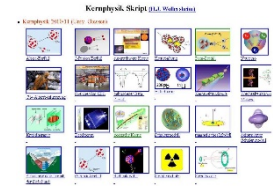


# Outline: Spectroscopy of $^{252}\text{Cf}$ fission

Lecturer: Hans-Jürgen Wollersheim

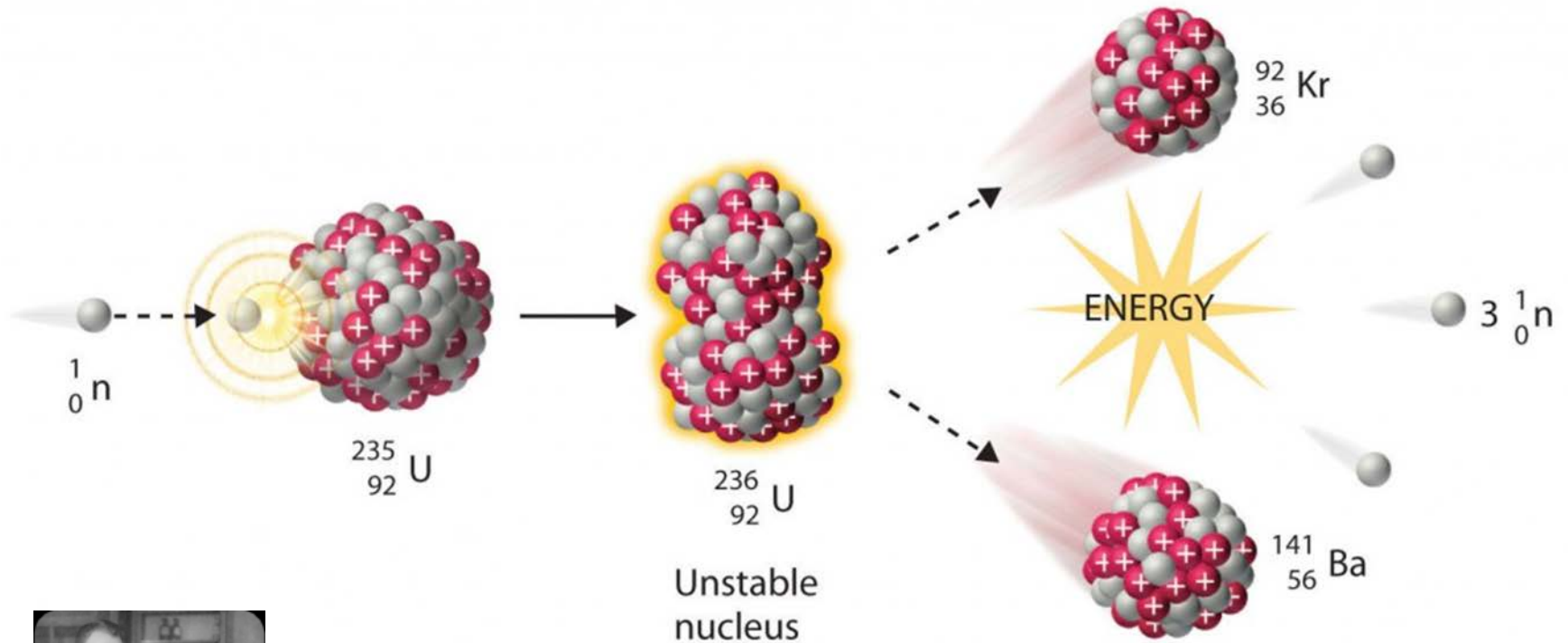
e-mail: [h.j.wollersheim@gsi.de](mailto:h.j.wollersheim@gsi.de)

web-page: <https://web-docs.gsi.de/~wolle/> and click on



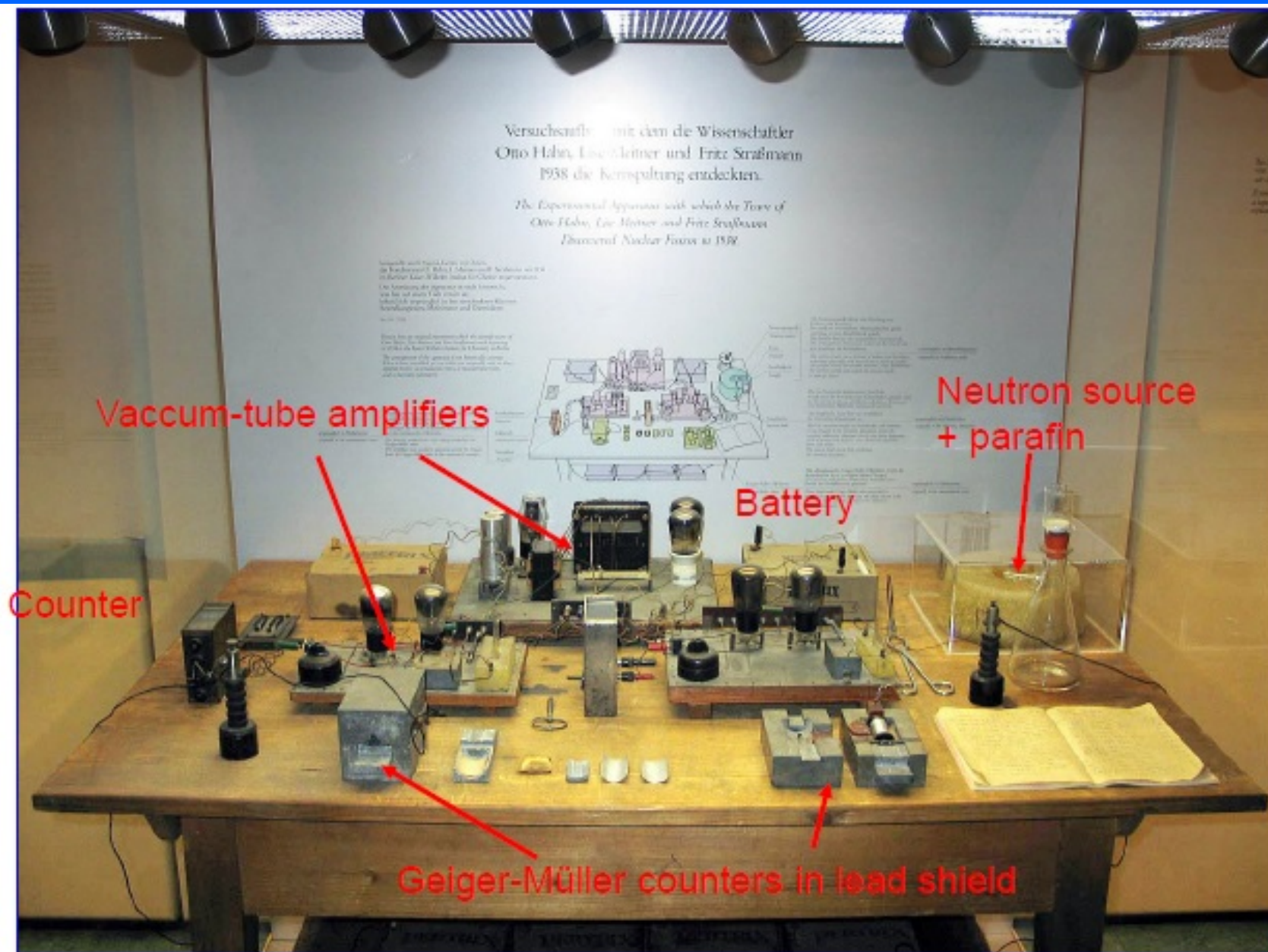
1. details of  $^{252}\text{Cf}$  decay
2.  $\gamma$ -ray angular distribution
3. fission fragment spectroscopy
4. ternary spontaneous fission

# Nuclear fission

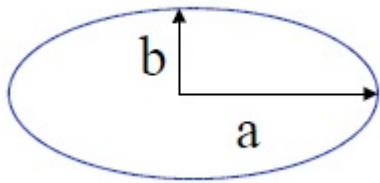


Otto Hahn, Lise Meitner

# Hahn-Meitner-Strassmann experimental set-up



# Nuclear fission – spontaneous fission



$$a = R \cdot (1 + \varepsilon)$$

$$b = R \cdot (1 + \varepsilon)^{-1/2}$$

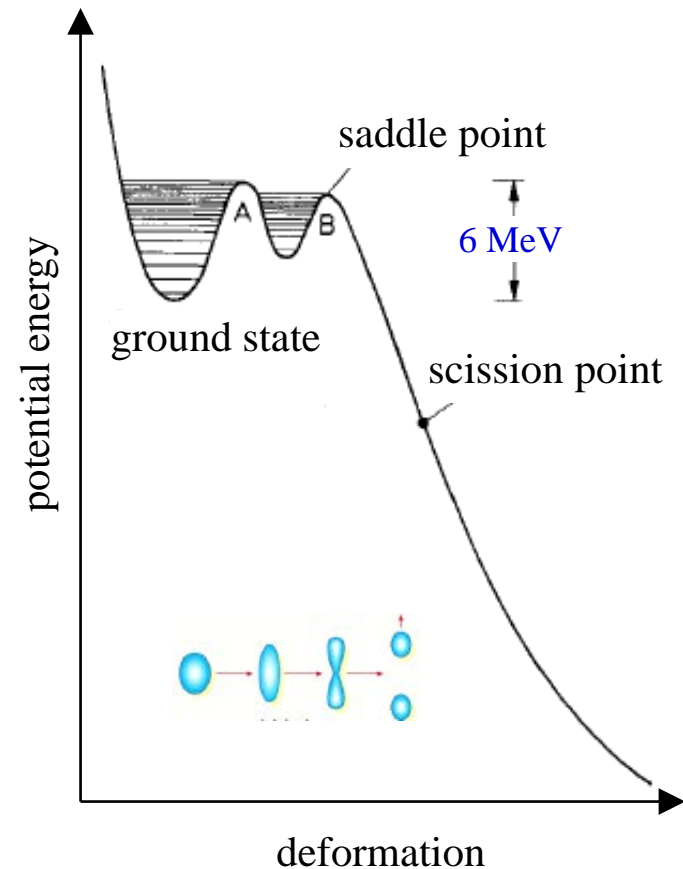
$$E_S = a_S \cdot A^{2/3} \cdot \left( 1 + \frac{2}{5} \varepsilon^2 + \dots \right)$$

$$E_C = a_C \cdot Z^2 \cdot A^{-1/3} \cdot \left( 1 - \frac{1}{5} \varepsilon^2 + \dots \right)$$

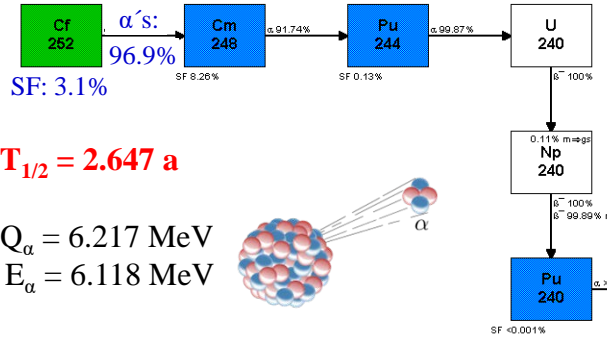
$$\Delta E = \frac{\varepsilon^2}{5} \cdot (2 \cdot a_S \cdot A^{2/3} - a_C \cdot Z^2 \cdot A^{-1/3})$$

fission barrier  $\Delta E$  disappears for  $\frac{Z^2}{A} \geq \frac{2a_S}{a_C} \approx 48$

This is the case for nuclei with  $Z > 114$  and  $A > 270$

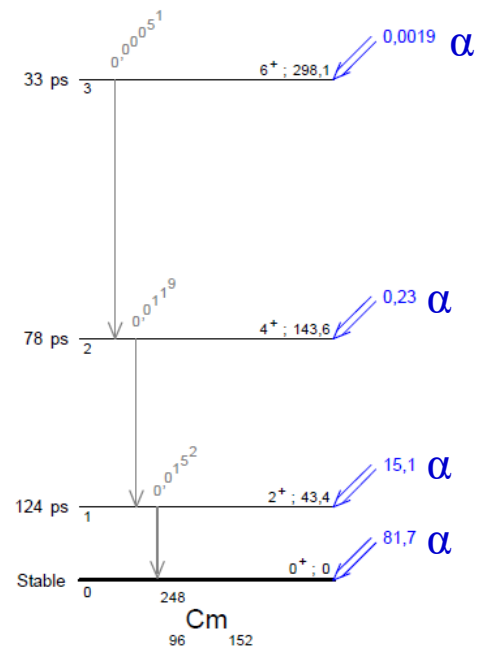
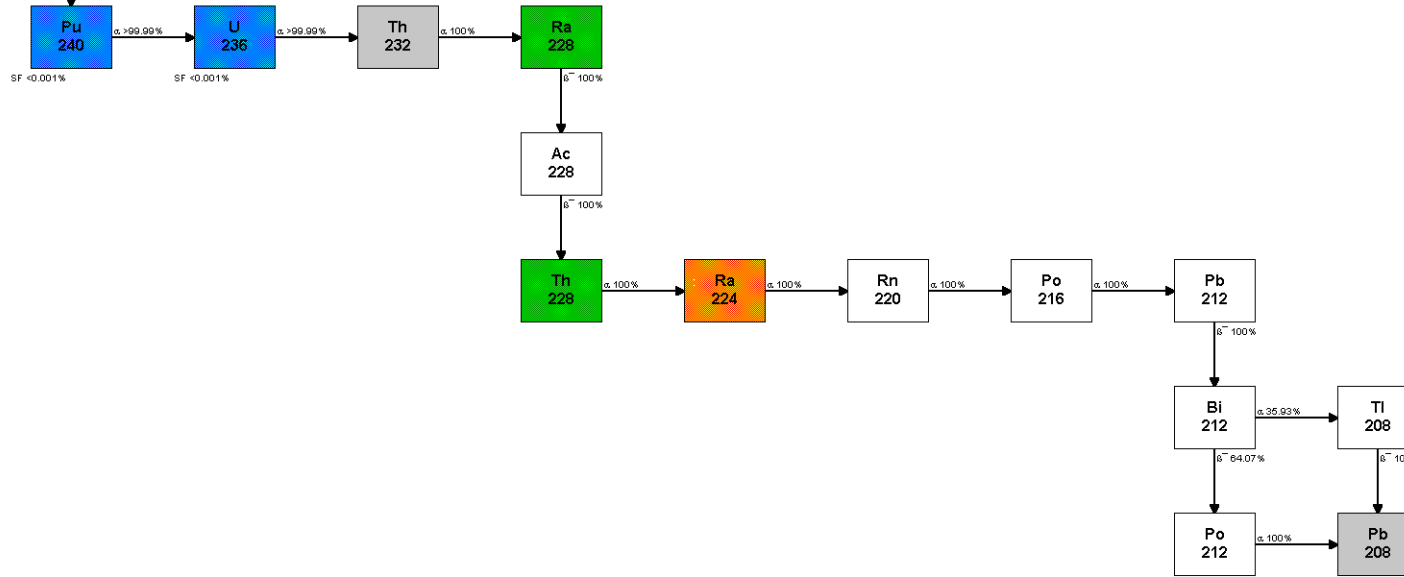
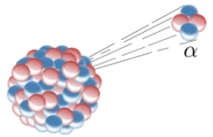


# Details of the $^{252}\text{Cf}$ decay



$T_{1/2} = 2.647 \text{ a}$

$Q_\alpha = 6.217 \text{ MeV}$   
 $E_\alpha = 6.118 \text{ MeV}$



# $\alpha$ -decay of $^{252}\text{Cf}$



**Mass data:**

[nucldata.nuclear.lu.se/database/masses/](http://nucldata.nuclear.lu.se/database/masses/)

$$\text{BE}(^{252}\text{Cf}) = 1881.275 \text{ MeV}$$

$$\text{BE}(^{248}\text{Cm}) = 1859.196 \text{ MeV}$$

$$\text{BE}(^4\text{He}) = 28.296 \text{ MeV}$$

$$Q_\alpha = 6.217 \text{ MeV}$$

momentum conservation:  $m_k \cdot v_k = m_\alpha \cdot v_\alpha \rightarrow v_k = \frac{m_\alpha}{m_k} \cdot v_\alpha$

energy conservation:

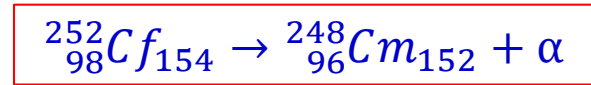
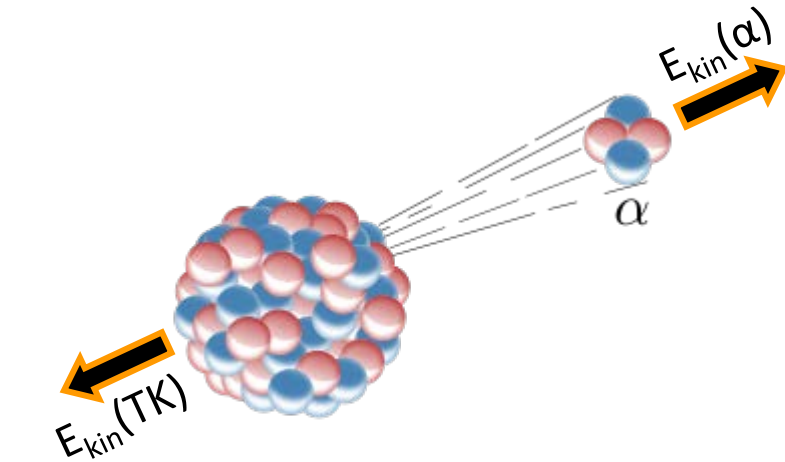
$$Q_\alpha = E_{kin}^k + E_{kin}^\alpha$$

$$= \frac{m_k}{2} \cdot v_k^2 + E_{kin}^\alpha$$

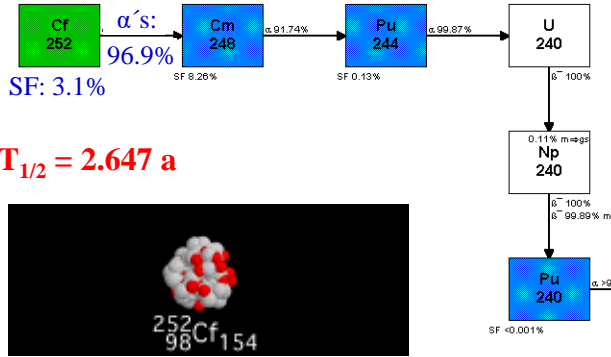
$$= \frac{m_k}{2} \cdot \frac{m_\alpha^2}{m_k^2} \cdot v_\alpha^2 + E_{kin}^\alpha$$

$$= \frac{m_\alpha}{m_k} \cdot E_{kin}^\alpha + E_{kin}^\alpha$$

$$= \frac{m_\alpha + m_k}{m_k} \cdot E_{kin}^\alpha \rightarrow E_{kin}^\alpha = Q_\alpha \cdot \frac{m_k}{m_k + m_\alpha} = 6.217 \text{ MeV} \cdot \frac{248}{252} = 6.118 \text{ MeV}$$



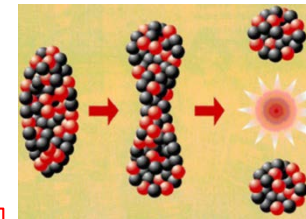
# Binary spontaneous fission of $^{252}\text{Cf}$



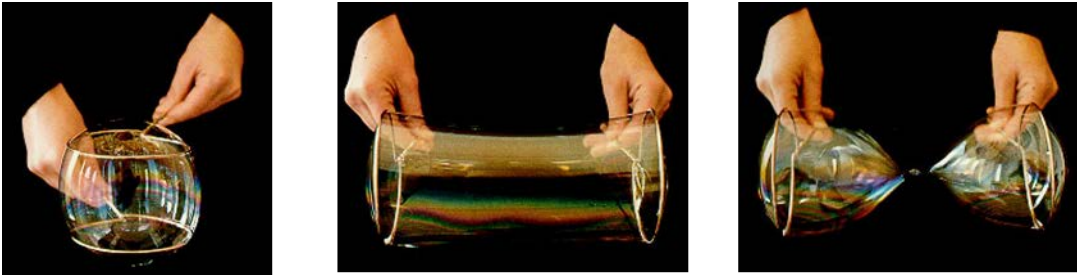
parameter	experimental value
$\langle A_L \rangle$	$108.9 \pm 0.5 \text{ u}$
$\langle A_H \rangle$	$143.1 \pm 0,5 \text{ u}$
$\langle E_L \rangle$	$103.5 \pm 0.5 \text{ MeV}$
$\langle E_H \rangle$	$78.3 \pm 0.5 \text{ MeV}$
$\langle \text{TKE} \rangle$	$181.8 \pm 0.7 \text{ MeV}$
$\langle A/Z \rangle_L$	2.50
$\langle A/Z \rangle_H$	2.56

$$V_C(R_{int}) = \frac{1.44 \cdot 43 \cdot 55}{14} = 244 \text{ MeV}$$

$$\text{TKE} = 0.1071 \cdot Z_C^2 / A_C^{1/3} + 22.3 = 185 \text{ MeV}$$



# Ternary spontaneous fission of $^{252}\text{Cf}$

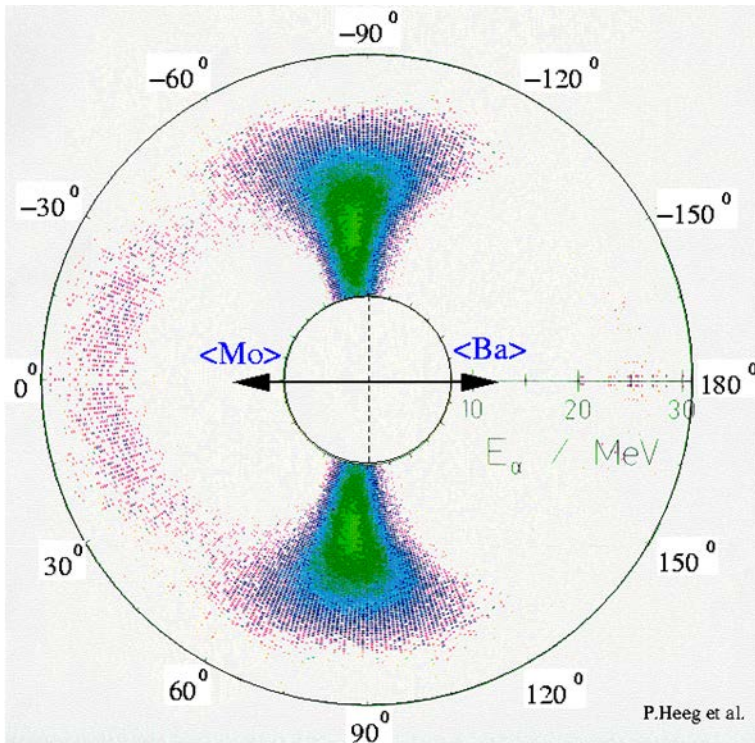


$^{252}\text{Cf}$  source

$T_{1/2} = 2.645 \text{ y}$

bin. fission/ $\alpha$ -decay = 1/31

ter. fission/ $\alpha$ -decay = 1/8308



ternary LPCs yields	
$^3\text{H}$	$950 \pm 90$
$^4\text{He}+^5\text{He}$	$10^4$
$^6\text{He}+^7\text{He}$	$270 \pm 30$
$^8\text{He}$	$25 \pm 5$
Li	$60 \pm 10$
Be	$175 \pm 30$
B	$13.5 \pm 4$
C	$80 \pm 30$



photographic emulsion



# Quaternary spontaneous fission of $^{252}\text{Cf}$

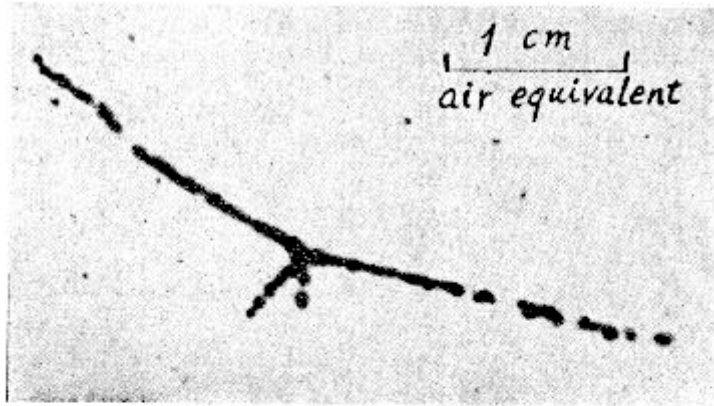


FIG. 4. Quaternary fission.

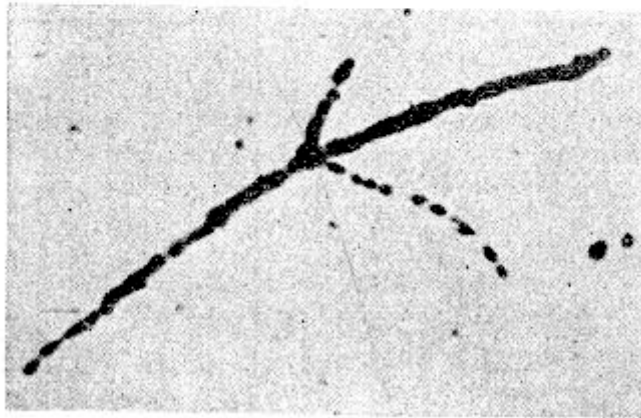
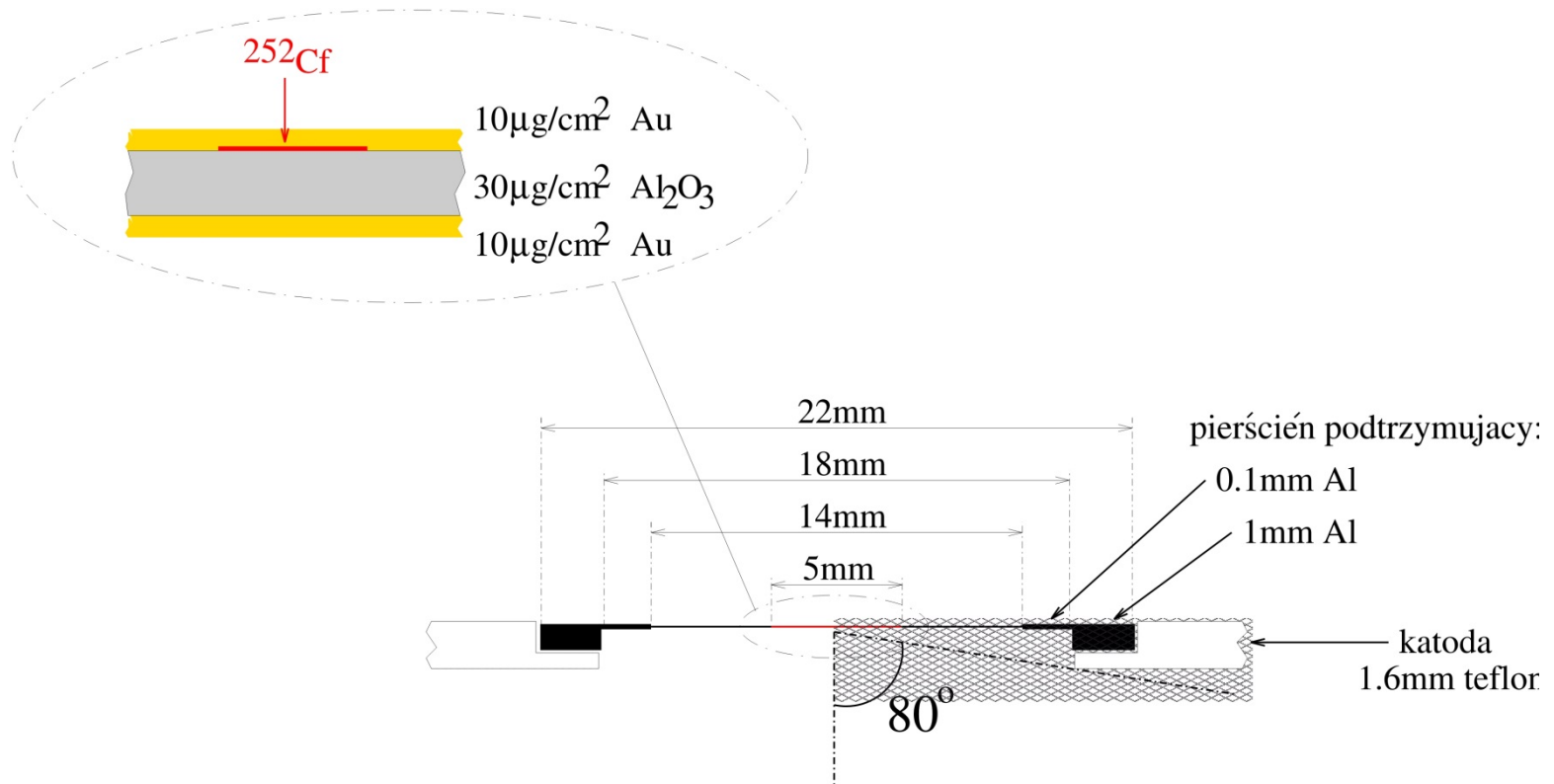
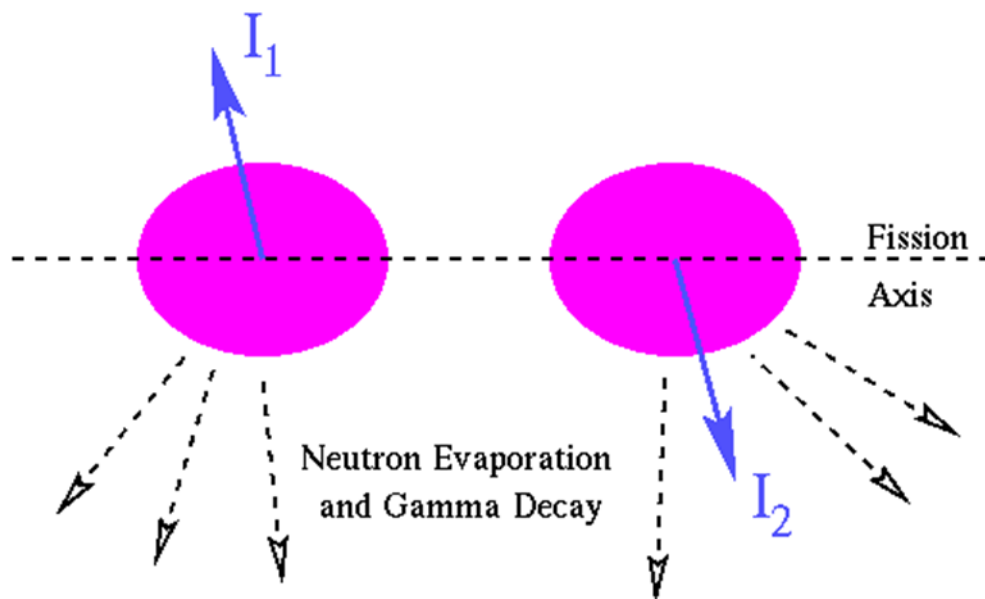


FIG. 5. Quaternary fission. (In same scale as Fig. 4.)

# Details of the $^{252}\text{Cf}$ source



# Spontaneous fission of $^{252}\text{Cf}$



$^{252}\text{Cf}$  spin  $J = 0$   
fragment spin  $J = \langle 7-8 \rangle$

$$\langle N_\gamma \rangle = 9.35$$

The origin of fragment spins and their alignment:

Collective vibrational modes like bending or wriggling at the saddle-to-scission stage and subsequent Coulomb excitation.

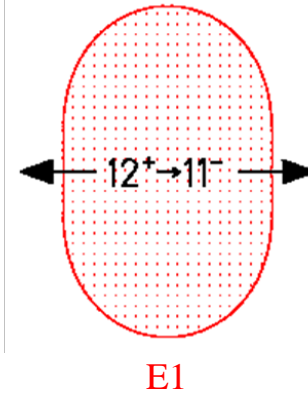
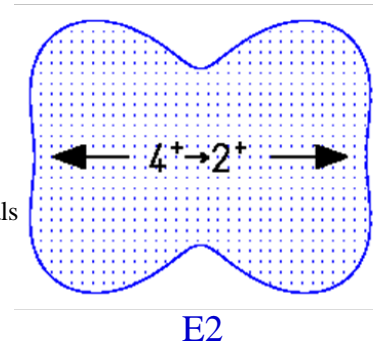
Experimental method:

**fragment –  $\gamma$ -ray angular correlation measurement**

# γ-ray emission from aligned nuclei

$$\frac{dW}{d\Omega_{rest}} = \sum_{Q=0,2,4} \frac{\sqrt{2Q+1}}{4\pi} \cdot \tau_{Q0}(J_i) \cdot F_Q(J_f, L, L, J_i) \cdot P_Q(\cos\theta_{\gamma p})$$

Legendre polynomials  
γ-γ correlation coefficients



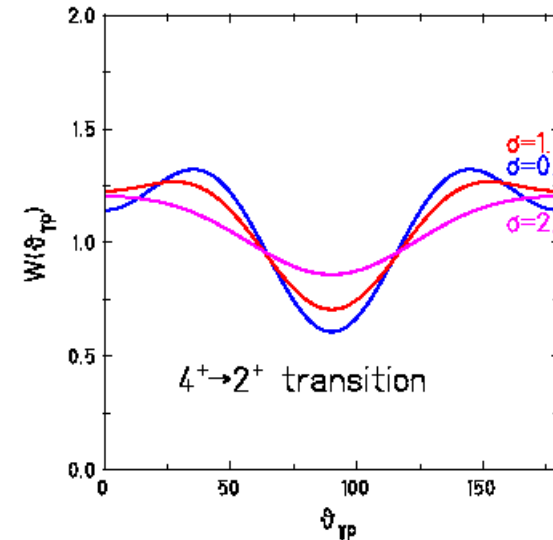
example:

$$\tau_{20}(J) = \left( \frac{J(J+1)}{(2J-1) \cdot (2J+3)} \right)^{1/2} \cdot \left( 3 \frac{\langle K^2 \rangle}{J(J+1)} - 1 \right)$$

$$\tau_{40}(J) = \left[ \frac{J^3(J+1)^3}{(2J-3)(2J-2)(2J-1)(2J+3)(2J+4)(2J+5)} \right]^{1/2} \cdot \left[ 35 \frac{\langle K^4 \rangle}{J^2(J+1)^2} - 30 \frac{\langle K^2 \rangle}{J(J+1)} \left( 1 - \frac{5}{6J(J+1)} \right) + 3 \left( 1 - \frac{2}{J(J+1)} \right) \right]$$

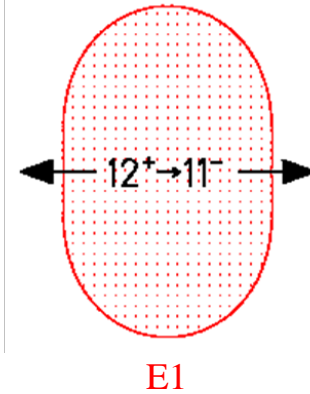
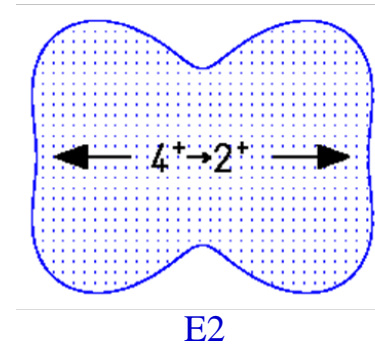
$$\langle K^n \rangle = \sum_K K^n \gamma_K \quad \text{with} \quad \gamma_K = \exp\left(-\frac{K^2}{2\sigma^2}\right) / \sum_{K'} \exp\left(-\frac{K'^2}{2\sigma^2}\right)$$

Gaussian distribution



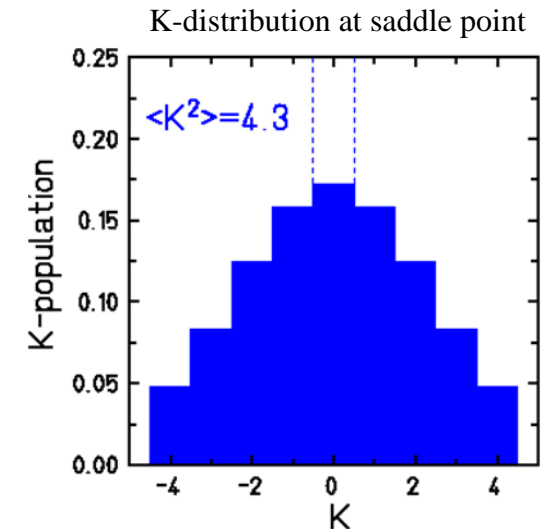
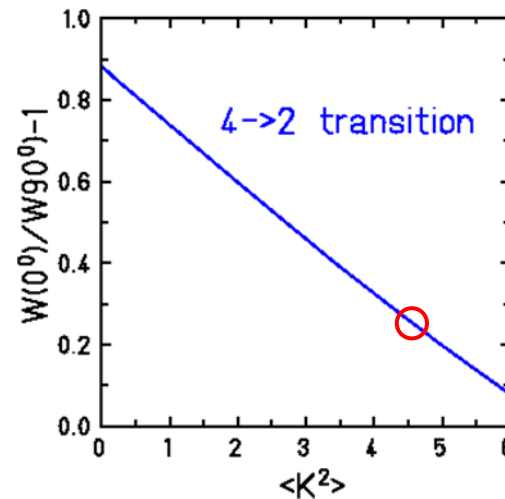
# $\gamma$ -ray emission from aligned nuclei

$$W(\theta) = \sum_{Q=0,2,4} \frac{\sqrt{2Q+1}}{4\pi} \cdot \tau_{Q0}(J_i) \cdot F_Q(J_f, L, L, J_i) \cdot P_Q(\cos\theta)$$

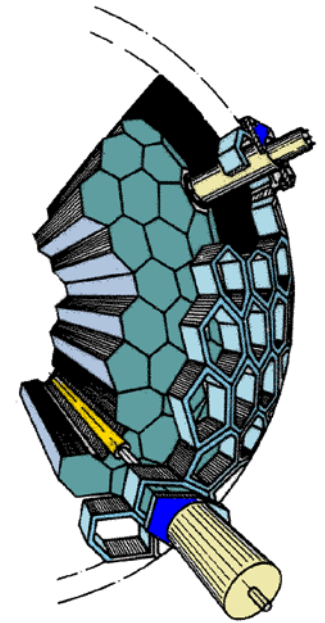
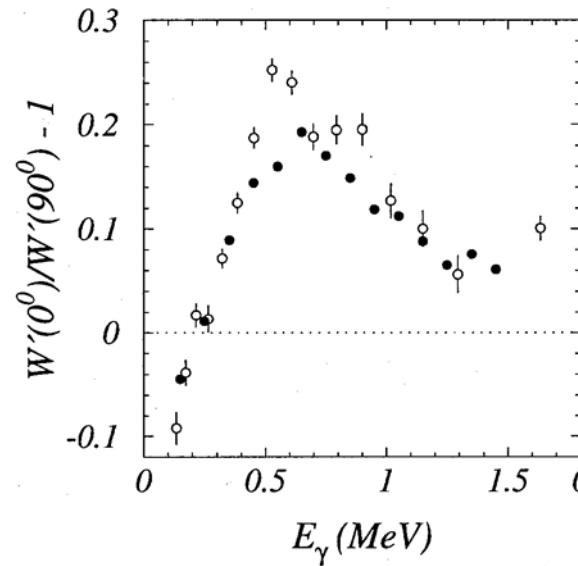
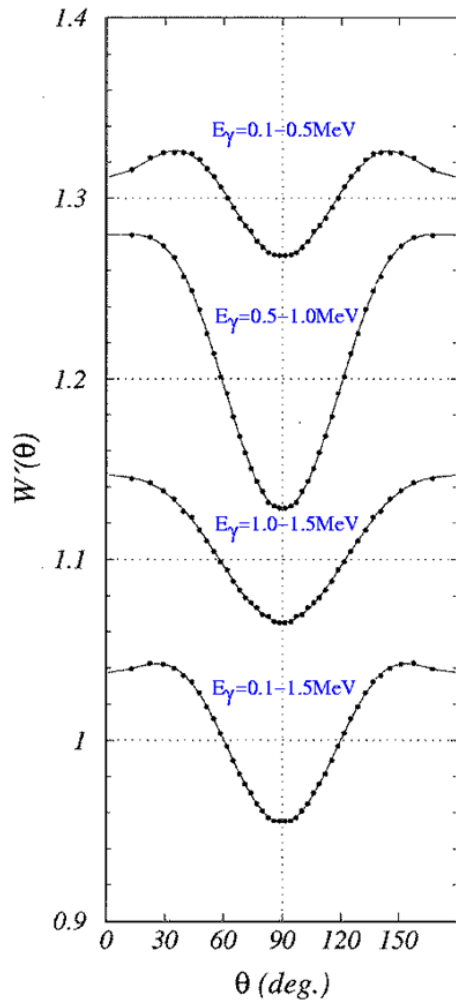


example:

$$\tau_{20}(J) = \left( \frac{J(J+1)}{(2J-1) \cdot (2J+3)} \right)^{1/2} \cdot \left( 3 \frac{\langle K^2 \rangle}{J(J+1)} - 1 \right)$$



# Anisotropy of $\gamma$ -ray in binary fission of $^{252}\text{Cf}$



Darmstadt Heidelberg  
Crystal Ball

$\Delta E_\gamma = 90 \text{ keV}$

fragment –  $\gamma$ -ray angular  
correlation measurement

(no discrimination between different multipole transitions)

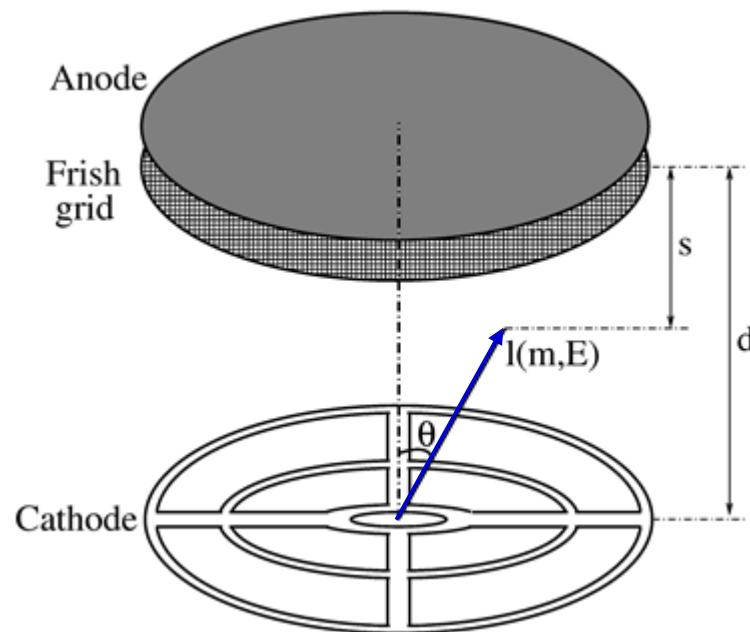
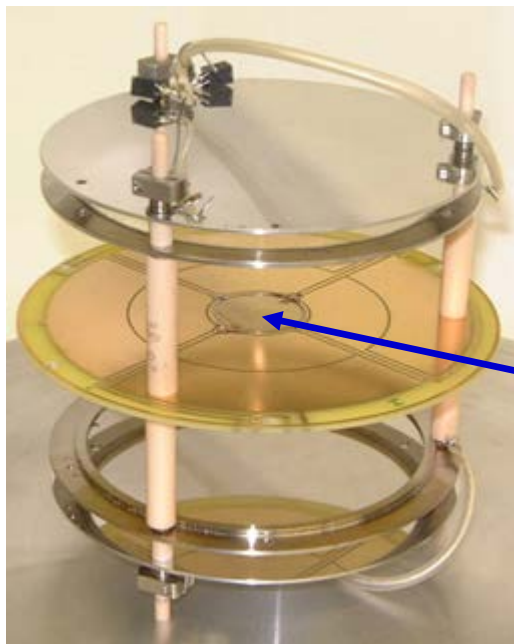
# $4\pi$ twin ionization chamber for fission fragments

measured quantities:

$E_H$  }  $\rightarrow A_H$   
 $E_L$  }

$e^-$  drift-time  $\rightarrow \vartheta$

segmented cathode  $\rightarrow \phi$



methane at 570 torr  
cathode diameter 15cm

$^{252}\text{Cf}$  source (25k f/s)

$T_{1/2} = 2.645 \text{ y}$   
 $E_\alpha = 6.118 \text{ and } 6.076 \text{ MeV}$   
bin. fission/ $\alpha$ -decay = 1/31  
ter. fission/ $\alpha$ -decay = 1/8308

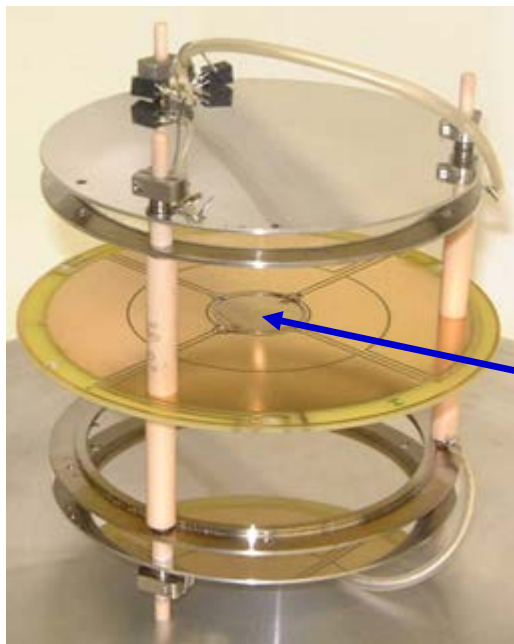
# 4 $\pi$ twin ionization chamber for fission fragments

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$E_H$  }  $\rightarrow A_H$   
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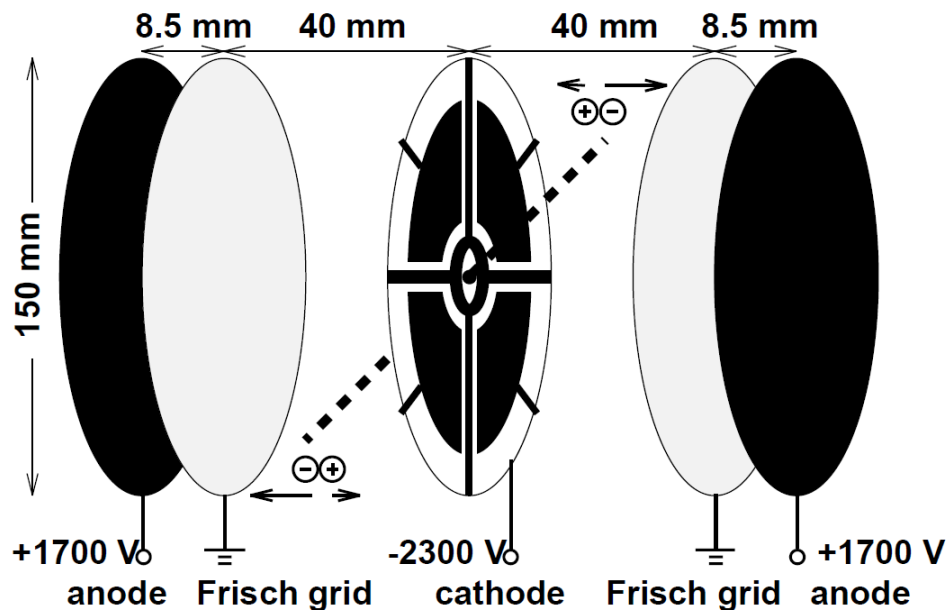
$e^-$  drift-time  $\rightarrow \vartheta$

segmented cathode  $\rightarrow \phi$



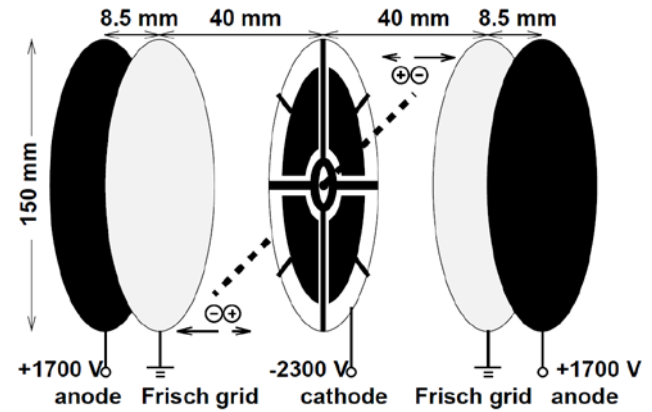
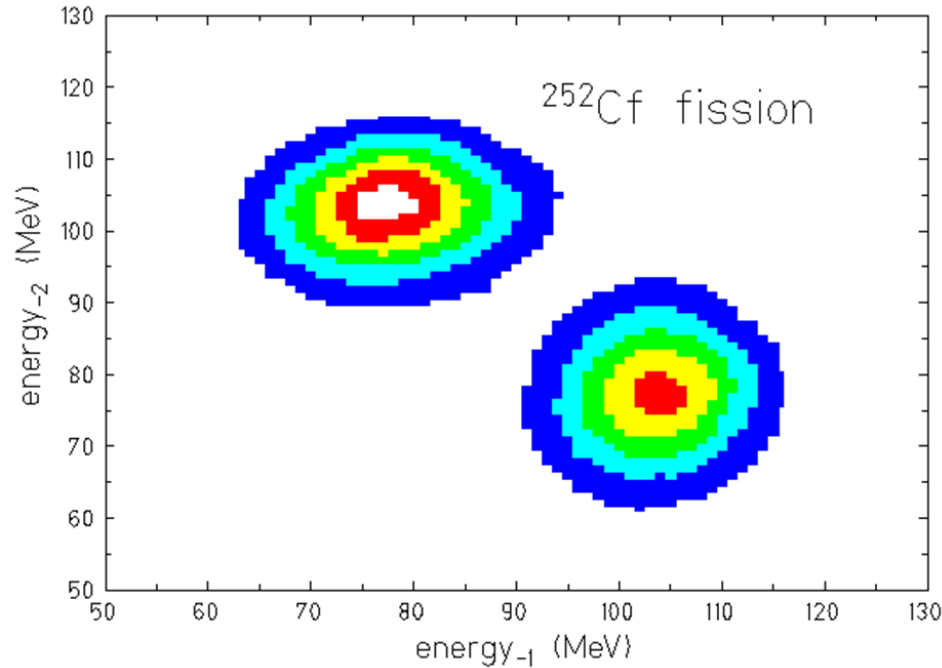
$^{252}\text{Cf}$  source (25k f/s)

$T_{1/2} = 2.645 \text{ y}$   
 $E_\alpha = 6.118 \text{ and } 6.076 \text{ MeV}$   
 bin. fission/ $\alpha$ -decay = 1/31  
 ter. fission/ $\alpha$ -decay = 1/8308





# Fission fragment mass measurement



The kinetic energies of the fragments are converted into ionization energy, and the fragments stop before reaching the Frisch grids.

$$m_1 v_1 + m_2 v_2 = 0 \rightarrow m_1 E_1 = m_2 E_2$$

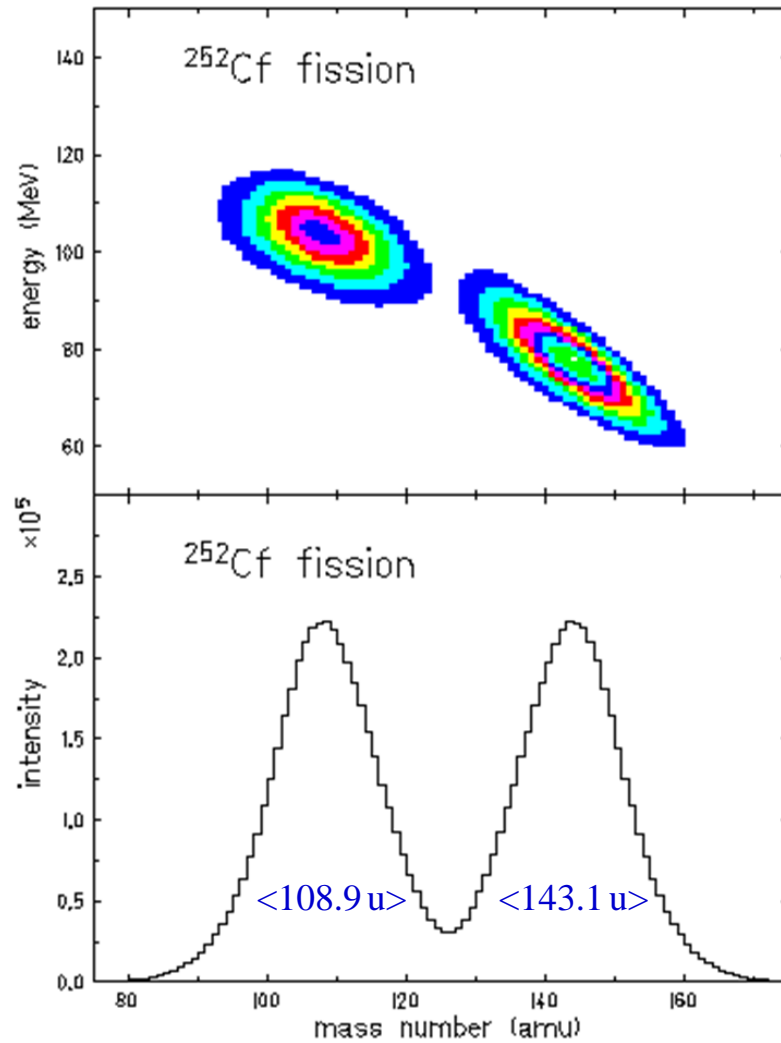
$$m_1 = (m_1 + m_2) \frac{E_2}{E_1 + E_2}$$

$$\langle E_L \rangle = 103.5 \pm 0.5 \text{ MeV} \rightarrow \langle A_L \rangle = 108.9 \pm 0.5$$

$$\langle E_H \rangle = 78.3 \pm 0.5 \text{ MeV} \rightarrow \langle A_H \rangle = 143.1 \pm 0.5$$

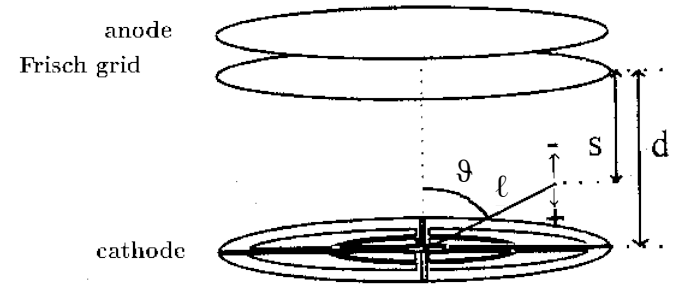
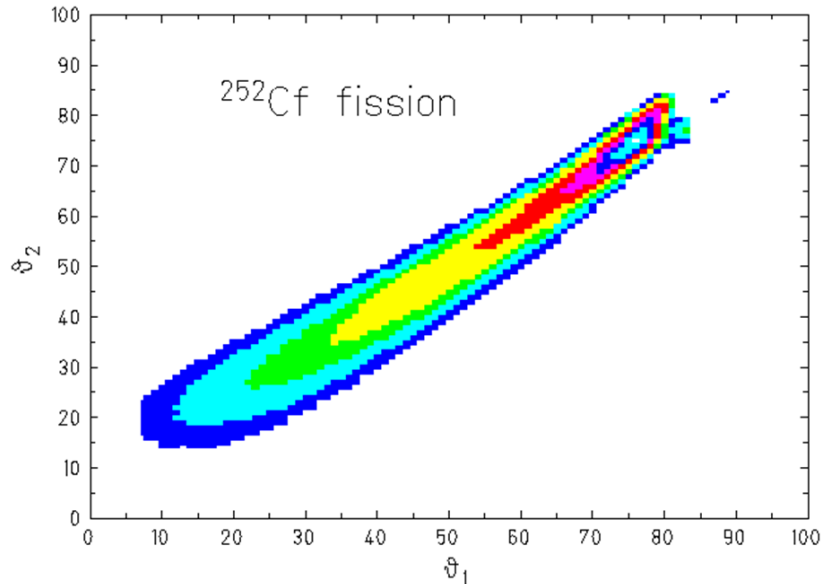
$$m_1 + m_2 = 252$$

# Fission fragment mass measurement



mass resolution  $\sigma = 3 \text{ u}$

# Determination of the polar angles



The anode time signals are caused by the first electrons which pass the Frisch grids and are thus linear dependent on both the lengths of the fragment tracks and the cosine of the polar angle  $\theta$ .

drift - time:  $T = s/v_{drift}$

$$s = d - \ell(E, A) \cdot \cos(\vartheta)$$

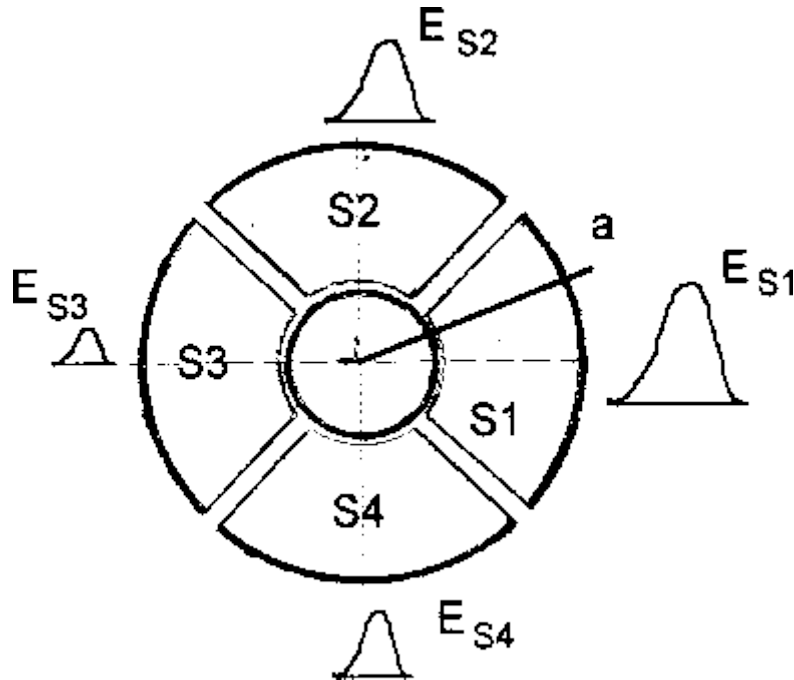
$$\cos(\vartheta) = \frac{d - T \cdot v_{drift}}{\ell(E, A)}$$

drift velocity:  $v_{drift} = 10 \text{ cm}/\mu\text{s}$   
 range of fragments in methane gas:  $\ell(E, A)$   
 distance cathode-anode:  $d = 3.8 \text{ cm}$

angular resolution	
$\vartheta$	$\sigma$
$30^\circ$	$4.2^\circ$
$50^\circ$	$2.5^\circ$
$70^\circ$	$2.3^\circ$

# Determination of the azimuthal angle

The energy signal of cathode sections  $\rightarrow$  azimuthal angle  $\varphi$



energy signals of the four sectors depend on the orientation of the fission axis

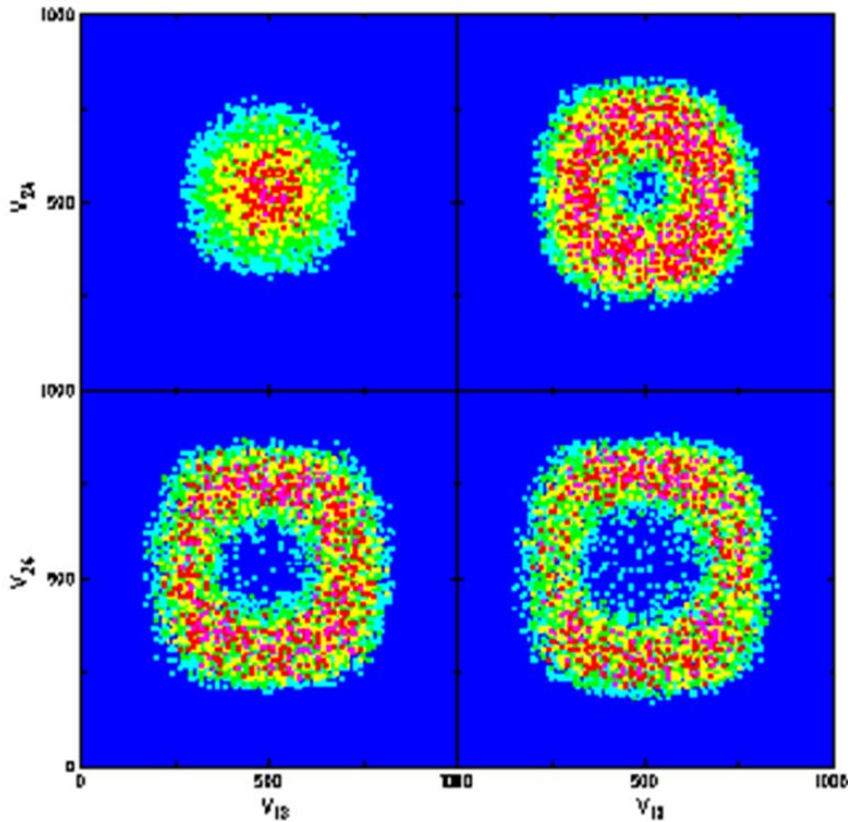
$$V_{13} = \frac{E_{S1}}{E_{S1} + E_{S3}}$$

$$V_{24} = \frac{E_{S2}}{E_{S2} + E_{S4}}$$

$$\tan\varphi = \frac{V_{24} - 0.5}{V_{13} - 0.5}$$

# Determination of the azimuthal angle

The energy ratios for different emission angles  $\vartheta$

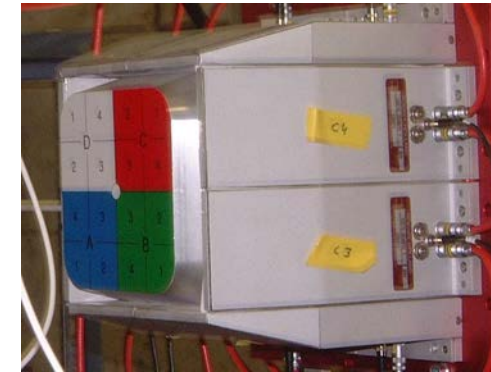
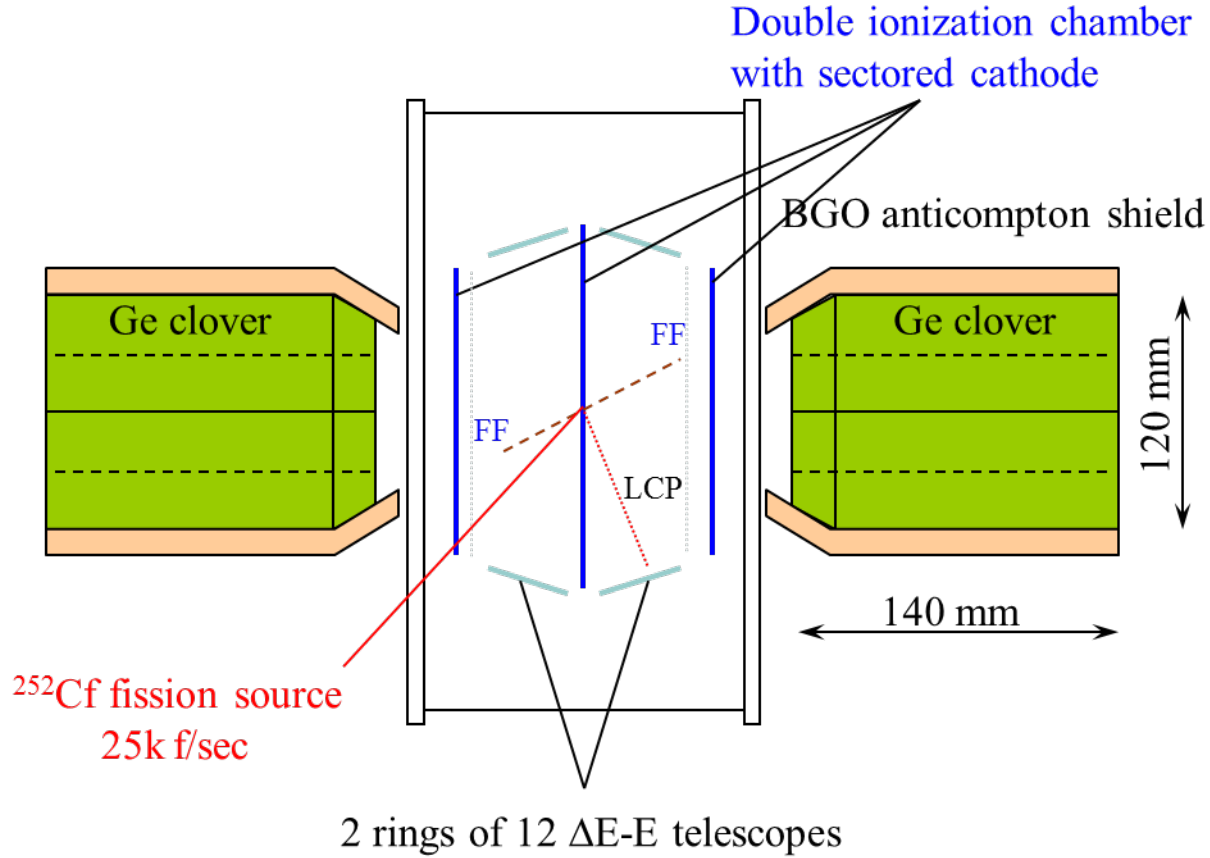


$$V_{13} = \frac{E_{S1}}{E_{S1} + E_{S3}}$$

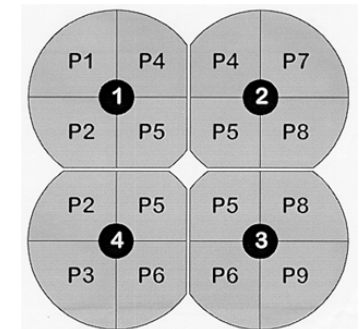
$$V_{24} = \frac{E_{S2}}{E_{S2} + E_{S4}}$$

$$\tan\varphi = \frac{V_{24} - 0.5}{V_{13} - 0.5}$$

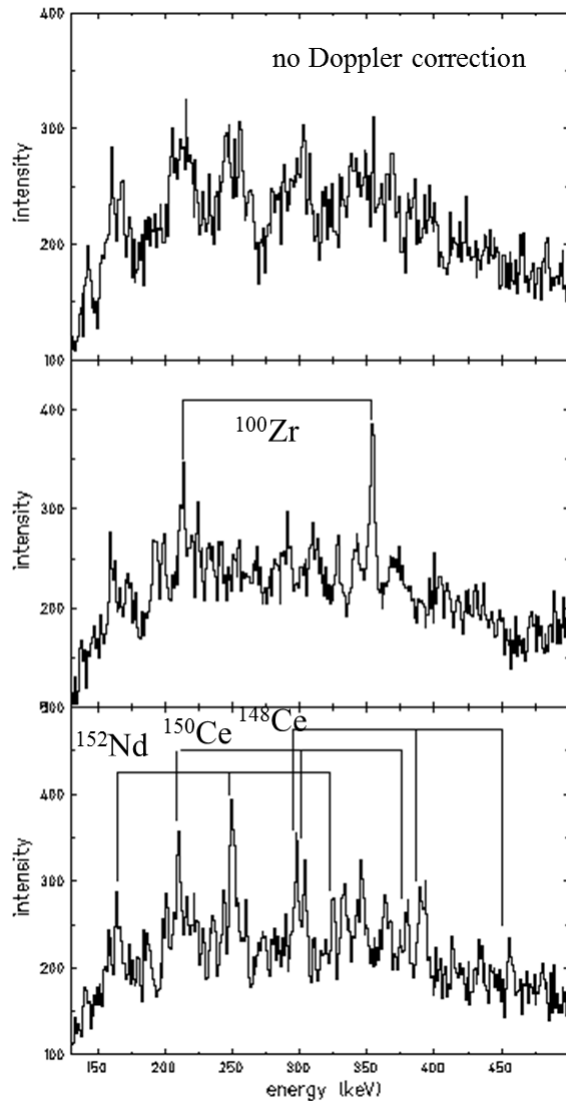
# Experimental set-up



4 segmented Clover detector



# Spectroscopy of binary fission fragments



$$\frac{v}{c} = 3.4 - 4.5 \%$$

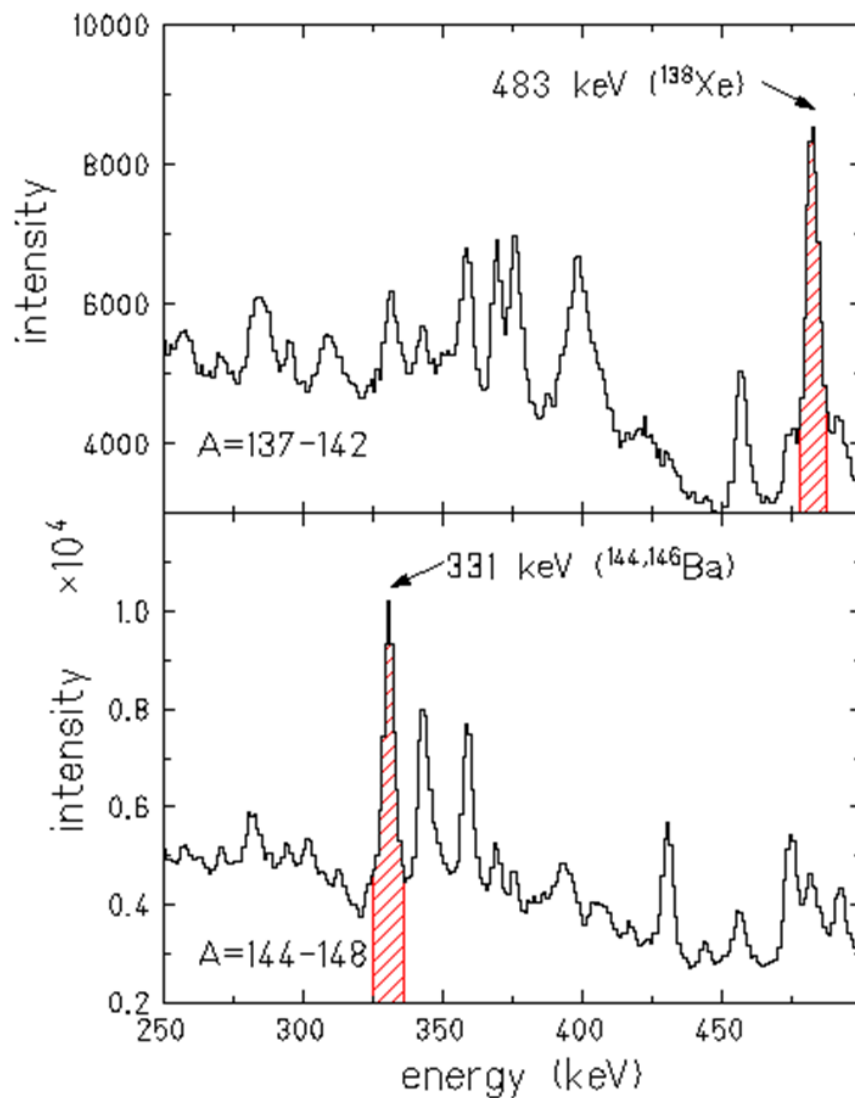
$$\Delta\vartheta_\gamma = 18^\circ$$

$$\frac{\Delta E_\gamma}{E_\gamma} = 1\%$$

$$\varepsilon_{\text{ph}} = 2.5\%$$

$$\frac{\Delta E_\gamma}{E_\gamma} = 1\%$$

# Analysis of the particle- $\gamma$ angular correlation

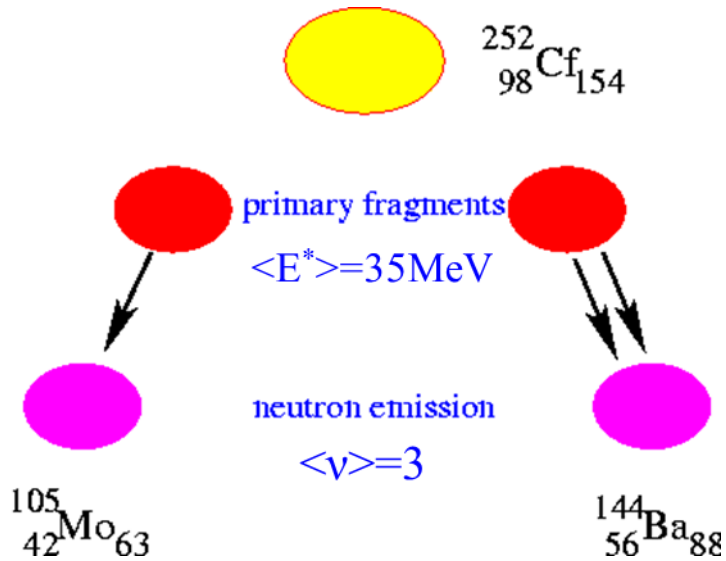


$$10^\circ \leq \vartheta_p \leq 80^\circ$$

$$-34^\circ \leq \vartheta_\gamma \leq 34^\circ$$

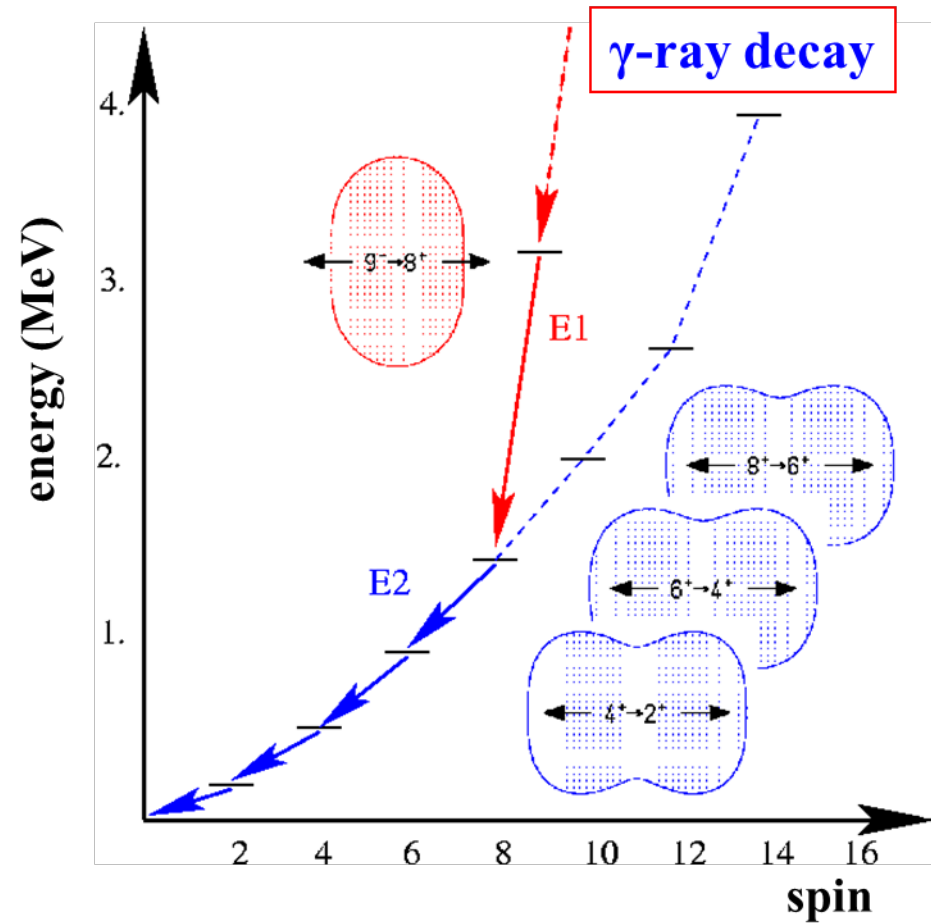


# Spontaneous fission process of $^{252}\text{Cf}$

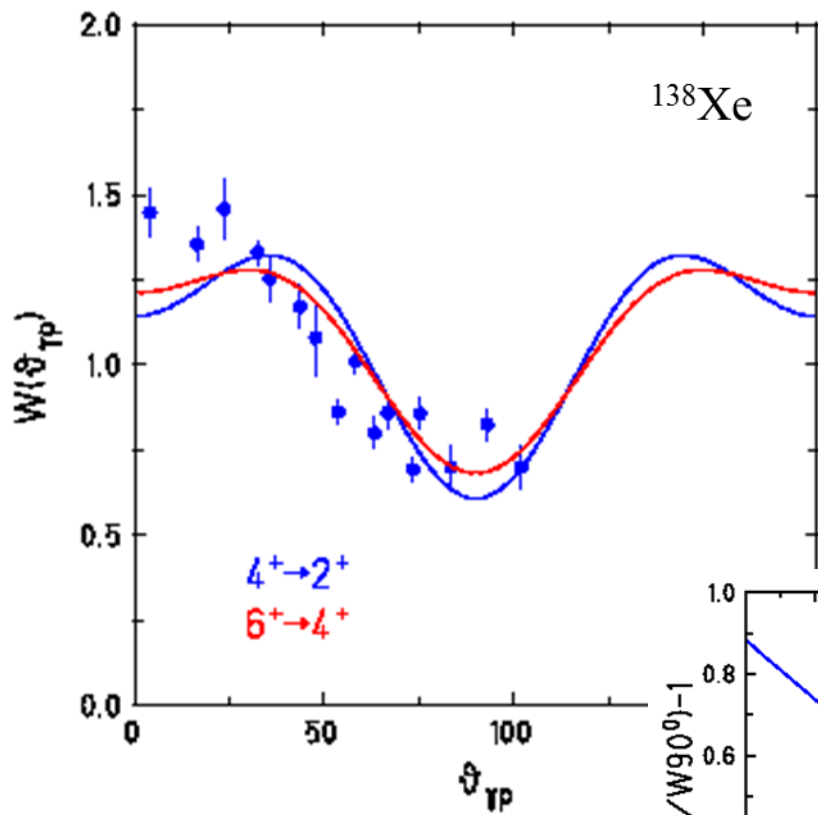


excitation energy of fission fragments **35 MeV**

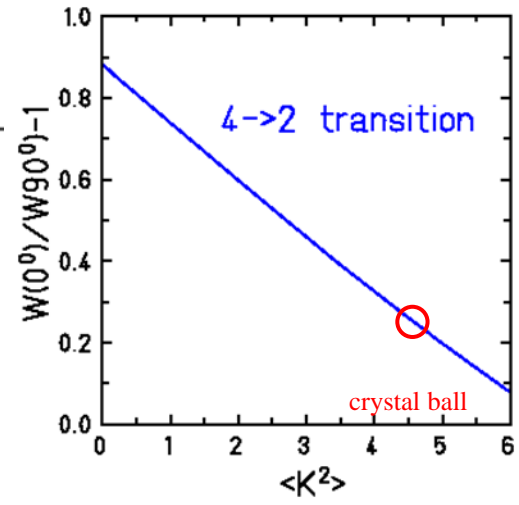
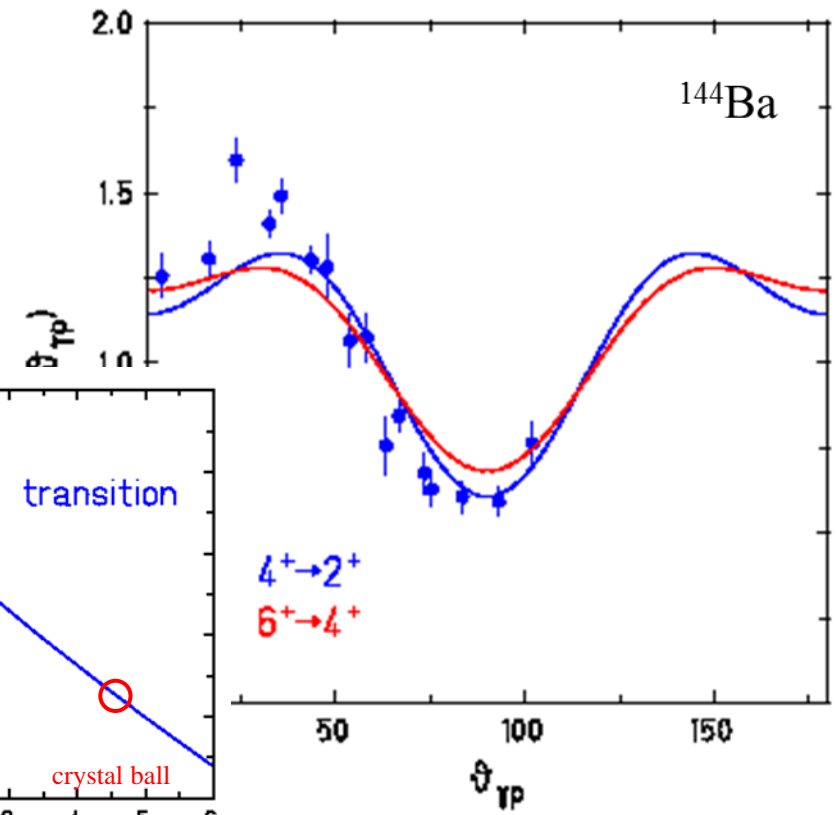
evaporation of 3 neutrons



# Fission fragment $\gamma$ -ray angular correlation

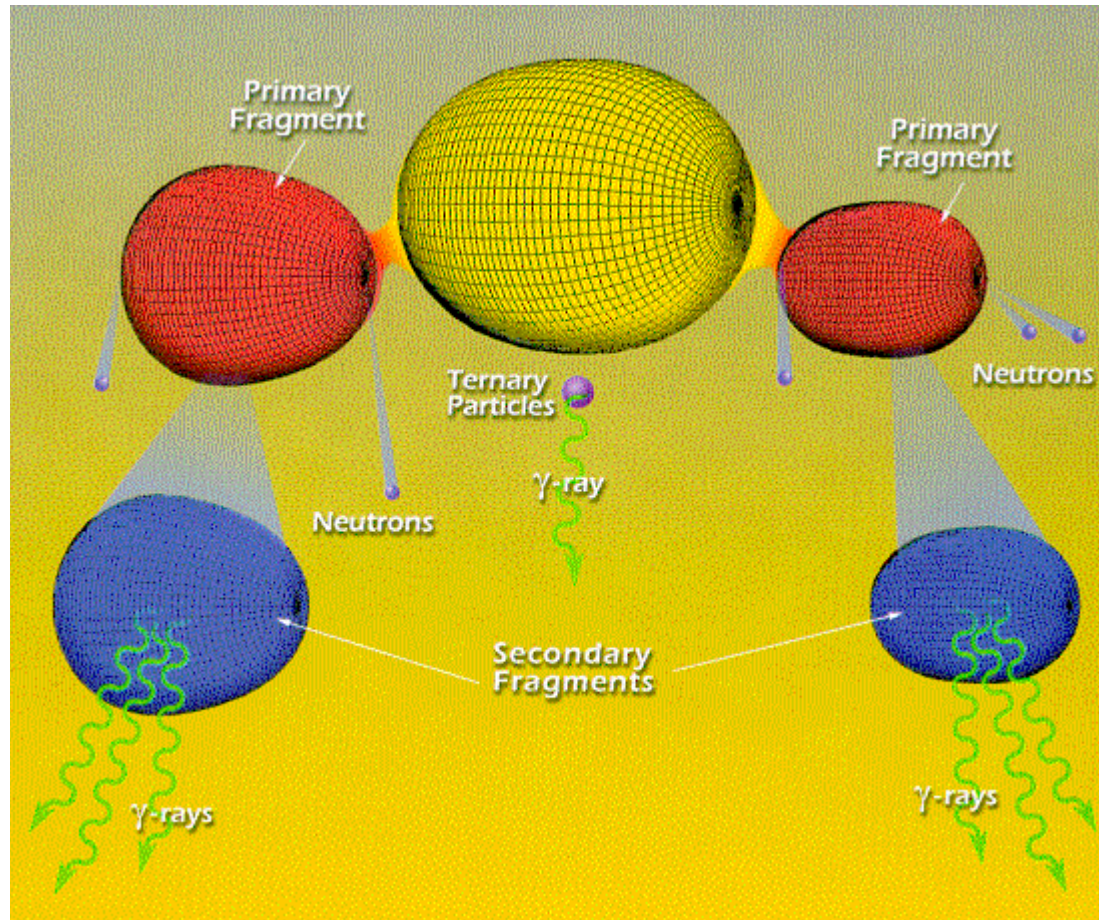


$4^+ \rightarrow 2^+$  transition

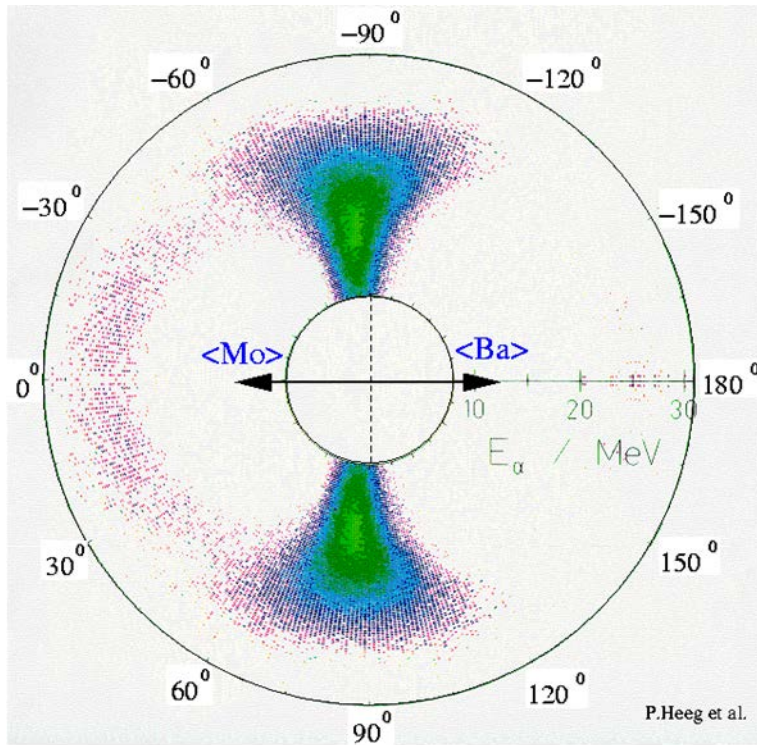


no loss of alignment!

# Ternary spontaneous fission of $^{252}\text{Cf}$



# Ternary spontaneous fission of $^{252}\text{Cf}$



ternary LPCs yields	
$^3\text{H}$	$950 \pm 90$
$^4\text{He}+^5\text{He}$	$10^4$
$^6\text{He}+^7\text{He}$	$270 \pm 30$
$^8\text{He}$	$25 \pm 5$
Li	$60 \pm 10$
Be	$175 \pm 30$
B	$13.5 \pm 4$
C	$80 \pm 30$

**Fragments**  $\rightarrow E_H, E_L, \vartheta, \varphi$

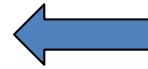
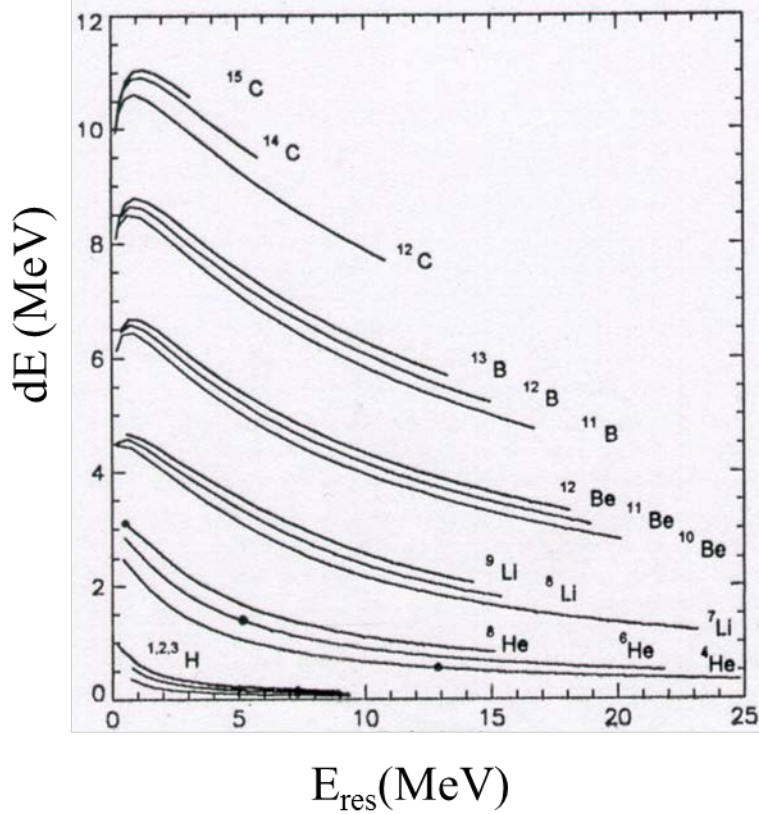
**LCPs**  $\rightarrow E, \Delta E, \vartheta, \varphi$

**$\gamma$ -rays**  $\rightarrow E, \vartheta, \varphi$

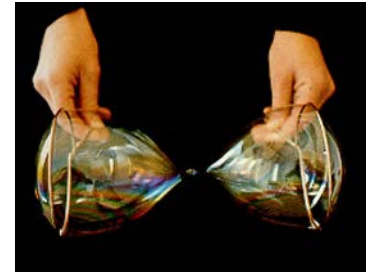


**2 rings of  $\Delta E$ -E telescopes**

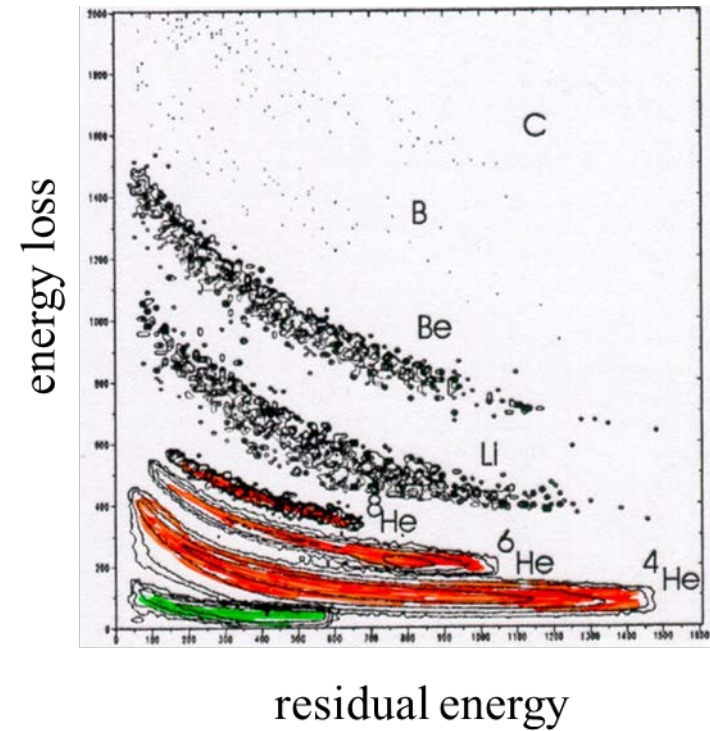
# Separation of light charged particles



simulation



data



# Summary

## ❖ $\gamma$ -ray spectroscopy of fission fragments

open fission source, Doppler-shift correction  
access to short-lived  $\gamma$ -ray transitions

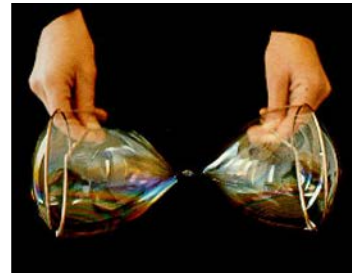
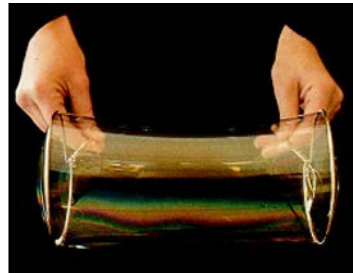
## ❖ angular anisotropy of $\gamma$ -rays

angular anisotropy of individual  $\gamma$ -ray transitions

- spin orientation
- changes in the spin population between binary and ternary fission

## ❖ fragment – LCP correlations

- isotope yields of heavier LCPs
- formation of LCPs in excited states
- quaternary fission (emission of 2 LCPs)



Soap Bubble Experiments (M. Schuyt, Seifenblasen, die Kugeln der Götter, 1988, Köln, Du Mont)