PHL424: Gravitational Waves – Ripples of Spacetime

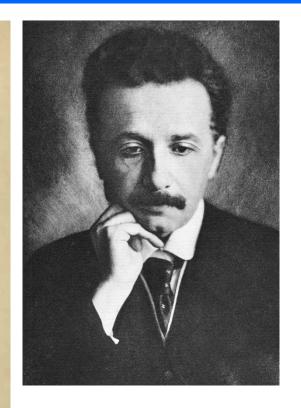
154 Gesamtsitzung vom 14. Februar 1918. — Mitteilung vom 31. Januar

Über Gravitationswellen.

Von A. EINSTEIN.

(Vorgelegt am 31. Januar 1918 [s. oben S. 79].)

Die wichtige Frage, wie die Ausbreitung der Gravitationsfelder erfolgt, ist schon vor anderthalb Jahren in einer Akademiearbeit von mir behandelt worden¹. Da aber meine damalige Darstellung des Gegenstandes nicht genügend durchsichtig und außerdem durch einen bedauerlichen Rechenfehler verunstaltet ist, muß ich hier nochmals auf die Angelegenheit zurückkommen.



First publication on gravitational waves in June 1916

Almost 100 years later

PRL 116, 061102 (2016)

Selected for a Viewpoint in Physics PHYSICAL REVIEW LETTERS

week ending 12 FEBRUARY 2016



Observation of Gravitational Waves from a Binary Black Hole Merger

B. P. Abbott et al.*

(LIGO Scientific Collaboration and Virgo Collaboration)

(Received 21 January 2016; published 11 February 2016)

On September 14, 2015 at 09:50:45 UTC the two detectors of the Laser Interferometer Gravitational-Wave Observatory simultaneously observed a transient gravitational-wave signal. The signal sweeps upwards in frequency from 35 to 250 Hz with a peak gravitational-wave strain of 1.0×10^{-21} . It matches the waveform predicted by general relativity for the inspiral and merger of a pair of black holes and the ringdown of the resulting single black hole. The signal was observed with a matched-filter signal-to-noise ratio of 24 and a false alarm rate estimated to be less than 1 event per 203 000 years, equivalent to a significance greater than 5.1 σ . The source lies at a luminosity distance of 410^{+160}_{-180} Mpc corresponding to a redshift $z=0.09^{+0.03}_{-0.05}$. In the source frame, the initial black hole masses are $36^{+5}_{-4}M_{\odot}$ and $29^{+4}_{-4}M_{\odot}$, and the final black hole mass is $62^{+4}_{-4}M_{\odot}$, with $3.0^{+0.5}_{-0.5}M_{\odot}c^2$ radiated in gravitational waves. All uncertainties define 90% credible intervals. These observations demonstrate the existence of binary stellar-mass black hole systems. This is the first direct detection of gravitational waves and the first observation of a binary black hole merger.

first direct evidence of gravitational waves signal indicates the merging of two black holes

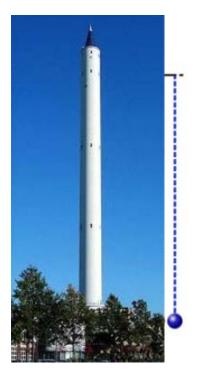
LIGO: Laser Interferometer Gravitational-Wave Observatory





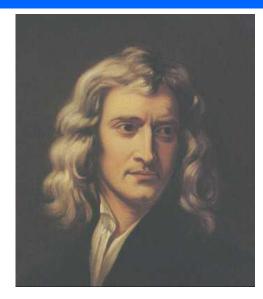
Equivalence Principle

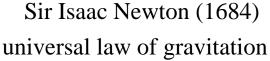
- ❖ Heavy mass: How strongly is a body attracted by the Earth?
- ❖ Inertial mass: How much power is needed to accelerate a body?
- ❖ Galileo Galilei (1590): All bodies fall equally fast (in vacuum)
- \rightarrow heavy mass = inertial mass



The Bremen drop tower

Gravity: The Old School





- Unified the gravity on Earth, the motion of the Moon, planets and comets
- Final confirmation of Newton's theory:
 - Halley's Comet returns as predicted in 1758





Electromagnetism

- ❖ James Clerk Maxwell (1864): Unification of electricity and magnetism
- \rightarrow electromagnetism



- ❖ Heinrich Hertz (1888): Light, radio waves, X-rays are electromagnetic waves velocity: 299792 km/s duration Sun – Earth ~ 8 min
- → interaction delayed, e.g. between electrical charges



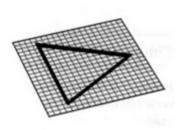
The Special Relativity

- Newton's gravitation:
 Foundation for classical mechanics.
 - no maximum velocity instantaneous interaction

- ❖ Albert Einstein (1905):
 Theory of special relativity:
 - velocity of light is the limit
 - instantaneous interactionis not allowed! contradiction with Newton!
 - Space and time (space-time) are curved
 - Matter causes this curvature
 - Space tells matter how to move
 - This looks to us like gravity

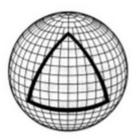


Curved Space



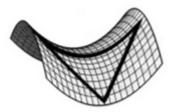
Flat Curvature

 Σ angles = 180°



Positive Curvature

 Σ angles > 180°



Negative Curvature

 Σ angles < 180°

❖ In 2 dimensions

flat space: plane

triangle: $\alpha + \beta + \gamma = 180^{\circ}$

positive curvature: sphere

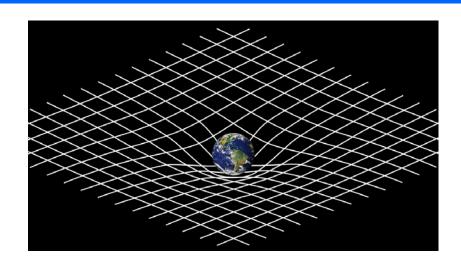
triangle: $\alpha + \beta + \gamma > 180^{\circ}$

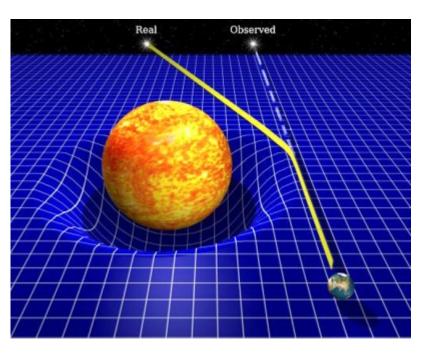
negative curvature: saddle

triangle: $\alpha + \beta + \gamma < 180^{\circ}$

Curved Space-Time

Space-time curved by the Earth mass





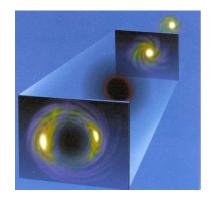
Arthur Eddington (1919):
 Deflection of light by sun's gravitational field

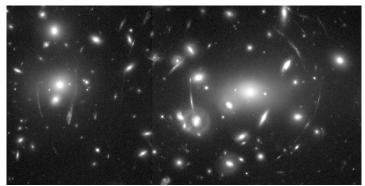
 First successful test of Einstein's theory
 Geometry bends light



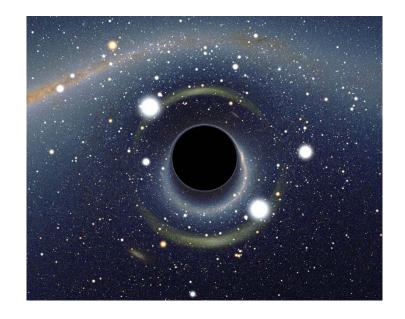
Other Phenomena

- Gravitational lenses
- \rightarrow Einstein rings





- * Karl Schwarzschild (1916): curvature can be as strong, that light can not escape.
- \rightarrow black hole



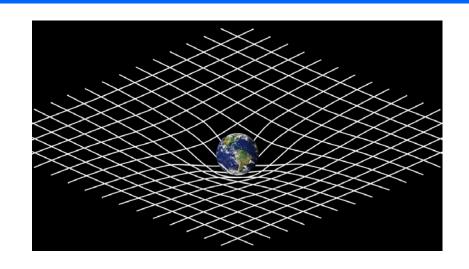


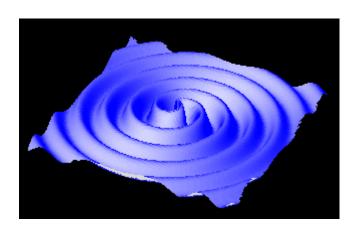


What are Gravitational Waves?

Einstein's General theory of relativity:

Gravity → Curvature of 4-dimensional space-time produced by matter

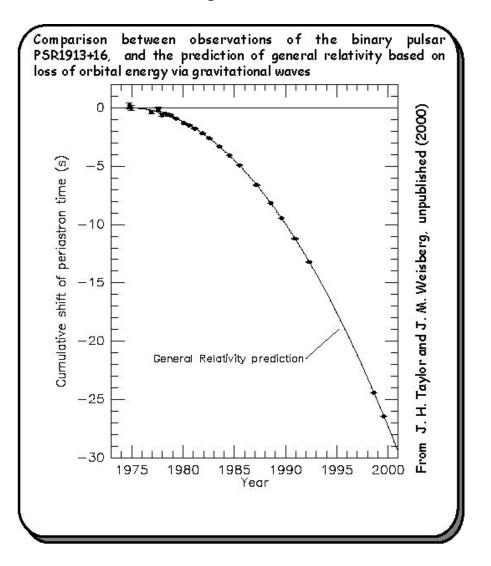




Gravitational waves:
 Ripples on space-time
 produced by accelerated matter

Orbital decay: strong indirect evidence

Emission of gravitational waves



- Binary systems emit gravitational waves
- Gravitational waves carry energy
- System looses energy, spiral inwards
- Orbit period decreases at a predicted rate
 0.0000758 sec/year
- Observed rate:

 $0.0000759 \pm 2 \ sec/year$



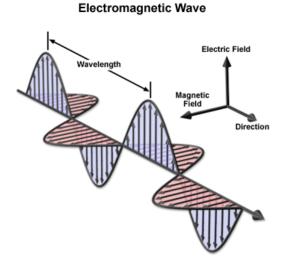


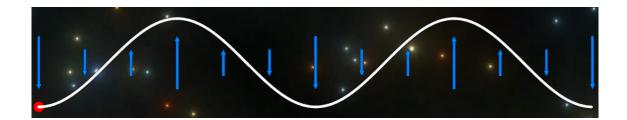
Joseph Taylor & Russell Hulse, NP 1993



Electromagnetic waves

- ❖ So far, nearly all our knowledge of the Universe comes from electromagnetic radiation
- Time-varying disturbance in electromagnetic field
- Arise as a direct consequence of relativity (causality)
 - Field of a stationary charge
 - Field of a moving charge
 - Field of an accelerated charge
- ◆ Oscillating charges → waves with characteristic lengths

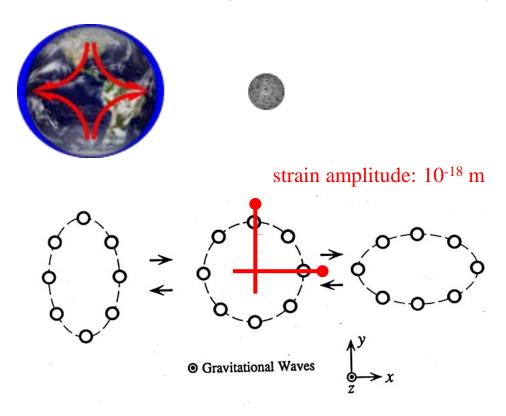


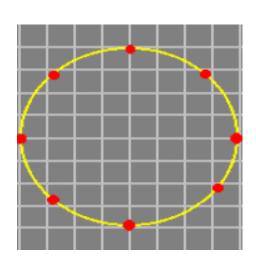




Gravitational waves

- The key property of gravity is that it affects all bodies equivalently, with a force that is proportional to the body's mass.
- This means that it is impossible to measure directly an overall gravitational field. The best one can do is to measure the change in the gravitational field.
- The effect of gravity from a remote object, such as the Sun or Moon, can be felt by the manner in which it changes from location to location, gravity tidal field.





How small is 10⁻¹⁸ meter?

One meter

Human hair, about 100 microns

Wavelength of light, about 1 micron



Atomic diameter, 10⁻¹⁰ meter



Nuclear diameter, 10⁻¹⁵ meter

LIGO sensitivity, 10⁻¹⁸ meter

Gravitational waves

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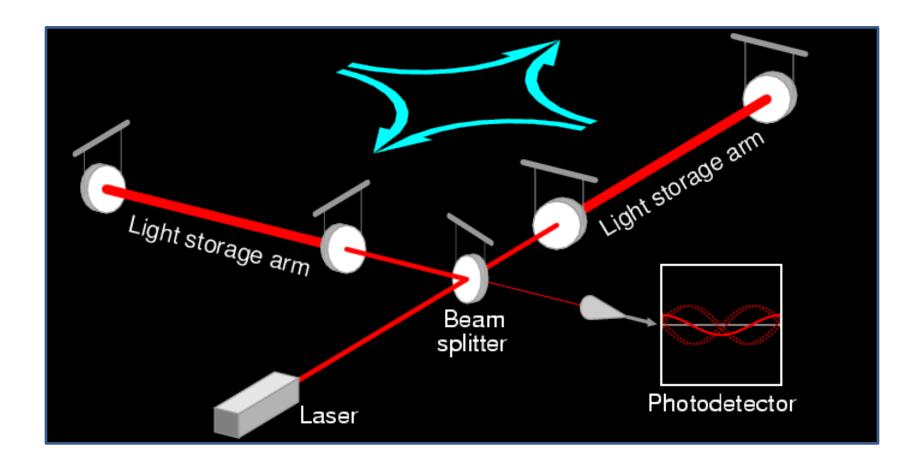




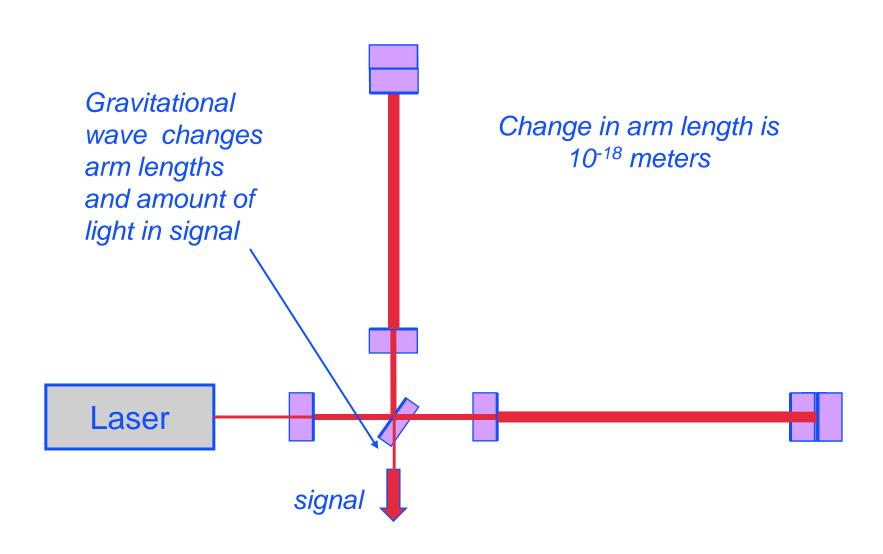


Detecting gravitational waves

• Laser interferometers: measure relative motions of separate, freely-hanging masses



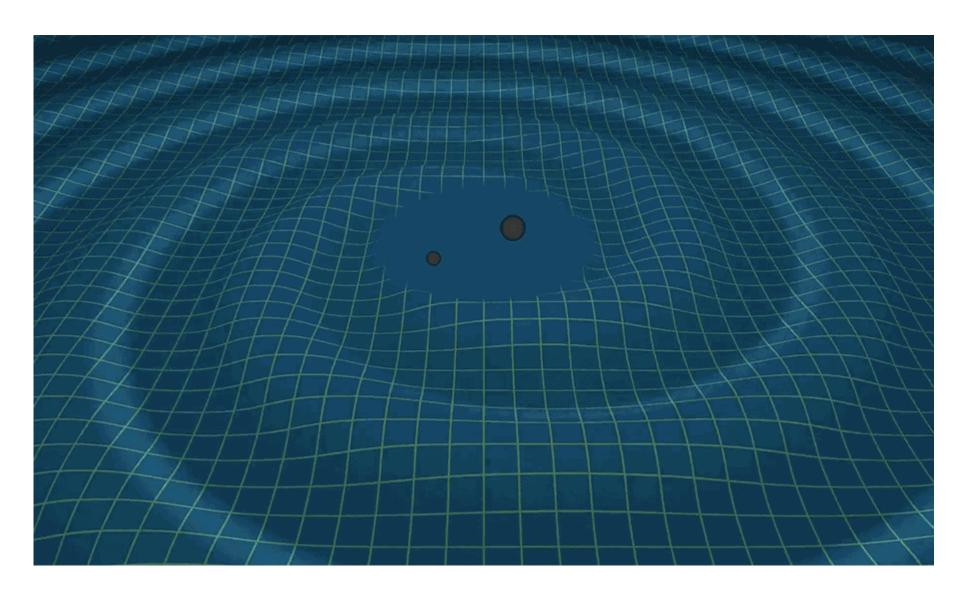
Sensing the Effect of a Gravitational Wave







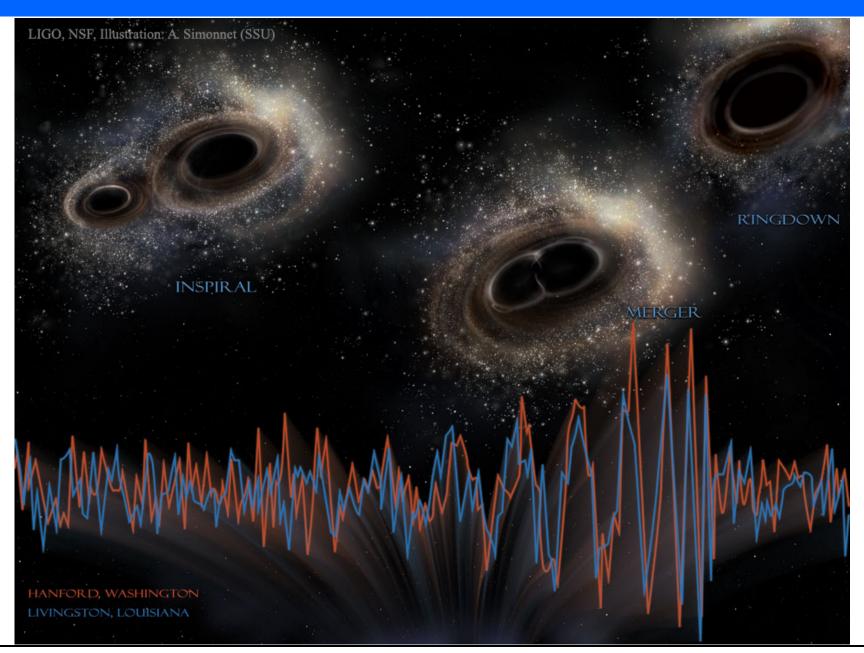
Gravitational waves







Gravitational waves



Inspiraling Compact Binaries

Ground-Based (hectahertz)

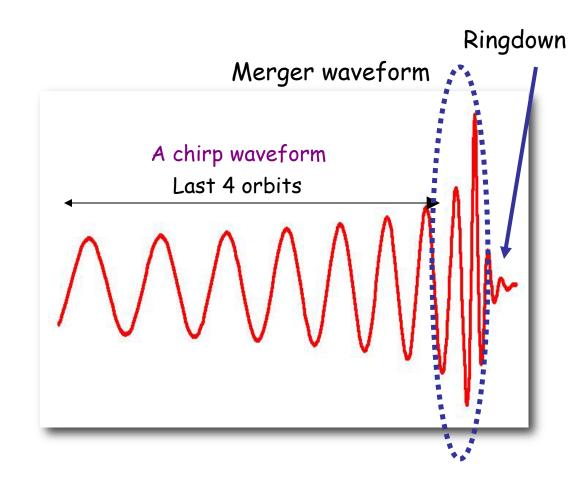
- Last few minutes (10K cycles) for NS-NS
- ■0.4 400 per year by 2018
- **BH-BH** could be 0.4 1000

Space-Based (millihertz)

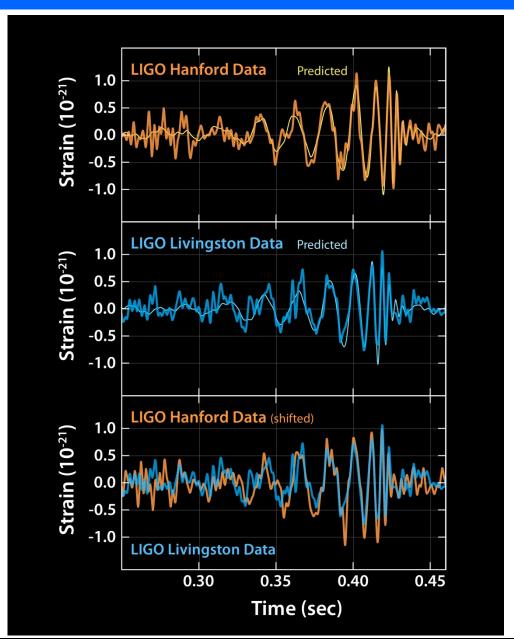
- ■MBH pairs (10⁵ 10⁷ M_s) in galaxies to large Z
- **EMRIs**
- Close WD binaries

Pulsar Timing Arrays (nanohertz)

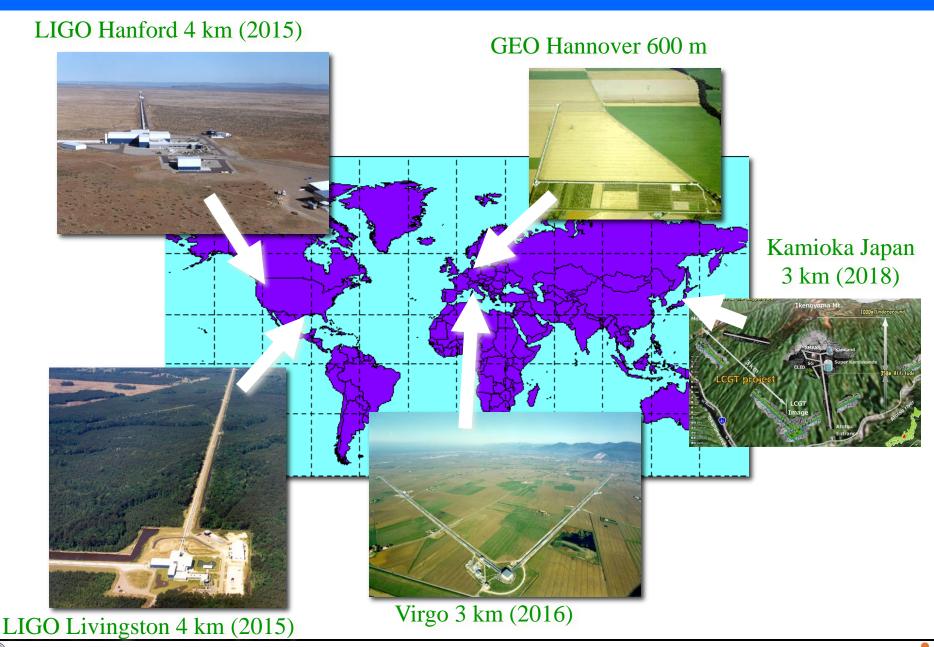
MBH pairs



Experimental results



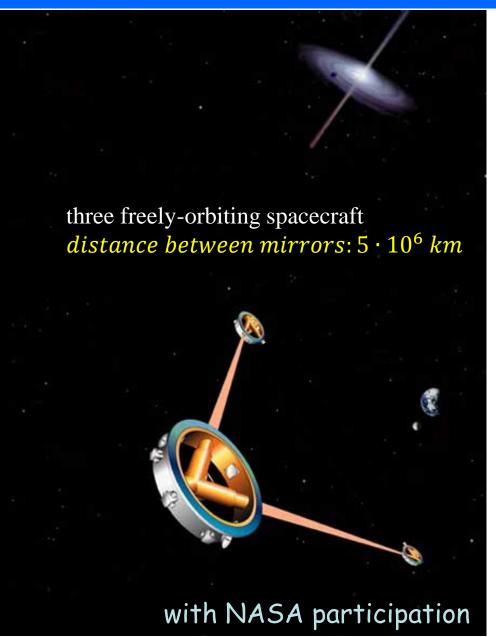
Global Network of Interferometers

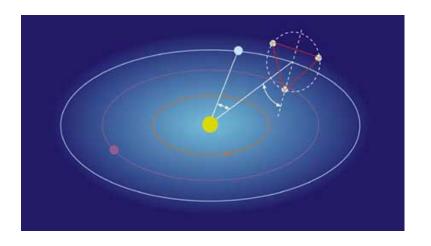


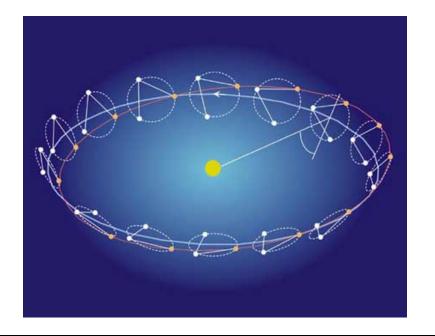




LISA: Laser Interferometer Space Antenna (ESA 2034)

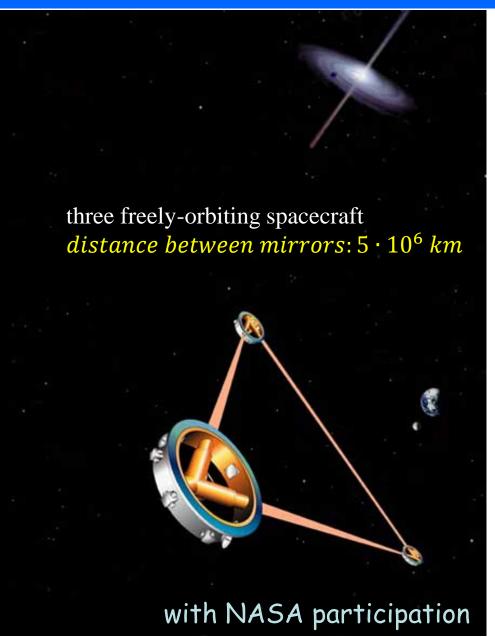


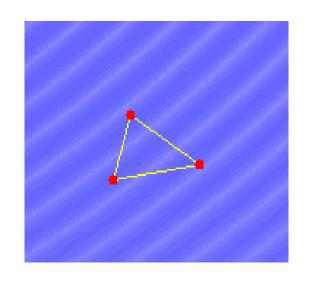


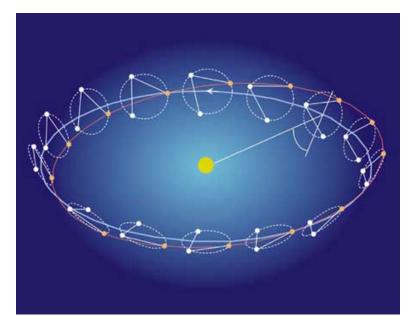




LISA: Laser Interferometer Space Antenna (ESA 2034)









Gravitational waves: differences from EM waves

Electromagnetism:

- A strong force, but with opposing charges (+ and)
- Fields built up incoherently from microscopic charge separations
- » Wavelengths smaller than the source
- Waves are easy to detect, but easily blocked
- » Show the surfaces of energetic bodies
- Used to construct *images* of celestial objects
- photon massless, J = 1

Gravity:

- A weak force, but with only one charge (mass)
- Fields built up coherently from bulk accumulation of matter
- » Wavelengths larger than the source
- Waves are hard to detect, but pass undisturbed through anything
- » Reveal the bulk motion of dense matter
- Can be though of as *sounds* emitted by those objects
- graviton massless, J = 2
- → A fundamentally different way of observing the Cosmos!



