



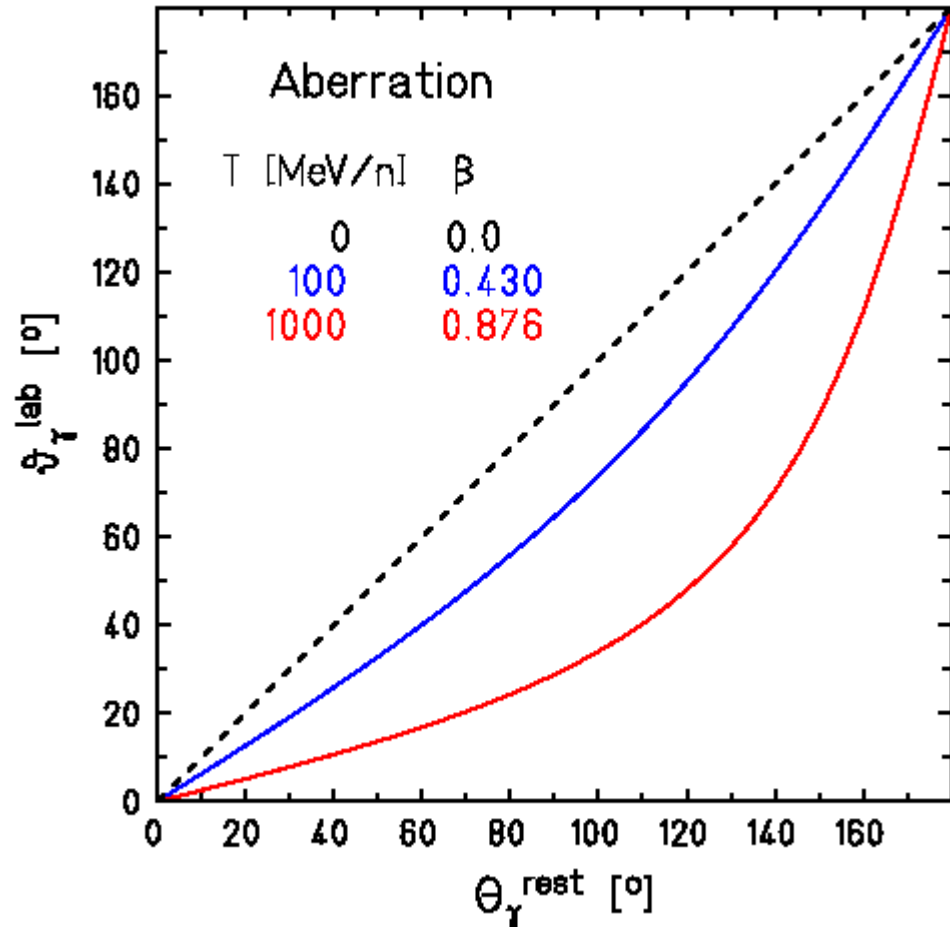
## Relativistic Aberration

$$\cos \vartheta_{\gamma}^{lab} = \frac{\cos \theta_{\gamma}^{rest} + \beta}{1 + \beta \cos \theta_{\gamma}^{rest}}$$

for  $\vartheta_p \cong 0^{\circ}$

$$\cos \theta_{\gamma}^{rest} = \frac{\cos \vartheta_{\gamma}^{lab} - \beta}{1 - \beta \cos \vartheta_{\gamma}^{lab}}$$

$$\phi_{\gamma}^{rest} = \phi_{\gamma}^{lab}$$



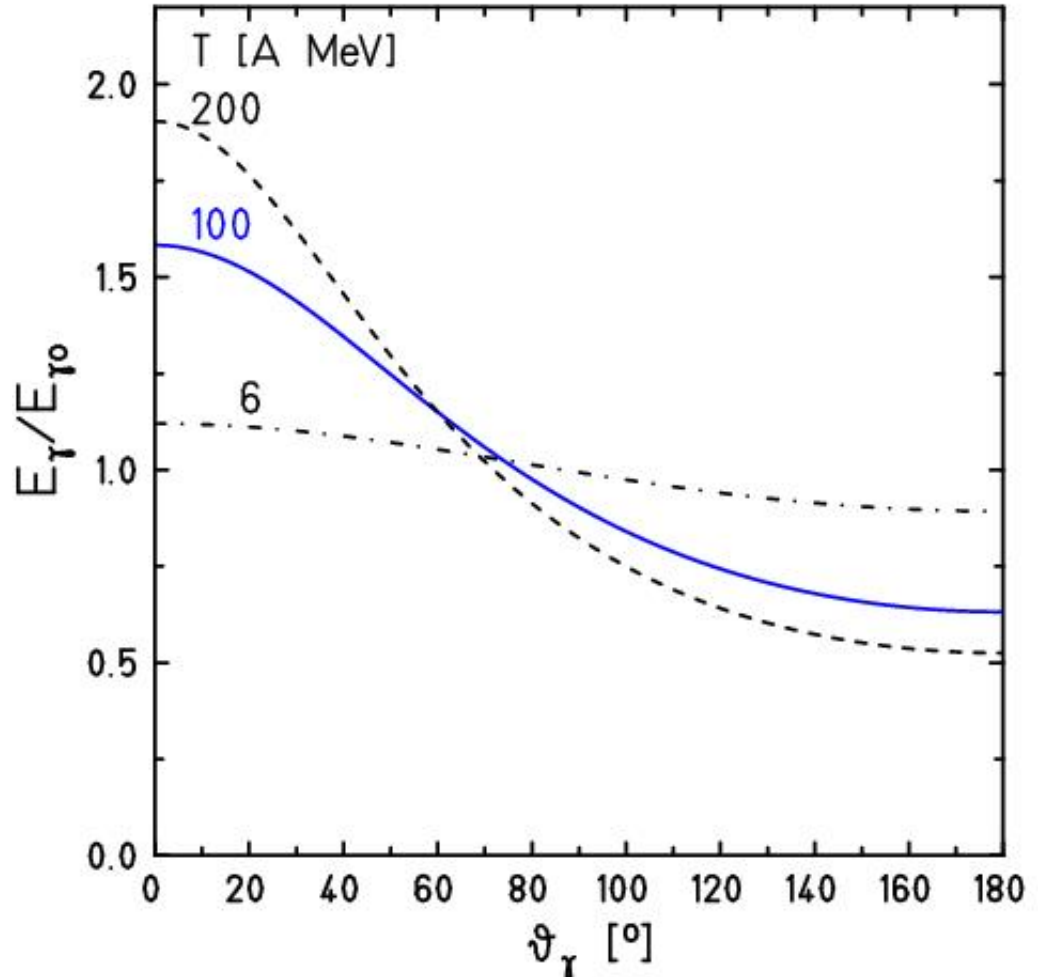


## Doppler Effect

$$\frac{E_{\gamma 0}}{E_{\gamma}} = \frac{1 - \beta \cdot \cos \vartheta_{\gamma}^{lab}}{\sqrt{1 - \beta^2}}$$

for  $\vartheta_p \cong 0^{\circ}$

$$\frac{d\Omega_{rest}}{d\Omega_{lab}} = \left( \frac{E_{\gamma}}{E_{\gamma 0}} \right)^2$$



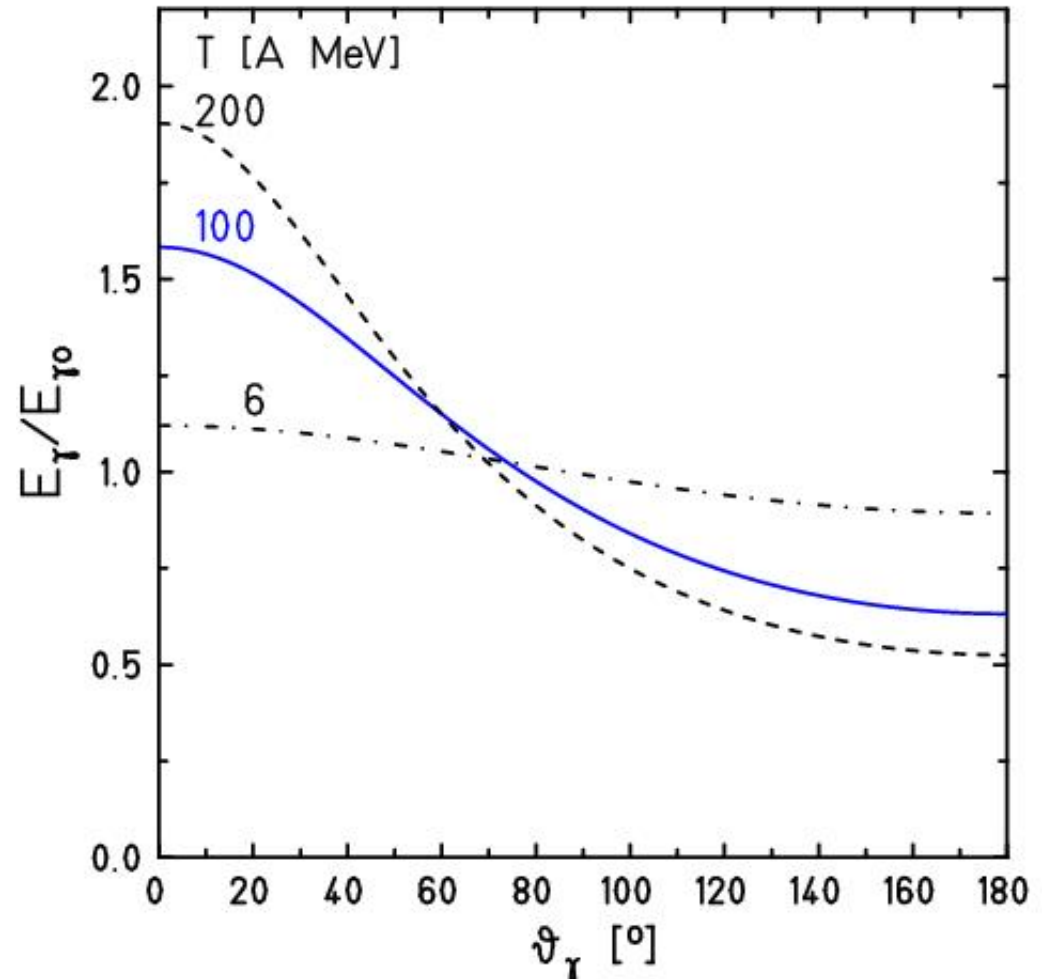


## Headlight Effect

$$\frac{d\Omega_{rest}}{d\Omega_{lab}} = \left( \frac{E_\gamma}{E_{\gamma 0}} \right)^2$$

for  $\vartheta_p \cong 0^\circ$

$$\frac{E_{\gamma 0}}{E_\gamma} = \frac{1 - \beta \cdot \cos \vartheta_\gamma^{lab}}{\sqrt{1 - \beta^2}}$$





## Doppler Effect

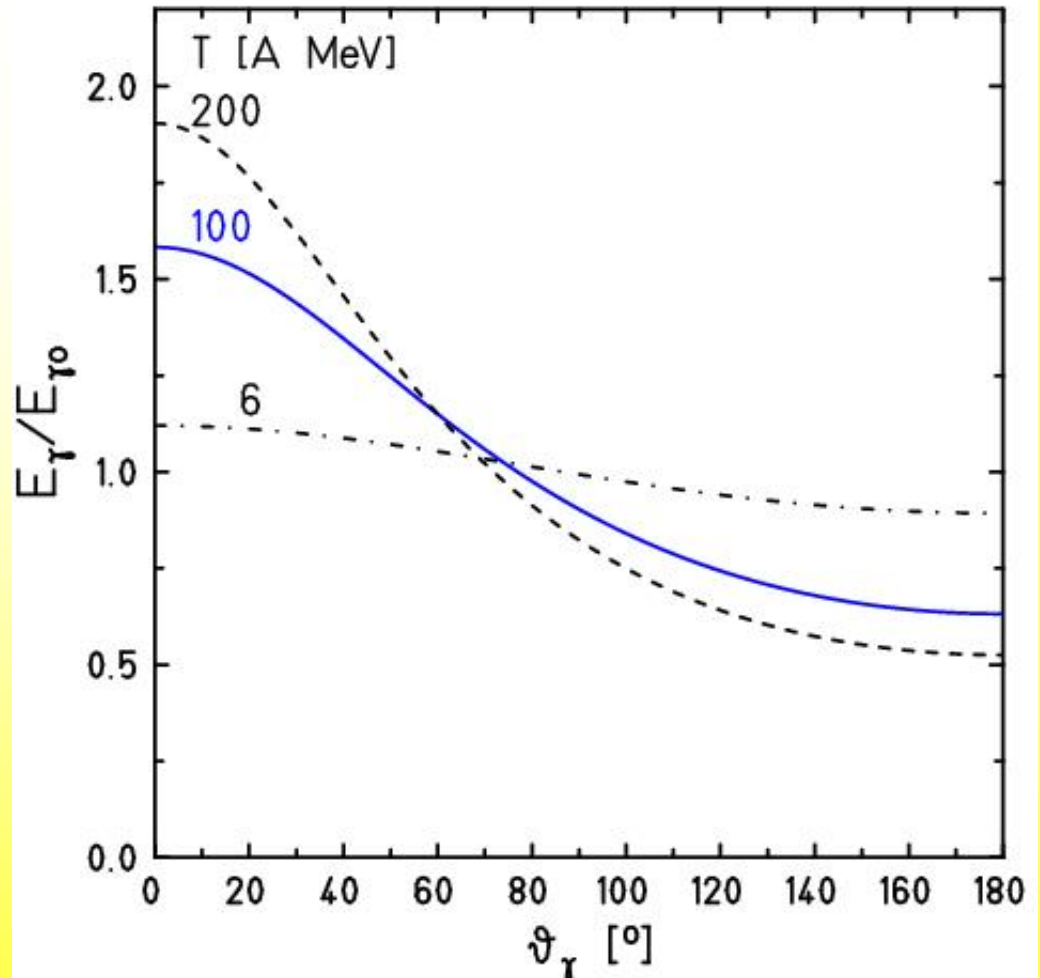
$$\frac{E_{\gamma 0}}{E_{\gamma}} = \frac{1 - \beta \cdot \cos \vartheta_{\gamma}}{\sqrt{1 - \beta^2}}$$

for  $\vartheta_p \cong 0^{\circ}$

$$\frac{d\Omega_{rest}}{d\Omega_{lab}} = \left( \frac{E_{\gamma}}{E_{\gamma 0}} \right)^2$$

$$\cos \theta_{\gamma}^{rest} = \frac{\cos \vartheta_{\gamma}^{lab} - \beta}{1 - \beta \cos \vartheta_{\gamma}^{lab}}$$

$$\phi_{\gamma}^{rest} = \phi_{\gamma}^{lab}$$





## Doppler Broadening

$$\frac{\Delta E_{\gamma 0}}{E_{\gamma 0}} = \frac{\beta \cdot \sin \vartheta_{\gamma}}{1 - \beta \cdot \cos \vartheta_{\gamma}} \cdot \Delta \vartheta_{\gamma}$$

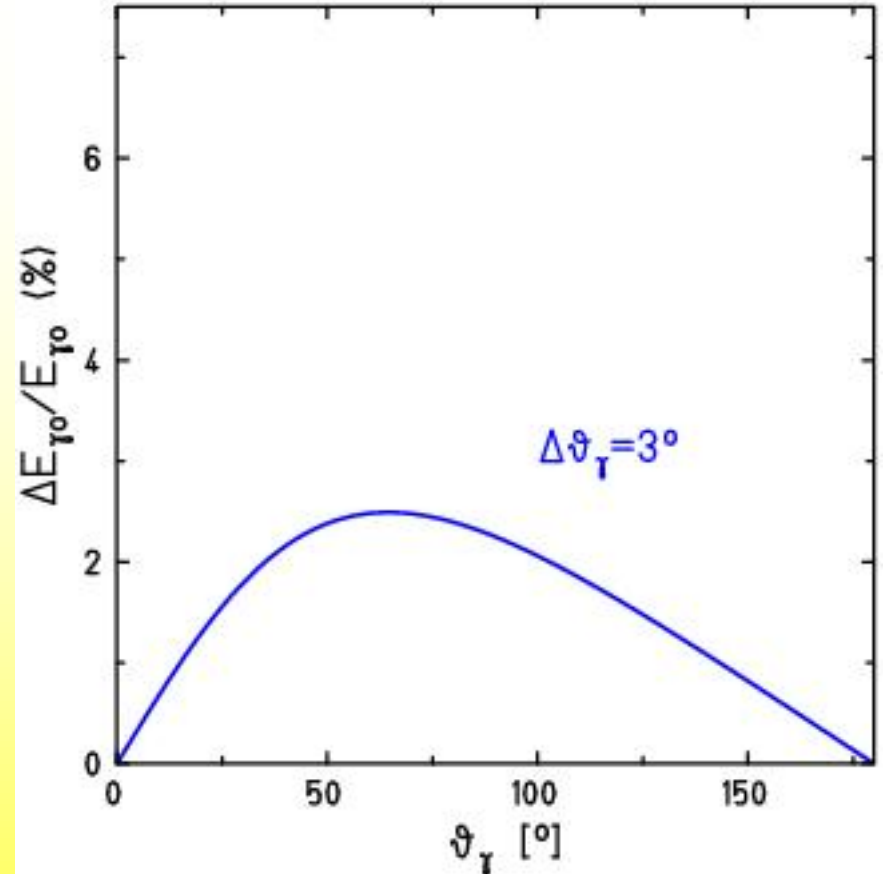
for  $\vartheta_p \cong 0^{\circ}$

with

$$\Delta \vartheta_{\gamma} = 0.622 \cdot \arctan \frac{d[\text{mm}]}{R[\text{mm}] + 30[\text{mm}]}$$

$$R = 700[\text{mm}]$$

$$d = 59[\text{mm}]$$





## Doppler Broadening

$$\frac{\Delta E_{\gamma 0}}{E_{\gamma 0}} = \frac{\beta - \cos \vartheta_{\gamma}}{(1 - \beta^2)(1 - \beta \cdot \cos \vartheta_{\gamma})} \cdot \Delta\beta$$

for  $\vartheta_p \cong 0^\circ$

with  $\Delta\beta = 6\%$

