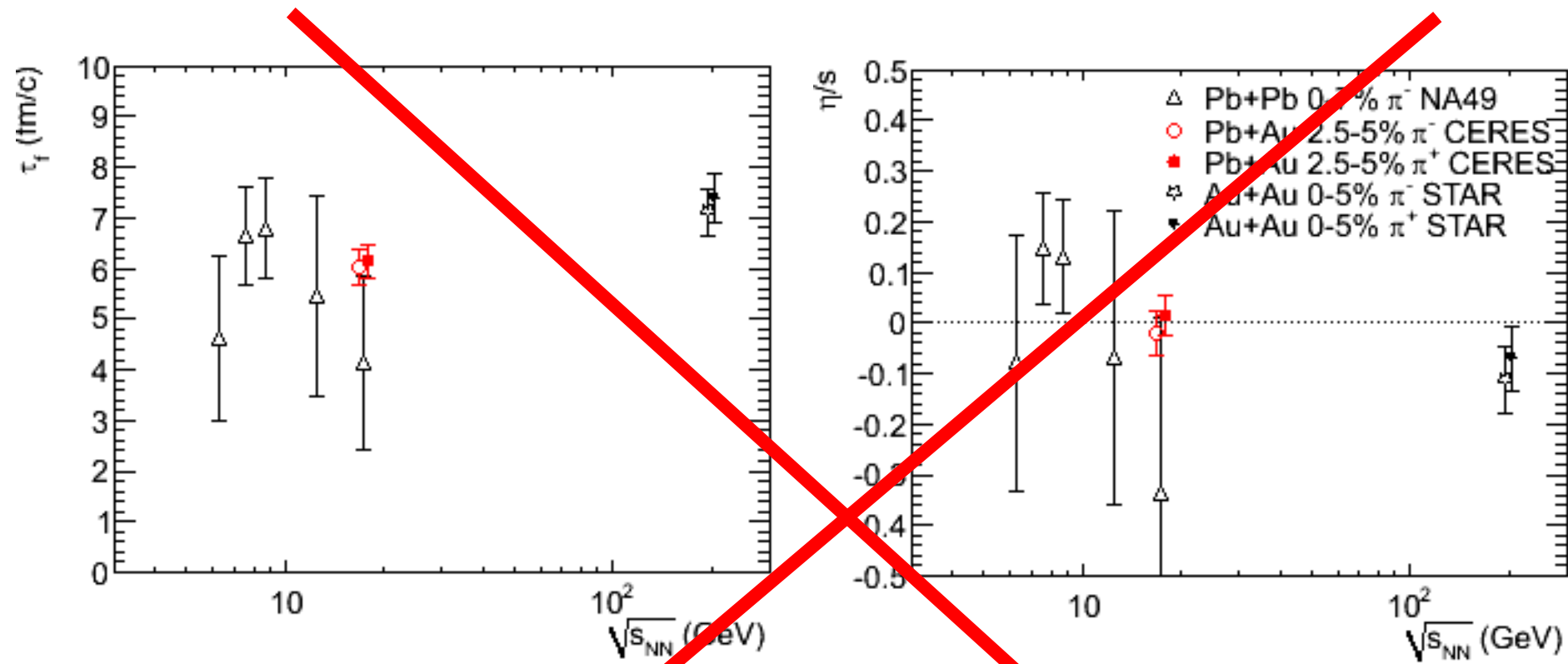
$$R_{long} = \tau_f \sqrt{\frac{T}{m_t}}$$

STAR points placed correctly



btw., Makhlin-Sinyukov fits much better...

Viscosity via R_{long} – fit to NA49, CERES, STAR data



η/s is small for all energies

Viscosity in nuclear collisions - observables

finite viscosity reduces velocity gradients



less in-plane, more out-of-plane expansion

☢ reduced v_2

less longitudinal, more transverse expansion

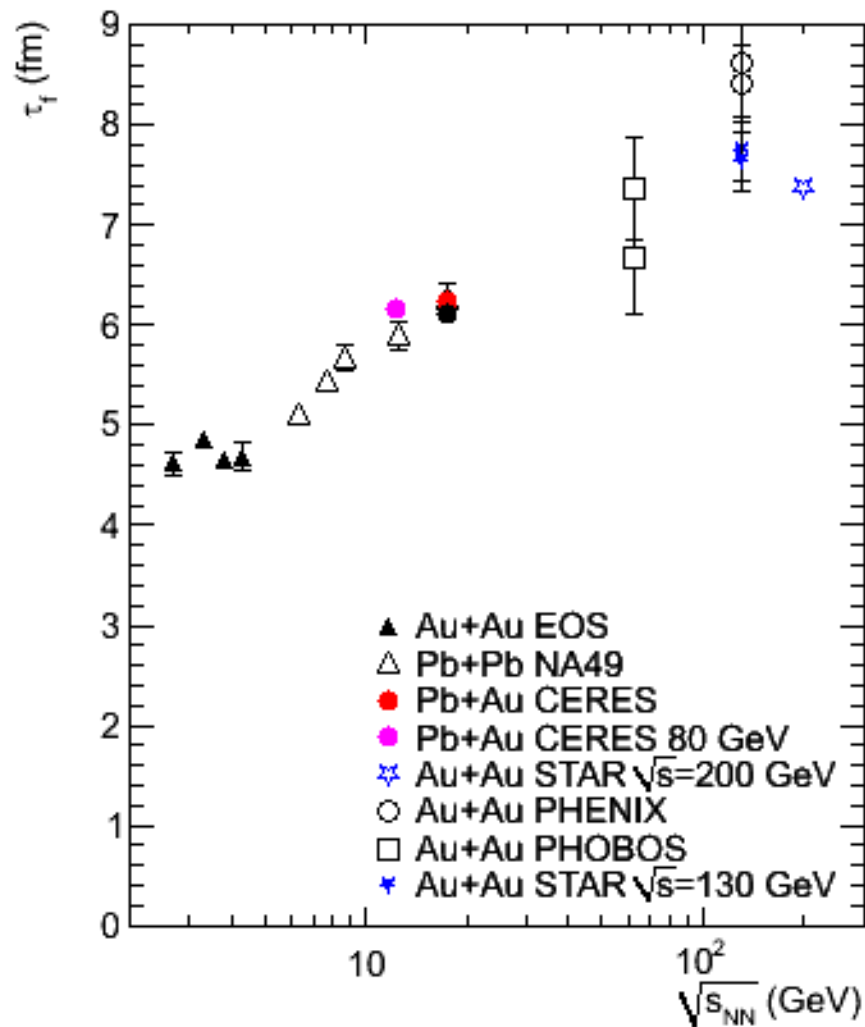
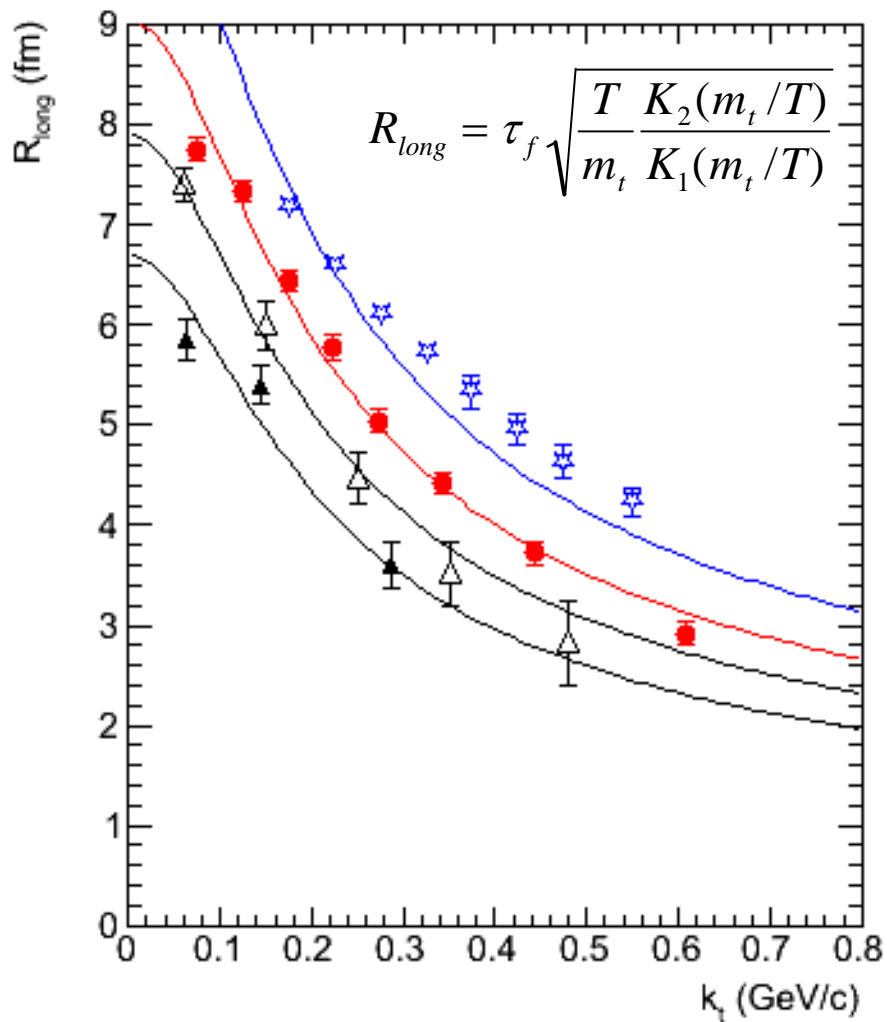
☢ narrower dN/dy distributions

☢ harder p_t spectra

☢ reduced R_{long}

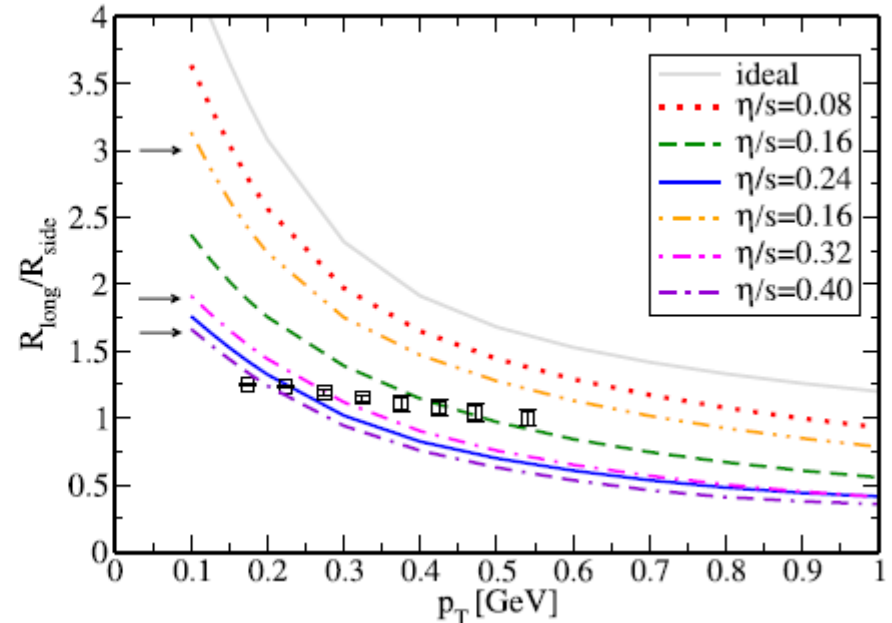
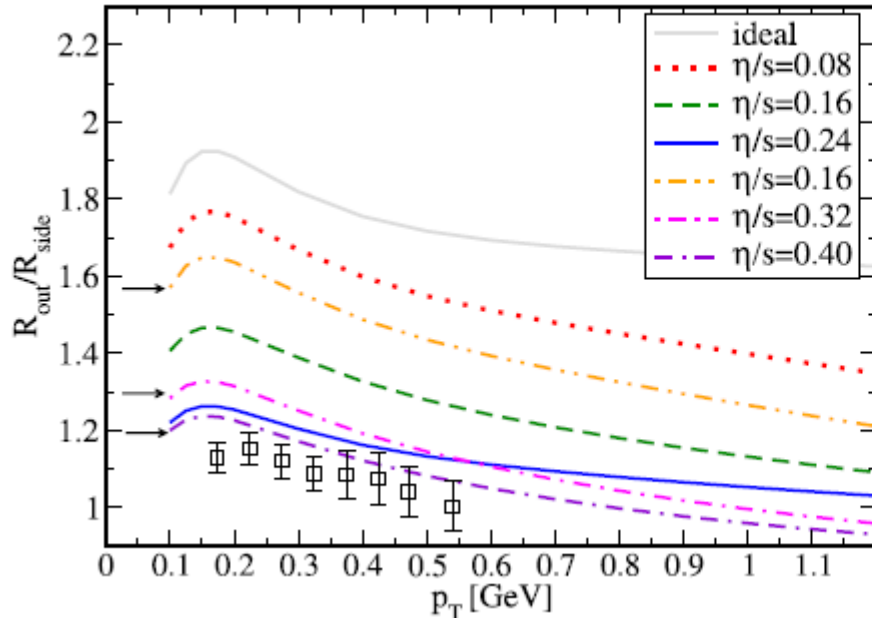
☢ reduced R_{out}

R_{long} systematics



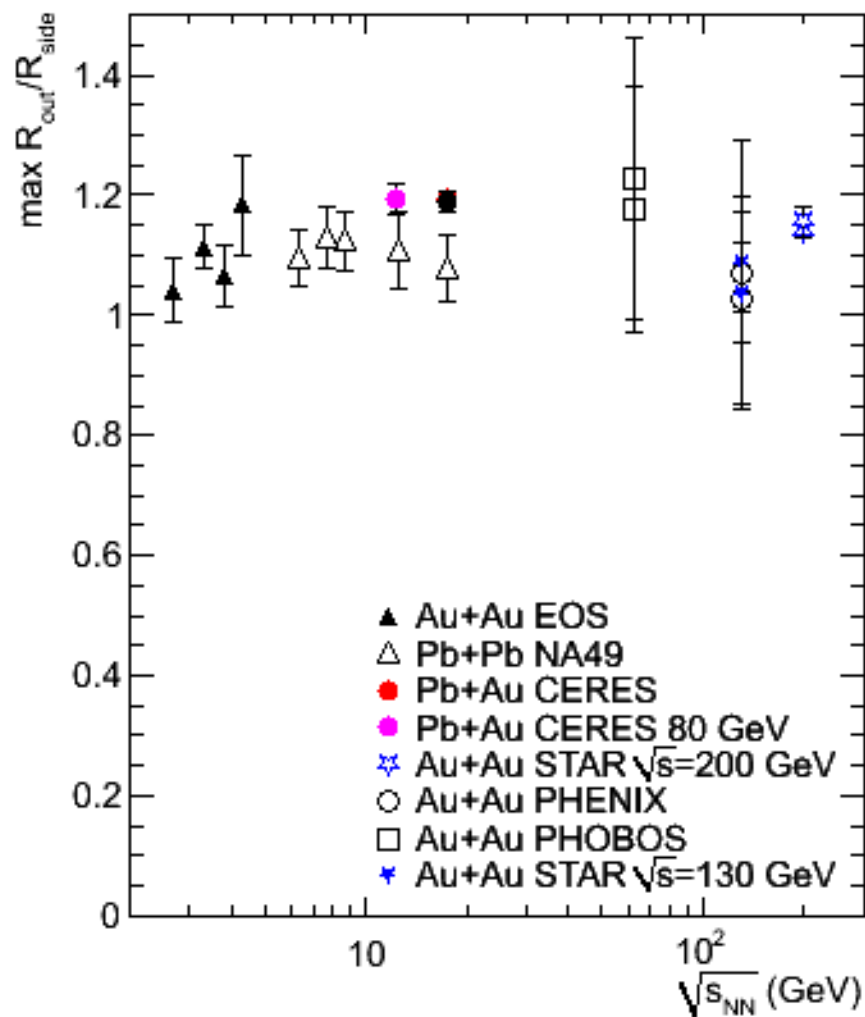
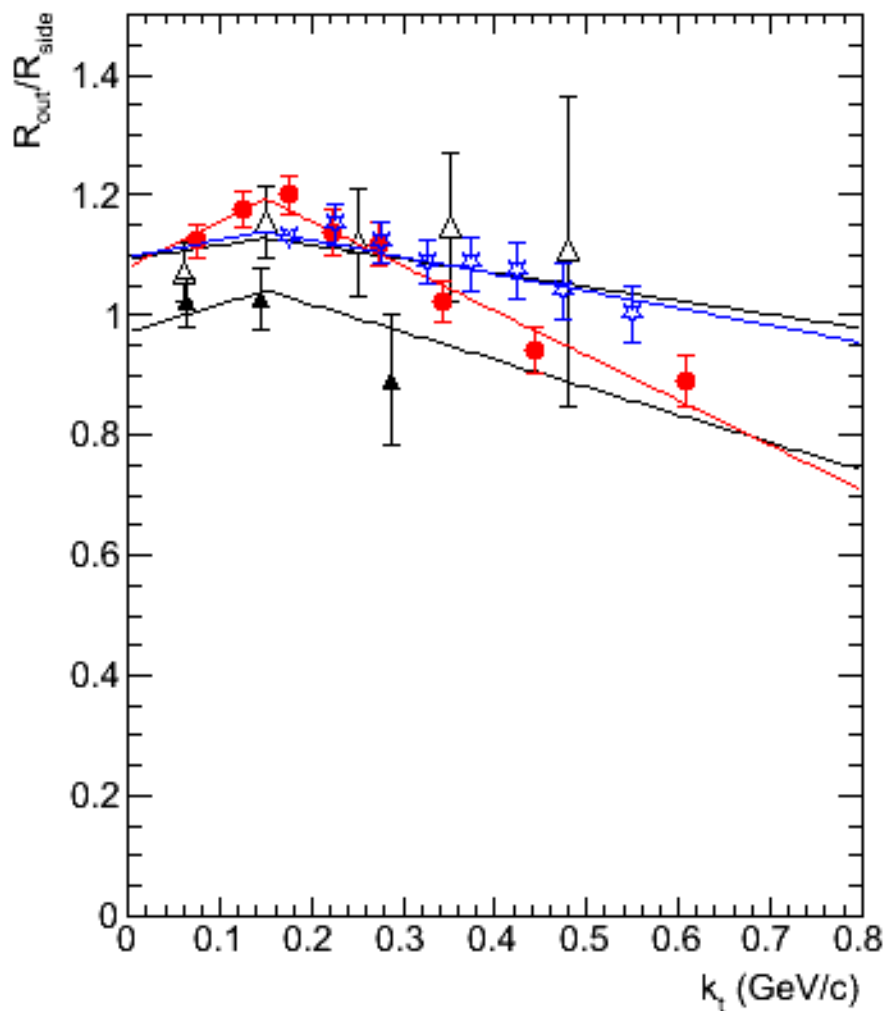
Viscosity via R_{out}/R_{side} and R_{long}/R_{side} ratios

P. Romatschke, Eur. Phys. J C 52 (2007) 203



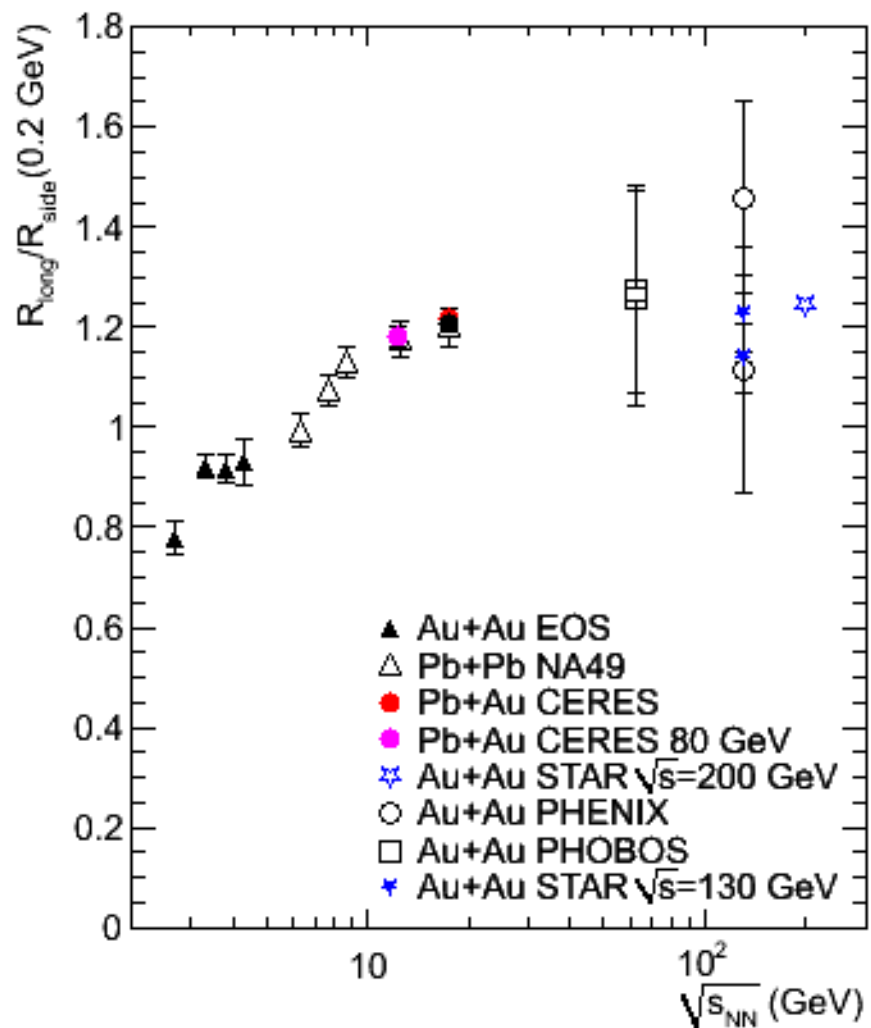
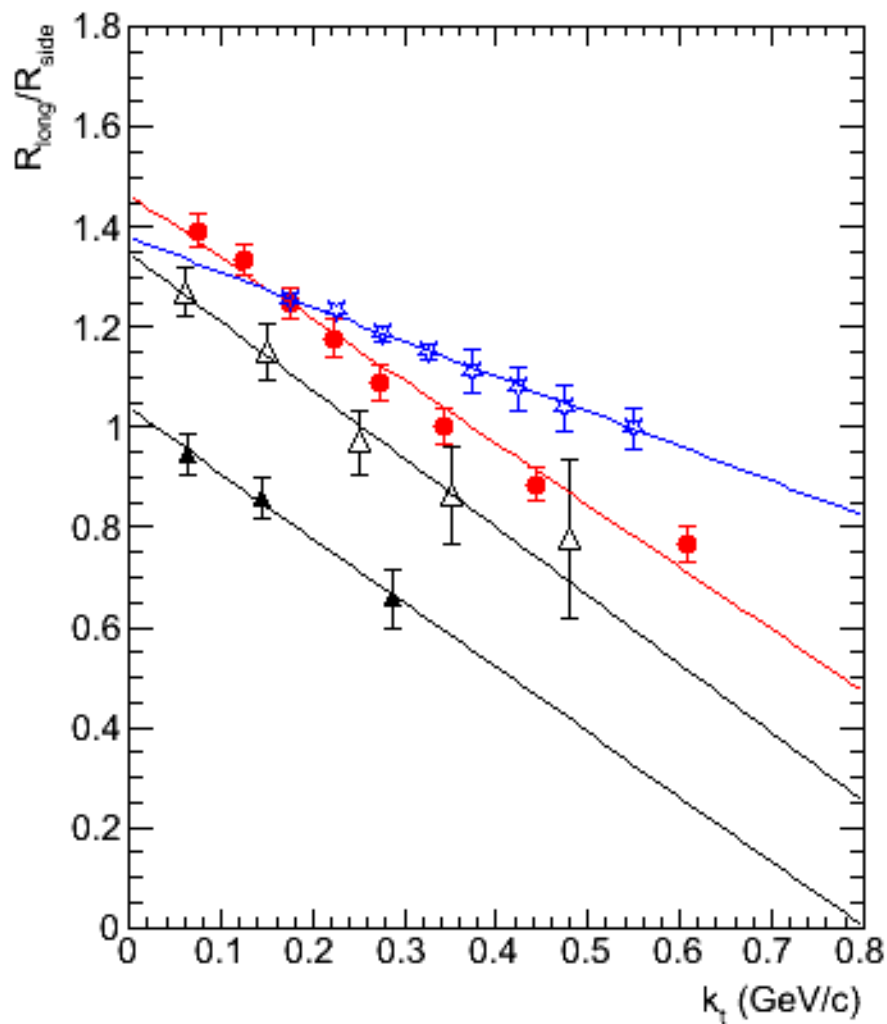
R_{out}/R_{side} and R_{long}/R_{side} ratios are sensitive to viscosity

R_{out}/R_{side} systematics



R_{out}/R_{side} ratio is constant from AGS to RHIC

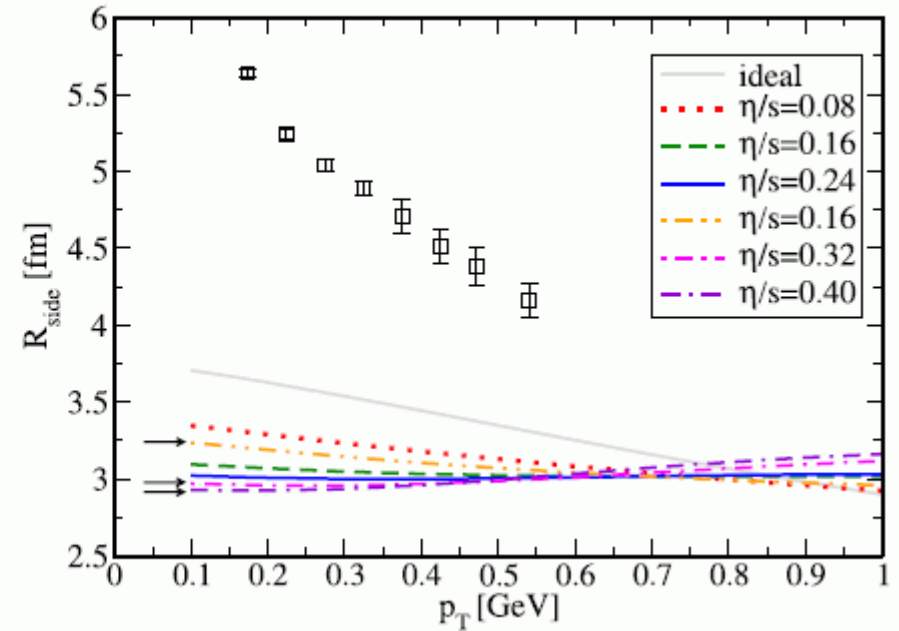
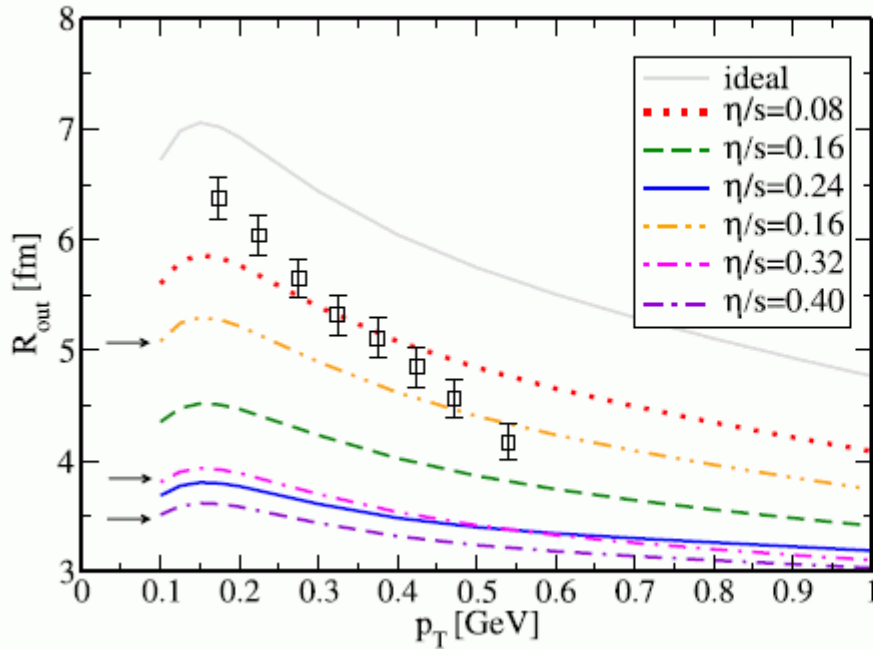
$R_{\text{long}}/R_{\text{side}}$



$R_{\text{long}}/R_{\text{side}}$ ratio is constant from top SPS to RHIC

Viscosity via R_{out}/R_{side} and R_{long}/R_{side} ratios

P. Romatschke, *Eur. Phys. J C* 52 (2007) 203



Quantitatively:

no statement can be made given the calculation does not reproduce the HBT radii but only their ratios

Qualitatively:

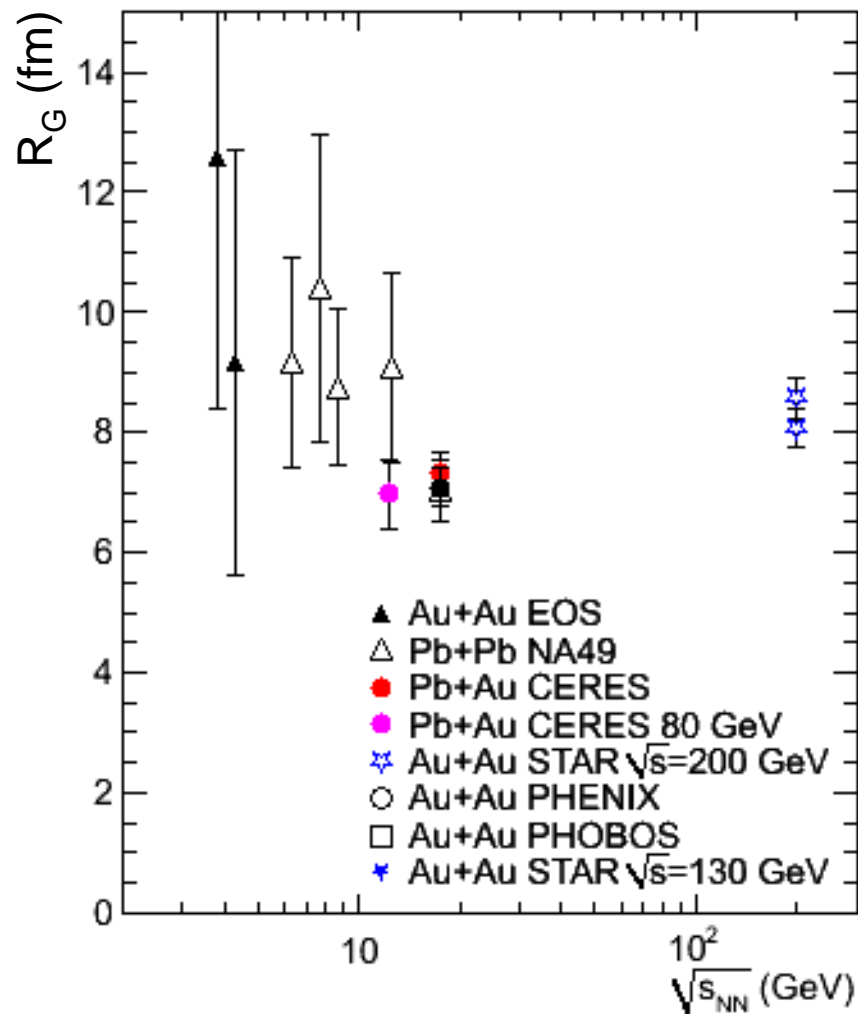
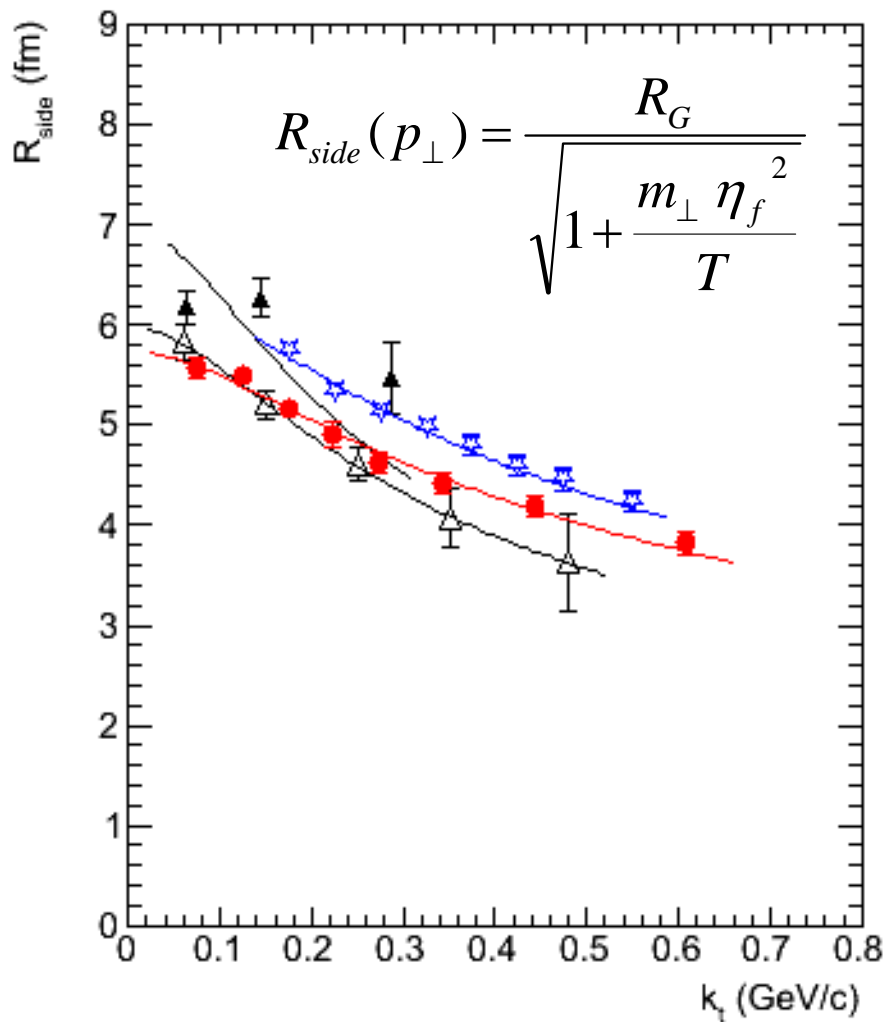
no indication of RHIC viscosity being lower than at SPS

summary

- 🚫 **our quantitative method was wrong for several reasons; the preprint will be withdrawn**
- 🚫 **however, the conclusion seems to hold:
no indication of increasing viscosity
when going from RHIC down to SPS**

BACKUP

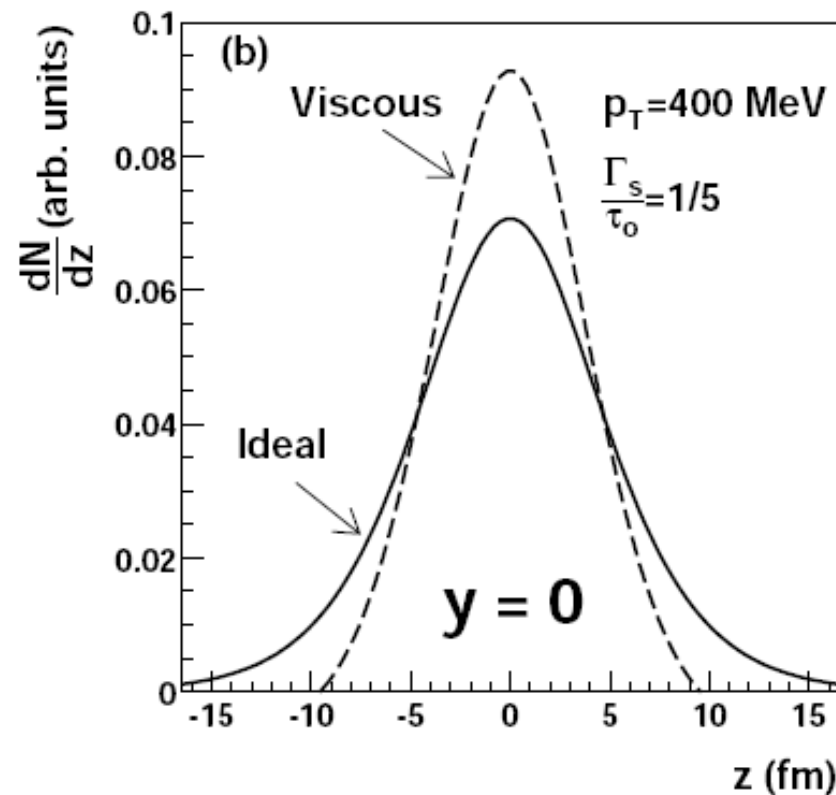
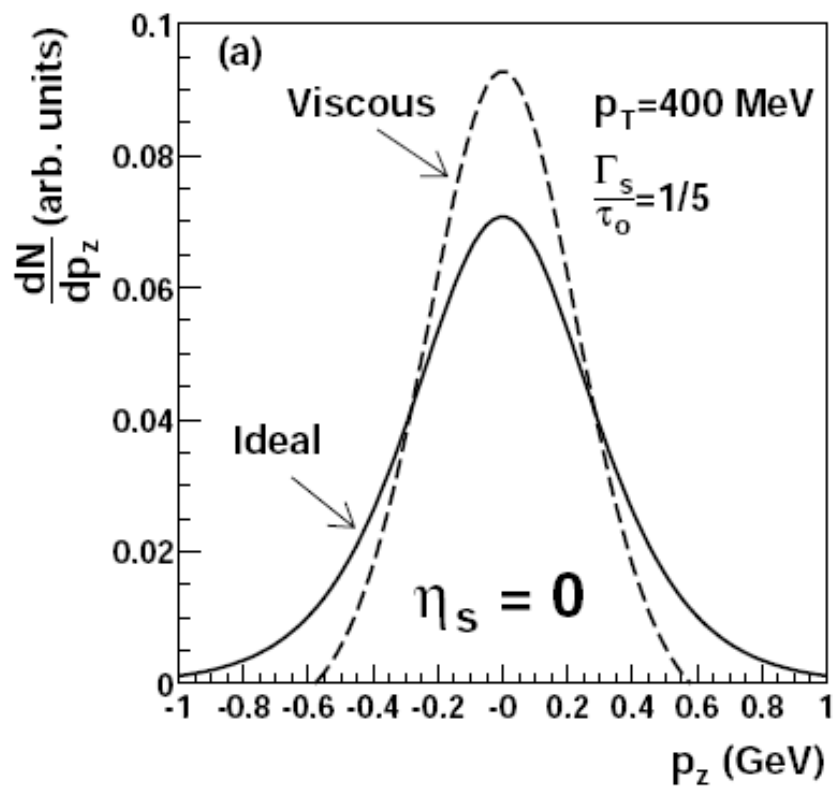
R_{side} systematics



Viscosity via R_{long}

D. Teaney, *Phys. Rev. C* 68,034913 (2003)

“Viscous corrections to a Bjorken expansion”



Viscous gas

$$\lambda = \frac{1}{n\sigma} \quad \begin{array}{l} \text{mean free path} \\ \text{hydrodynamics applies when } \lambda \text{ small} \end{array}$$

$$\eta = \frac{np\lambda}{3} = \frac{p}{3\sigma} \quad \begin{array}{l} \text{dynamical viscosity} \\ \text{(independent on } n) \\ \text{(infinite for ideal gas)} \\ \text{(not quite 0 for inf. } \sigma) \end{array}$$

$$\nu = \frac{\eta}{\rho} = \frac{\langle v \rangle \lambda}{3} \quad \text{kinematical viscosity}$$

$$\begin{array}{l} \eta \sim np\lambda \\ s \sim n \end{array} \quad \begin{array}{l} \text{uncertainty principle provides} \\ \text{lower bound} \end{array}$$

$$\frac{\eta}{s} \sim p\lambda \sim \frac{\text{mean free path}}{\text{de Broglie wavelength}} \geq \text{const}$$

$$\frac{\eta}{s} = \frac{3}{4} \lambda T \quad \text{Teaney}$$

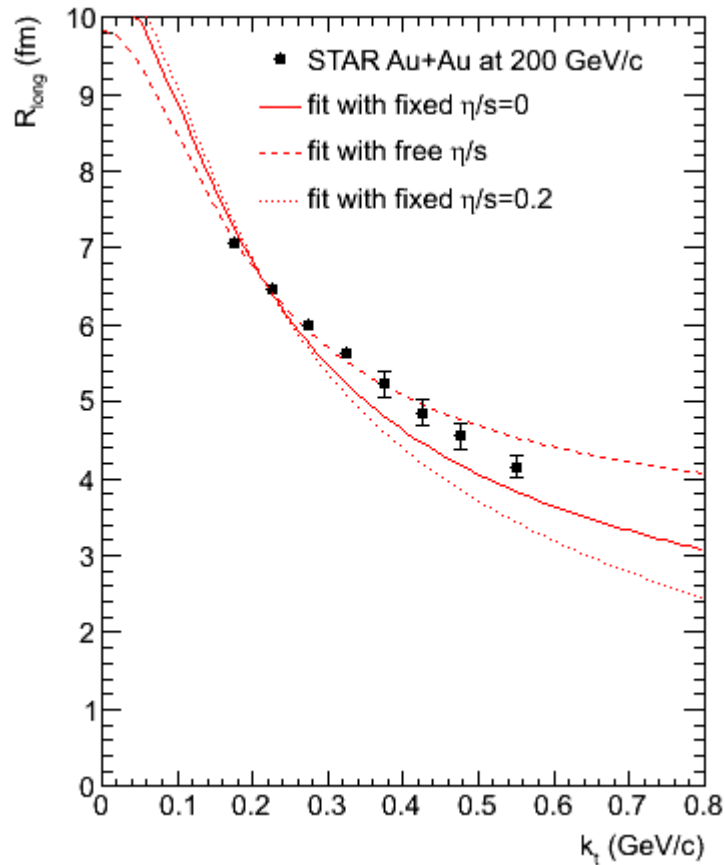
Teaney's formulas

$$(R_L^2)^{(0)} = \tau_o^2 \frac{T}{m_T} \frac{K_2(x)}{K_1(x)} \quad x \equiv \sqrt{m^2 + K_T^2} / T$$

$$\frac{\delta R_L^2}{(R_L^2)^{(0)}} = - \frac{\Gamma_s}{\tau} \left[\frac{6}{4} \frac{x K_3(x)}{K_2(x)} - x^2 \frac{1}{8} \left(\frac{K_3(x)}{K_2(x)} - 1 \right) \right]$$

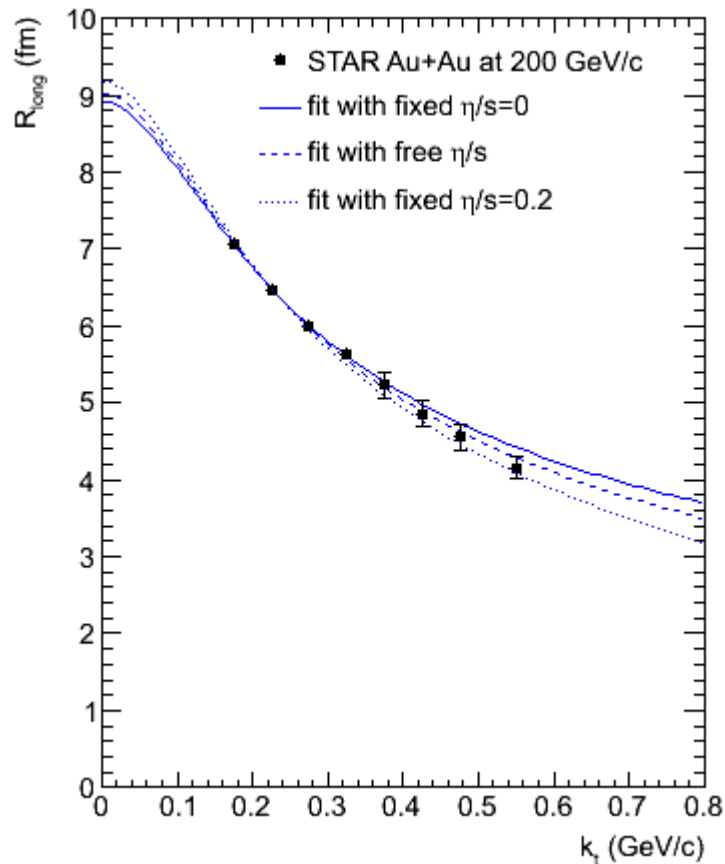
$$(R_L^2)^{(0)} = \tau_o^2 \frac{T}{m_T} \quad (R_L^2)^{(0)} + \delta R_L^2 = \tau_o^2 \left(\frac{T}{m_T} - \frac{19}{16} \frac{\Gamma_s}{\tau_o} \right) \quad \Gamma_s \equiv \frac{4}{3} \frac{\eta}{sT}$$

Fit to STAR Rlong, full formula



| fitfun | tau0 (fm) | T (GeV) | eta/s |
|-----------------|--------------|--------------|--------------|
| fixed eta/s=0 | 7.224+-0.022 | 0.120+-0.000 | 0.000+-0.000 |
| free eta/s | 1.850+-1.721 | 0.120+-0.000 | 1.956+-1.596 |
| fixed eta/s=0.2 | 8.926+-0.022 | 0.120+-0.000 | 0.200+-0.000 |

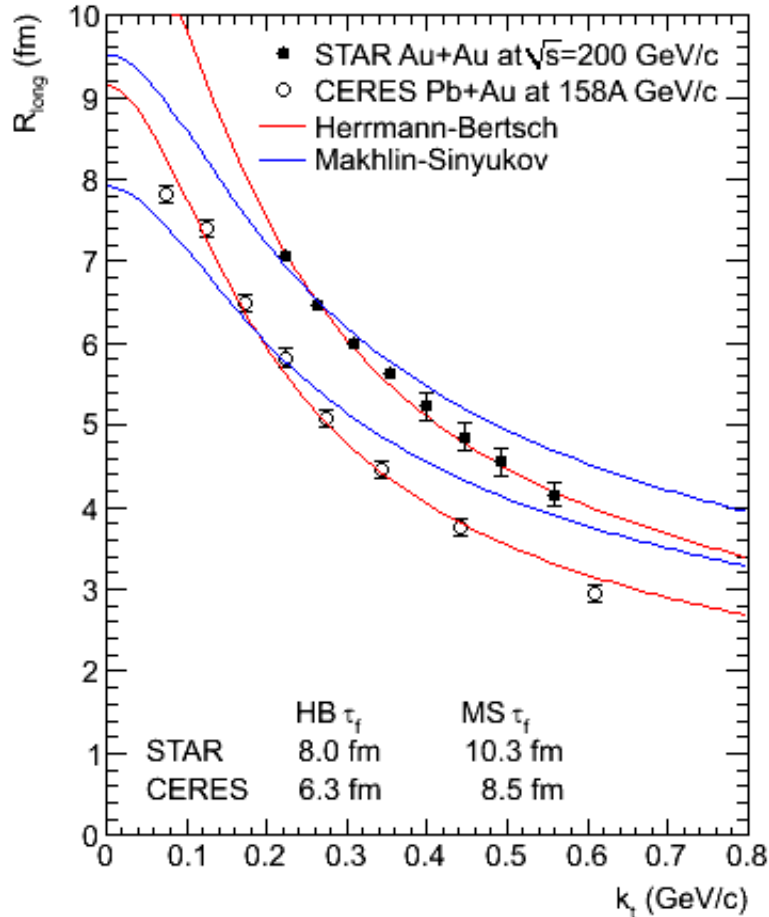
Fit to STAR Rlong, simplified formula



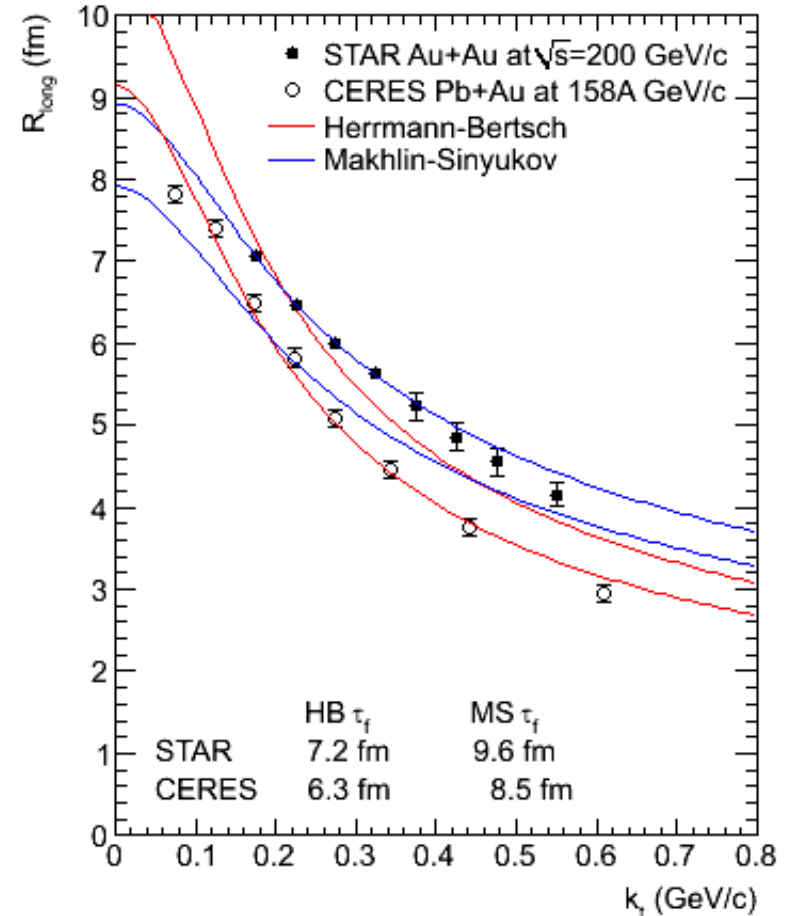
| fitfun | tau0 (fm) | T (GeV) | eta/s |
|-----------------|---------------|--------------|--------------|
| fixed eta/s=0 | 9.618+-0.030 | 0.120+-0.000 | 0.000+-0.000 |
| free eta/s | 9.861+-0.131 | 0.120+-0.000 | 0.084+-0.044 |
| fixed eta/s=0.2 | 10.205+-0.030 | 0.120+-0.000 | 0.200+-0.000 |

mistake when interpreting STAR data (m_t vs k_t)

STAR points misplaced

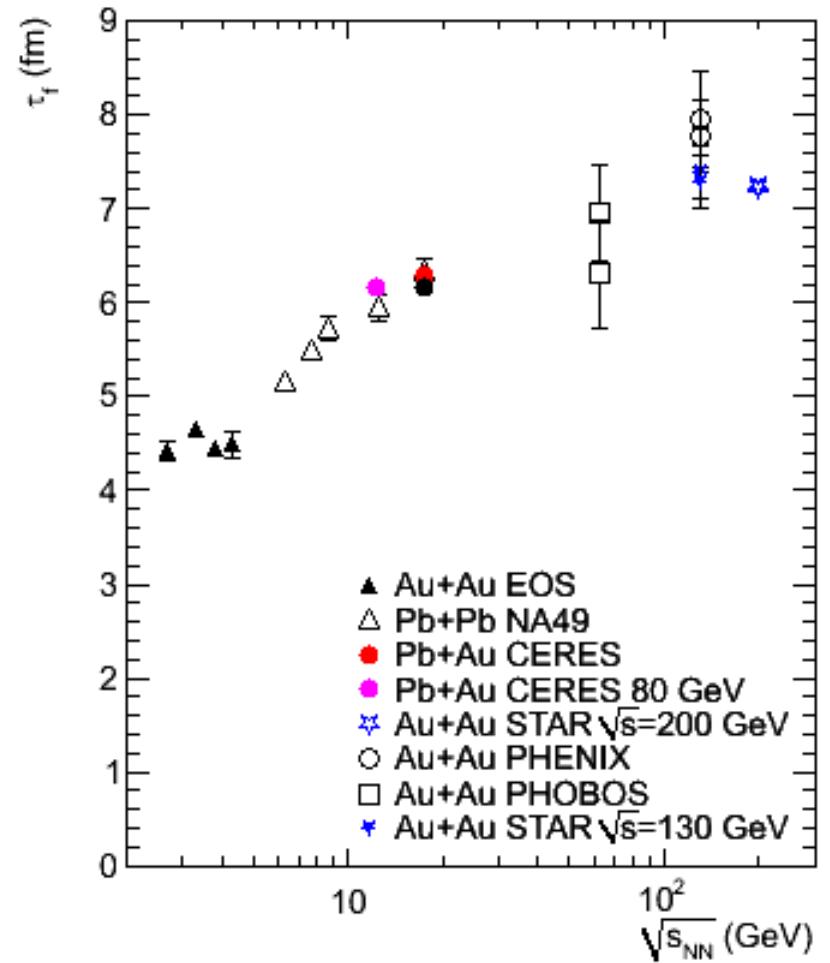
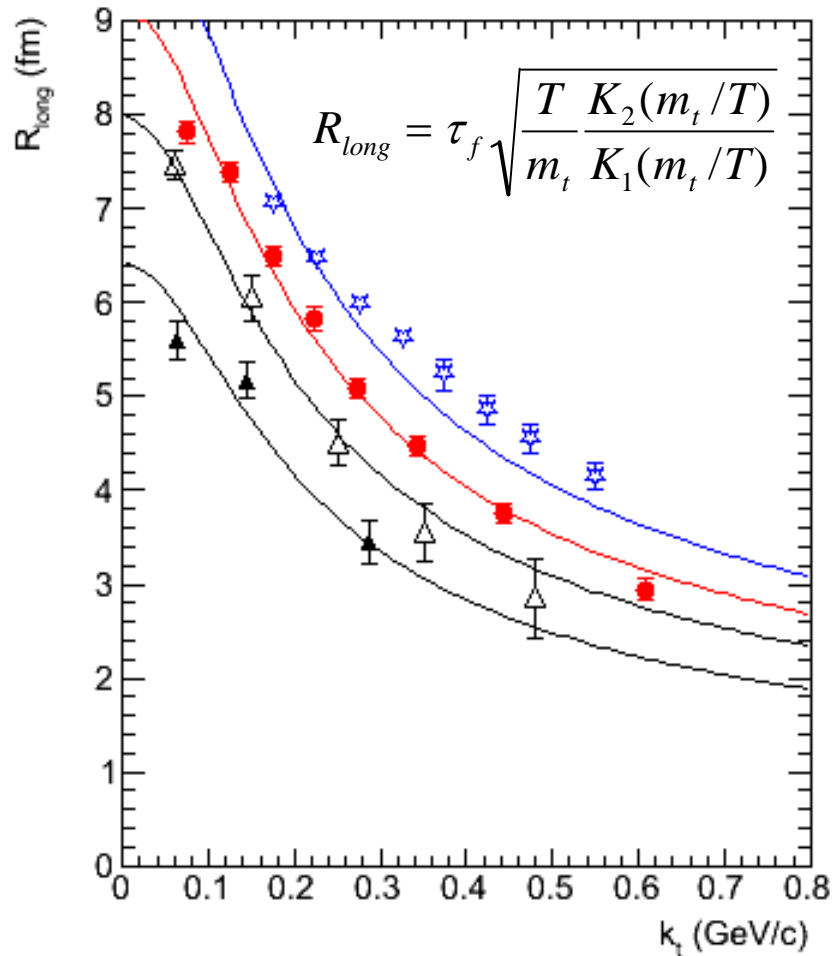


STAR points placed correctly

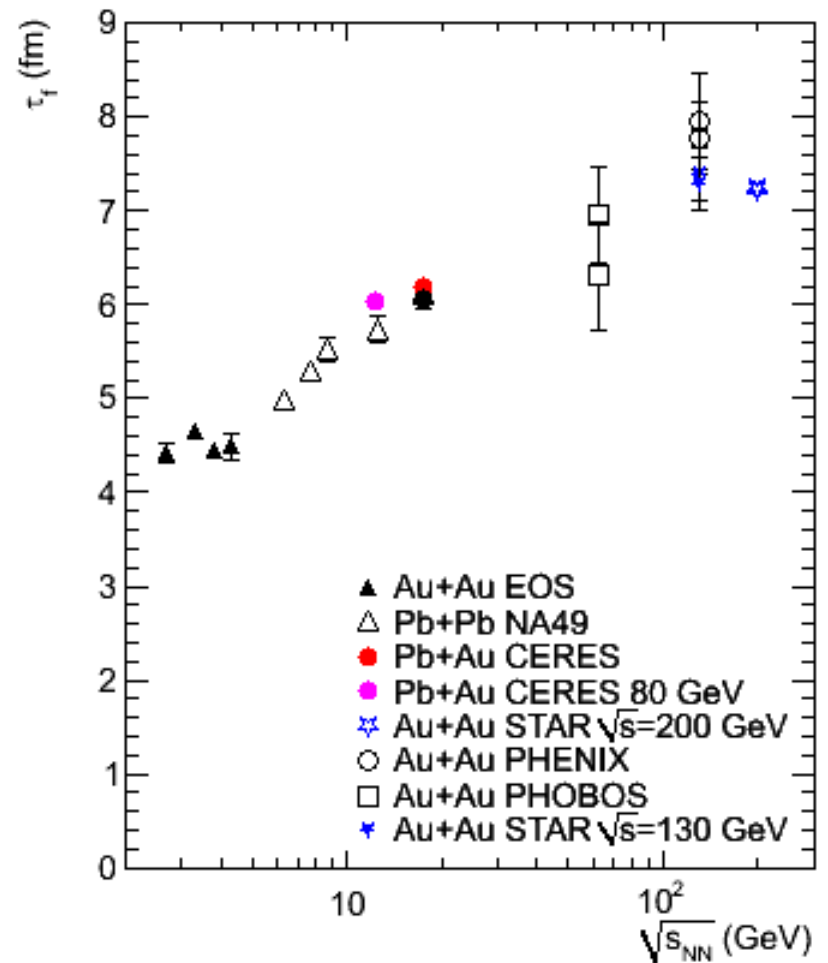
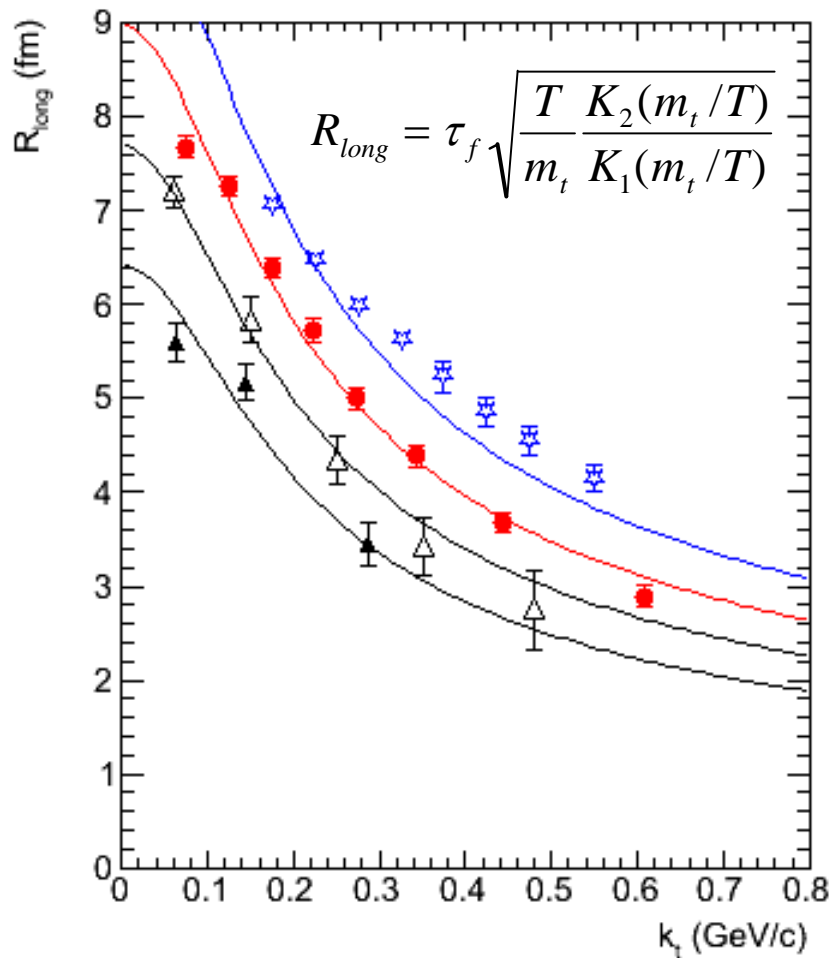


Herrmann-Bertsch vs Makhlin-Sinyukov

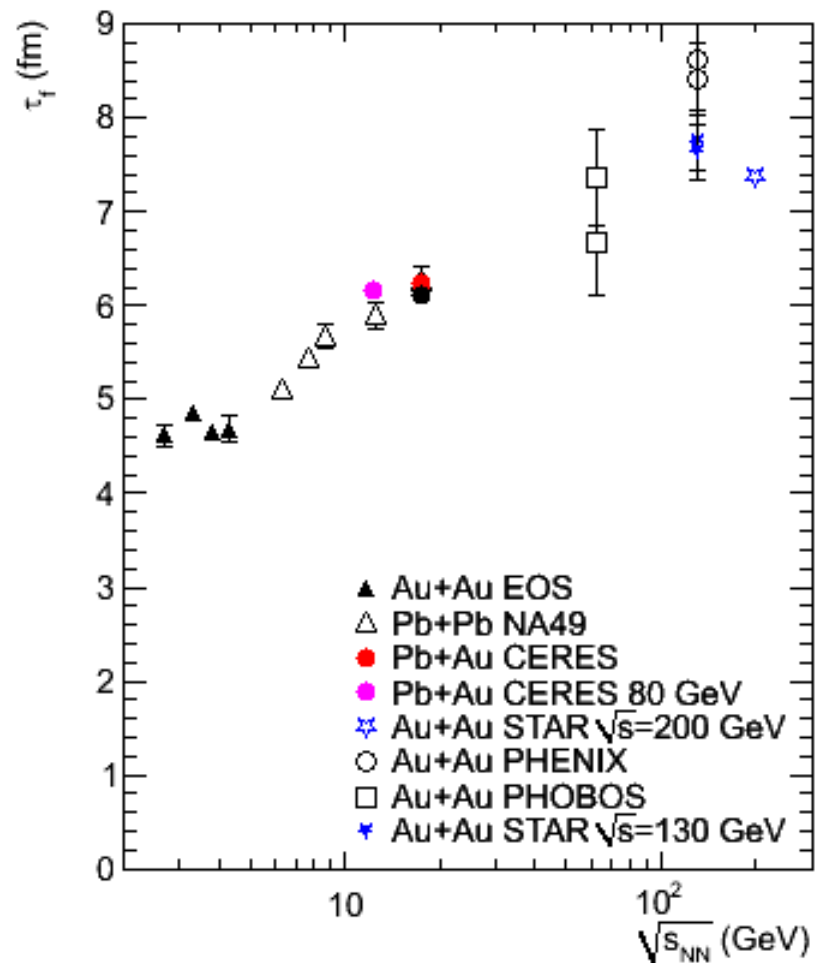
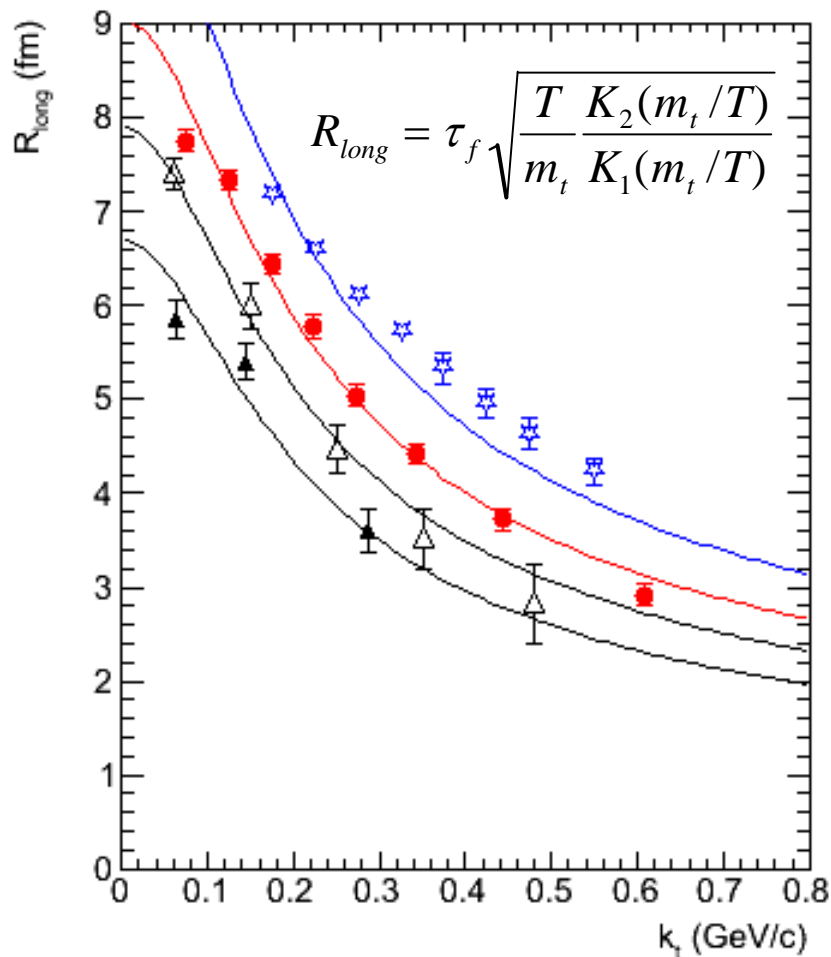
R_{long}



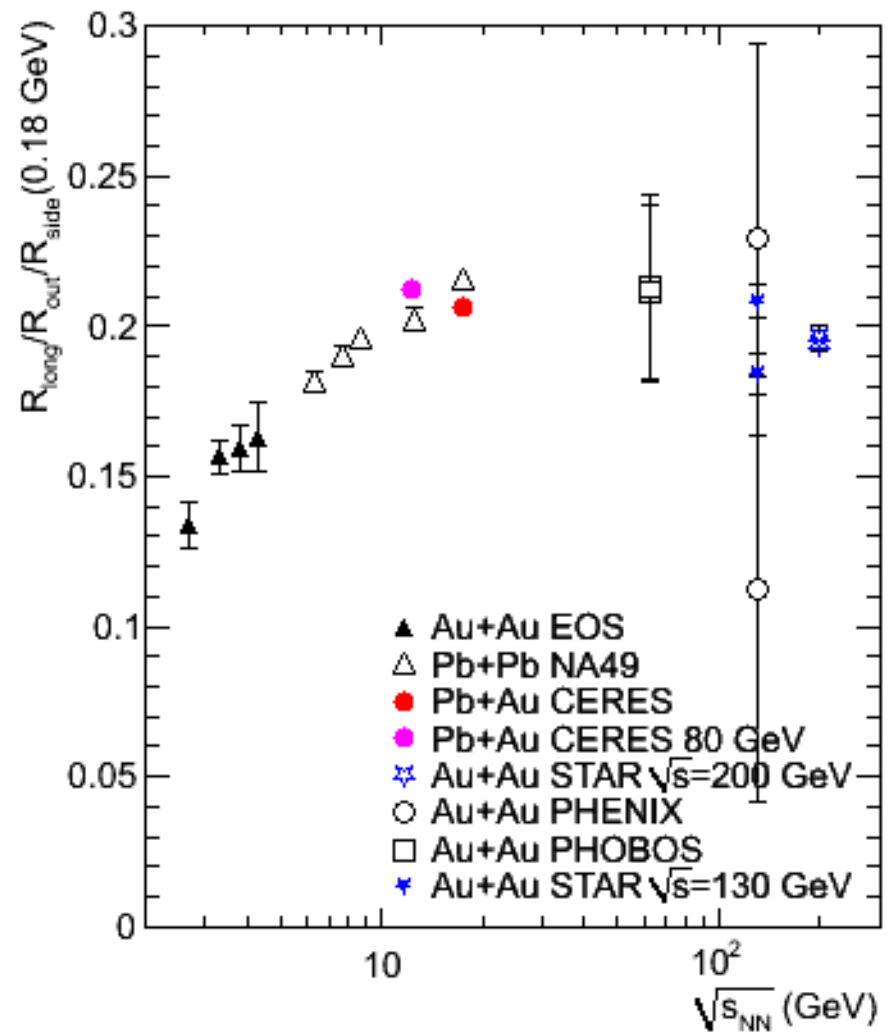
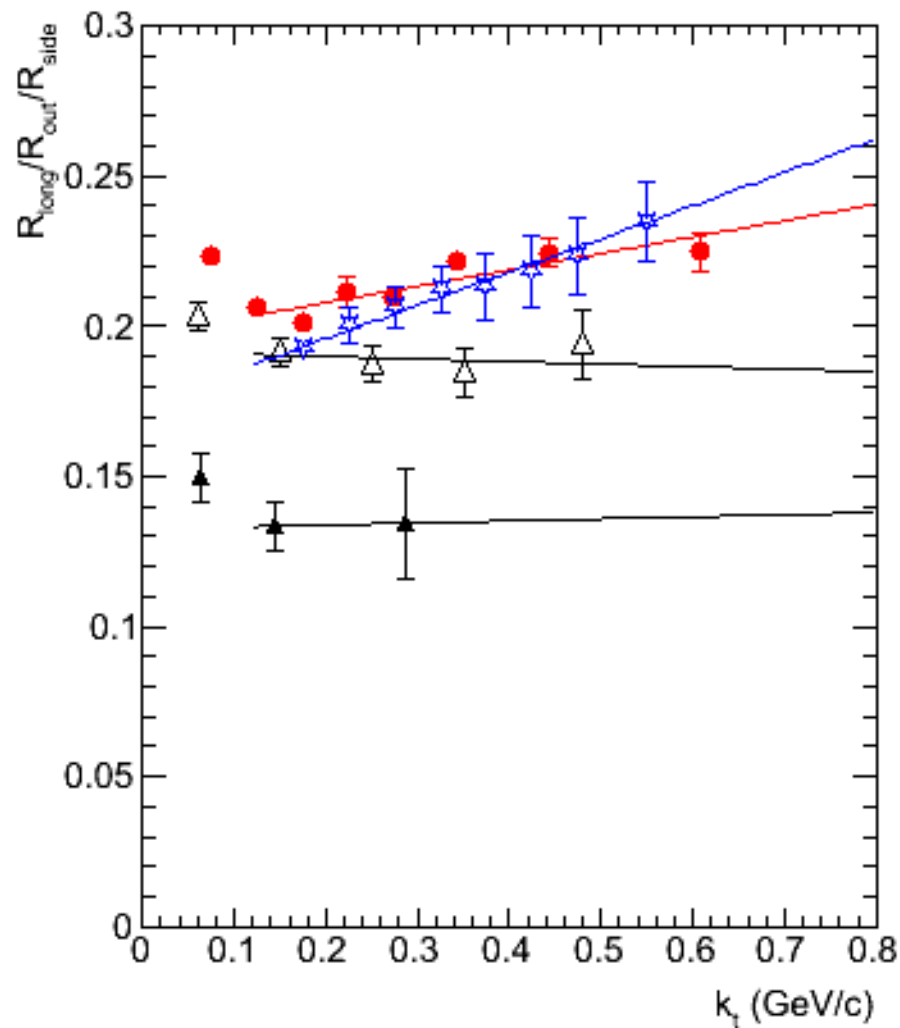
R_{long} corrected by $(A/197)^{1/3}$



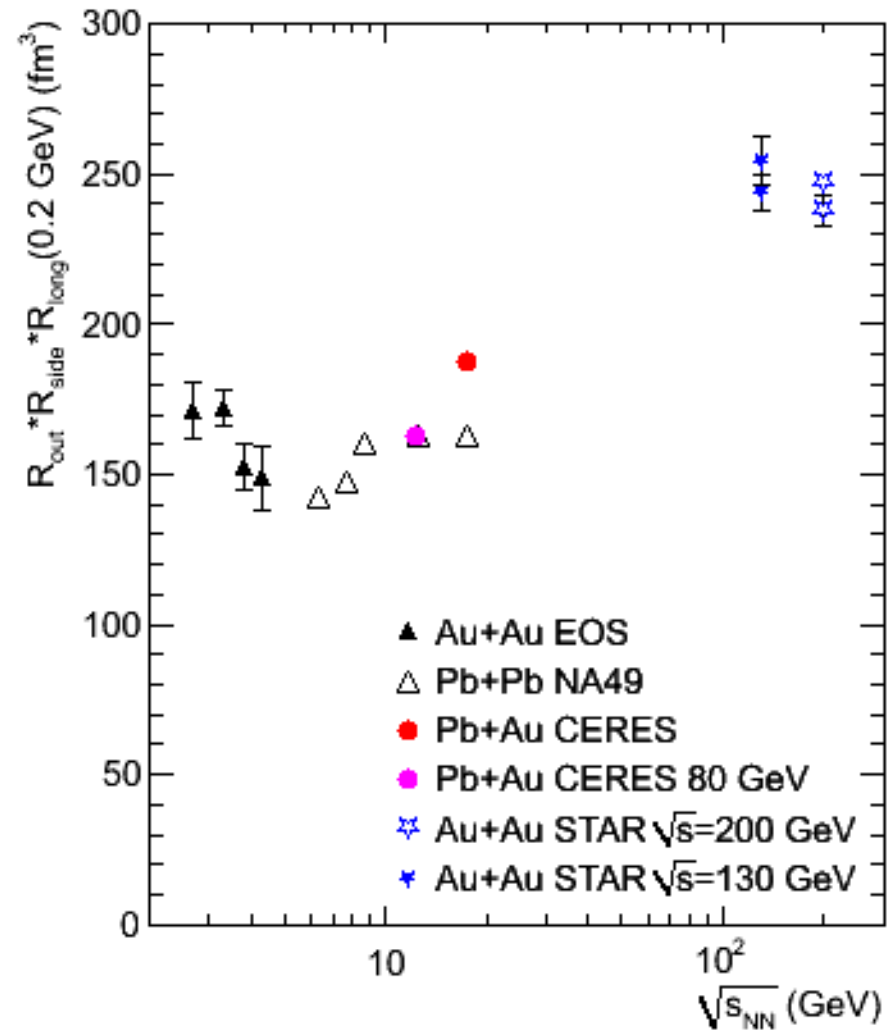
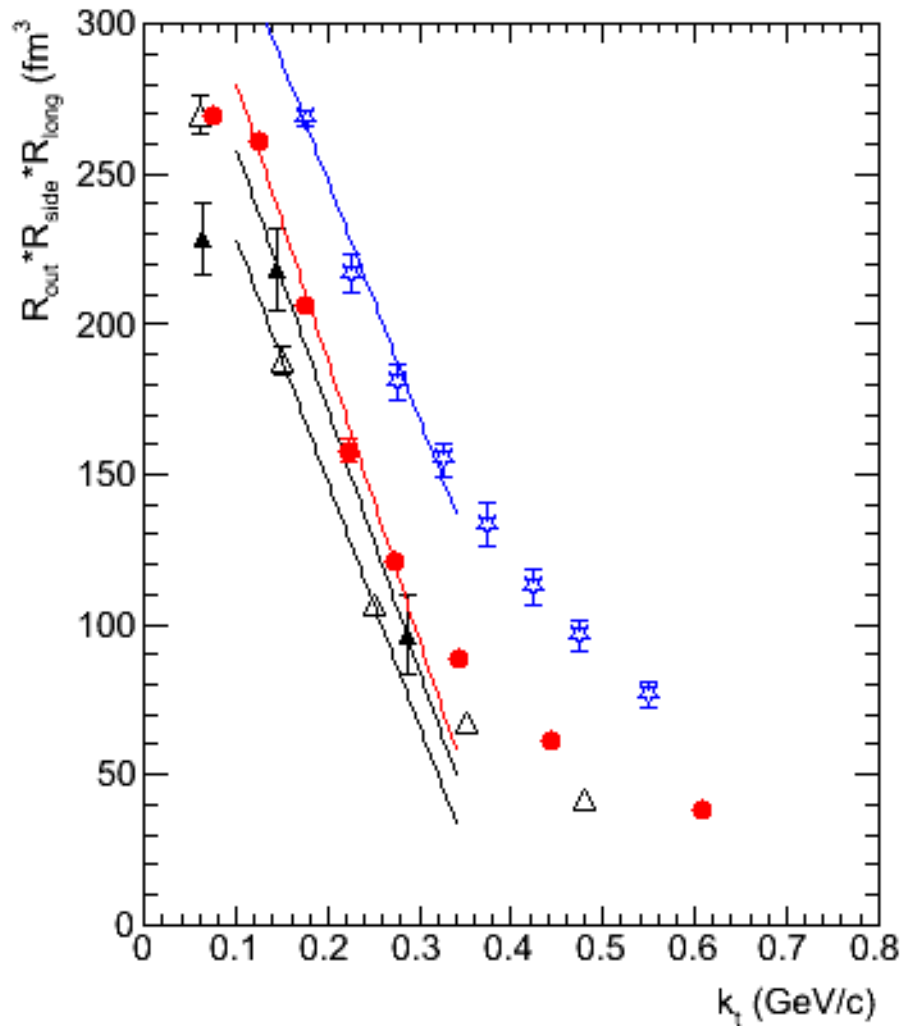
R_{long} corrected by $(A/197)^{1/3}$ and for centrality



$R_{\text{long}}/R_{\text{out}}/R_{\text{side}}$



$$R_{\text{out}} * R_{\text{side}} * R_{\text{long}}$$



$$R_{\text{side}} * R_{\text{side}} * R_{\text{long}}$$

