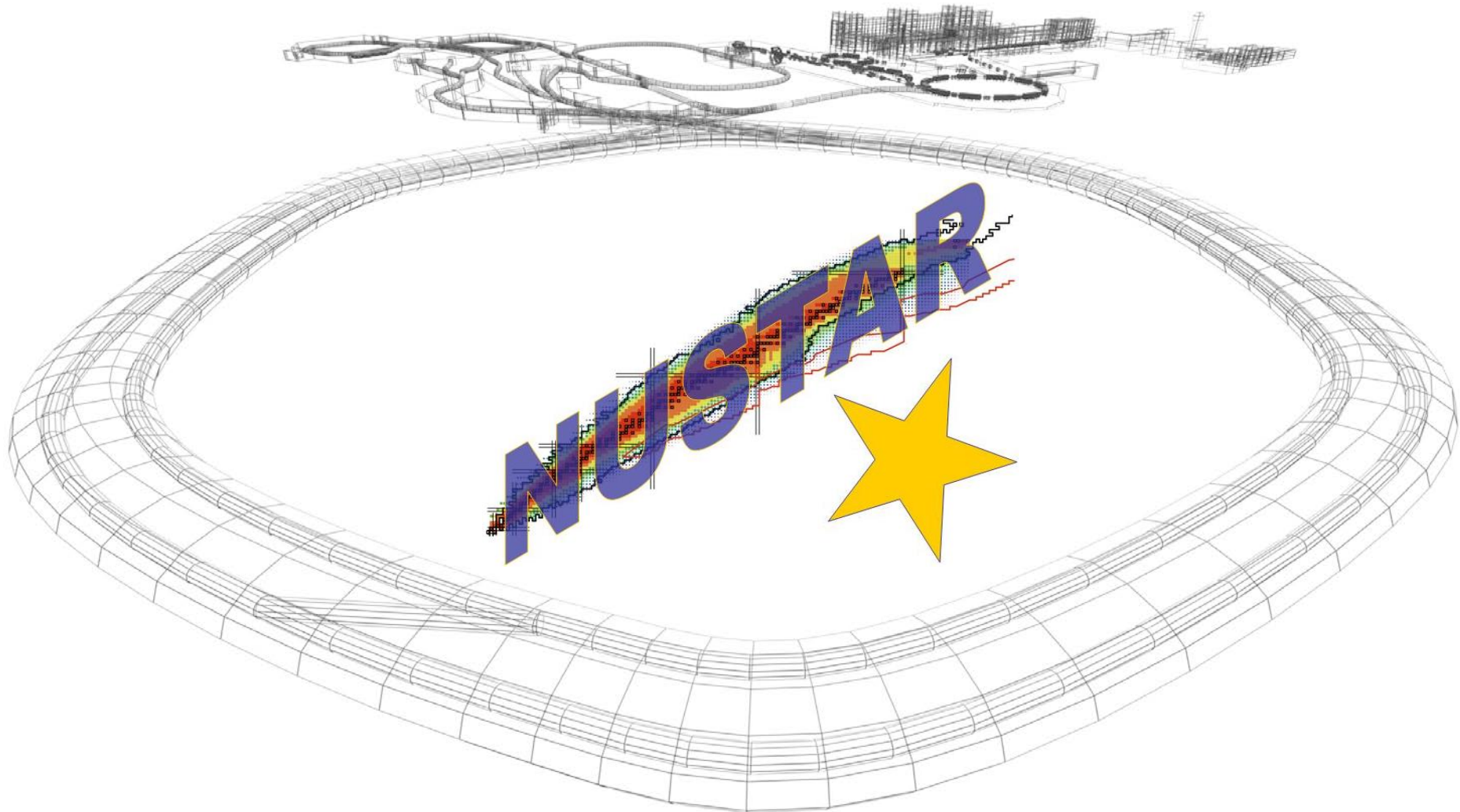


Physics with Exotic Nuclei

Hans-Jürgen Wollersheim



Outline

❖ Scattering Experiments with RIBs – Nuclear Structure Results

- Experimental evidence for closed-shell nuclei
- Scattering experiments at relativistic energies
- Projectile-like identification (Z , A) and scattering angle θ
- Doppler-shift correction of the emitted γ -rays

Physics with Exotic Nuclei

Experimental evidence for magic numbers close to stability

S. Raman et al., Atomic Data & Nuclear Data Tables 78, 1

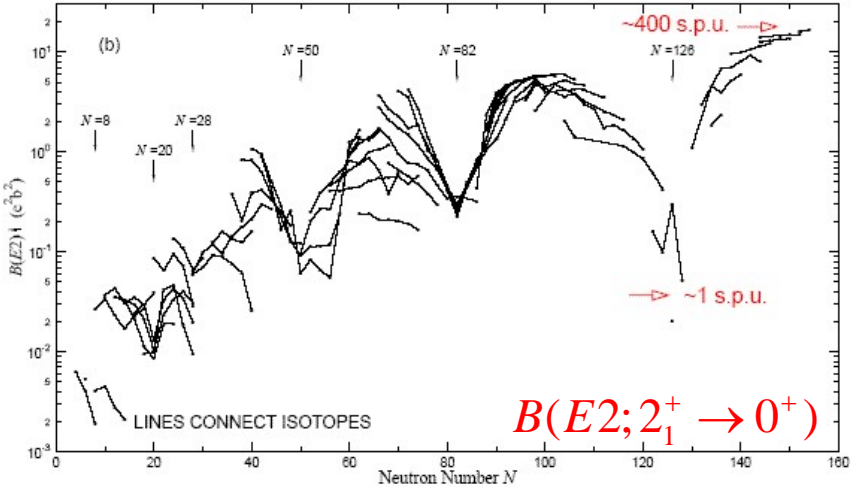
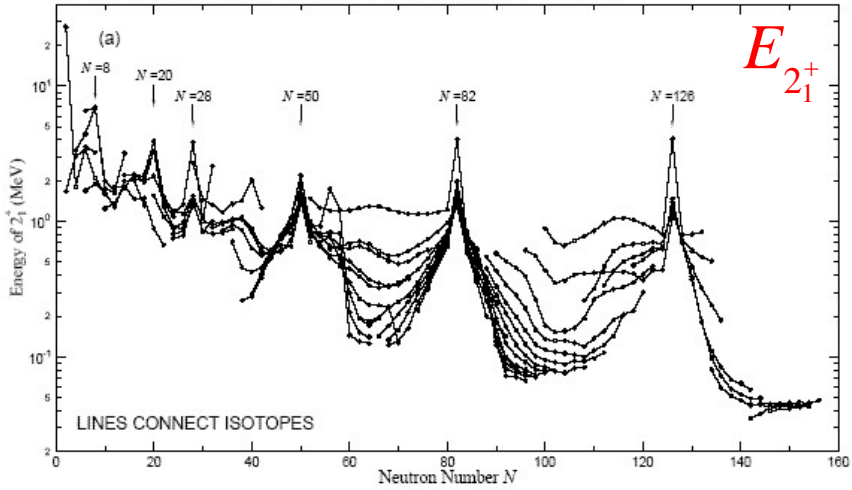


Table 1 -- Nuclear Shell Structure (from *Elementary Theory of Nuclear Shell Structure*, Maria Goeppert-Mayer & J. Hans D. Jensen, John Wiley & Sons, Inc., New York, 1955.)

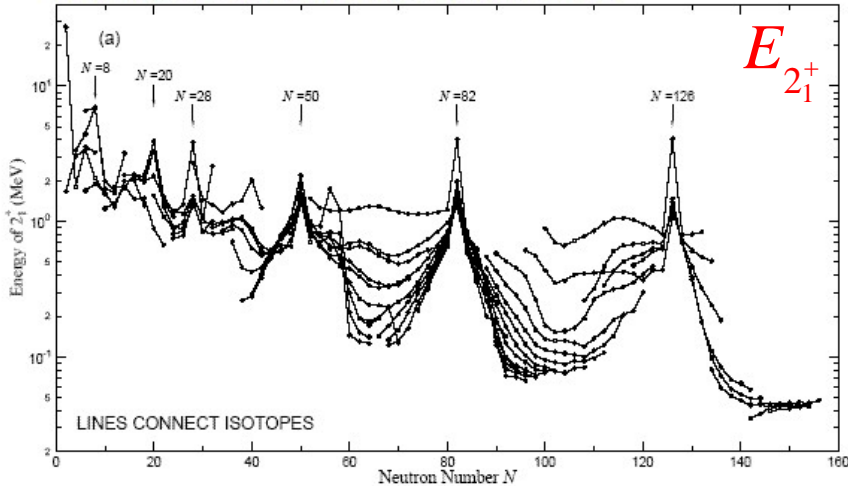
Angular Momentum (h $\Omega/2\pi$)	Spin-Orbit Coupling (1/2, 3/2, 5/2, 7/2...)	Number of Nucleons Shell	Magic Number Total
7	1j	16	[184] -- {184}
6	4s	2	[168] -- {168}
6	3d	8	[162] -- {162}
6	2g	6	[154] -- {154}
6	1i	10	[142] -- {142}
6	1i	14	[126] -- {126}
5	3p	2	[112] -- {112}
5	3p	4	[110] -- {110}
5	2f	6	[106] -- {106}
5	2f	8	[100] -- {100}
5	1h	10	[92] -- {92}
5	1h	14	[82] -- {82}
4	3s	2	[70] -- {70}
4	2d	4	[68] -- {68}
4	2d	6	[64] -- {64}
4	1g	8	[58] -- {58}
4	1g	10	[50] -- {50}
3	2p	2	[40] -- {40}
3	2p	6	[38] -- {38}
3	1f	4	[32] -- {32}
3	1f	8	[28] -- {28}
2	1d	4	[20] -- {20}
2	2s	2	[16] -- {16}
2	1d	6	[14] -- {14}
1	1p	2	[8] -- {8}
1	1p	4	[6] -- {6}
0	1s	2	[2] -- {2}



Physics with Exotic Nuclei

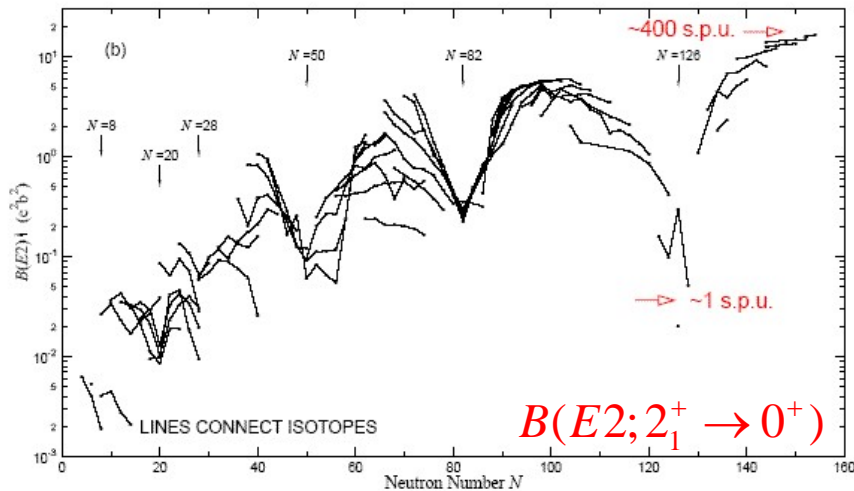
Experimental evidence for magic numbers close to stability

S. Raman et al., Atomic Data & Nuclear Data Tables 78, 1



Nuclei with magic numbers
of neutrons/protons

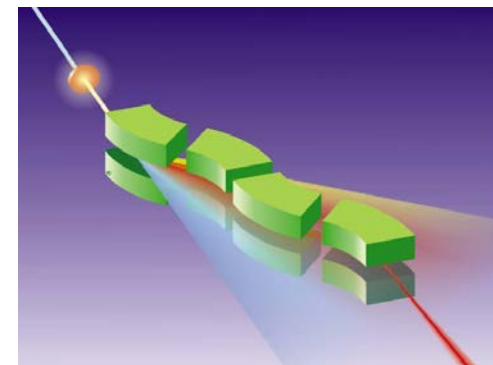
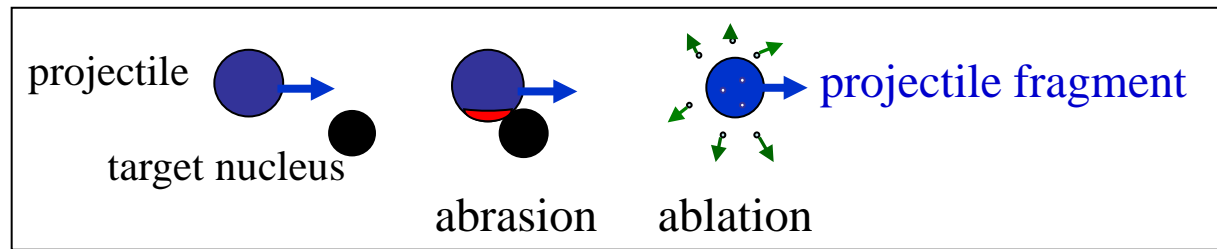
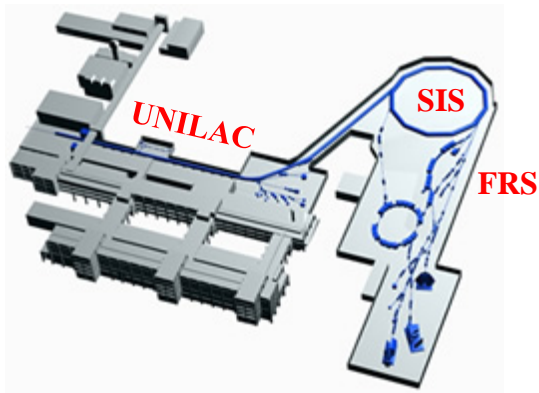
high energy of 2_1^+ state



low $B(E2; 2_1^+ \rightarrow 0^+)$ values
transition probability measured in
single particle units (spu)

If we move away from stability?

Production, Separation, Identification



FRagment
Separator

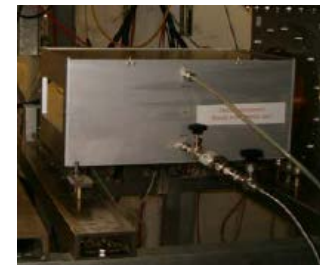
Standard FRS detectors



TPC-**x,y**
position
@ S2,S4

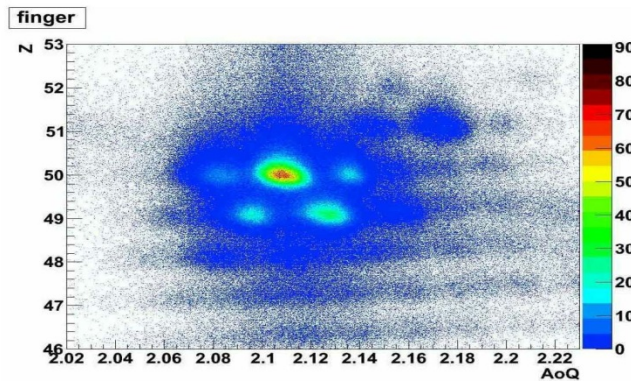
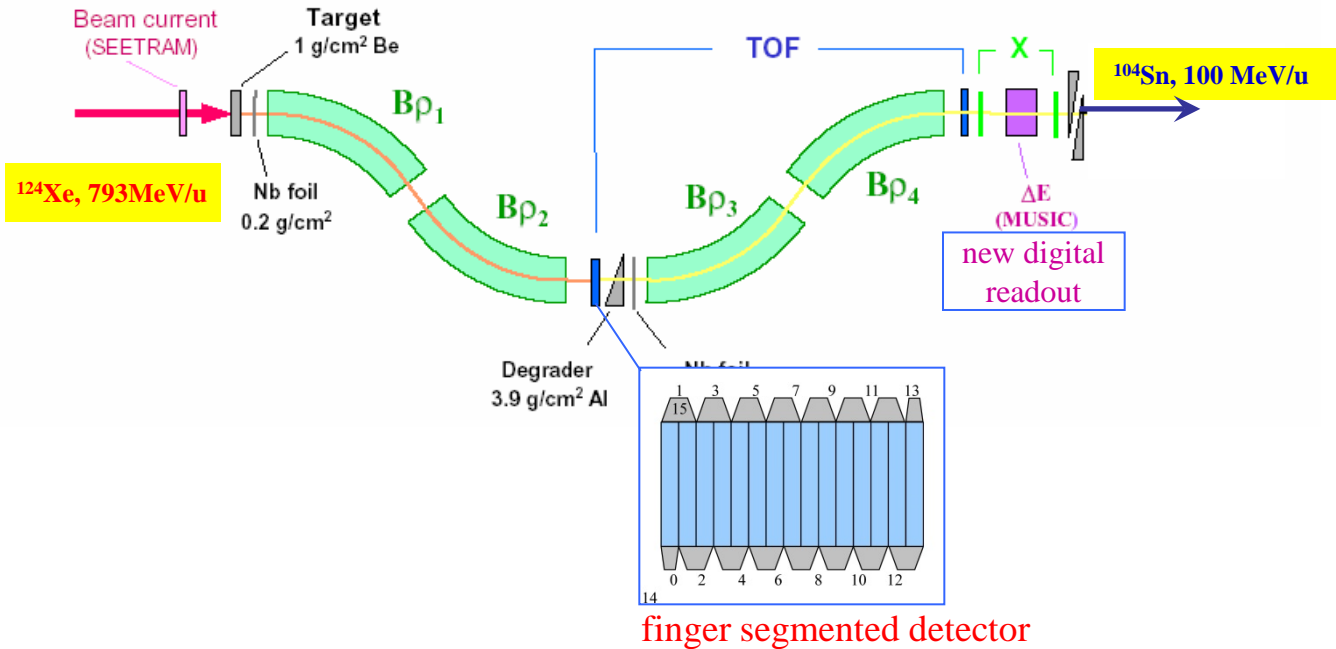


Plastic
scintillator
(**TOF**)
@ S4



MUSIC
(**ΔE**)
@ S4

Scattering Experiment at Relativistic Energies

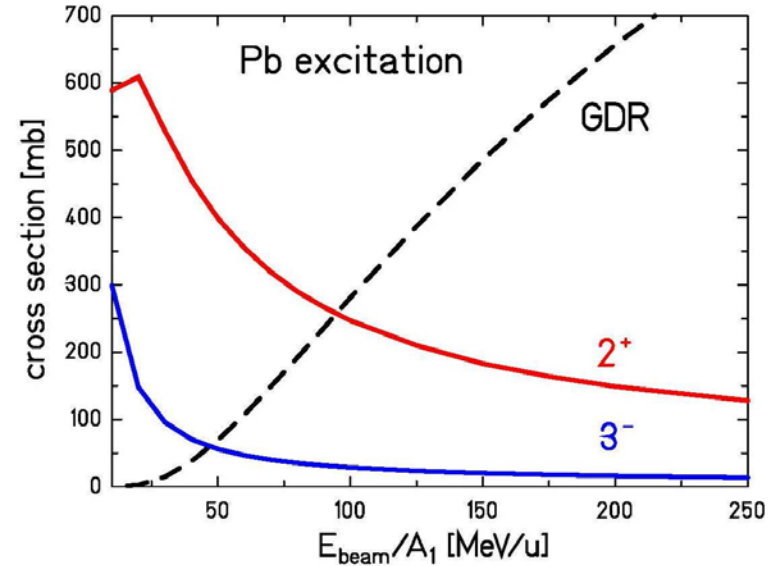
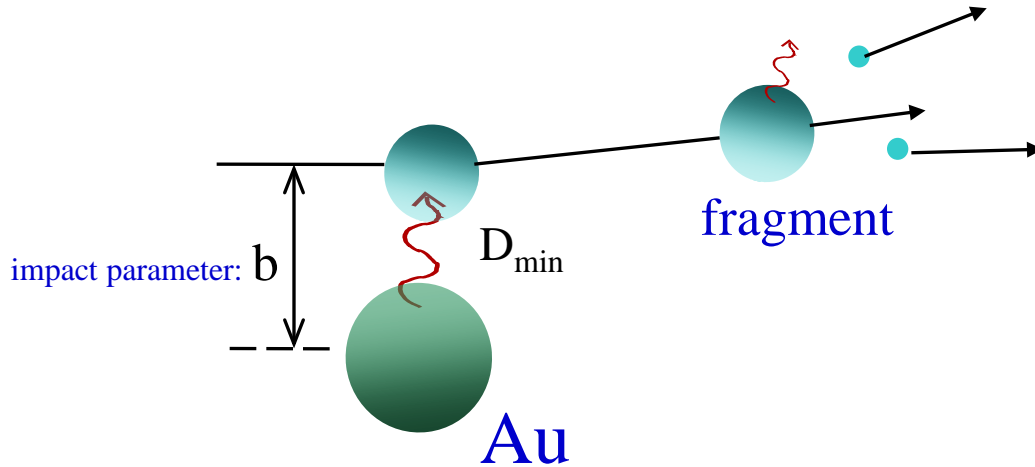


^{104}Sn fragments
using ^{124}Xe at 793 MeV/u

high rate at S2 $\sim 10^6 \text{ s}^{-1}$

- $\sim 2400\%$ more tracking efficiency
- good A/Q resolving power

Scattering Experiment at Relativistic Energies

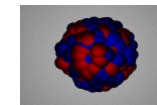


Rutherford scattering only if distance of closest approach D_{\min} is large compared to **nuclear radii + surfaces**:

$$D_{\min} > C_P + C_T + 5 \text{ fm}$$

C_P, C_T half-density radii

$$\sigma_{\pi\lambda} \approx \left(\frac{Z_p e^2}{\hbar c} \right)^2 \cdot \frac{\pi}{e^2 b^{2\lambda-2}} \cdot B(\pi\lambda; 0 \rightarrow \lambda) \cdot \begin{cases} (\lambda-1)^{-1} & \text{for } \lambda \geq 2 \\ 2 \ln(b_a/b) & \text{for } \lambda = 1 \end{cases}$$



$$E^* \cong 13.3 \text{ MeV}$$

$$B(E1; 0 \rightarrow 1^-) \cong 0.55 e^2 b$$



$$E^* = 4.086 \text{ MeV}$$

$$B(E2; 0 \rightarrow 2^+) = 9 Wu$$



$$E^* = 2.615 \text{ MeV}$$

$$B(E3; 0 \rightarrow 3^-) = 34 Wu$$

Atomic Background Radiation

➤ Radiative electron capture (REC)

capture of target electrons into bound states of the projectile:

$$\sigma \sim Z_p^2 \cdot Z_t$$

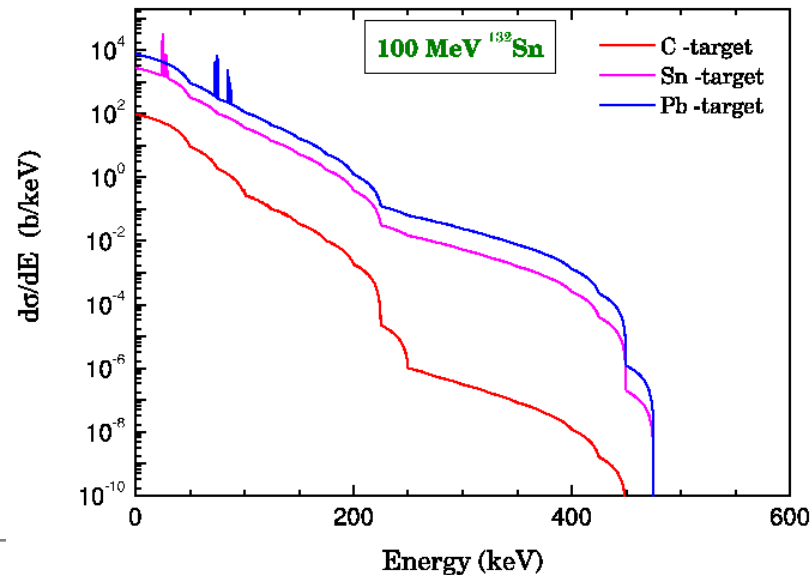
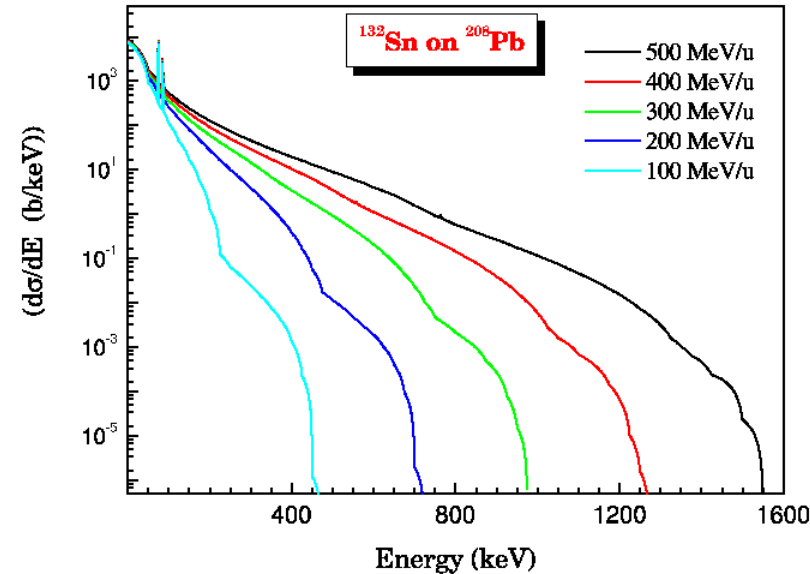
➤ Primary Bremsstrahlung (PB)

capture of target electrons into continuum states of the projectile:

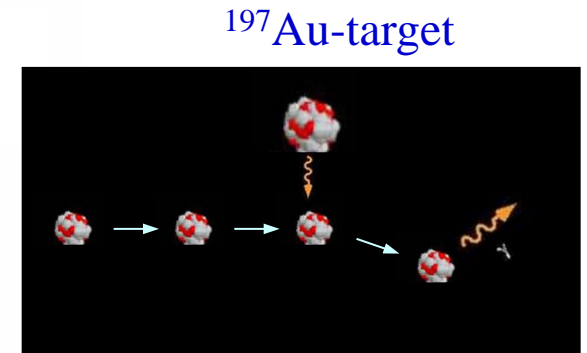
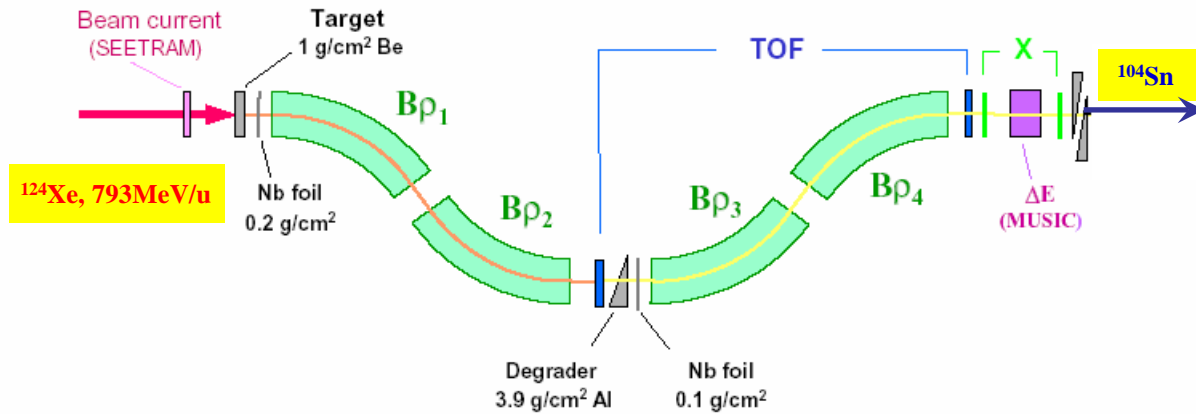
$$\sigma \sim Z_p^2 \cdot Z_t$$

➤ Secondary Bremsstrahlung (SB)

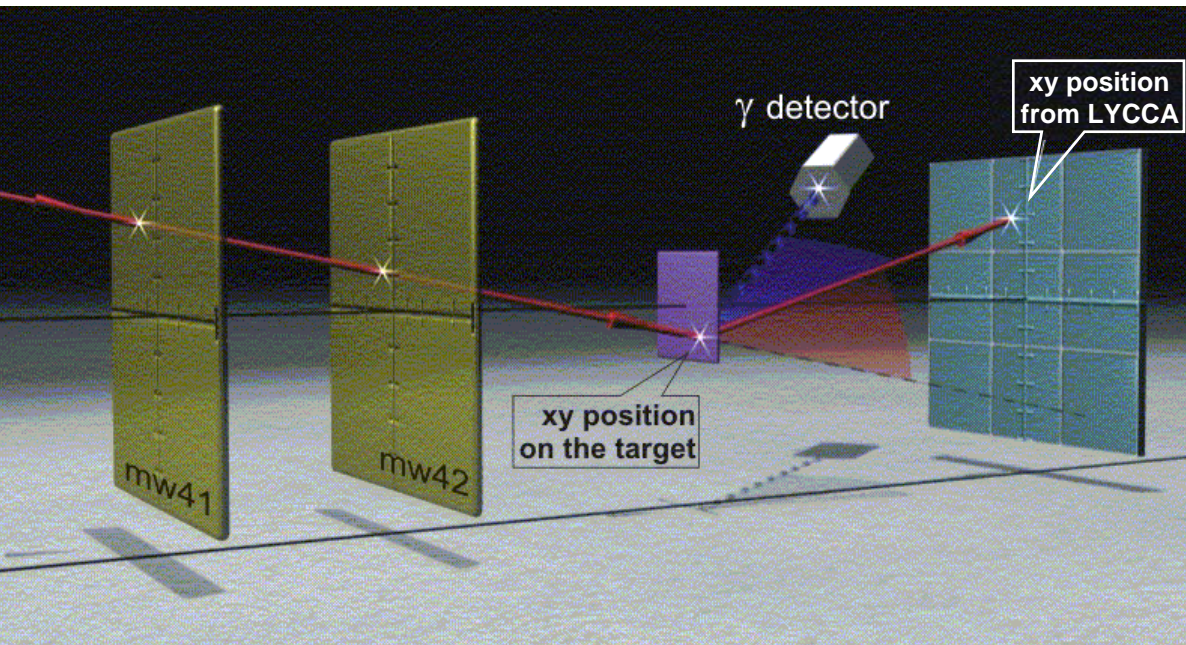
Stopping of high energy electrons in the target: $\sigma \sim Z_p^2 \cdot Z_t^2$



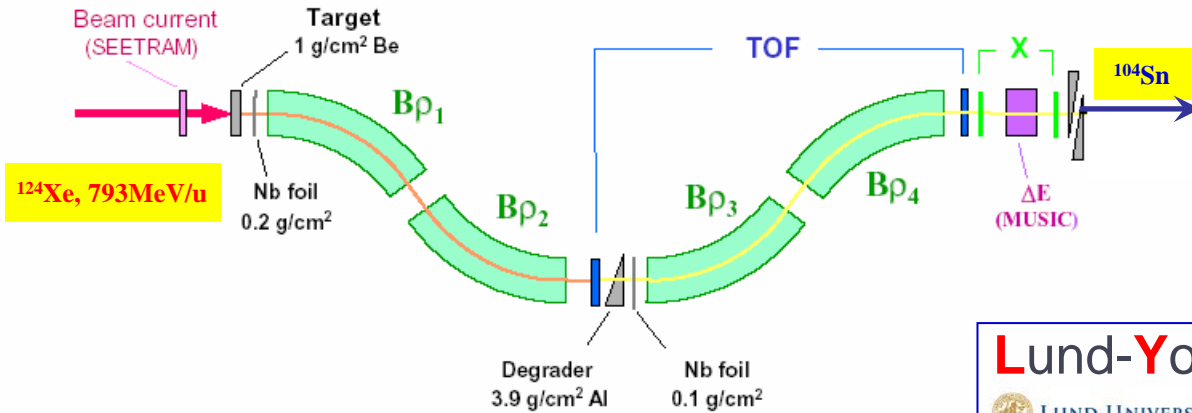
Scattering Experiment at Relativistic Energies



relativistic Coulomb excitation

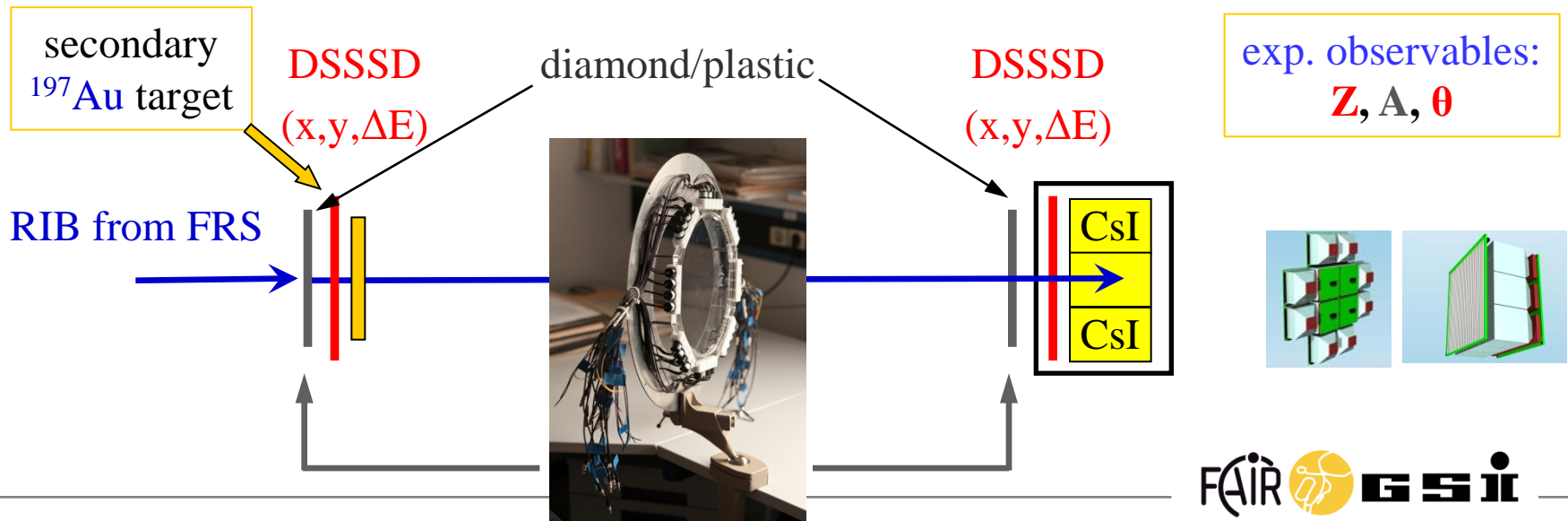


Scattering Experiment at Relativistic Energies

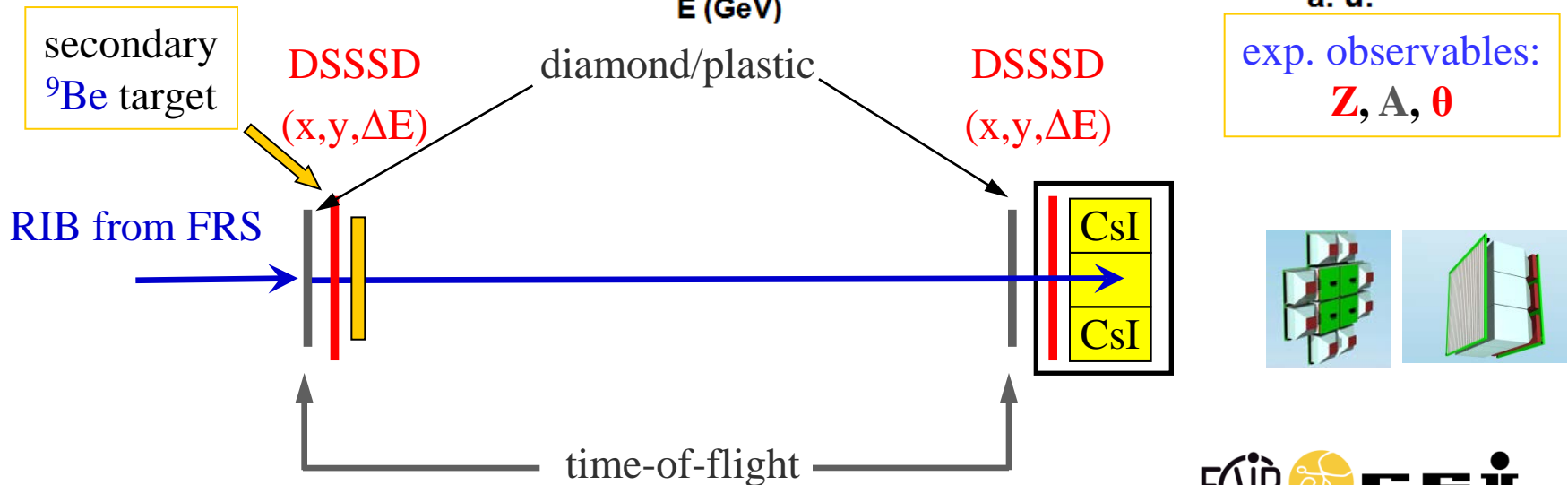
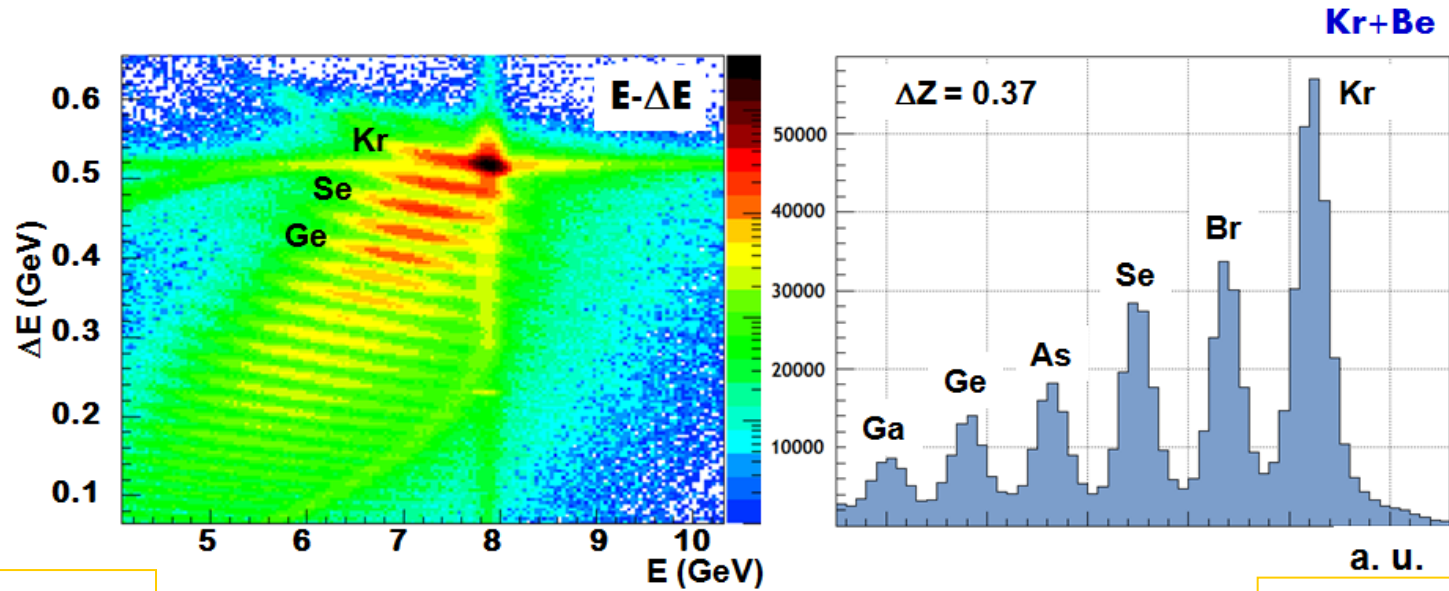


Lund-York-Cologne CALorimeter

LUND UNIVERSITY THE UNIVERSITY of York University of Cologne



Scattering Experiment at Relativistic Energies



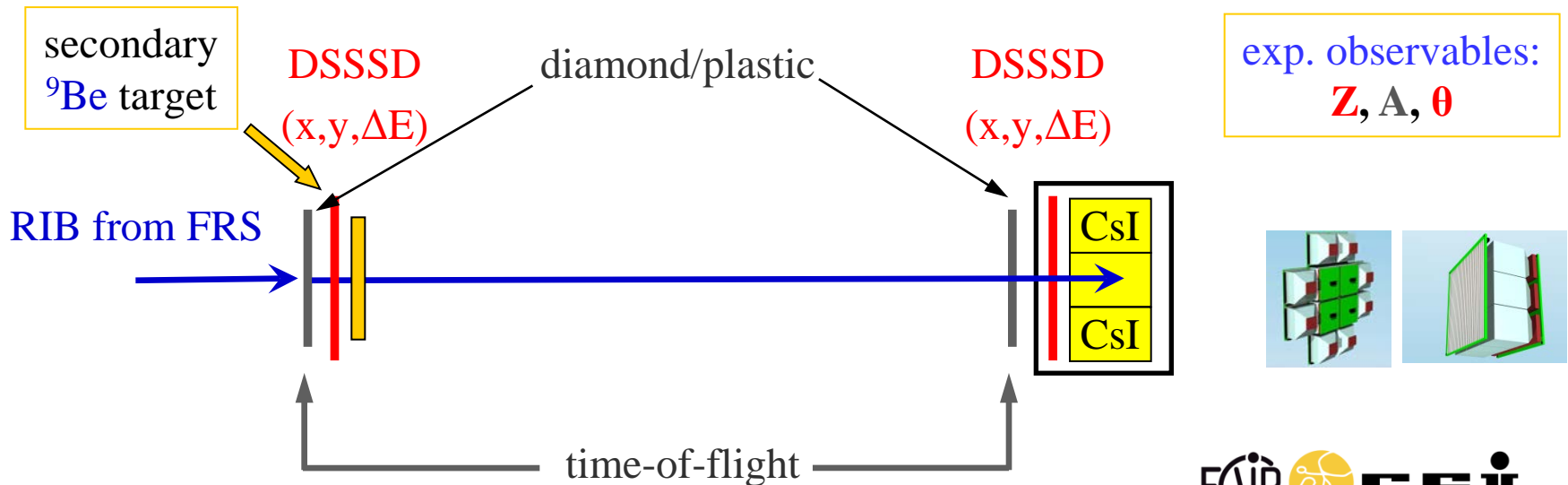
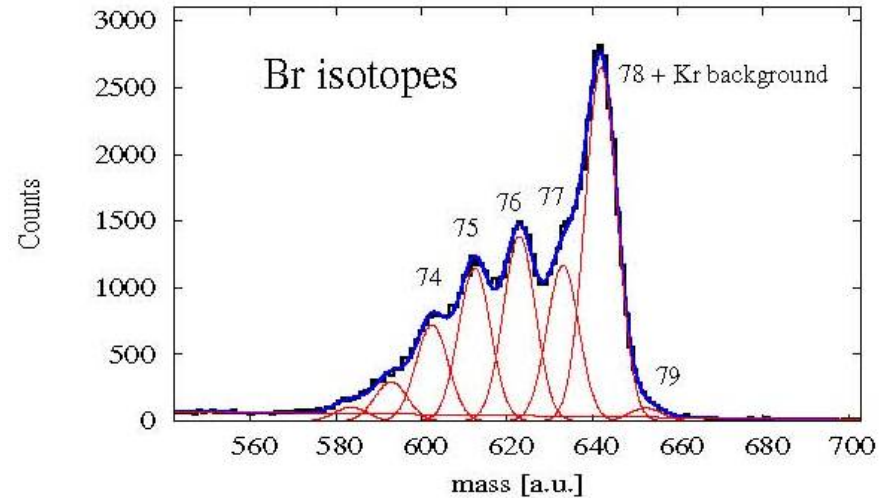
Scattering Experiment at Relativistic Energies

$$m \cdot c^2 = \frac{E_{kin}}{\gamma - 1}$$

with $E_{kin} = E_{CsI} + \Delta E_{DSSSD}$

and
$$\gamma = \frac{1}{\sqrt{1 - (v/c)^2}}$$

with v from LYCCA-ToF



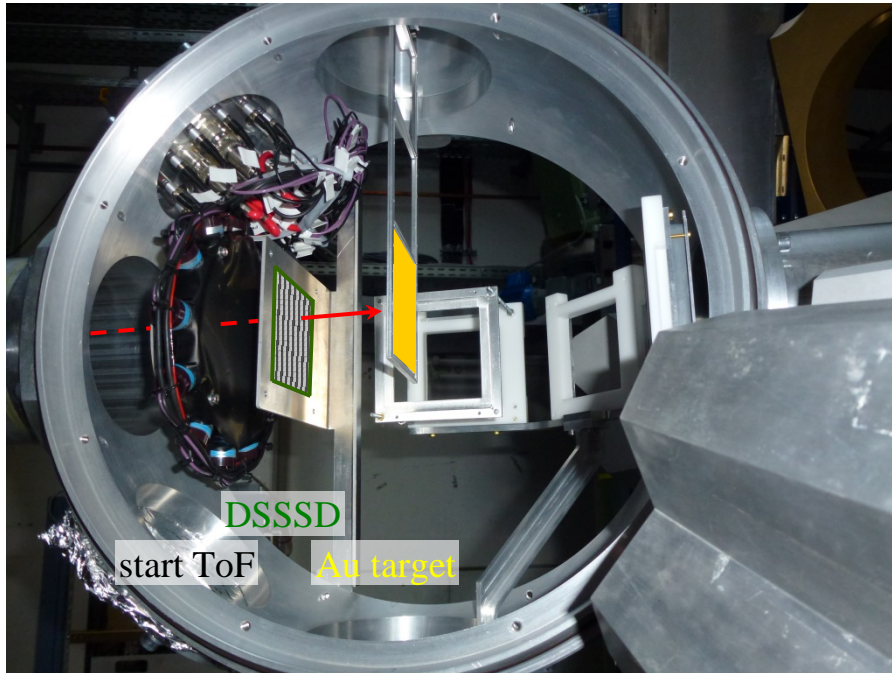
Lund-York-Cologne CAlorimeter



LUND UNIVERSITY



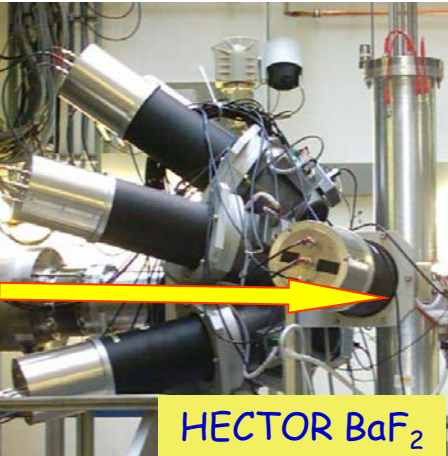
University of Cologne



*PreSPEC target chamber
variable target position (13cm, 23cm)*



Additional γ -Ray Background Radiation



^{37}Ca beam
at 196 MeV/u

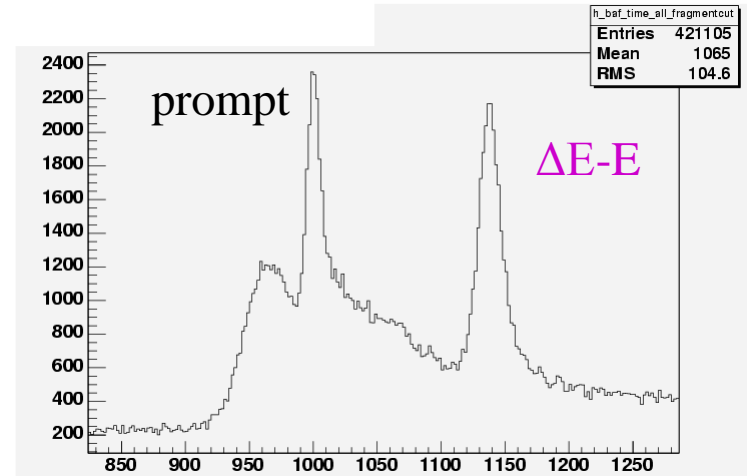
Coulomb excitation:

A/Q - ^{37}Ca
all Ca detected in $\Delta E-E$

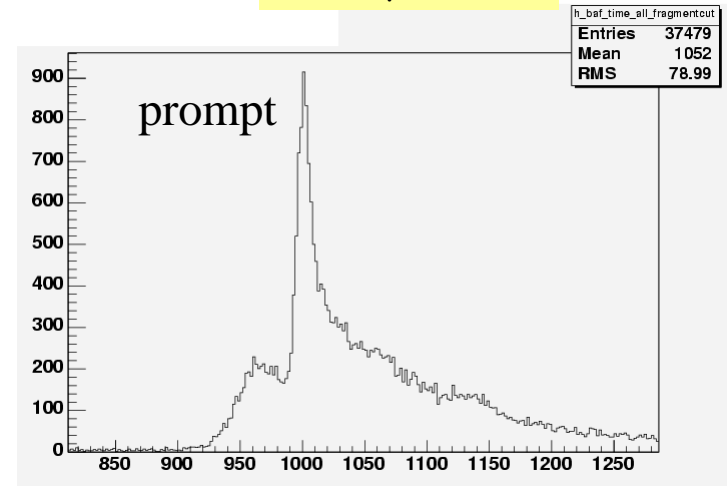
1% interaction target
most γ -rays from CATE

Fragmentation:

A/Q - ^{37}Ca
K detected (mainly ^{36}K)

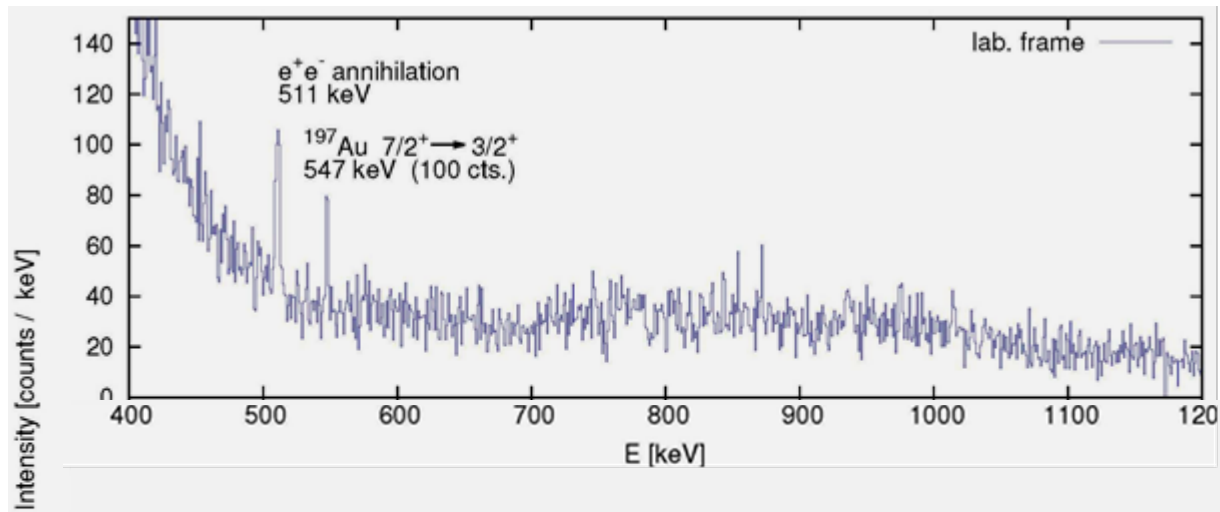


time spectrum



Scattering Experiment at Relativistic Energies

$^{80}\text{Kr} \rightarrow ^{197}\text{Au}$, 150 A MeV



Doppler effect

• ←---

$$\frac{E_{\gamma 0}}{E_{\gamma}} = \frac{1 - \beta \cdot \cos \vartheta_{\gamma}^{\text{lab}}}{\sqrt{1 - \beta^2}}$$

Scattering Experiment at Relativistic Energies

Doppler effect:

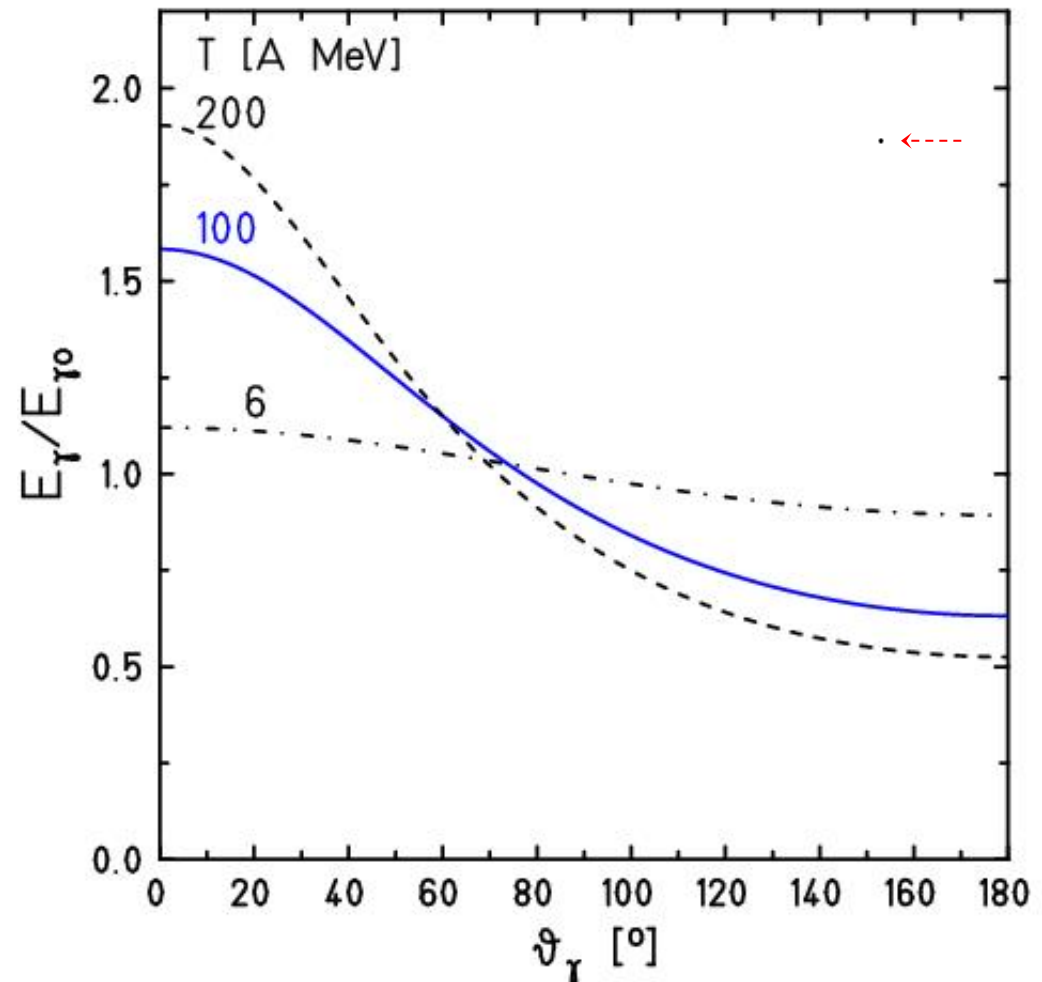
$$\frac{E_{\gamma 0}}{E_{\gamma}} = \frac{1 - \beta \cdot \cos \vartheta_{\gamma}^{\text{lab}}}{\sqrt{1 - \beta^2}} \quad \text{for } \vartheta_p \cong 0^\circ$$

Lorentz boost:

$$\frac{d\Omega_{\text{rest}}}{d\Omega_{\text{lab}}} = \left(\frac{E_{\gamma}}{E_{\gamma 0}} \right)^2$$

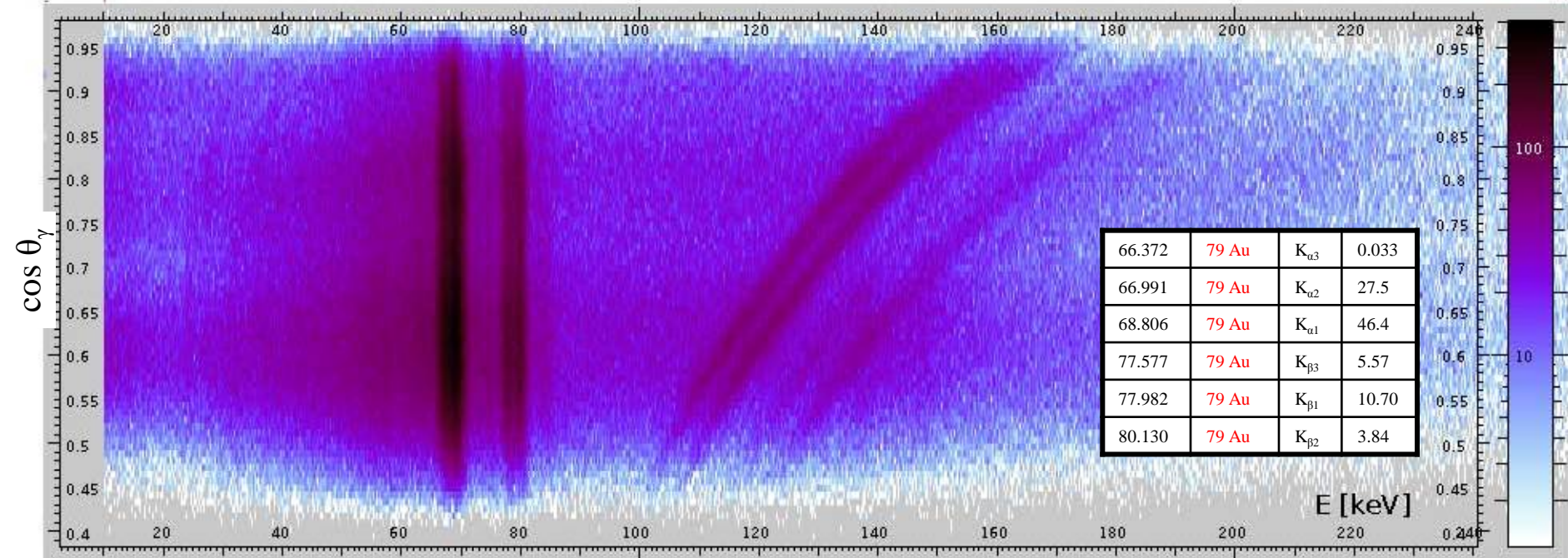
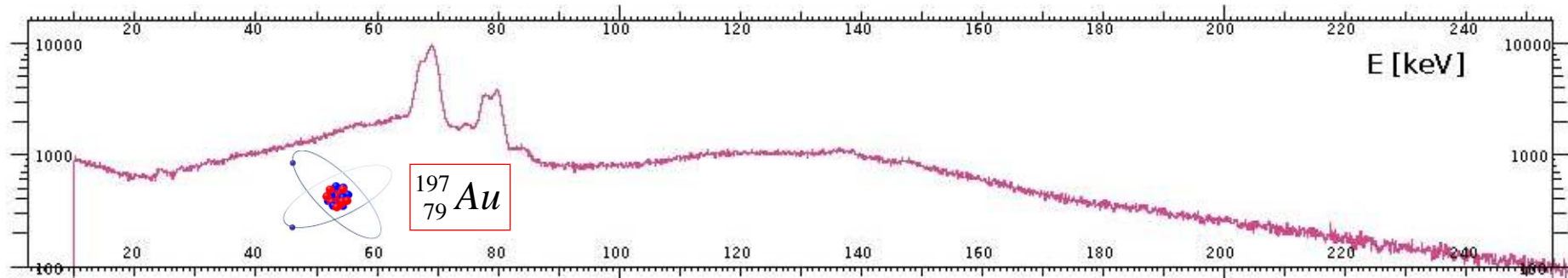


beam
←



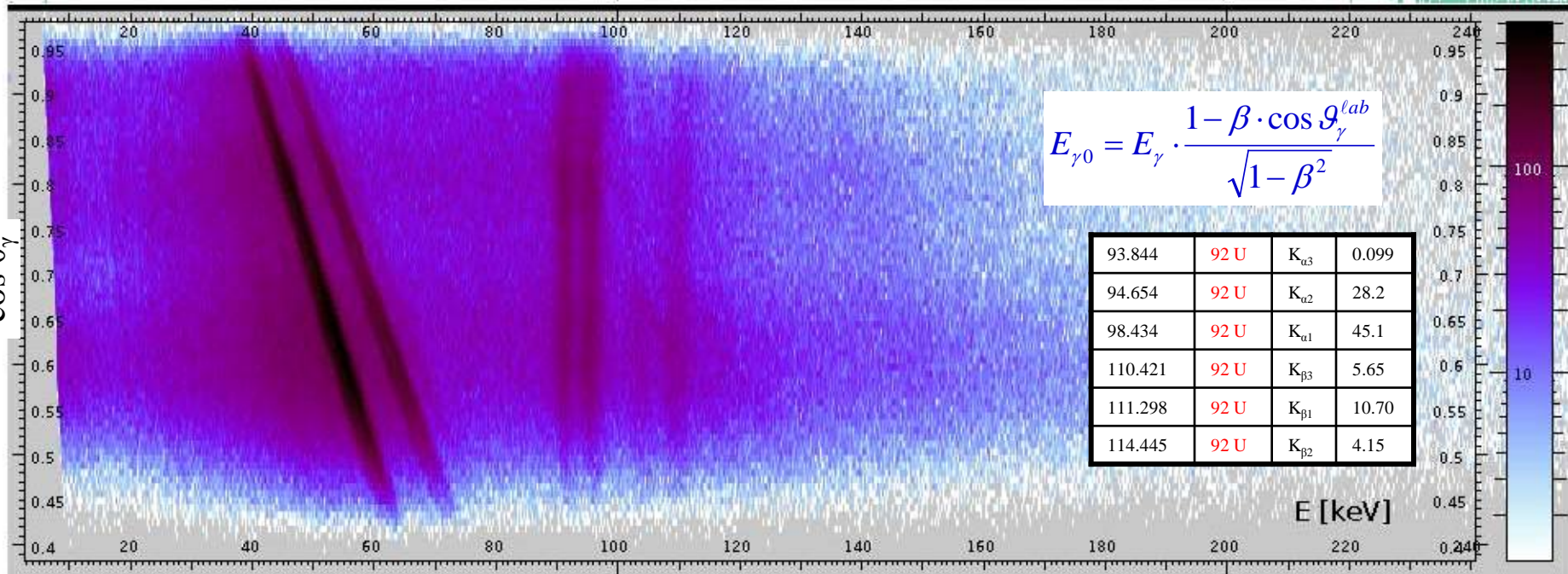
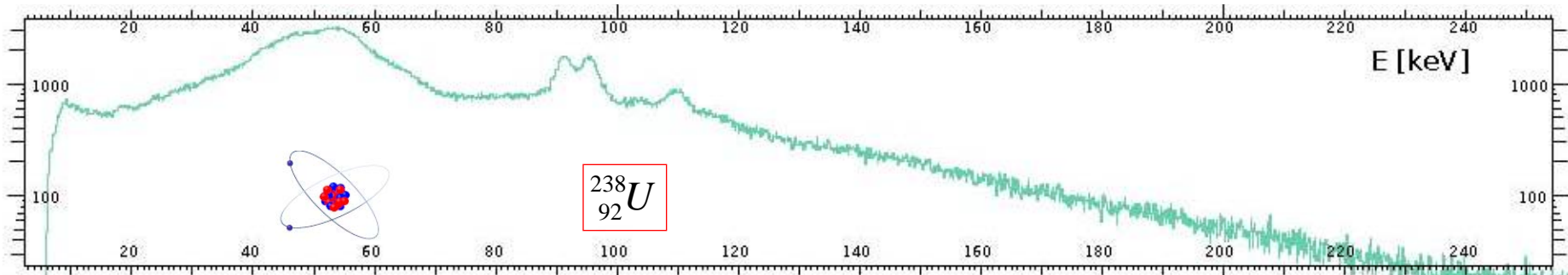
Doppler-Shift Correction

^{238}U on ^{197}Au (386 mg/cm²) at 183 AMeV

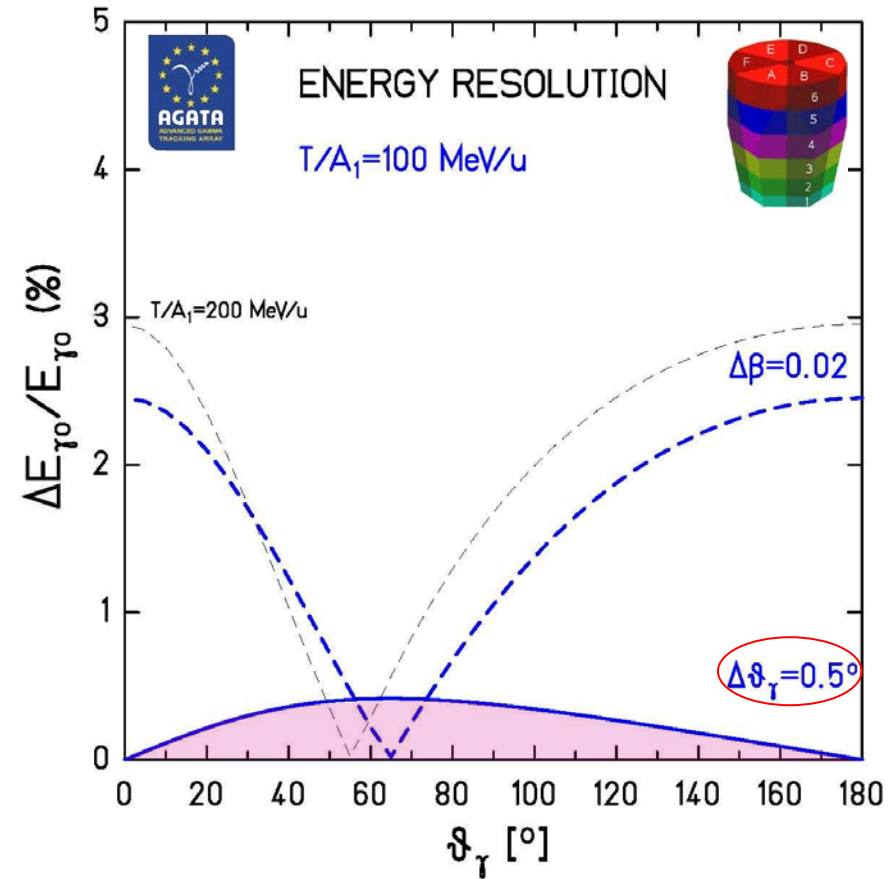
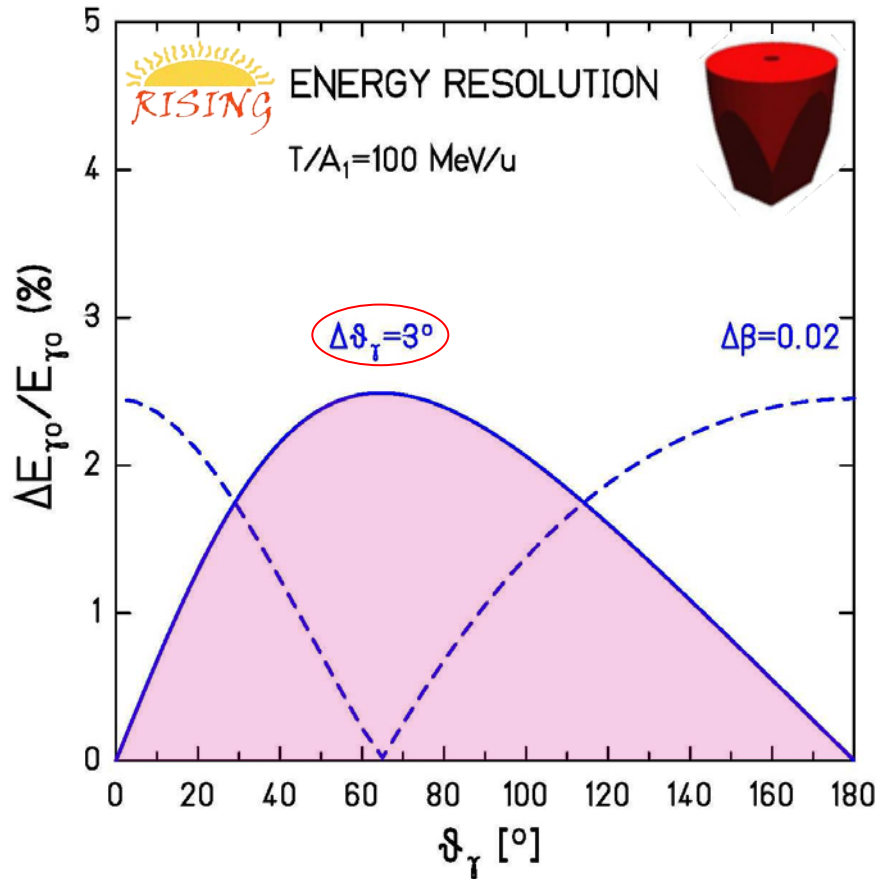


Doppler-Shift Correction

^{238}U on ^{197}Au (386 mg/cm²) at 183 AMeV



Doppler Broadening



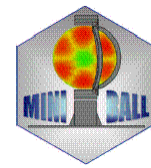
opening angle:

$$\frac{\Delta E_{\gamma 0}}{E_{\gamma 0}} = \frac{\beta \cdot \sin \vartheta_\gamma}{1 - \beta \cdot \cos \vartheta_\gamma} \cdot \Delta \vartheta_\gamma$$

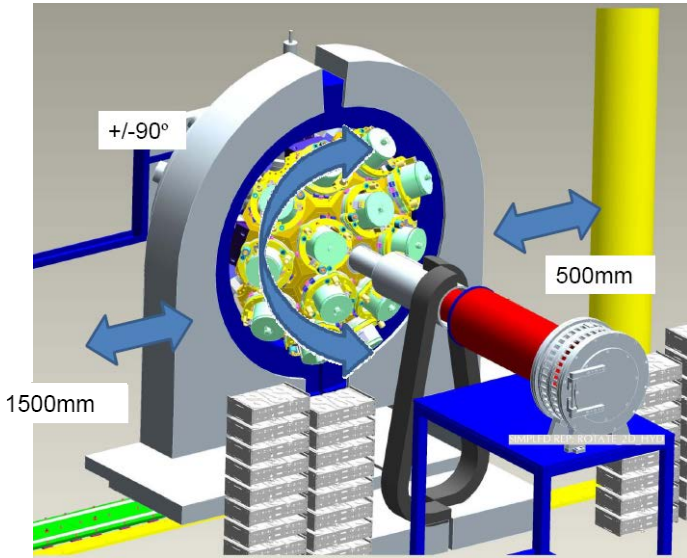
slowing down in target:

$$\frac{\Delta E_{\gamma 0}}{E_{\gamma 0}} = \frac{\beta - \cos \vartheta_\gamma}{(1 - \beta^2) \cdot (1 - \beta \cdot \cos \vartheta_\gamma)} \cdot \Delta \beta$$

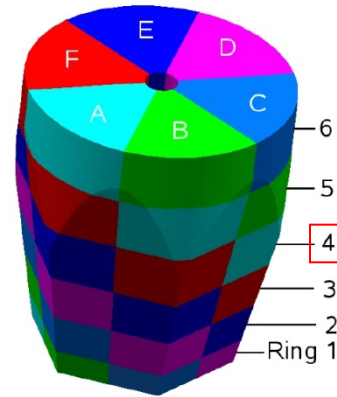
γ -ray set-up with higher efficiency



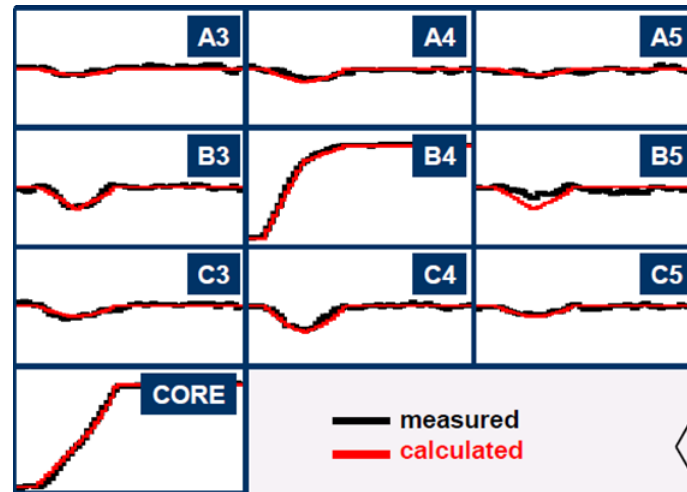
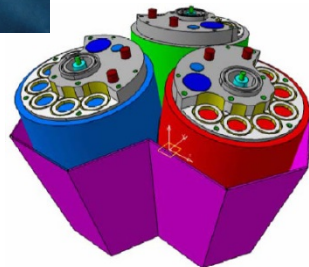
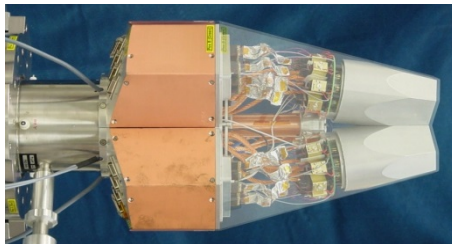
Advanced GAMMA Tracking Array



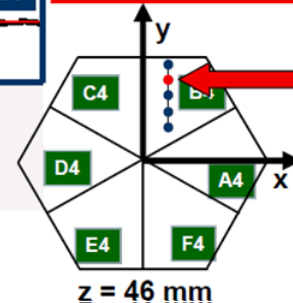
John Strachan



Signals from 36 segments + core are measured as a function of time (γ -ray interaction point)



Result of
Grid Search
Algorithm
(10, 25, 46)



791 keV deposited in segment B4

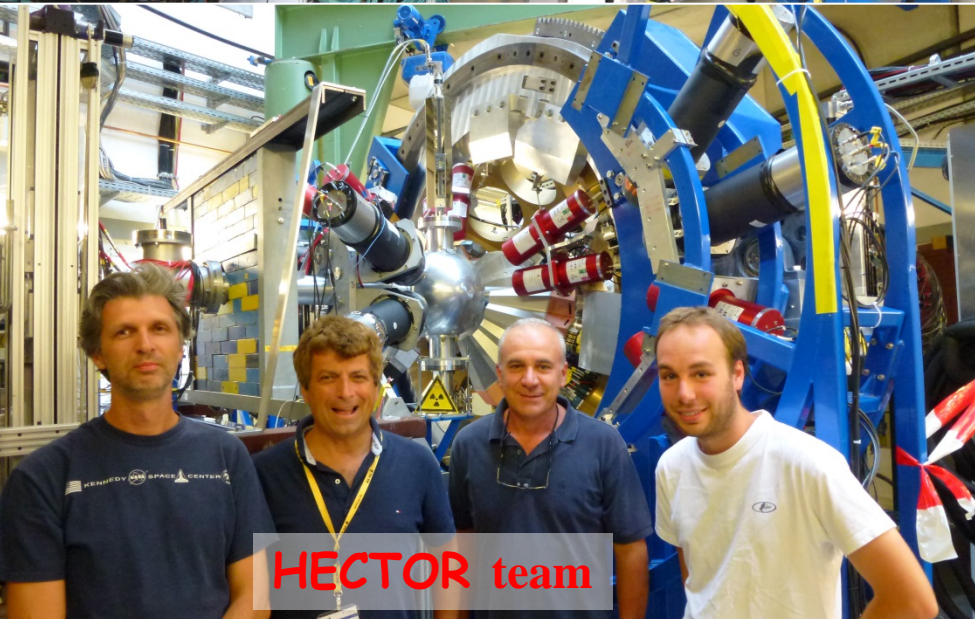
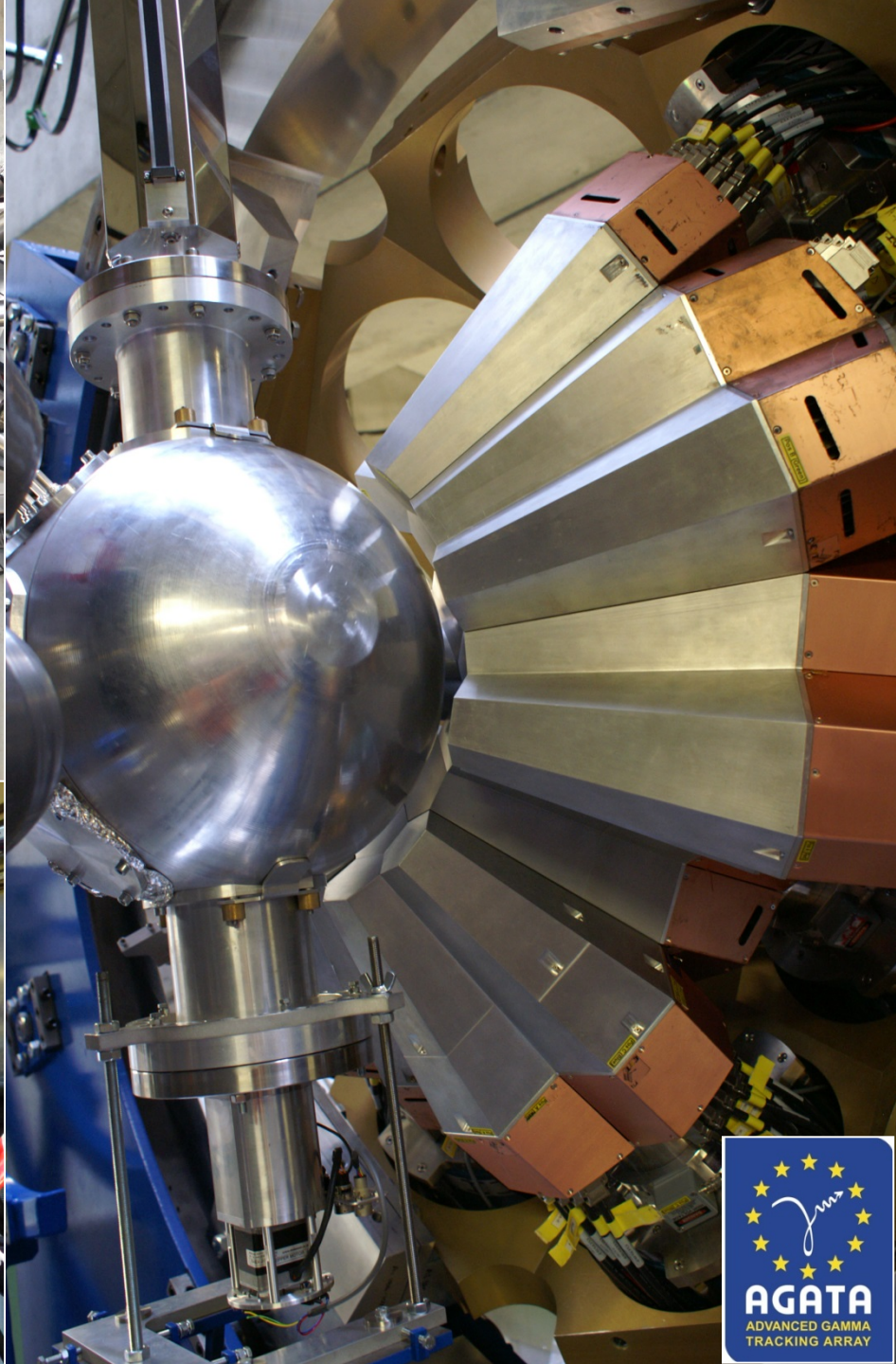
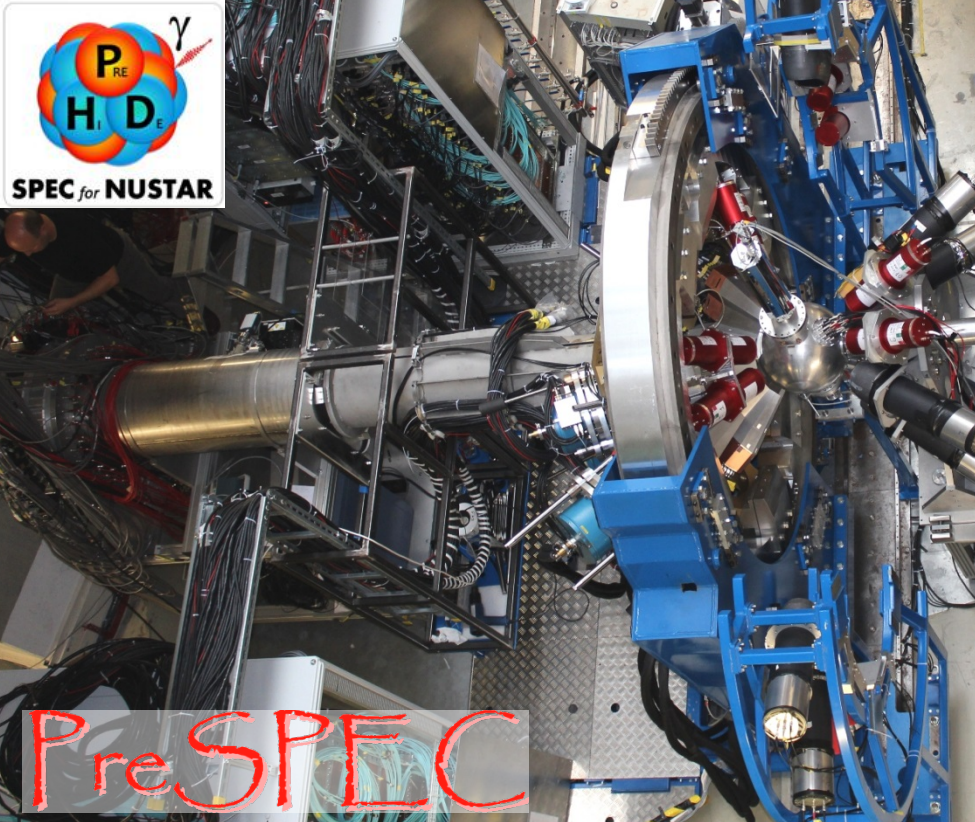
LYCCA

Au, Be target

AGATA Cluster array

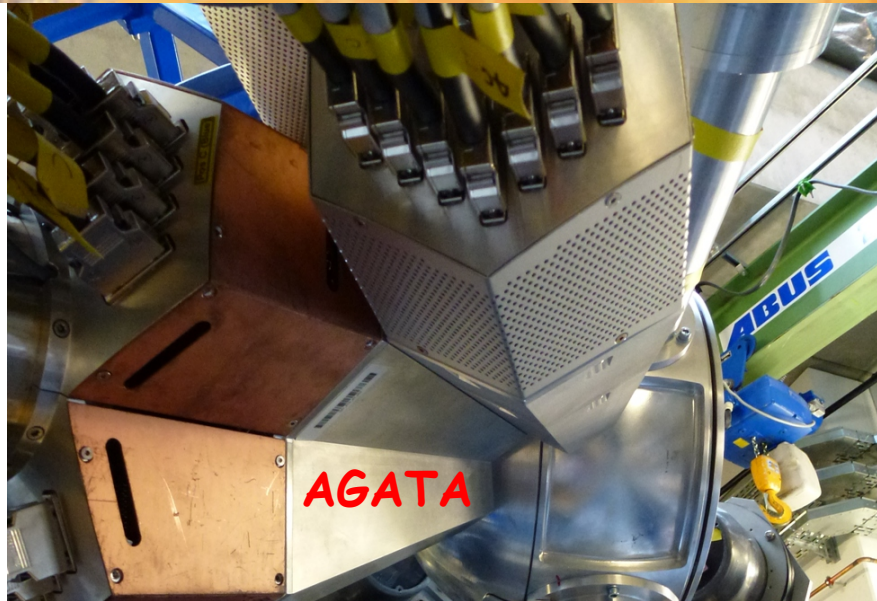
HECTOR BaF₂ array

PreSPEC

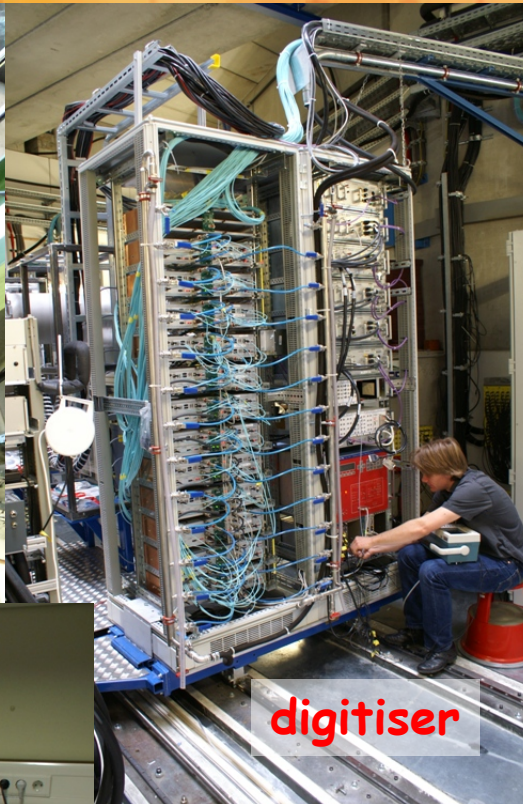




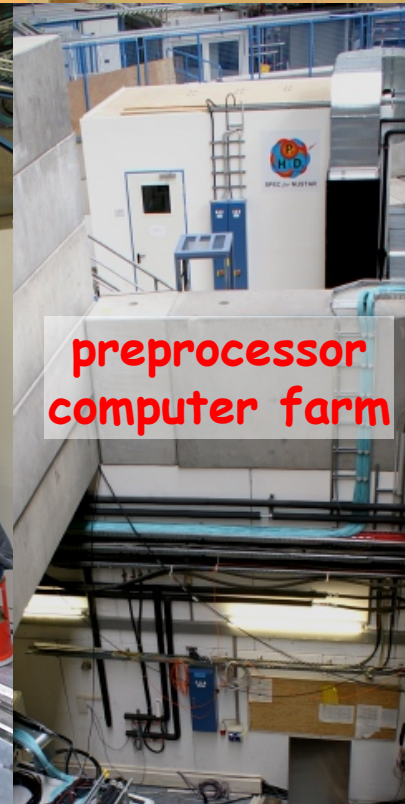
AGATA at PreSPEC



AGATA



digitiser



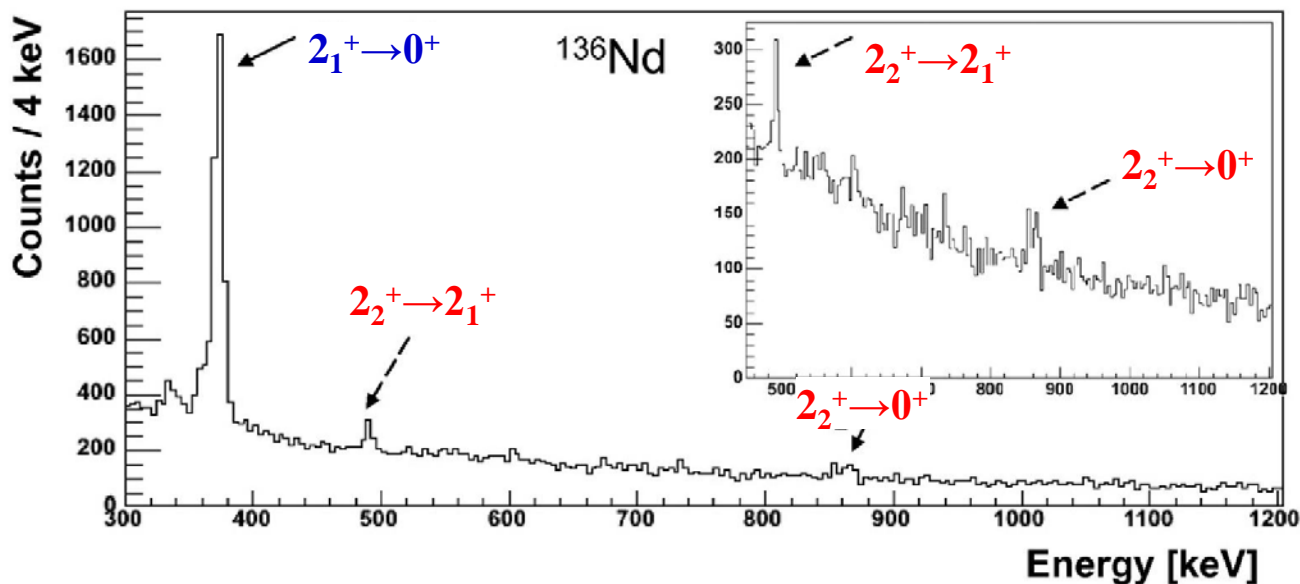
preprocessor
computer farm



*Damian Ralet,
Stephane Pietri*

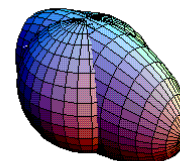


High-energy Coulomb excitation triaxiality in even-even nuclei ($N=76$)



First observation of a second excited 2^+ state
populated in a Coulomb experiment at 100 A MeV
using EUROBALL and MINIBALL Ge-detectors.

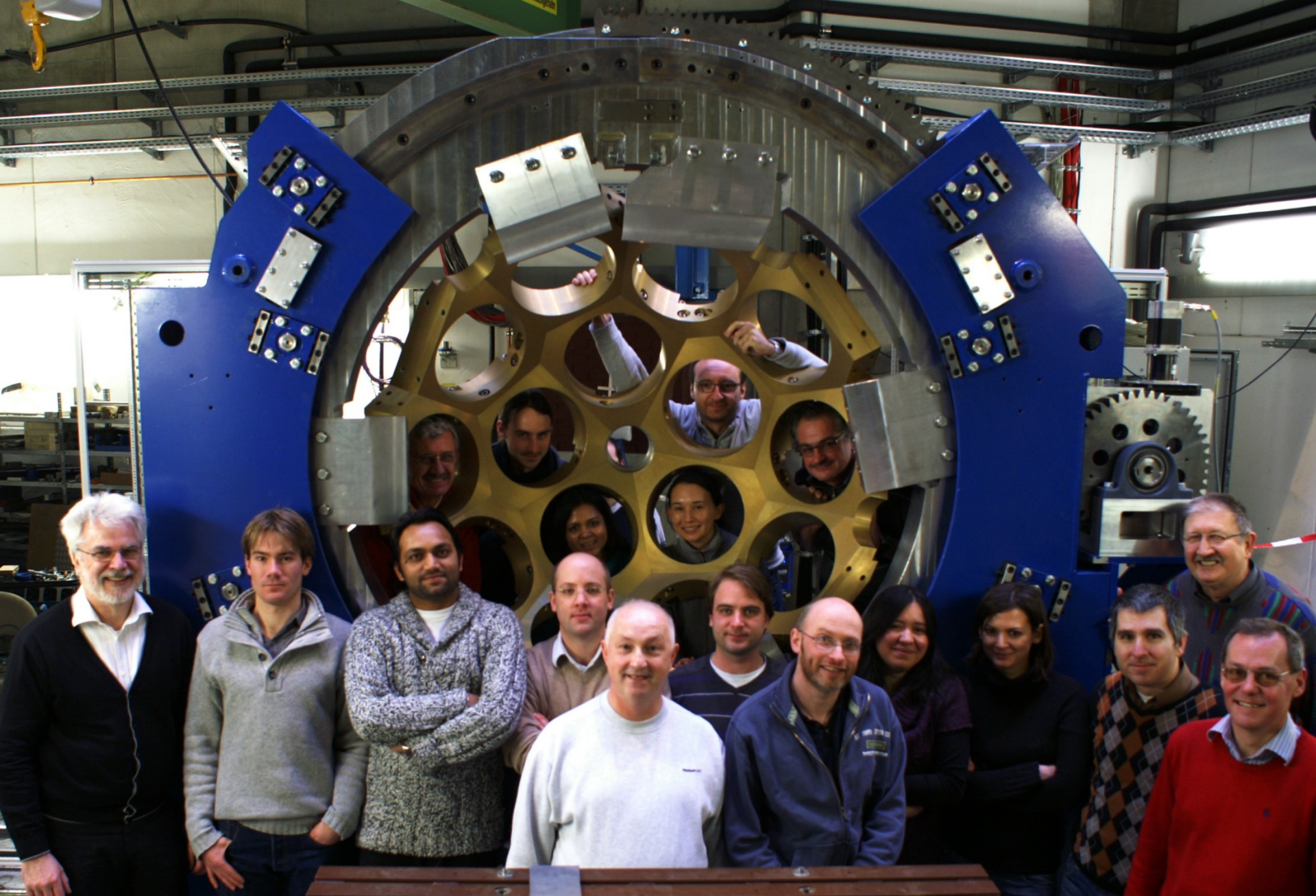
- shape symmetry
- collective strength



$$\frac{B(E2; 2_2 \rightarrow 2_1)}{B(E2; 2_1 \rightarrow 0)} = \frac{20 \sin^2(3\gamma)}{7 \sqrt{9 - 8 \sin^2(3\gamma)}} \frac{1}{1 + \frac{3 - 2 \sin^2(3\gamma)}{\sqrt{9 - 8 \sin^2(3\gamma)}}}$$

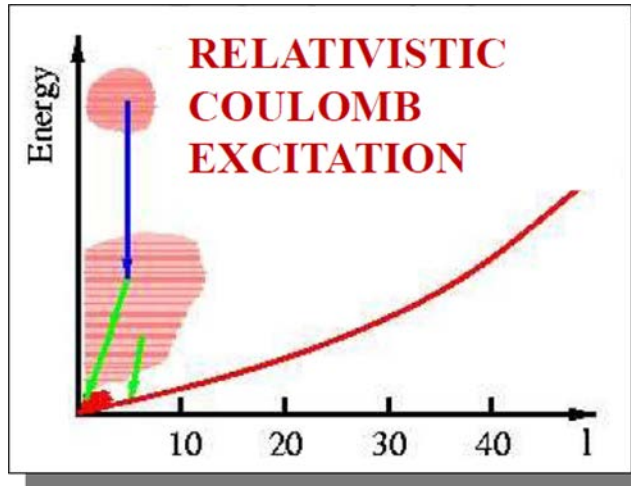
$$\frac{B(E2; 2_2 \rightarrow 0)}{B(E2; 2_1 \rightarrow 0)} = \frac{1 - \frac{3 - 2 \sin^2(3\gamma)}{\sqrt{9 - 8 \sin^2(3\gamma)}}}{1 + \frac{3 - 2 \sin^2(3\gamma)}{\sqrt{9 - 8 \sin^2(3\gamma)}}}$$

$$\frac{E_2(2)}{E_1(2)} = \frac{3 + \sqrt{9 - 8 \sin^2 3\gamma}}{3 - \sqrt{9 - 8 \sin^2 3\gamma}}$$

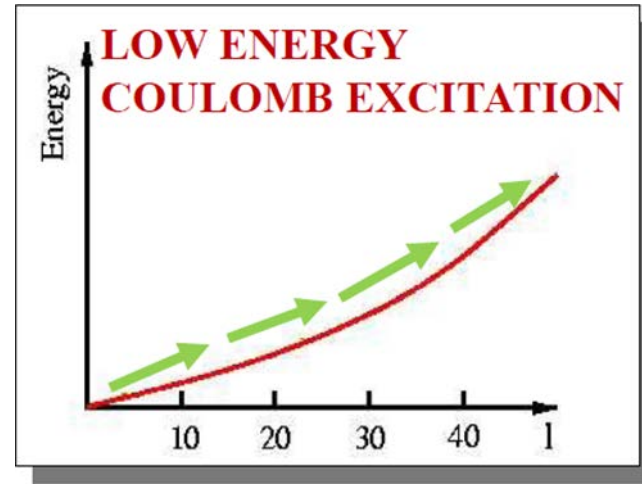


Ivan Kojouharov, Michael Reese, Namita Goel, Liliana Cortes, Frederic Ameil, Bogdan Szczepanczyk
H.-J. W., Damian Ralet, Pushpendra Singh, Stephane Pietri, Tobias Habermann, Edana Merchan, Giulia Guastalla, Plamen Boutachkov, Adolf Brünle,
Ian Burrows, Jonathan Strachan, (Paul Morral), Jürgen Gerl, (Henning Schaffner, Magda Gorska)

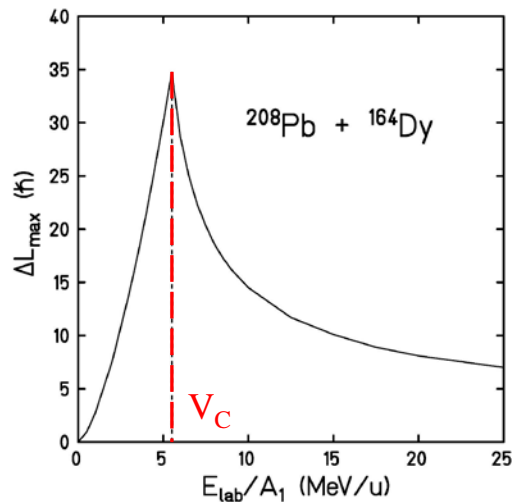
Slowed down beams – new experimental perspectives



collective strength



nuclear shape



angular momentum transfer:

$$\Delta L_{\text{max}} \cong \frac{Z_P \cdot e^2 \cdot Q_0}{4 \cdot \hbar \cdot v \cdot a^2} \cdot (1 - \cos \theta_{cm})$$

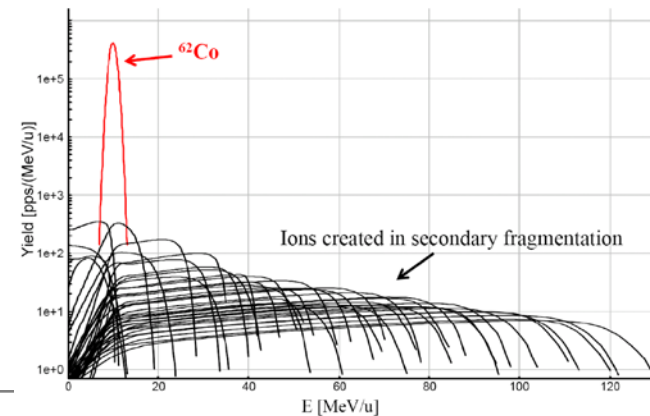
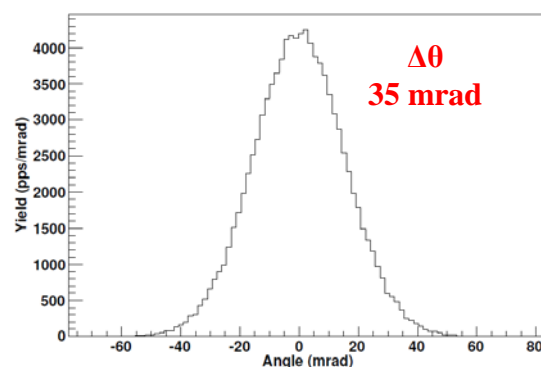
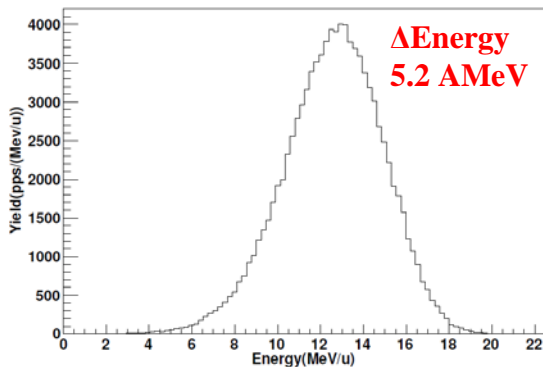
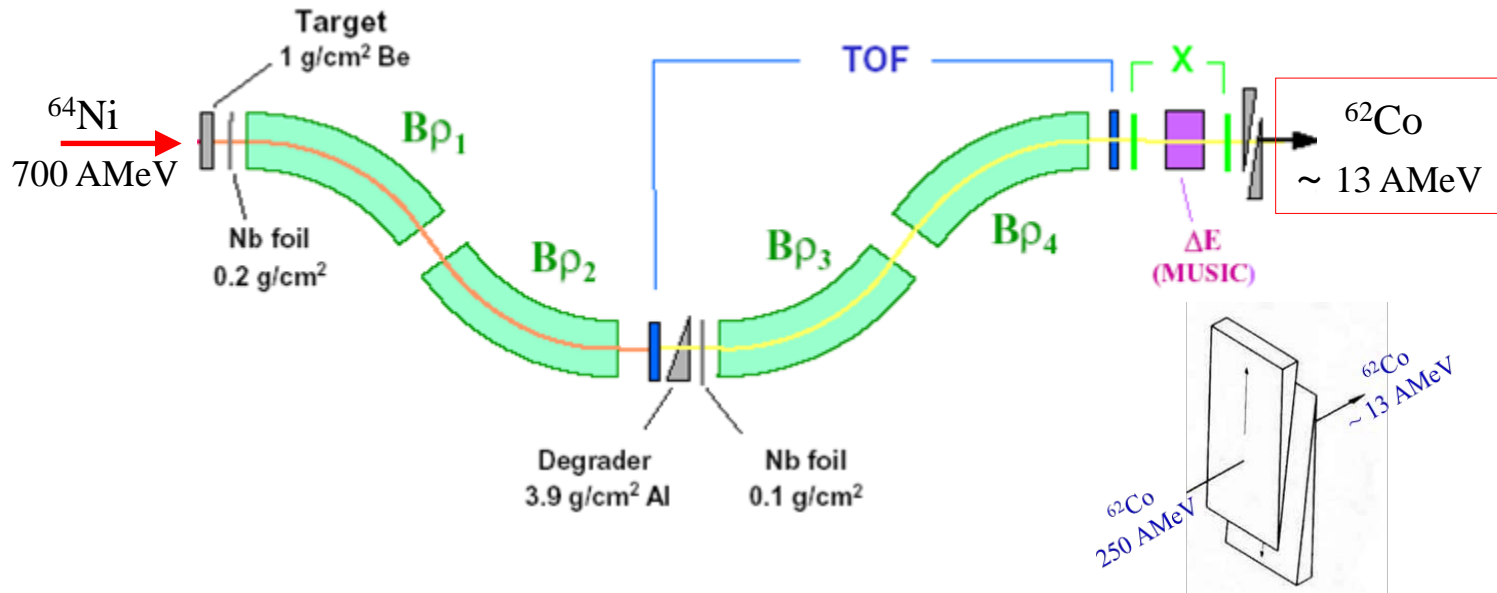
Slowed down beams – beam characteristics

10^9 pps

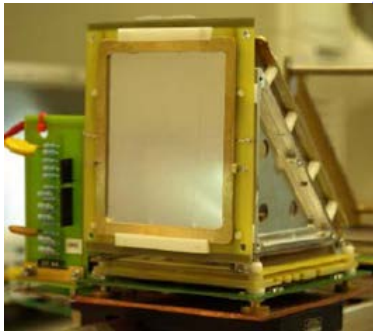
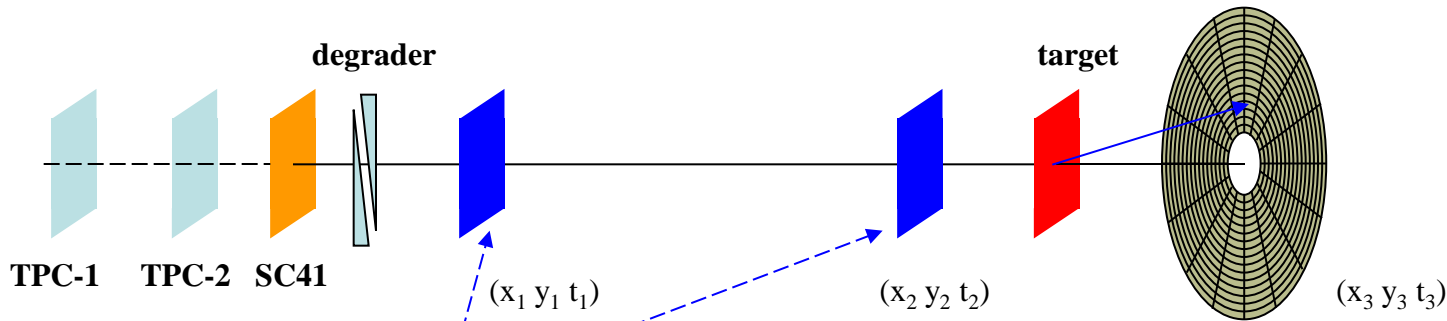
10^7 pps

$3 \cdot 10^6$ pps

10^5 pps

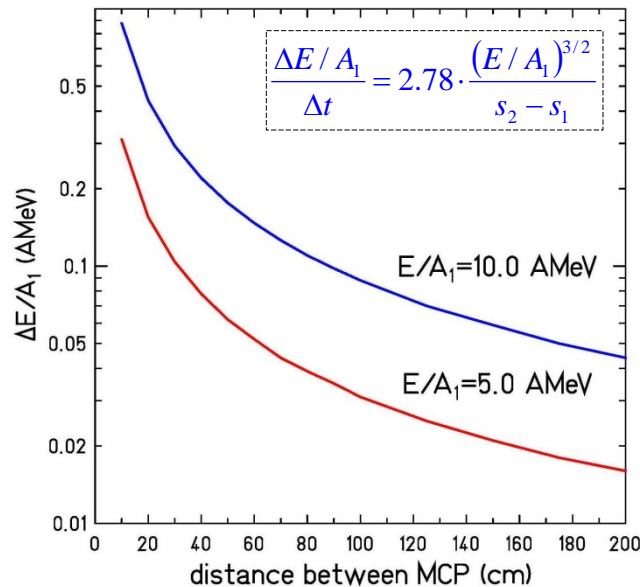


Slowed down beams – experimental set-up



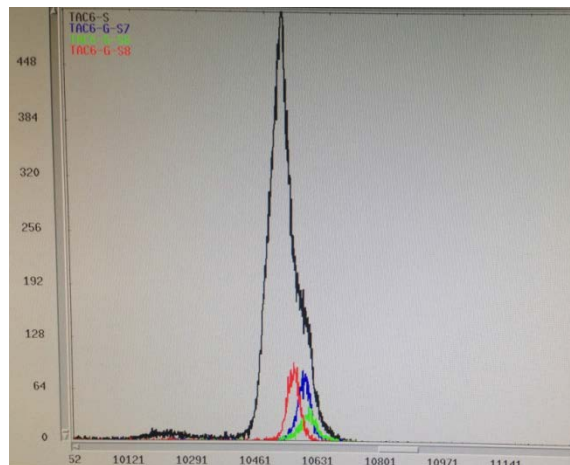
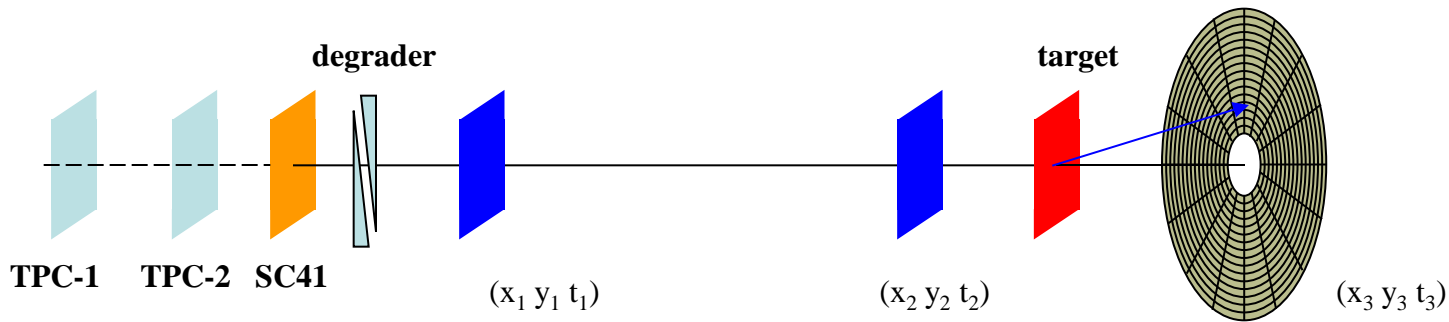
electrostatic mirror + MCP detector

position resolution ~ 1 mm
time resolution ~ 100 ps

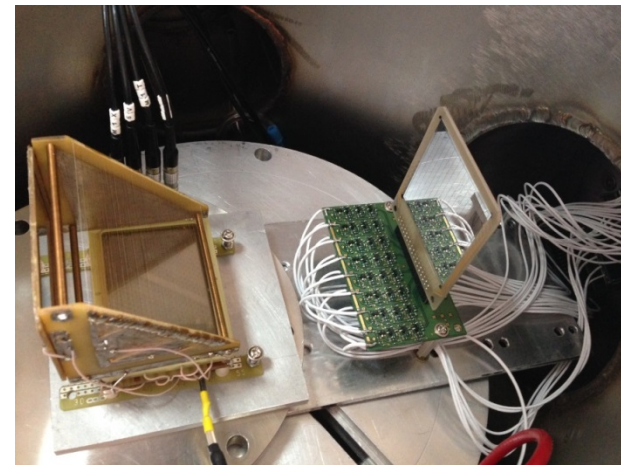


experimental results:
velocity β
beam energy E/A_1
scattering angle θ_{cm}

Slowed down beams – experimental set-up



TOF between MCP and DSSSD



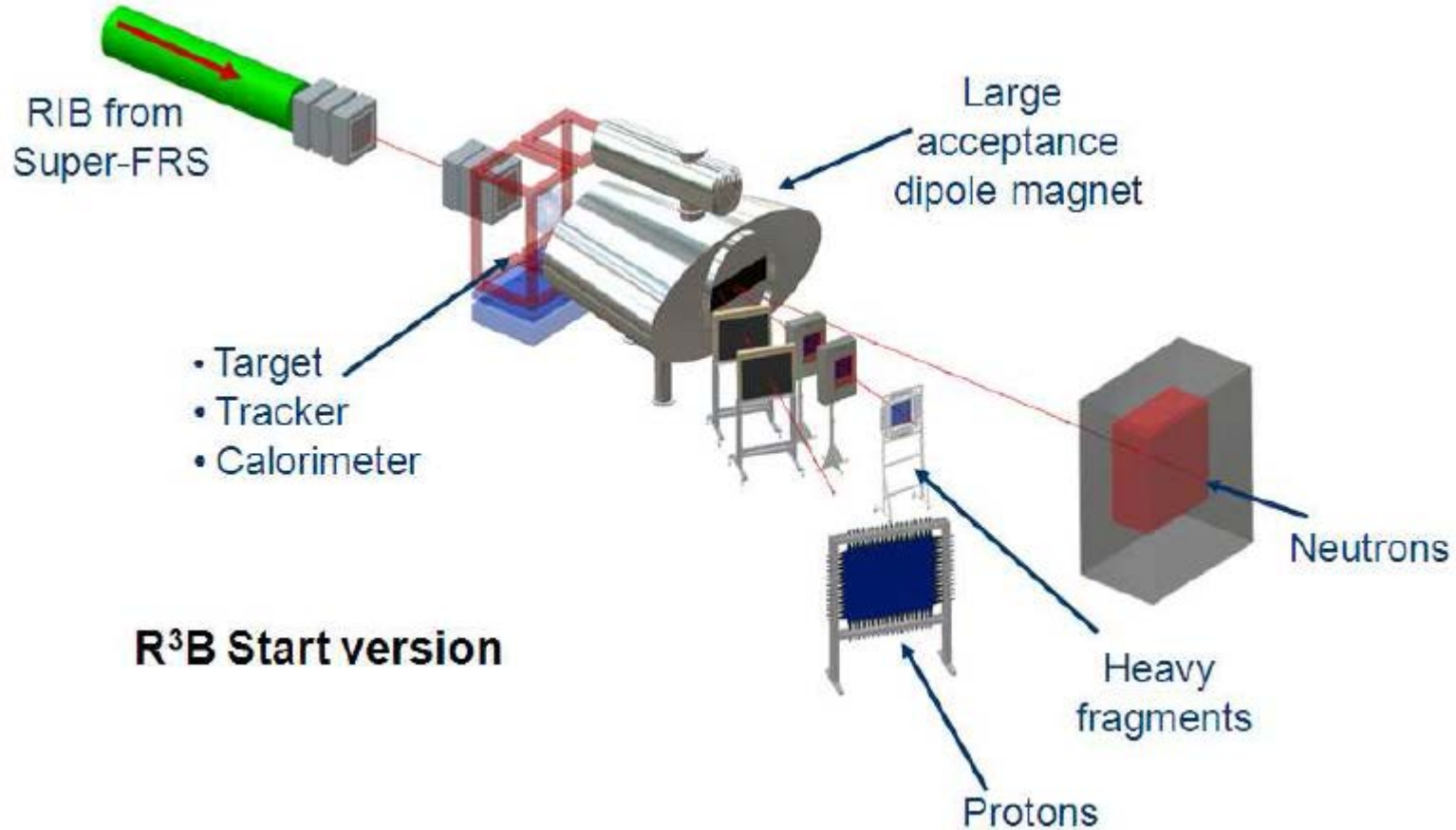
MCP

DSSSD

Time resolution 200 ps for one of the 256 detector pixels

Akhil Jhingan (IUAC)

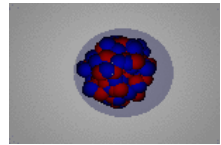
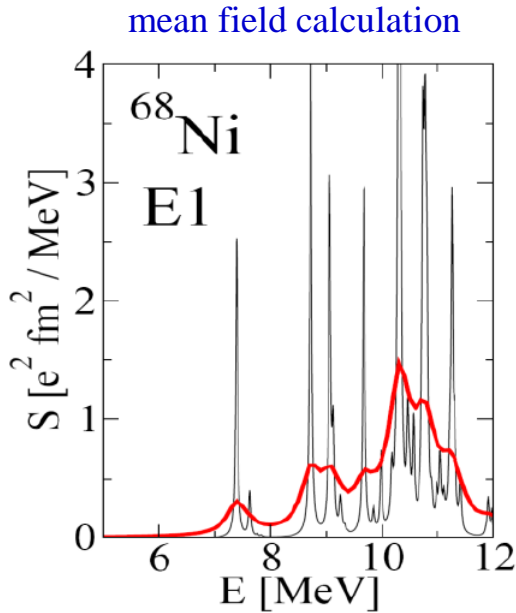
Reactions with Relativistic Radioactive Beams – R³B



Excitation energy E^* from kinematically complete measurement of all outgoing particles

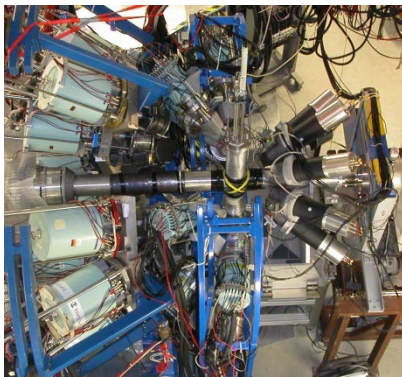
$$E^* = \left(\sqrt{\sum_i m_i^2 + \sum_{i \neq j} m_i m_j \gamma_i \gamma_j (1 - \beta_i \beta_j \cos \vartheta_{ij})} - m_{proj} \right) c^2 + E_{\gamma, sum}$$

Dipole strength distribution of ^{68}Ni

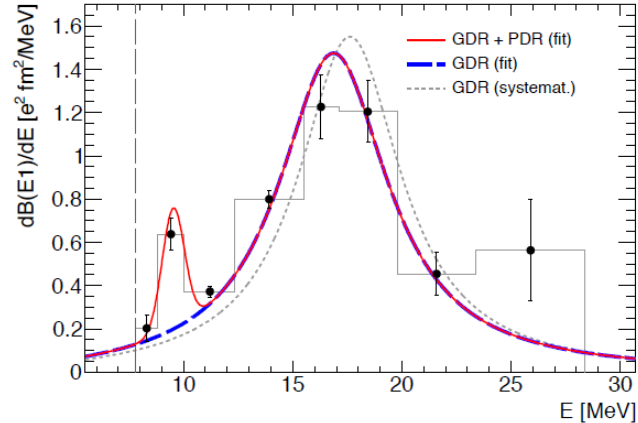


Pygmy resonance

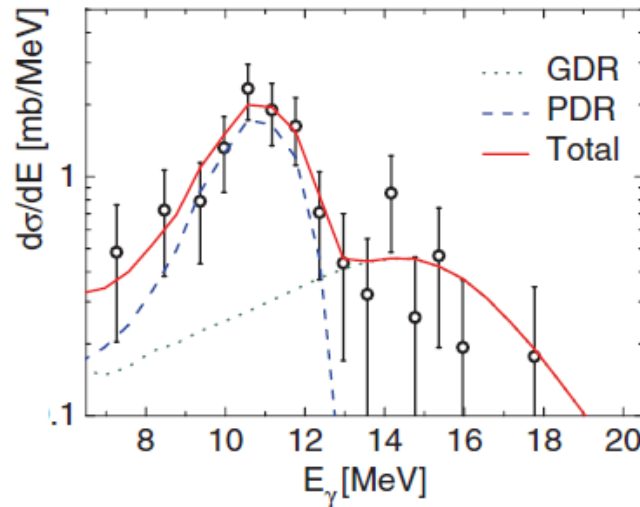
E.Litvinova et al.; PRC 79, (2009) 054312



O. Wieland et al.; Phys. Rev. Lett 102, 092502 (2009)



neutron decay data



γ -ray decay data

direct γ -decay
branching ratio:

$$\Gamma_0/\Gamma = 7(2)\%$$

D. Rossi et al.; Phys. Rev. Lett 111, 242503 (2013)