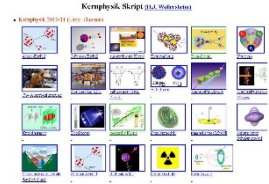


# Outline: Nuclear isomers

Lecturer: Hans-Jürgen Wollersheim

e-mail: [h.j.wollersheim@gsi.de](mailto:h.j.wollersheim@gsi.de)

web-page: <https://web-docs.gsi.de/~wolle/> and click on



1. nuclear isomers (shape-, spin-, K-traps)
2. In-flight separation of excited **R**adioactive **I**on **B**eams
3. nuclear shell closure in  $^{98}\text{Cd}$  and  $^{130}\text{Cd}$
4. T=1 isospin symmetry – mirror nuclei

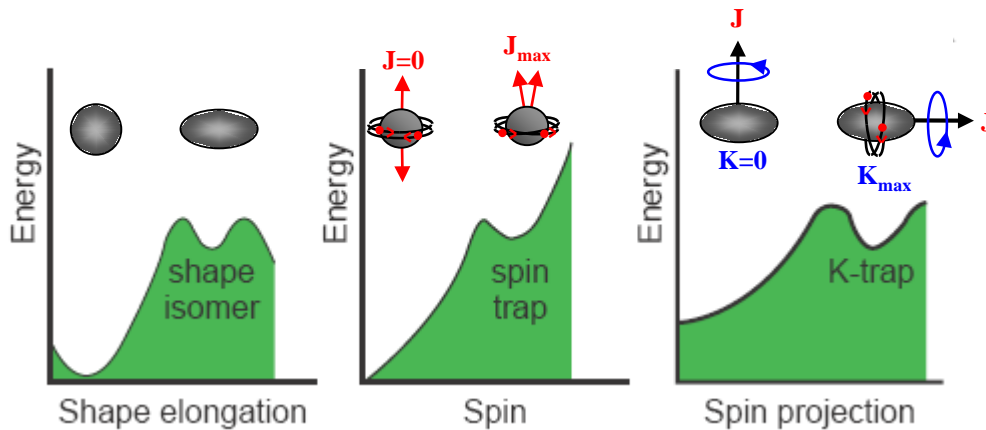
# What is a nuclear isomer?

Nuclear Isomer – a long-lived excited nuclear state ( $T_{1/2} > 1 \text{ ns}$ )  
decays by emission of  $\alpha$ ,  $\beta$ ,  $\gamma$ ,  $p$ , fission, cluster

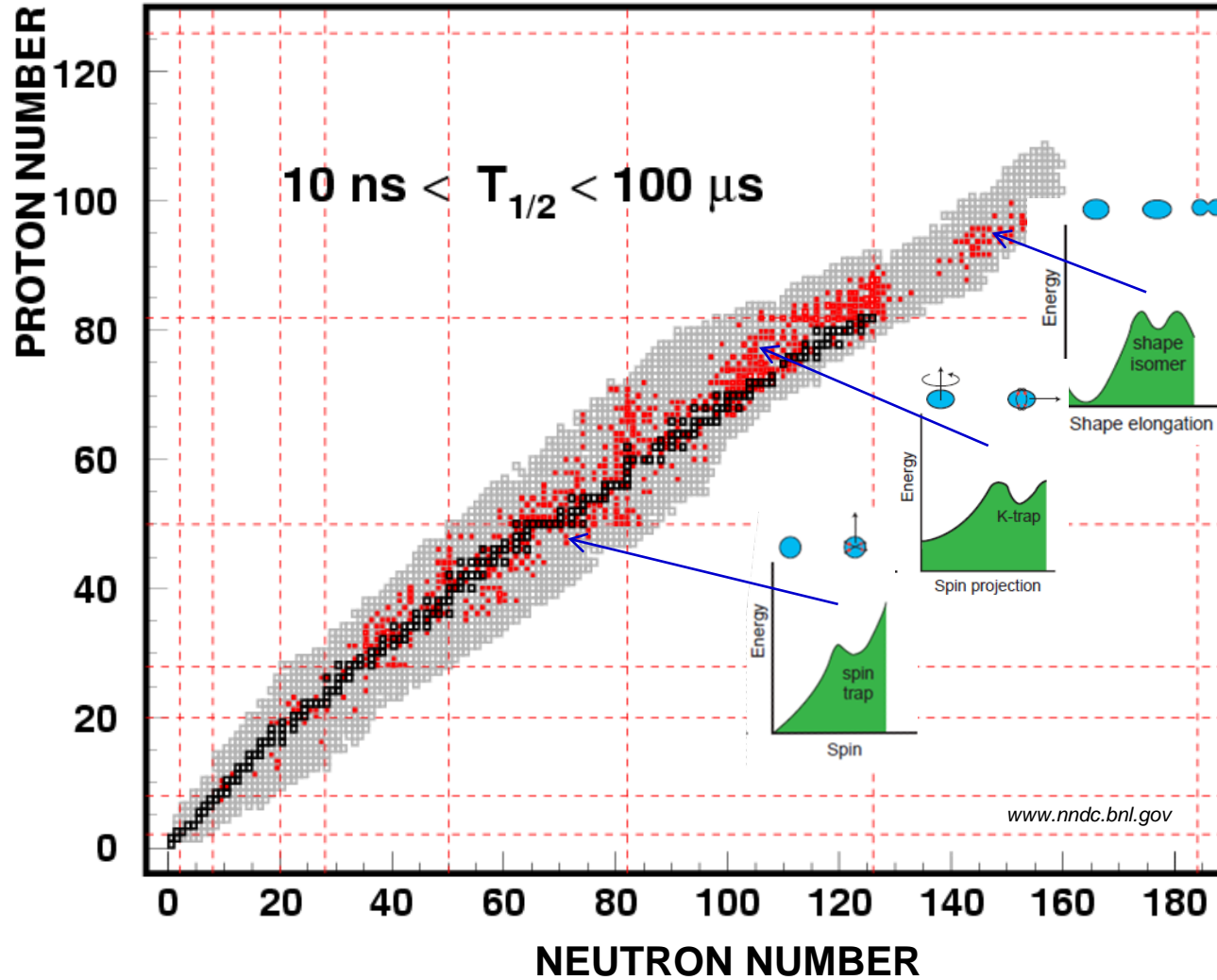


The first one discovered by O. Hahn in Berlin in 1921 – decay of  $^{234}\text{Pa}$  (70 s)  
von Weizsacker, A. Bohr & B. Mottelson

$$1/\tau \sim E_\gamma^{2\lambda+1} |\langle \psi_f | \mathbf{T} | \psi_i \rangle|$$

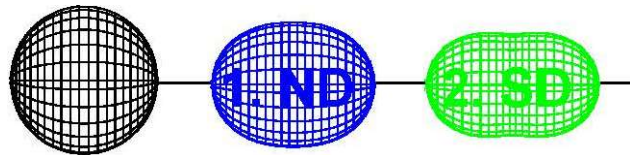
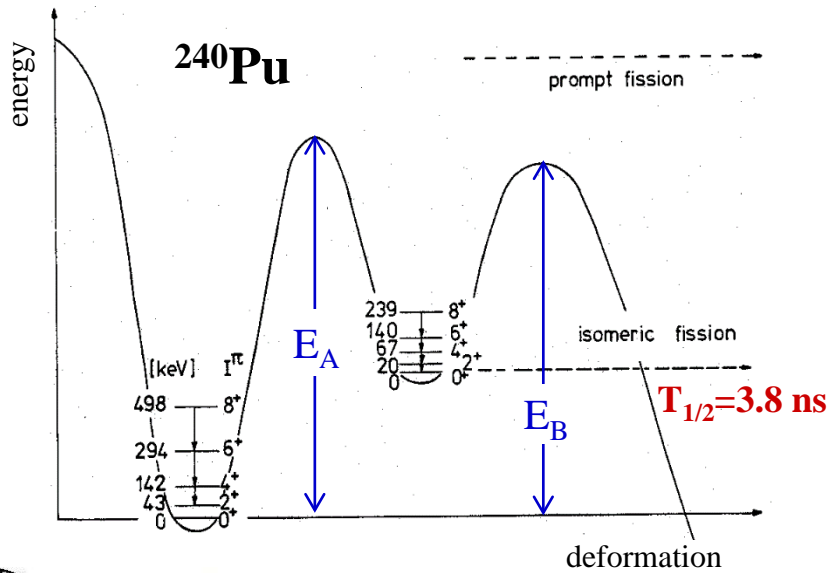


# Three types of isomers



# 1. Shape isomers

- **fission isomer** (discovered by S.M. Polikanov Sov. Phys. JEPT 15 (1962) 105)

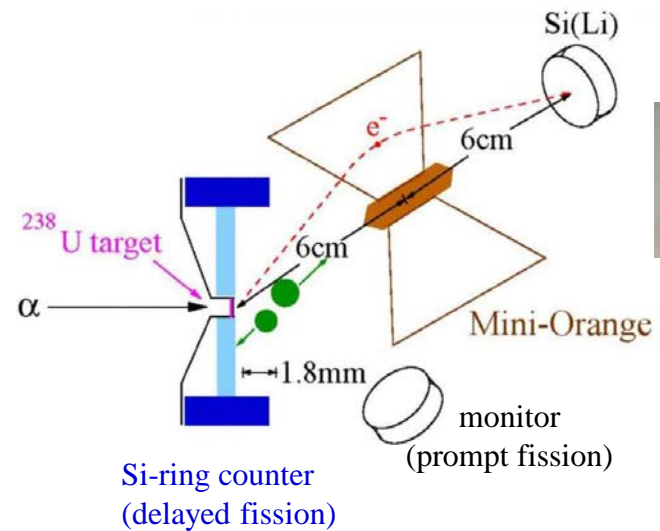
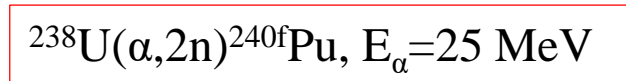


$$\frac{\hbar^2}{2\mathcal{I}} = 3.34 \text{ keV}$$

axis ratio 2:1

$$E_A = 5.8 \pm 0.3 \text{ MeV}$$

$$E_B = 5.45 \pm 0.3 \text{ MeV}$$

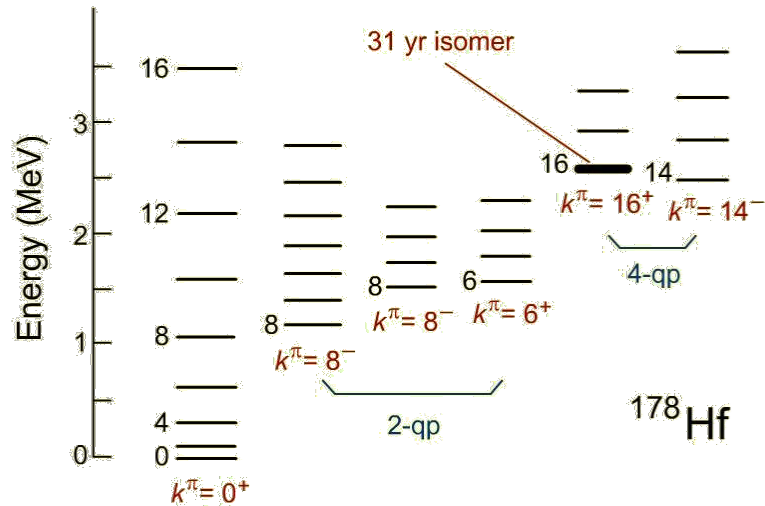


*D. Pansegrau et al., Phys. Lett. B484 (2000) 1*  
*D. Gassmann et al., Phys. Lett. B497 (2001) 181*

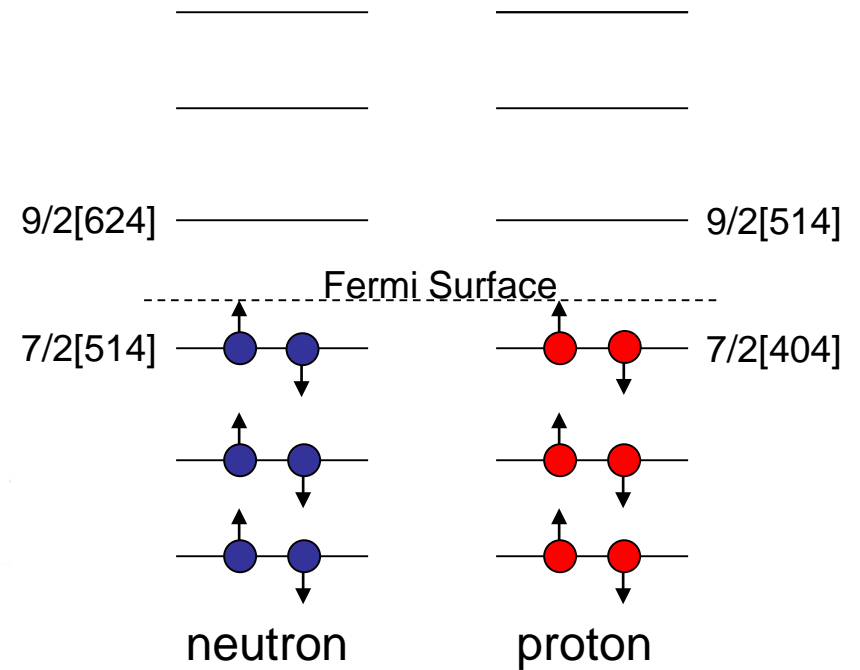
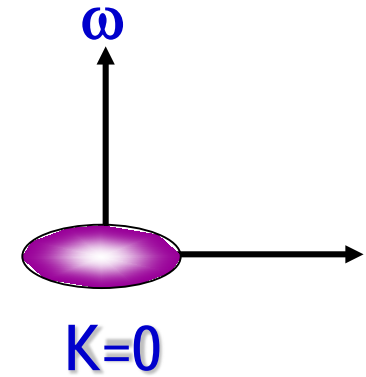
## 2. K-isomers

- A well-known example:

High-K isomers in  $^{178}\text{Hf}$



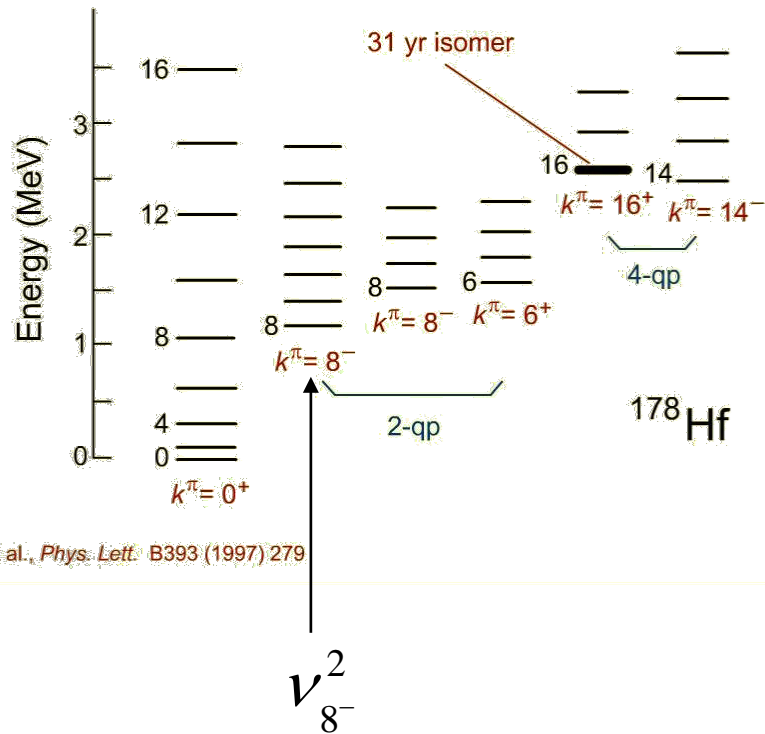
Mullins et al., *Phys. Lett. B* 393 (1997) 279



## 2. K-isomers

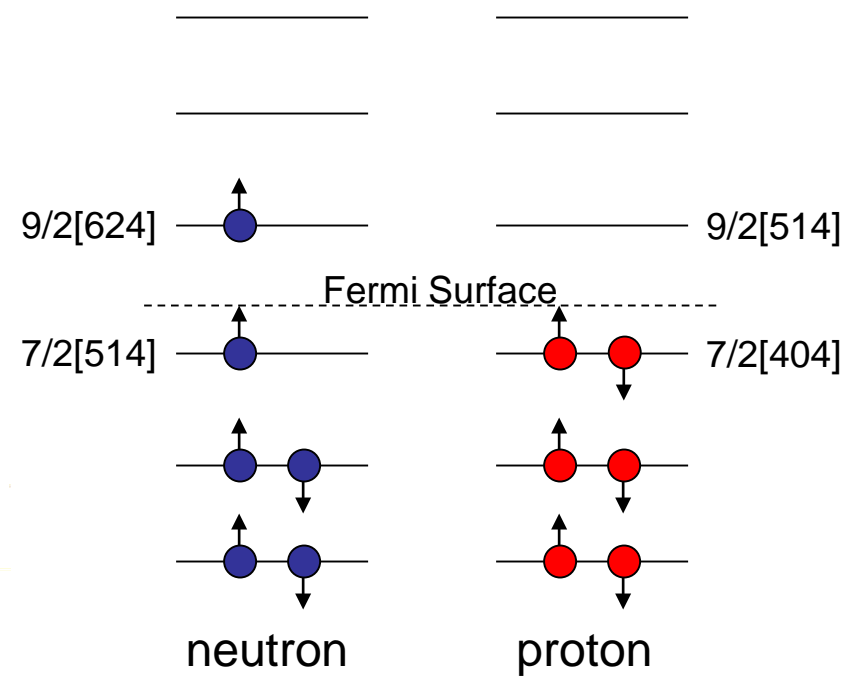
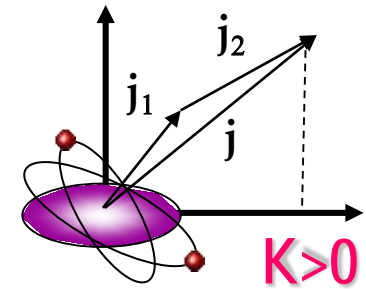
- A well-known example:

High-K isomers in  $^{178}\text{Hf}$



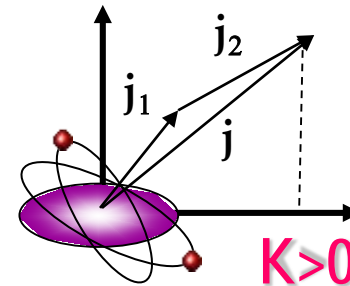
Mullins et al., *Phys. Lett. B* 393 (1997) 279

$\nu_{8^-}^2$



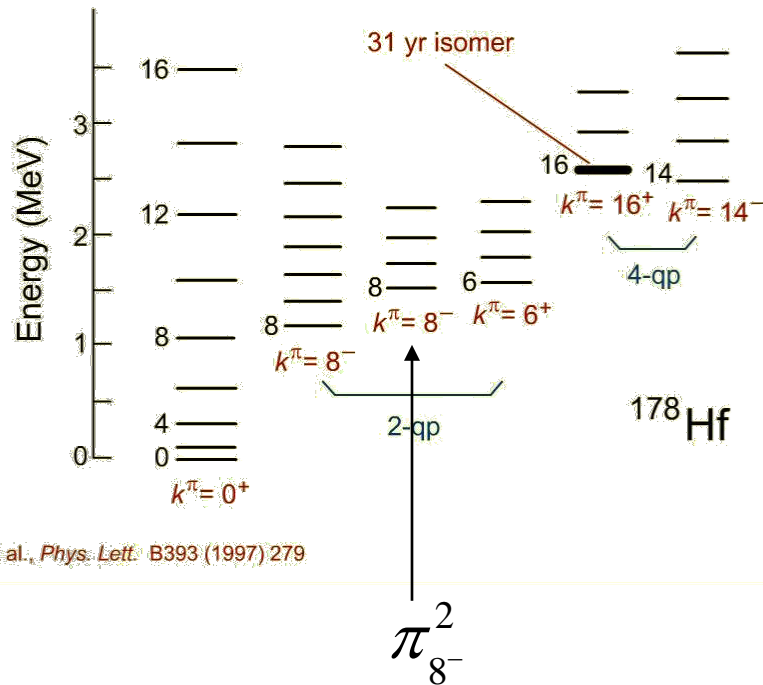
## 2. K-isomers

- A well-known example:

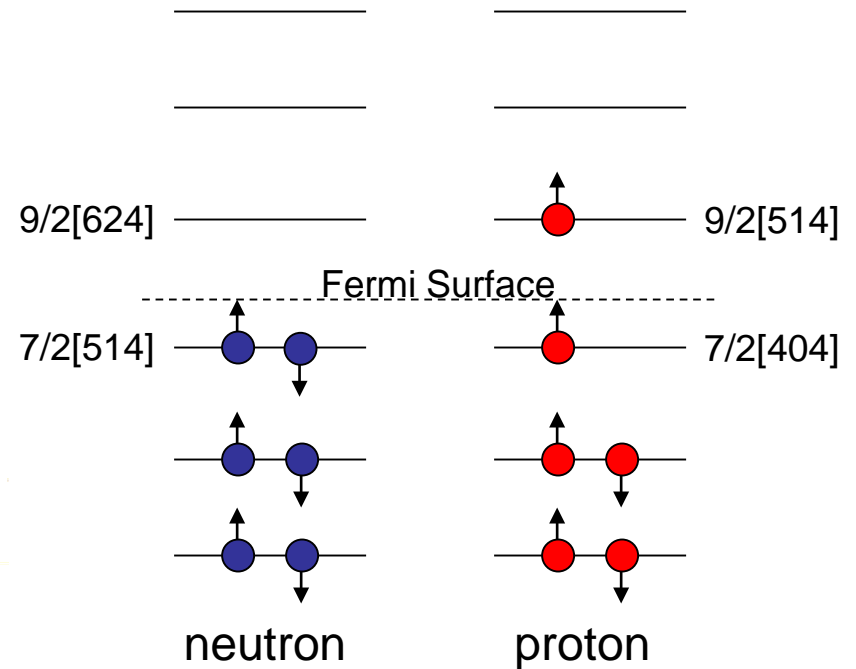


$\pi_{8^-}^2$

High-K isomers in  $^{178}\text{Hf}$



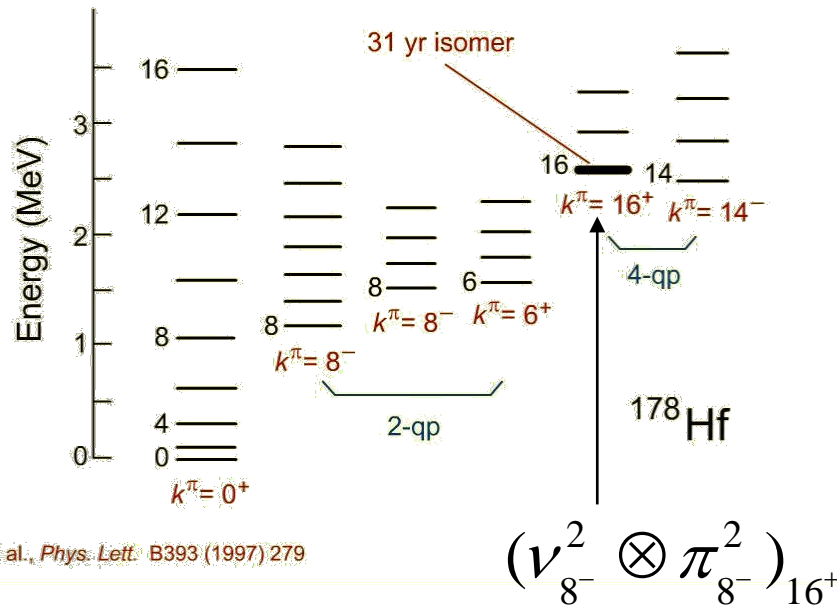
Mullins et al., *Phys. Lett. B* 393 (1997) 279



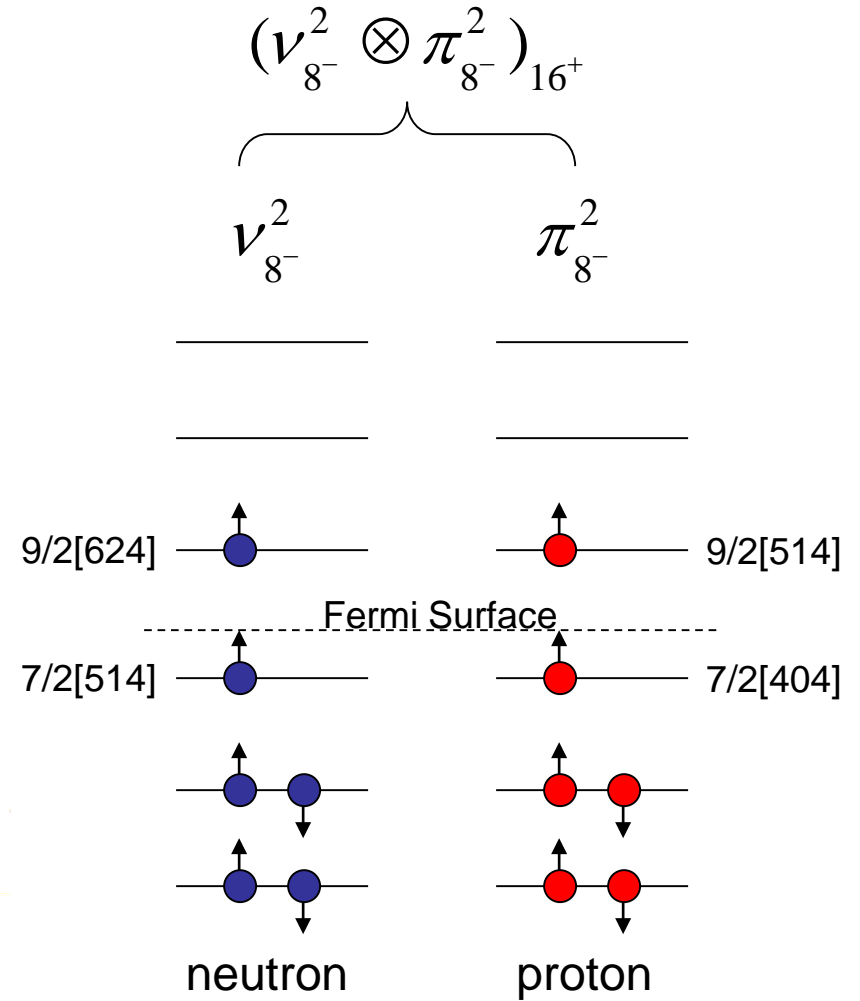
## 2. K-isomers

- A well-known example:

High-K isomers in  $^{178}\text{Hf}$



Mullins et al., *Phys. Lett. B* 393 (1997) 279







# Magnetic moments in $^{178}\text{Hf}$

$$g(j) = \begin{cases} \frac{2 \cdot \ell \cdot g_\ell + g_s}{2 \cdot \ell + 1} & \text{for } j = \ell + 1/2 \\ \frac{2 \cdot (\ell + 1) \cdot g_\ell - g_s}{2 \cdot \ell + 1} & \text{for } j = \ell - 1/2 \end{cases}$$

**proton**  $g_\ell = 1$   $g_s = 5.59$

**neutron**  $g_\ell = 0$   $g_s = -3.83$

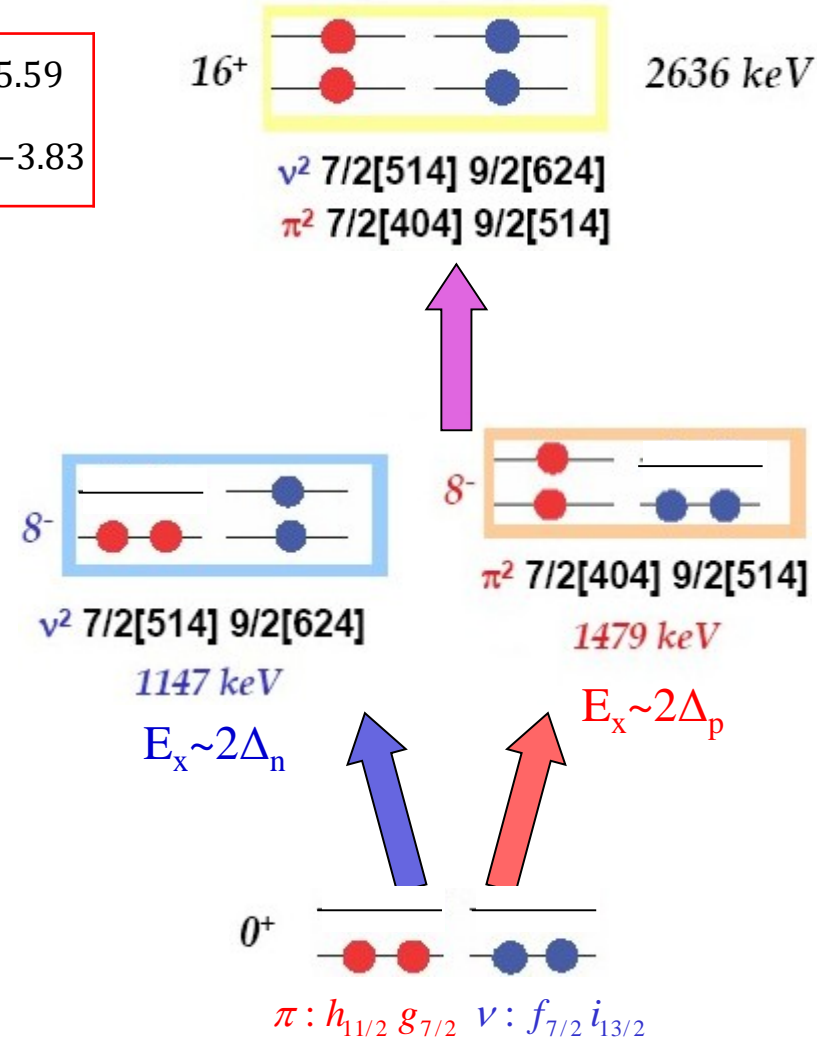
$$g(\mathbf{h}_{11/2}) = 1.42 \quad g(\mathbf{g}_{7/2}) = 0.49 \quad g(\mathbf{f}_{7/2}) = -0.55 \quad g(\mathbf{i}_{13/2}) = -0.29$$

$$g(j_1 \times j_2; J) = \frac{1}{2} \cdot (g_1 + g_2) + \frac{j_1 \cdot (j_1 + 1) - j_2 \cdot (j_2 + 1)}{2 \cdot J \cdot (J + 1)} \cdot (g_1 - g_2)$$

$$g(\mathbf{h}_{11/2} \times \mathbf{g}_{7/2}; 8^-) = 1.08 \quad g(\mathbf{f}_{7/2} \times \mathbf{i}_{13/2}) = -0.36$$

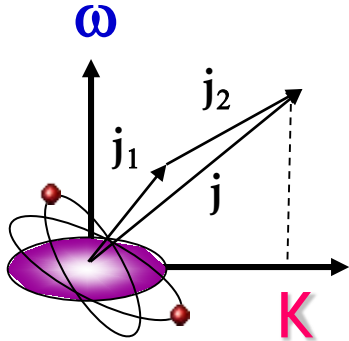
$g(8^- \times 8^-; 16^+) = 0.36 \quad \rightarrow \quad \mu = g \cdot I = 5.76 \text{ nm}$

$7.26 \pm 0.16 \text{ nm}$

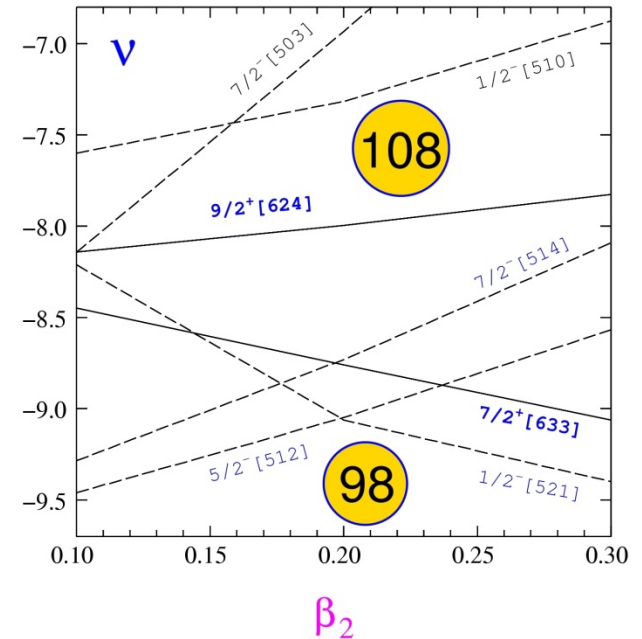
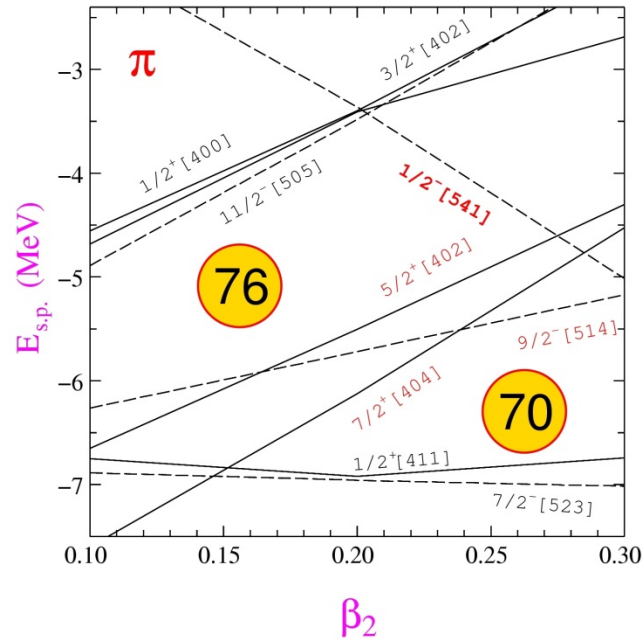


# K-isomers: where to find them?

- Deformed nuclei with axially-symmetric shape



## Mass 180 region : Yb (Z=70) - Ir (Z=77)



- High-K orbitals near the Fermi surface

$\pi$ : 7/2[404], 9/2[514], 5/2[402]

$\nu$ : 7/2[514], 9/2[624], 5/2[512], 7/2[633]

# 3. Spin isomers

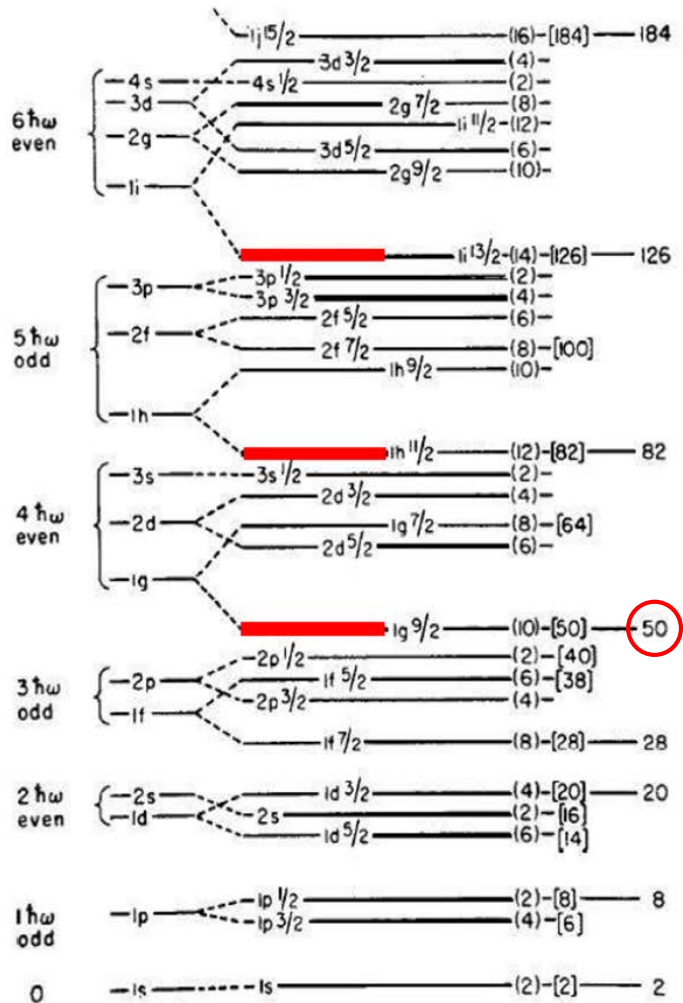
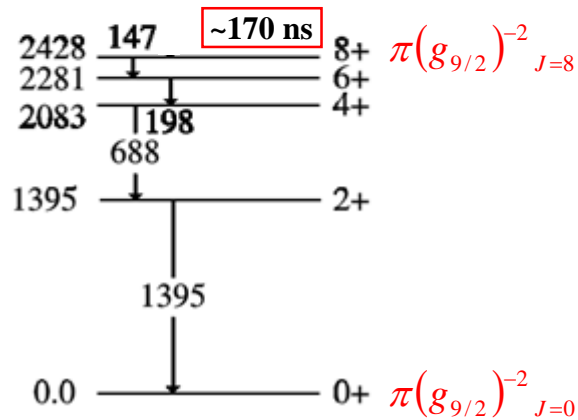


Fig. 7. Realistic level diagram for protons.



# 3. Spin isomers

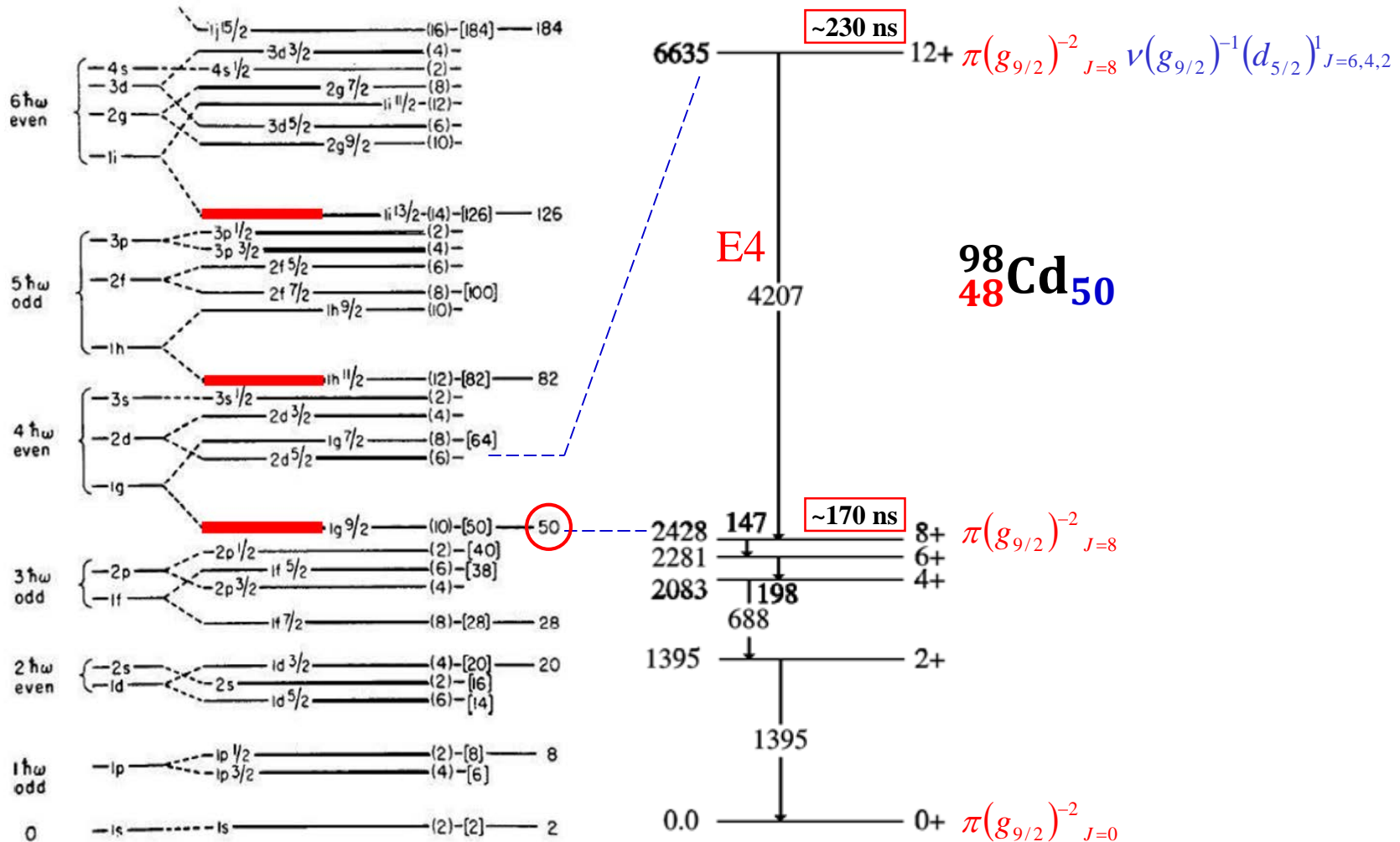
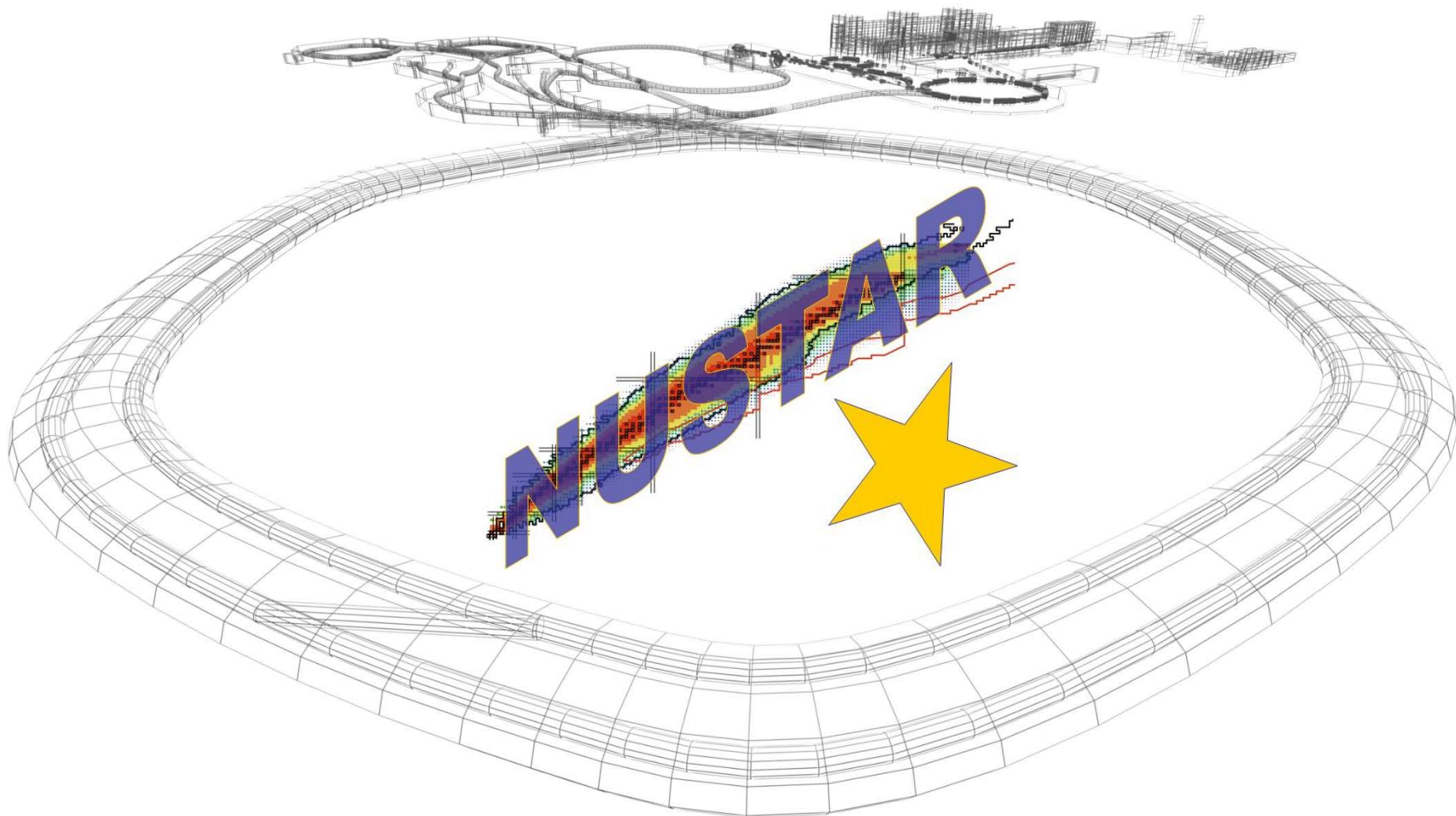
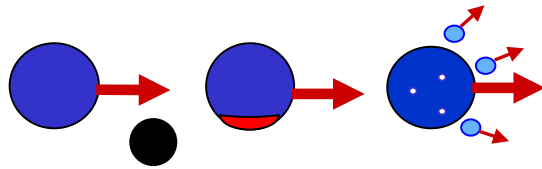


Fig. 7. Realistic level diagram for protons.

# Physics with exotic nuclei

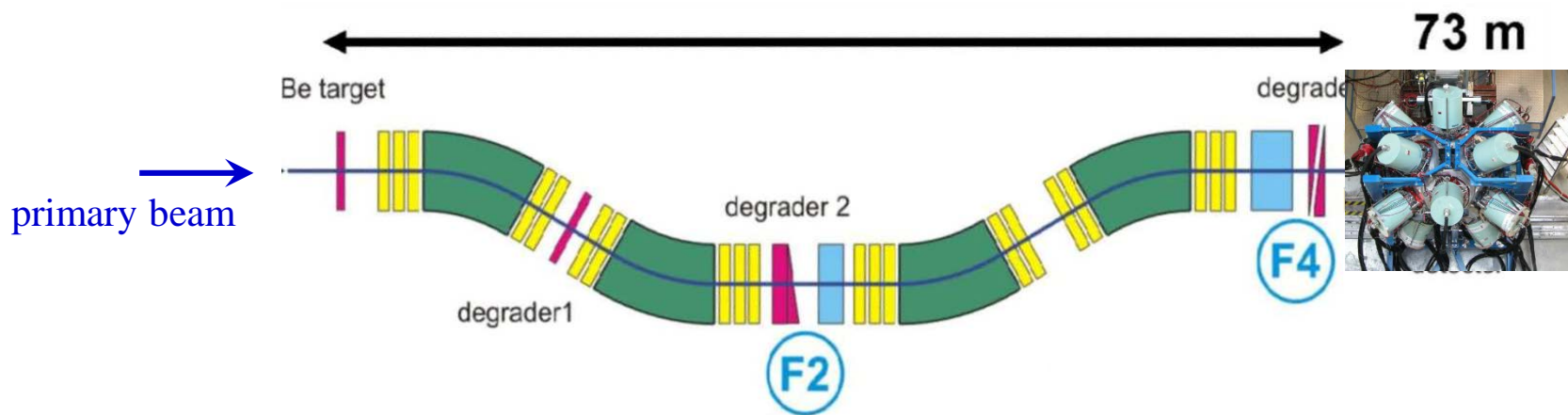


# Production of Radioactive Ion Beams



## Fragmentation

in ~20% of all cases the fragment is excited



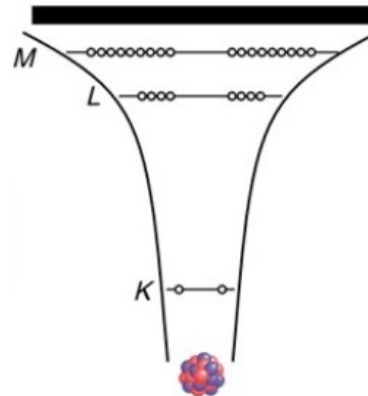
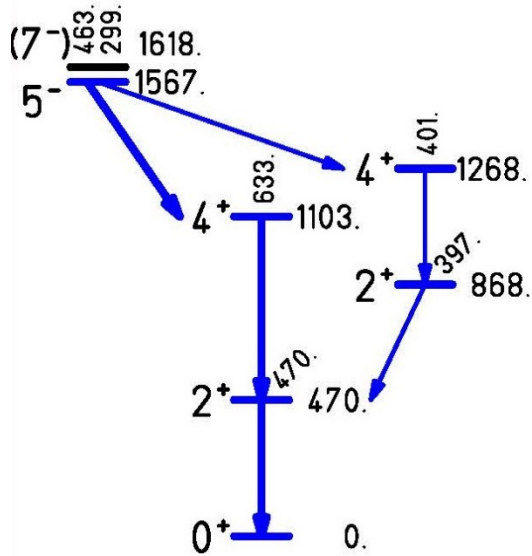
time-of-flight through the fragment separator FRS ~300 ns

Isomeric states can be investigated!

# Longer lifetime for bare atoms

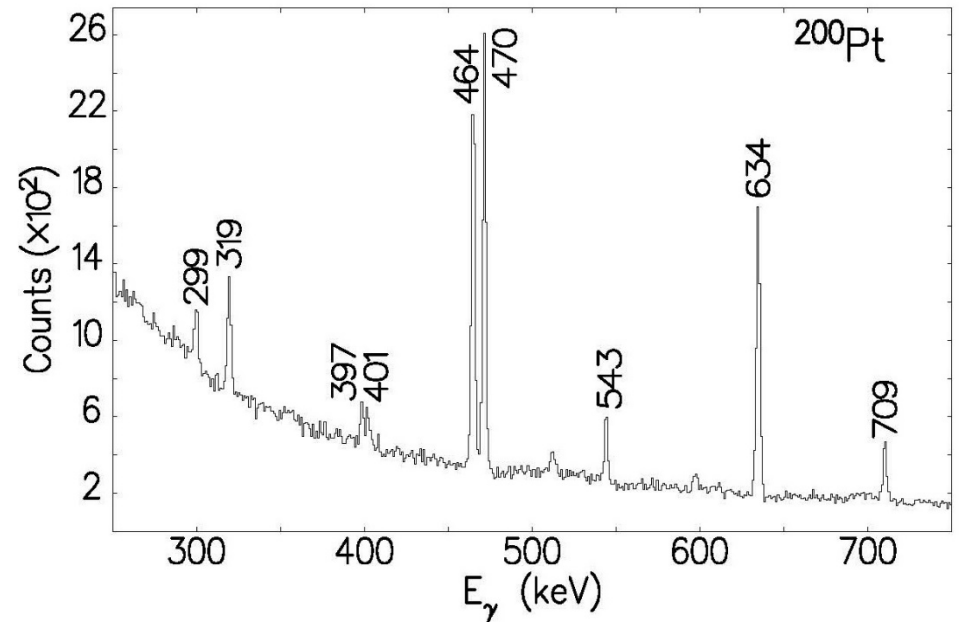
$^{200}\text{Pt}$

$t_{1/2} = 14.3\text{ ns}$   $\longrightarrow$   $t_{1/2}^{\text{r}} = 1.43\text{ }\mu\text{s}$

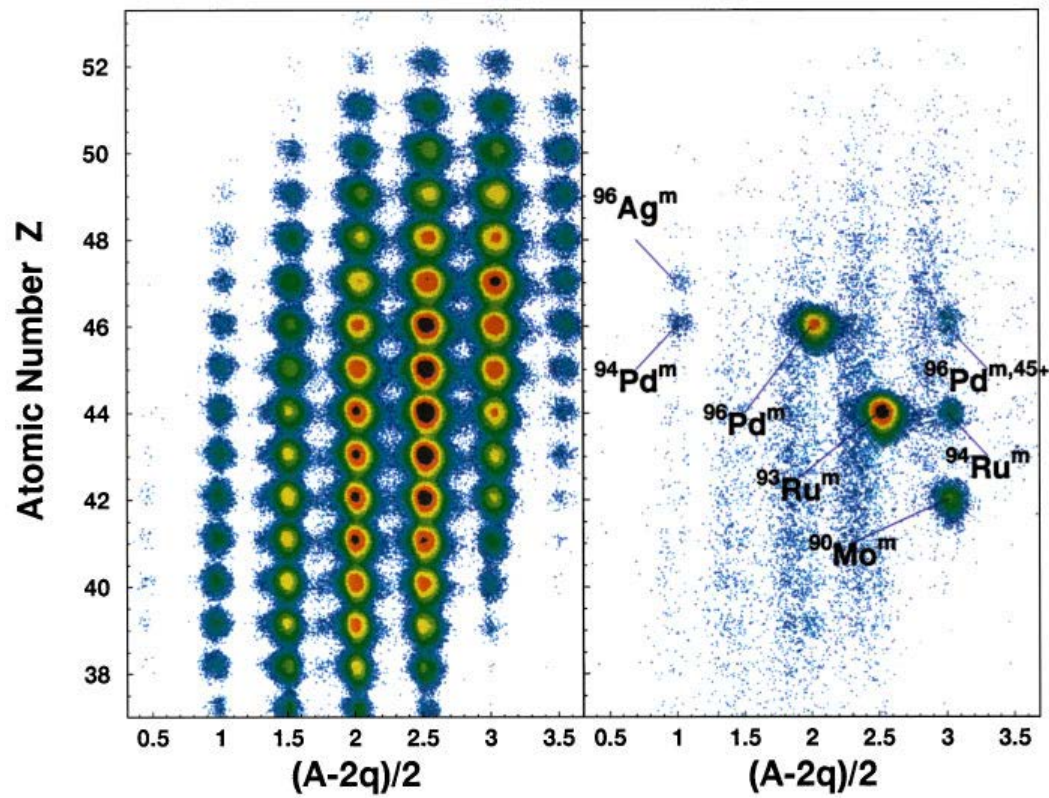
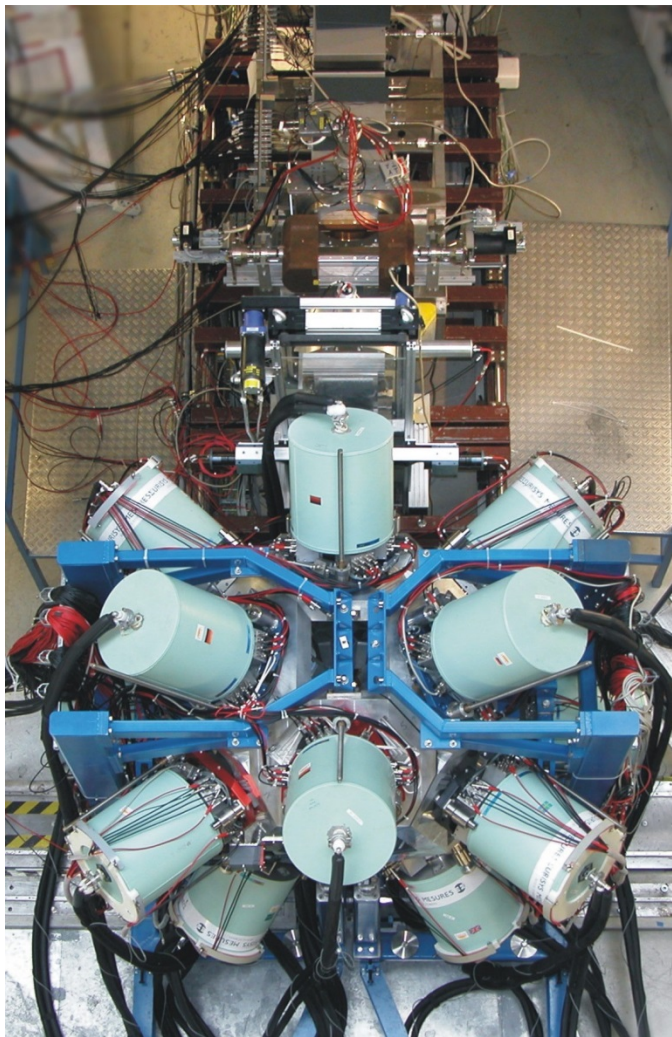


no conversion electrons

$\gamma$ -spectrum after  $\sim 300\text{ ns}$  ToF

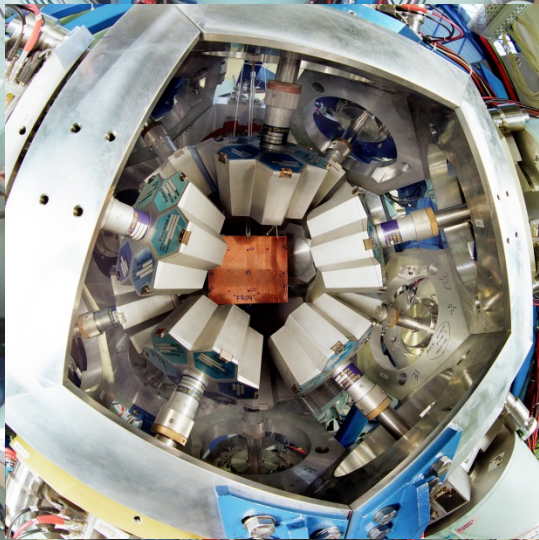


# Experimental set-up for isomer decay gateway to nuclear structure



R. Grzywacz et al., Phys. Rev C55, 1126 (1997)





scintillator  
(SC41)

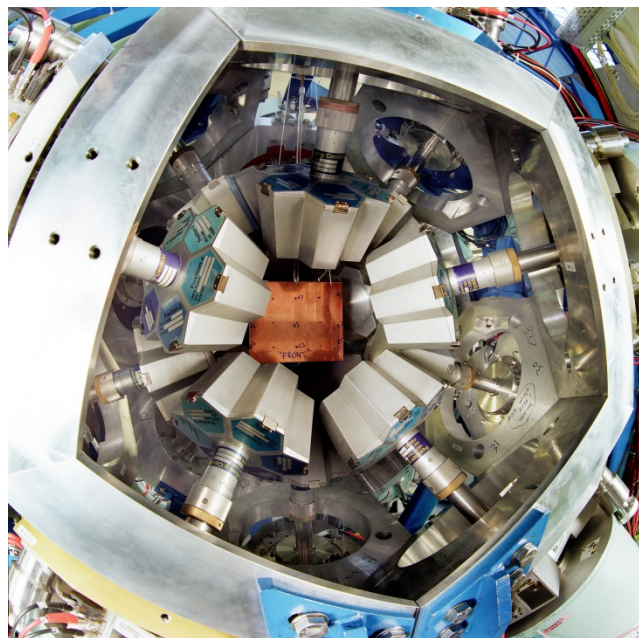
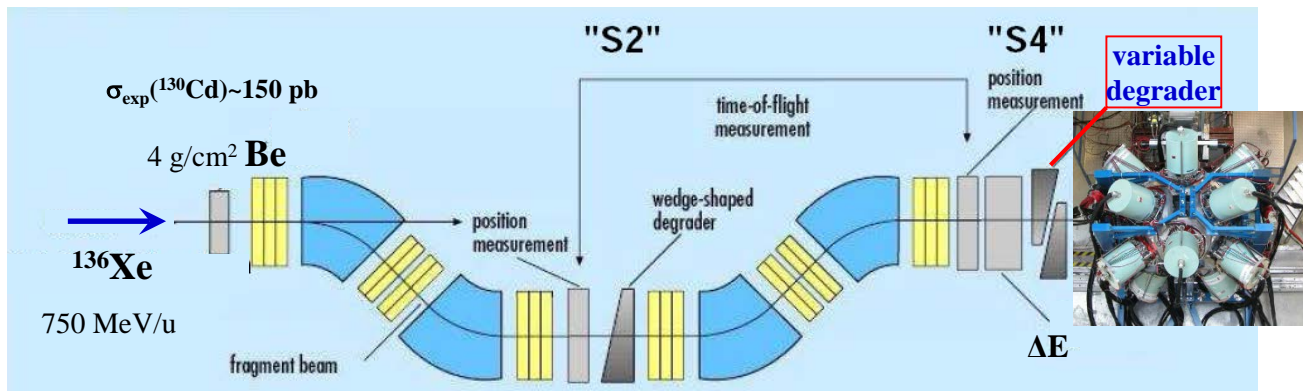
ionization  
chambers  
(MUSIC41,42)

beam  
←

degrader

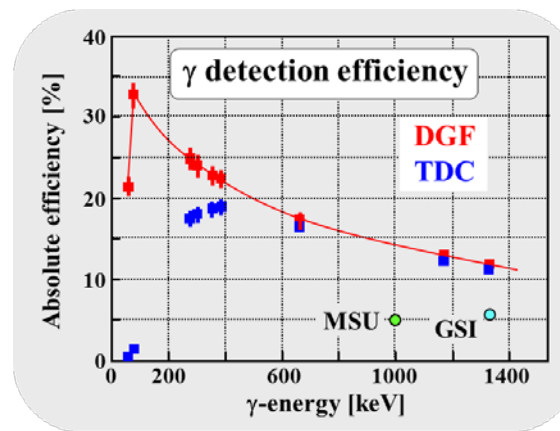
multiwire  
chambers  
(MW41,MW42)

# Experimental set-up with passive target



**implantation in Cu-plate**

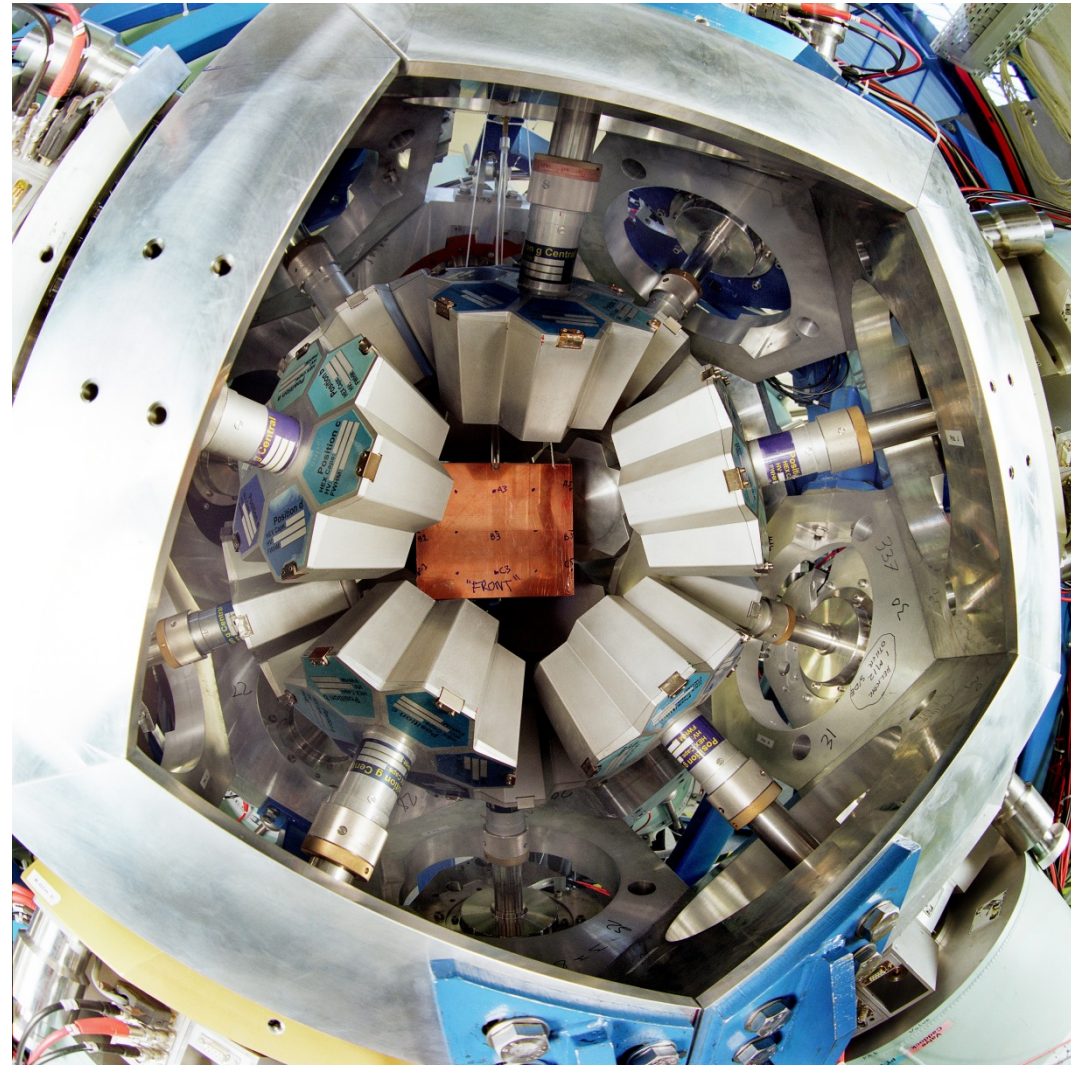
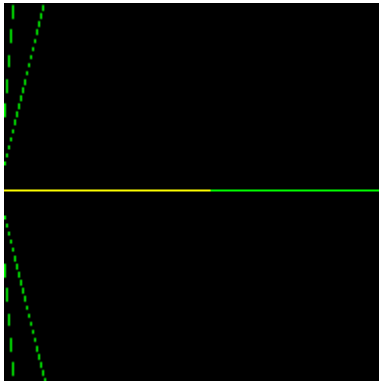
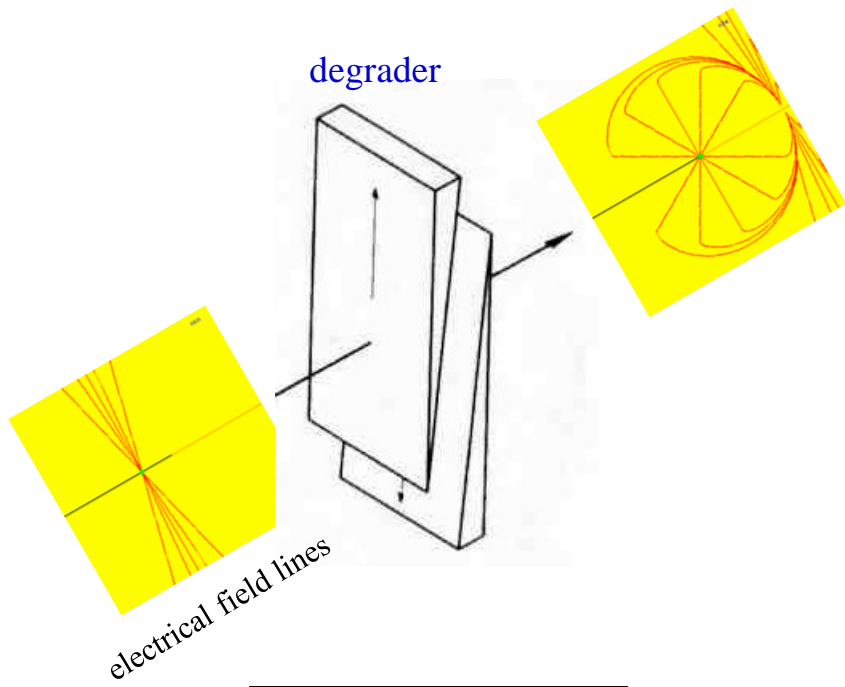
15 Cluster detectors with 105 Ge crystals  
 $\epsilon_{\gamma} = 11\%$  at 1.3 MeV, 20% at 550 keV, 35% at 100 keV



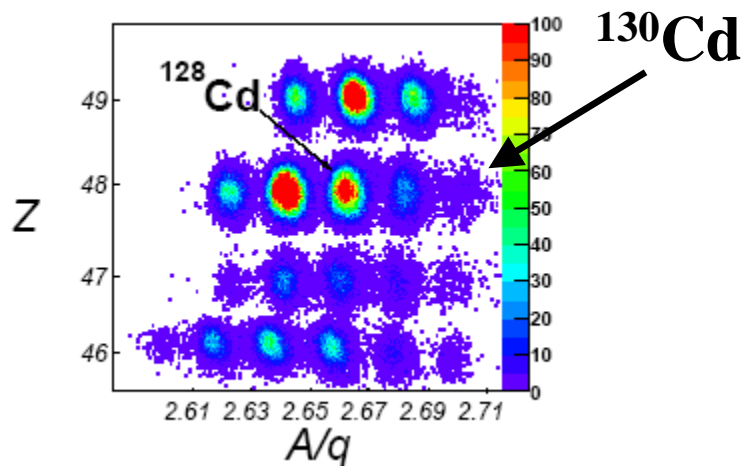
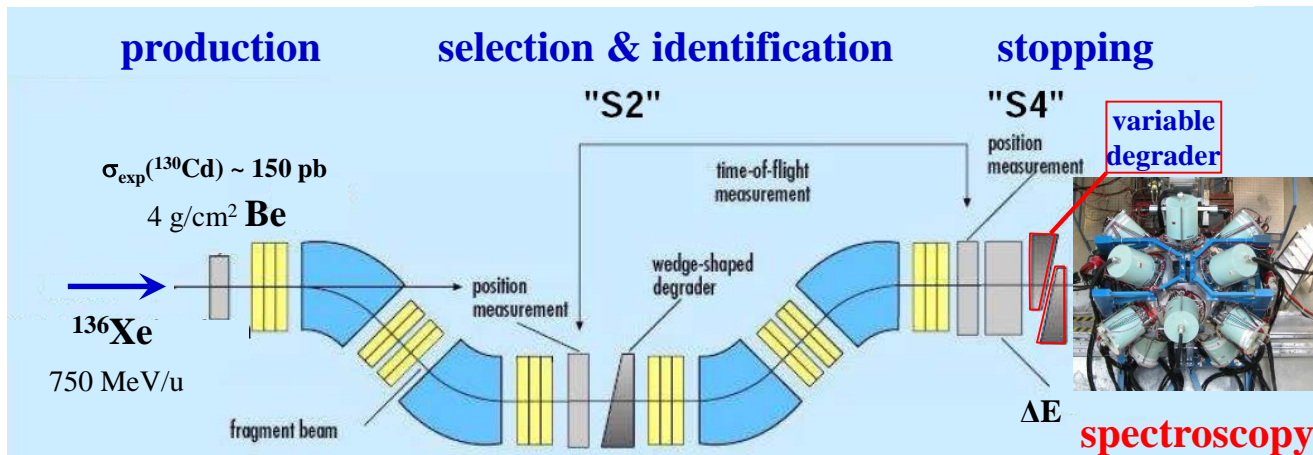
- very high  $\gamma$ -ray efficiency
- high granularity (prompt flash problem)

S. Pietri et al., NIM B261 (2007), 1079

# Limitations in isomeric spectroscopy



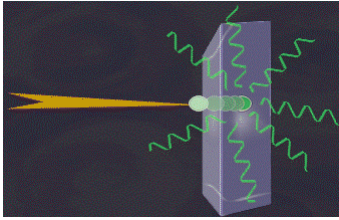
# Identification of $^{130}_{48}\text{Cd}_{82}$



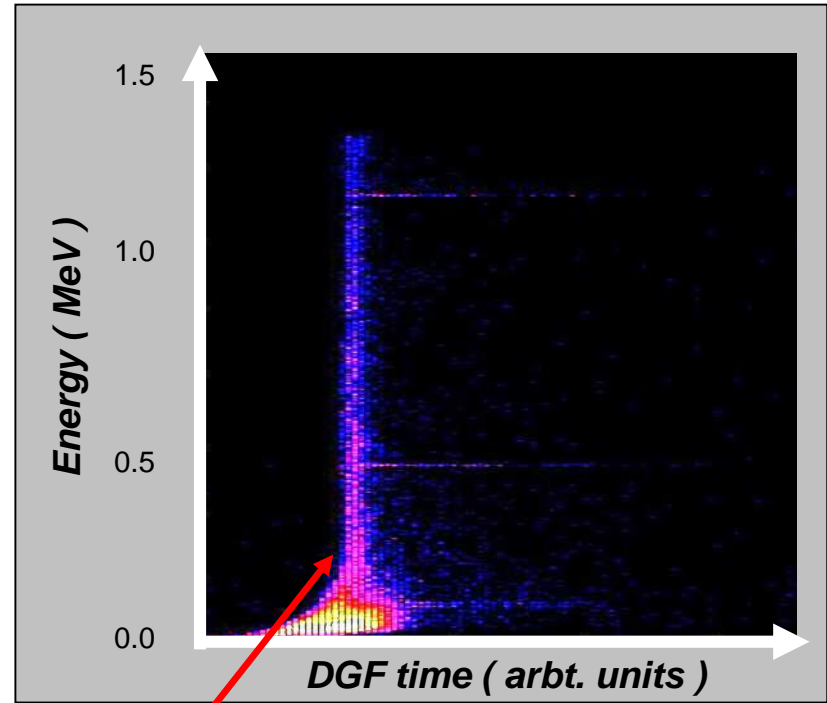
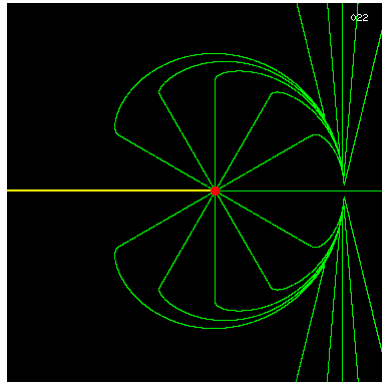
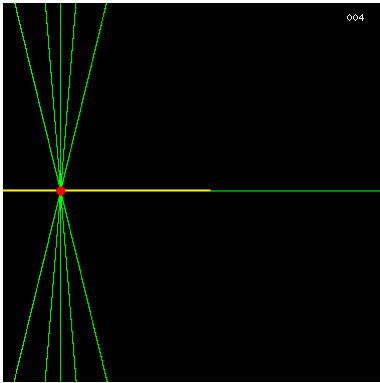
➡ 4000 identified  $^{130}\text{Cd}$  ions  
in fragmentation

# Limitations in isomer spectroscopy

## $^{130}\text{Cd}$ : DGF-timing



slowing down of a  
moving point-charge

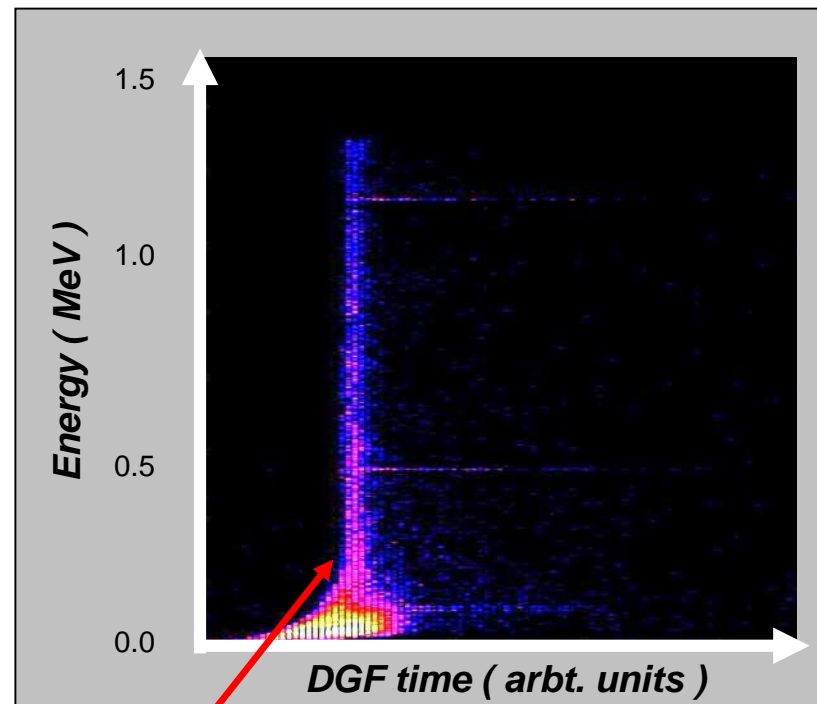
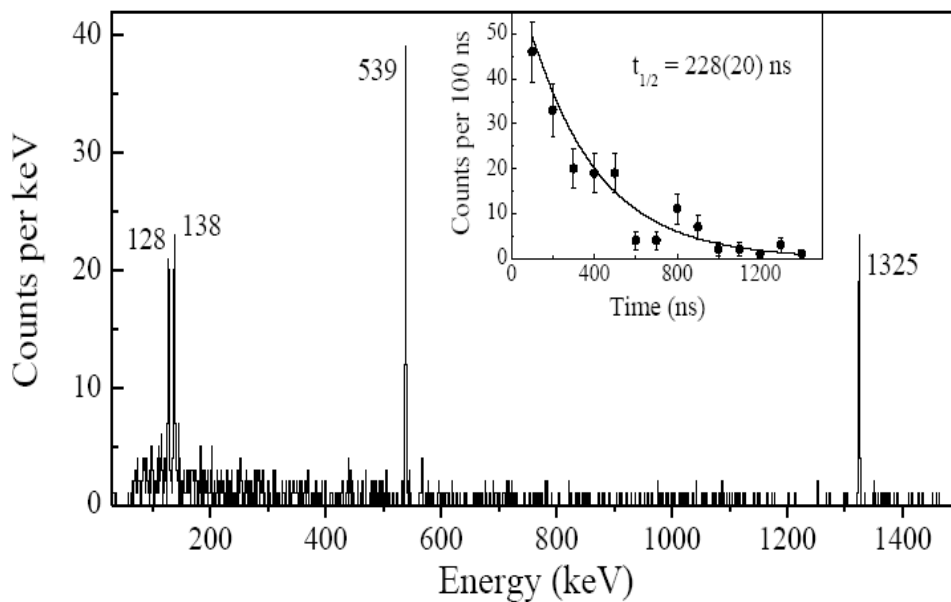


Prompt  $\gamma$ -flash

Decay time range: 20 ns ... 20  $\mu$ s

# Decay spectroscopy probes shell closures

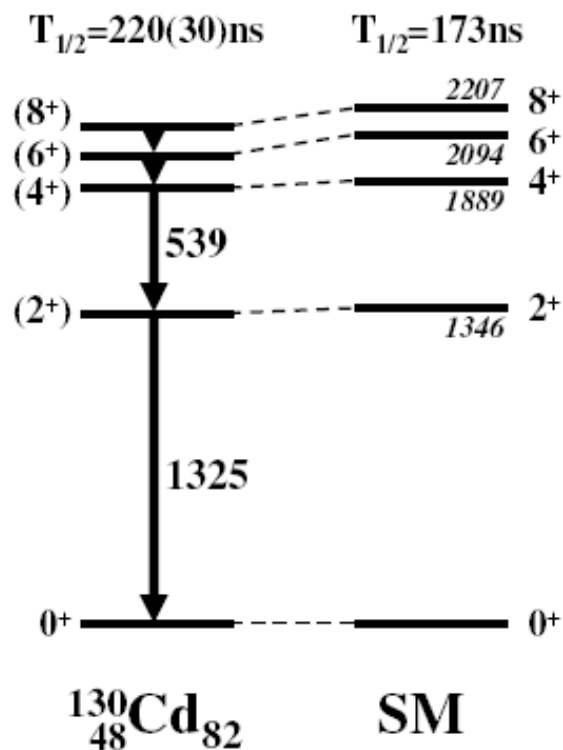
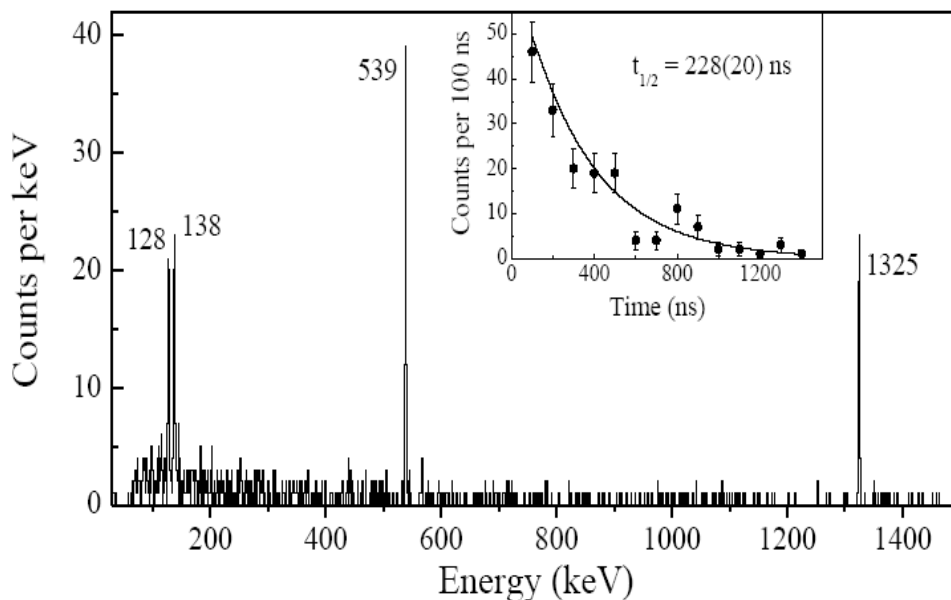
$^{130}\text{Cd}$ : DGF-timing



**Prompt  $\gamma$ -flash**

Decay time range: 20 ns ... 20  $\mu\text{s}$

# Decay spectroscopy probes shell closures



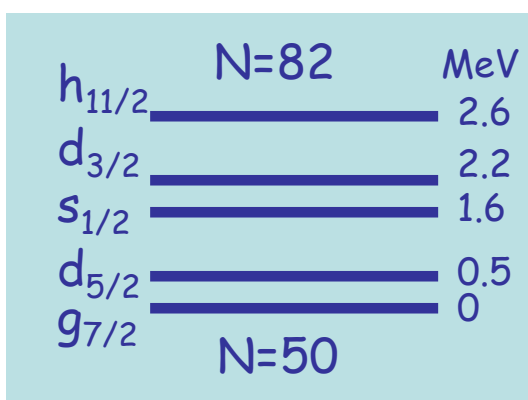
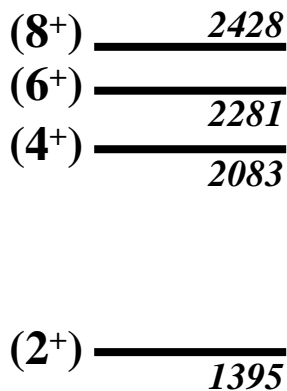
No Shell quenching observed

# $8^+(g_{9/2})^{-2}$ seniority isomers in $^{98}\text{Cd}$ and $^{130}\text{Cd}$

Sn100 0.94 s 0+	Sn101 3 s 0+	Sn102 4.5 s 0+	Sn103 7 s 0+	Sn104 20.8 s 0+	Sn105 31 s 0+	Sn106 115 s 0+	Sn107 2.90 m (5/2+)	Sn108 10.30 m 0+	Sn109 18.9 m 5/2(+)	Sn110 411 h 0+	Sn111 35.3 m 7/2+	Sn112 0.97 s 0+	Sn113 115.09 d 1/2+	Sn114 0.65 s 0+	Sn115 0.54 s 1/2+	Sn116 14.5 s 0+	Sn117 7.68 s 1/2+	Sn118 24.23 s 0+	Sn119 8.59 s 1/2+	Sn120 31.59 s 0+	Sn121 27.06 h 3/2+	Sn122 119.2 d 0+	Sn123 119.2 d 11/2-	Sn124 0.6 s 0+	Sn125 9.64 d 9/2+	Sn126 1E+5 y (11/2-)	Sn127 2.10 h (11/2-)	Sn128 59.07 m 0+	Sn129 2.15 m (3/2-)	Sn130 3.72 m 0+	Sn131 56.9 s (3/2-)	Sn132 39.7 s 0+
In99	In100	In101	In102	In103	In104	In105	In106	In107	In108	In109	In110	In111	In112	In113	In114	In115	In116	In117	In118	In119	In120	In121	In122	In123	In124	In125	In126	In127	In128	In129	In130	In131
Cd98	Cd99	Cd100	Cd101	Cd102	Cd103	Cd104	Cd105	Cd106	Cd107	Cd108	Cd109	Cd110	Cd111	Cd112	Cd113	Cd114	Cd115	Cd116	Cd117	Cd118	Cd119	Cd120	Cd121	Cd122	Cd123	Cd124	Cd125	Cd126	Cd127	Cd128	Cd129	Cd130

**Cd98**  
9.2 s  
0+  
EC

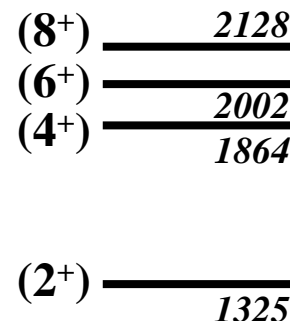
N=50  
Z=48



participating neutron-orbitals

**Cd130**  
0.20 s  
0+  
β-n

N=82  
Z=48



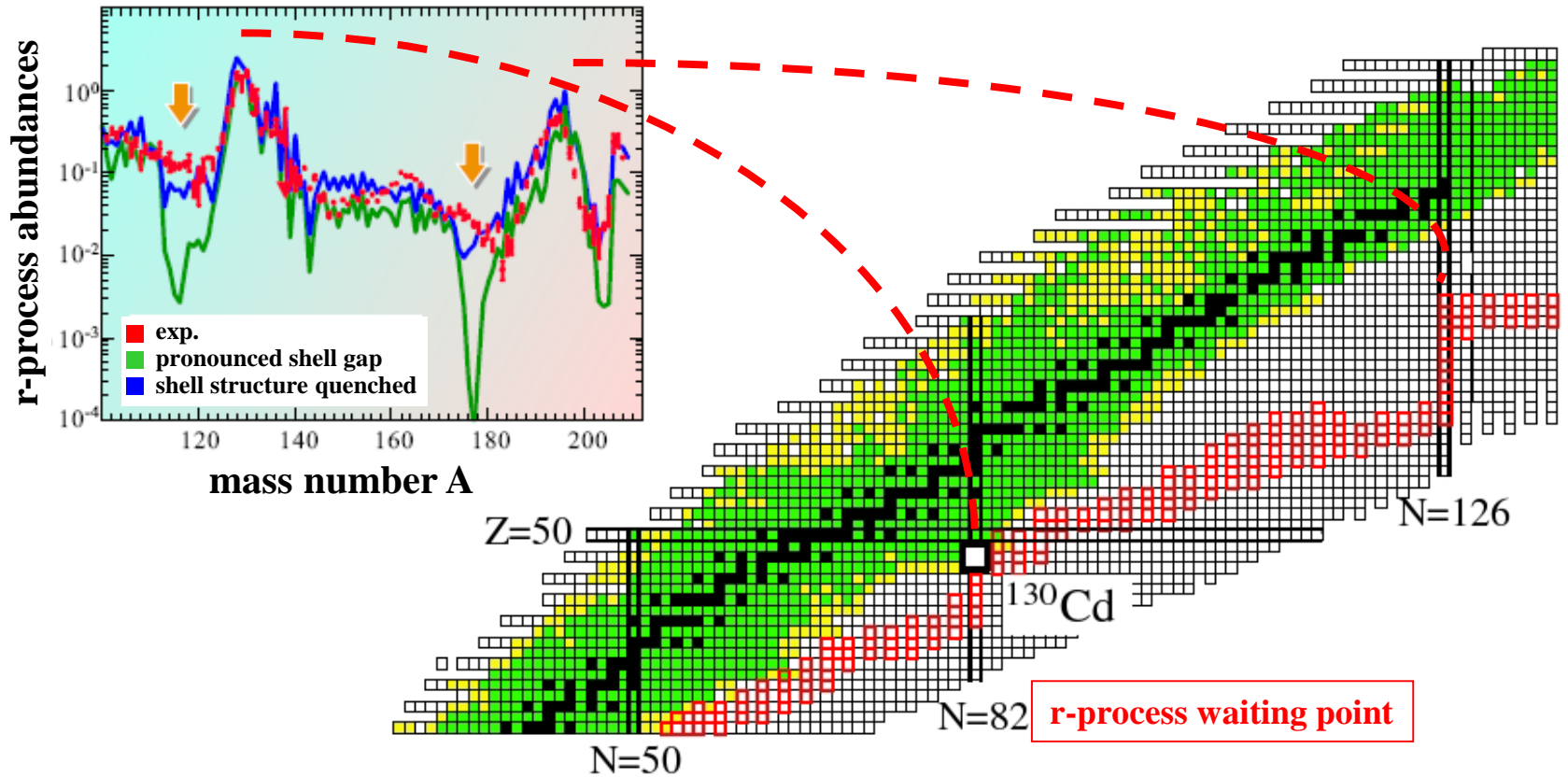
two proton holes in the  $g_{9/2}$  orbit

No dramatic shell quenching!



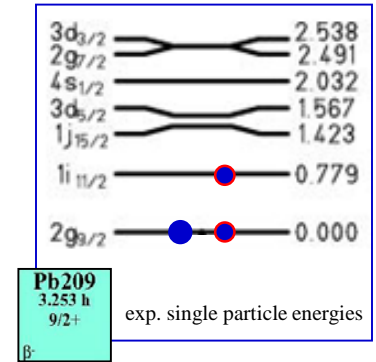
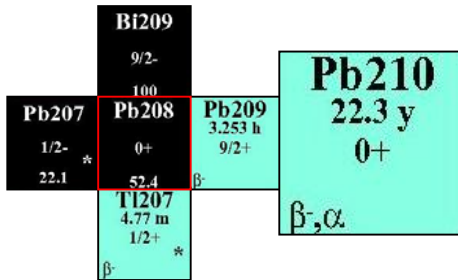


# The astrophysical r-process 'path'



Assumption of a N=82 shell quenching leads to a considerable improvement in the global abundance fit in r-process calculations !

# Level scheme of $^{210}\text{Pb}$



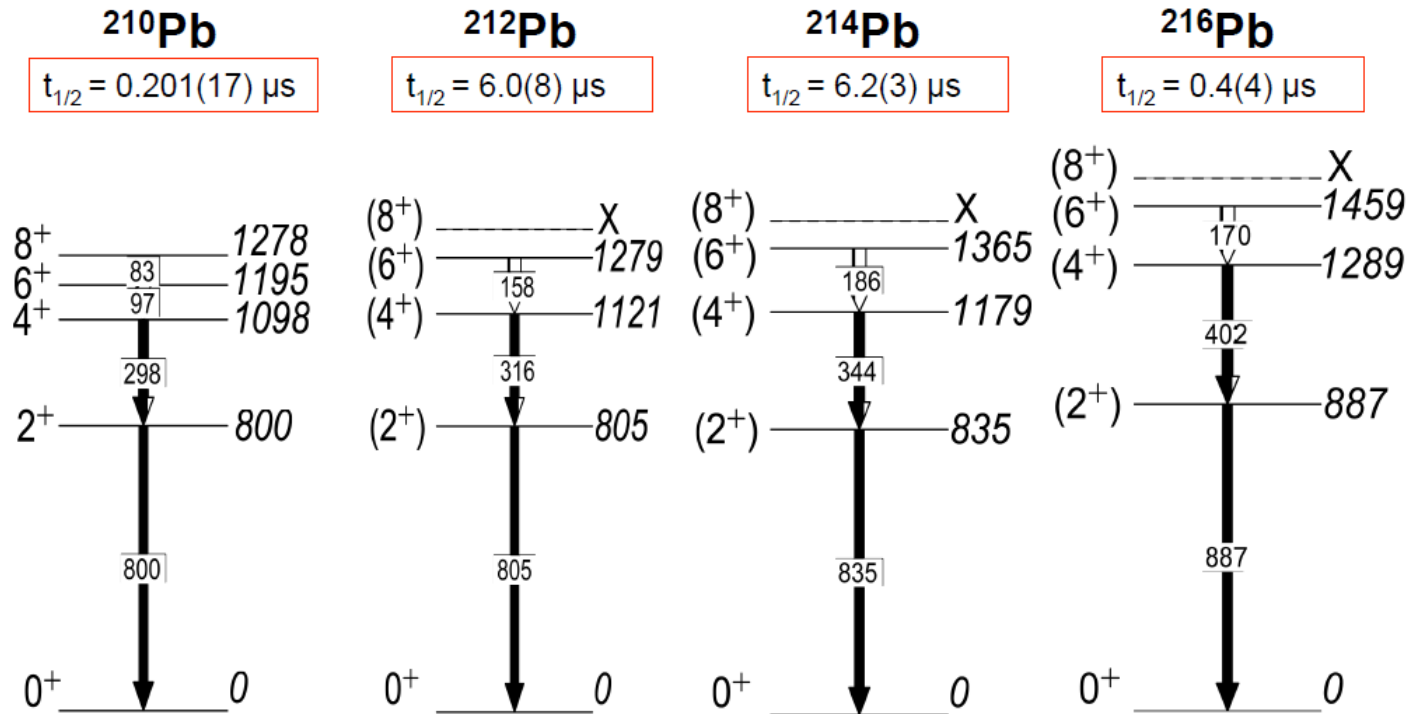
(pairing energy)  
residual interaction !

# Level schemes of neutron-rich Pb-isotopes

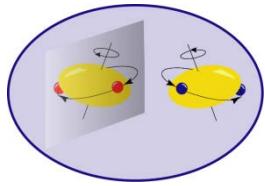
Pb205 1.53E+7 y 5/2- *	Pb206 0+ 24.1	Pb207 1/2- *	Pb208 0+ 52.4	Pb209 3.253 h 9/2+	Pb210 22.3 y 0+	Pb211 36.1 m 9/2+	Pb212 10.64 h 0+	Pb213 10.2 m (9/2+)	Pb214 26.8 m 0+	Pb215 36 s (5/2+)	Pb216	Pb217	Pb218
EC				$\beta^-$	$\beta^-, \alpha$	$\beta^-$	$\beta^-$	$\beta^-$	$\beta^-$	$\beta^-$			

←—————→

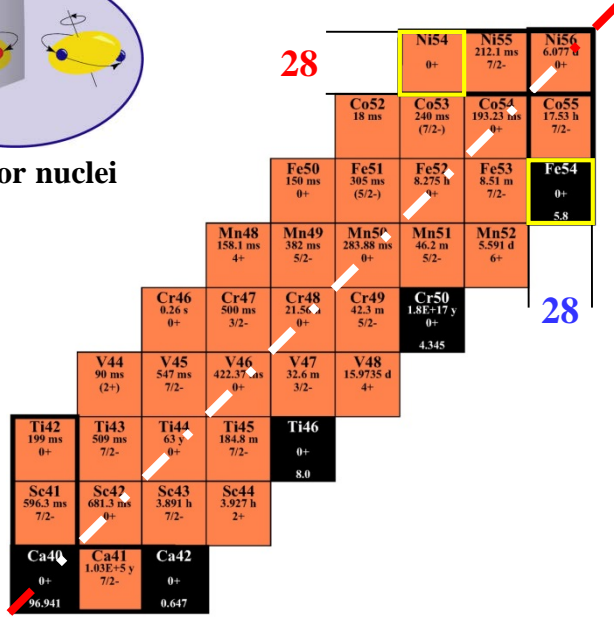
$g_{9/2}$



# T=1 isospin symmetry in pf-shell nuclei search for isospin breaking effects

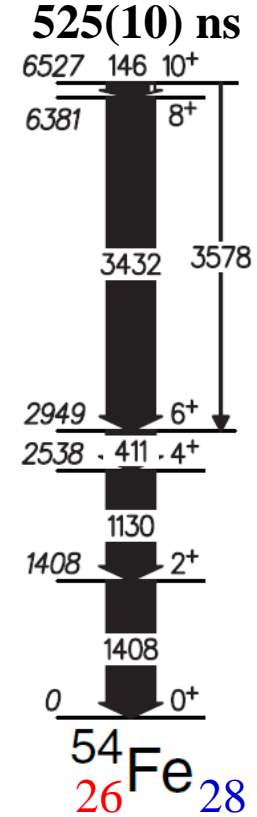
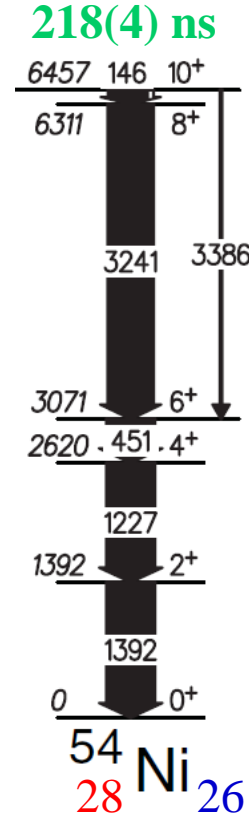


mirror nuclei

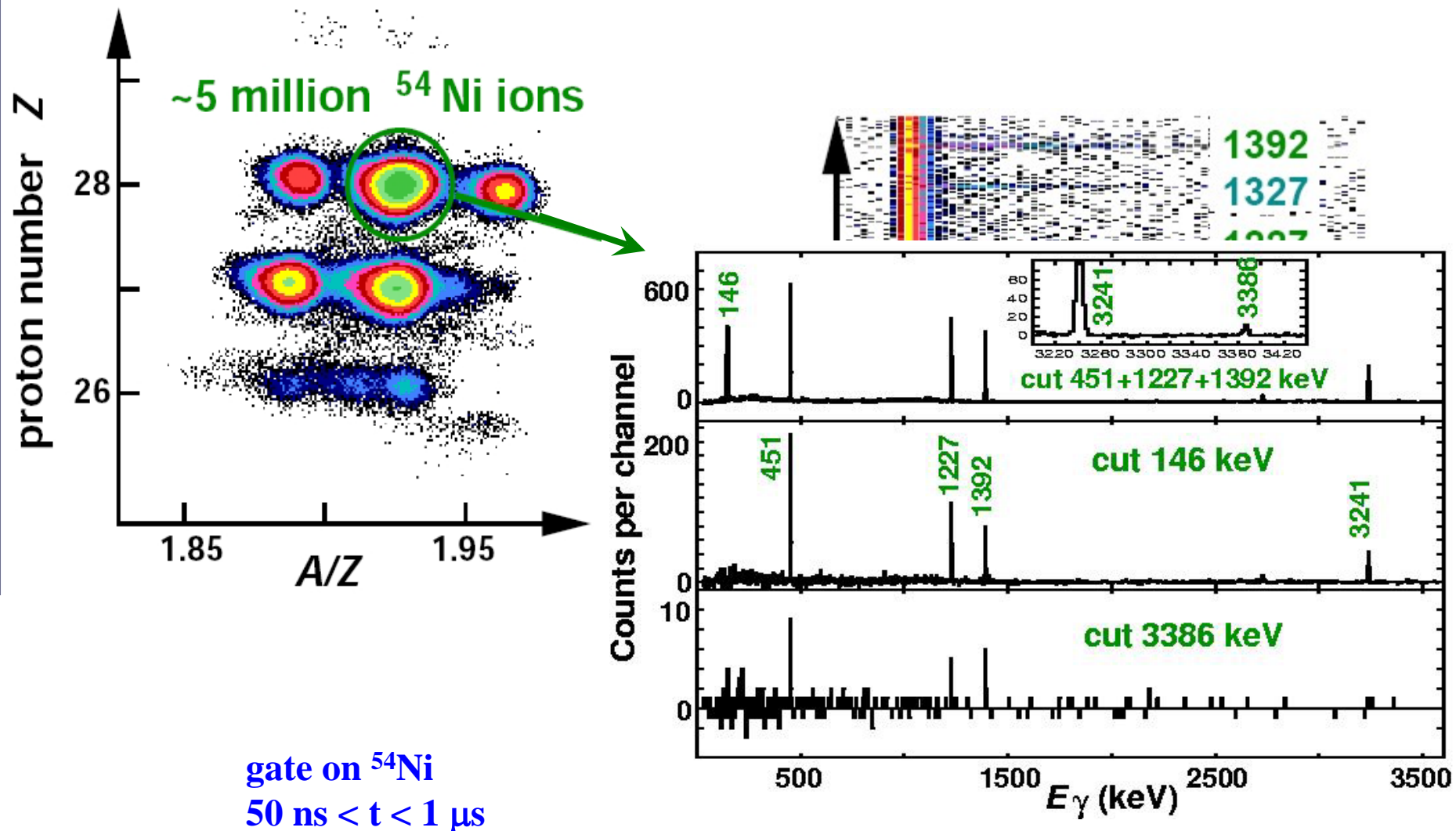


decay of the excited 10<sup>+</sup>-state by proton emission and  $\gamma$ -radiation

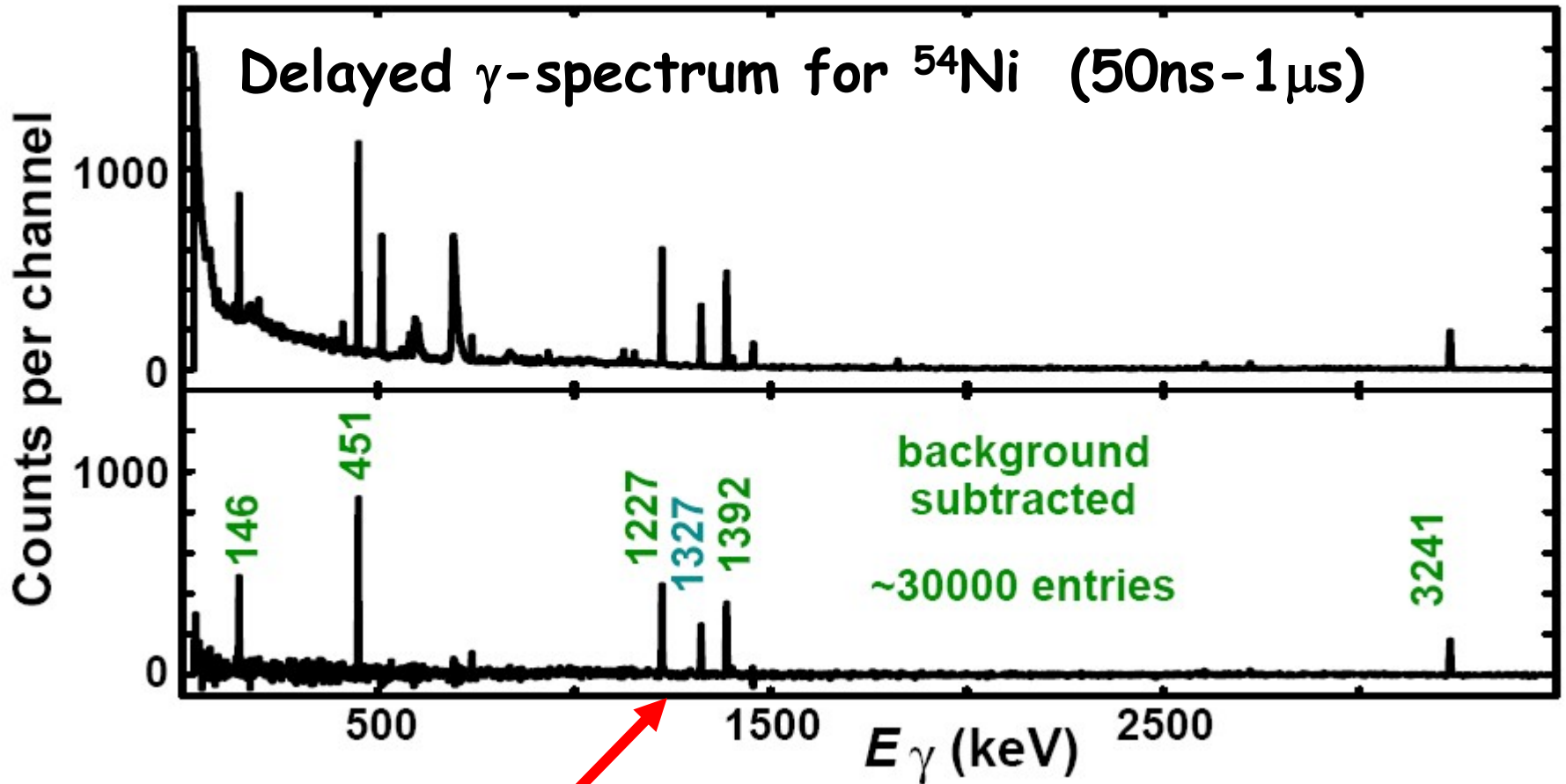
**N=Z**



# Identification of $^{54}\text{Ni}$

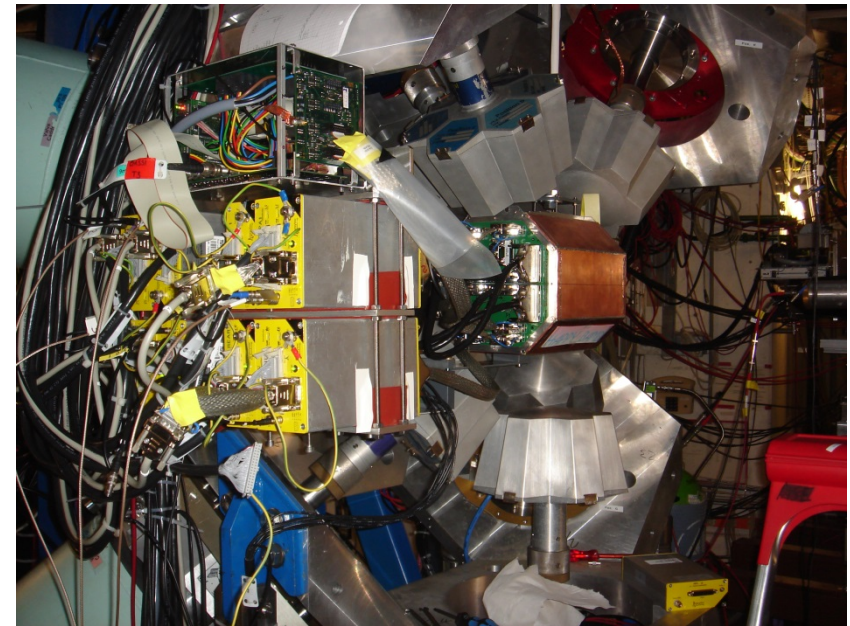
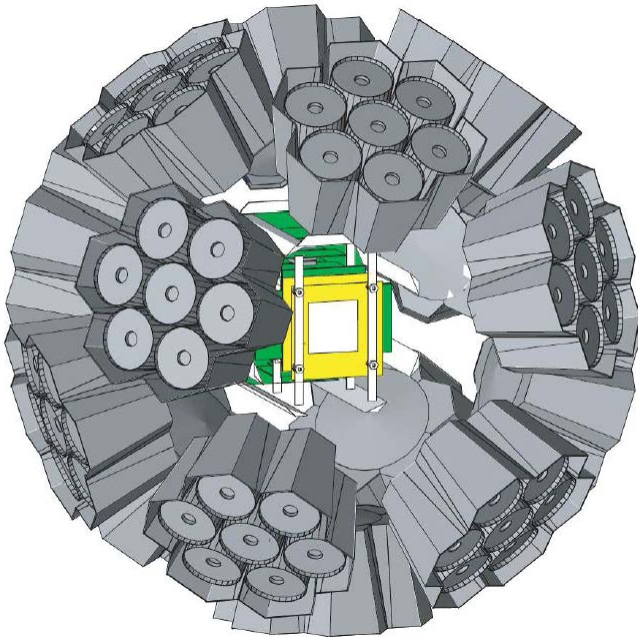
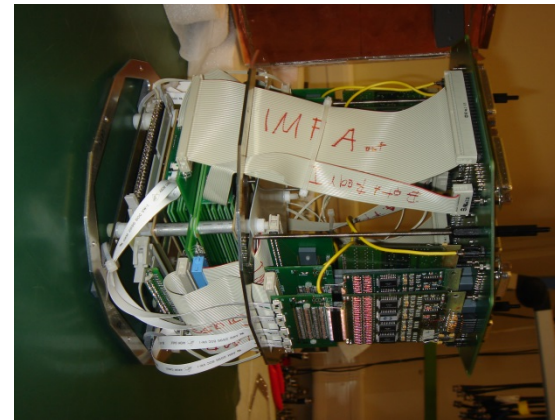
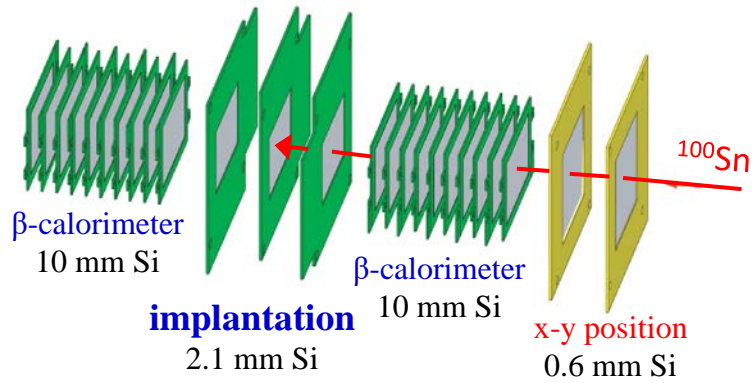


# The big surprise ...

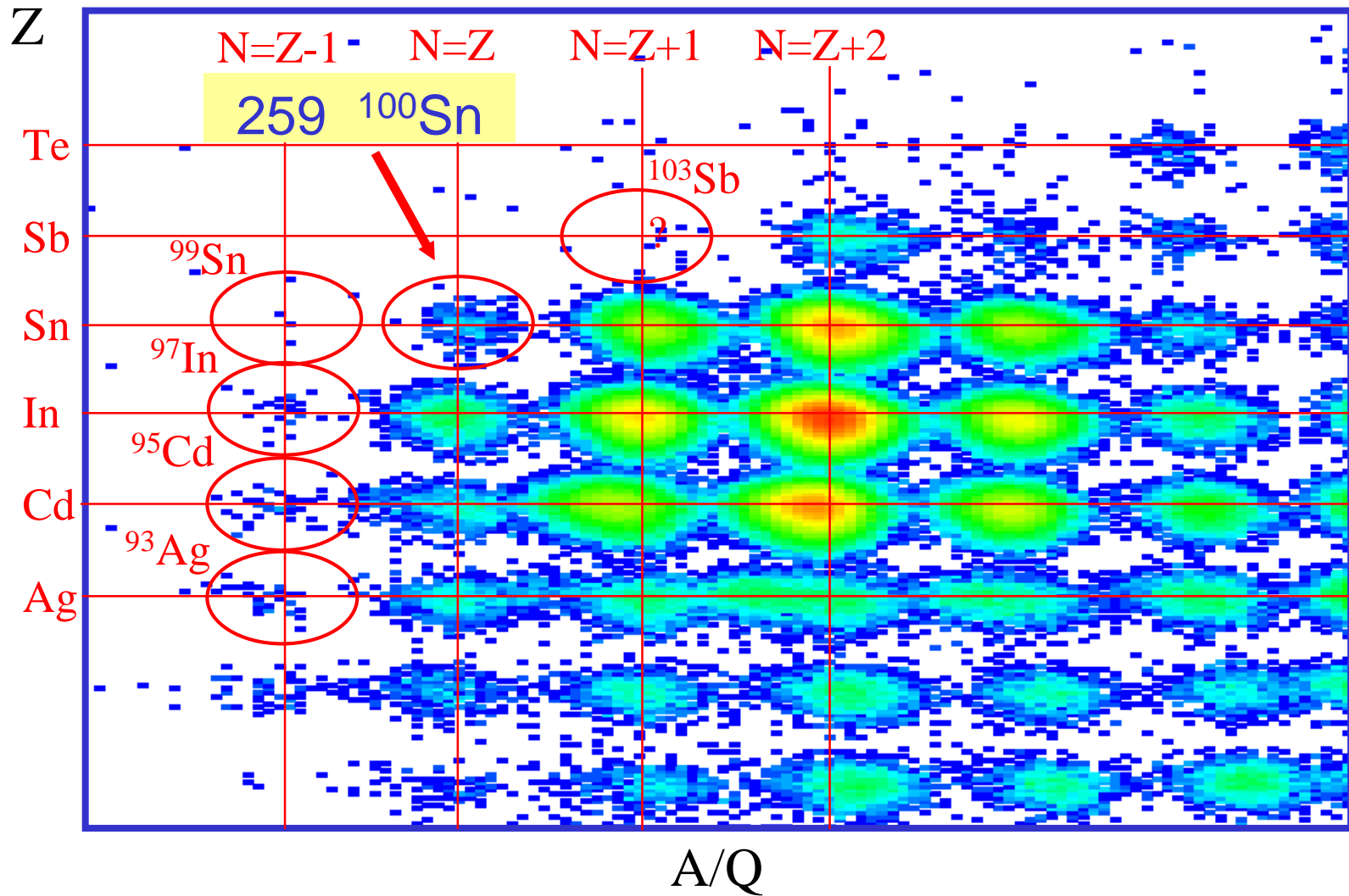


Where does the 1327 keV line come from ???

# Active target Silicon IMplantation detector and Beta Absorber



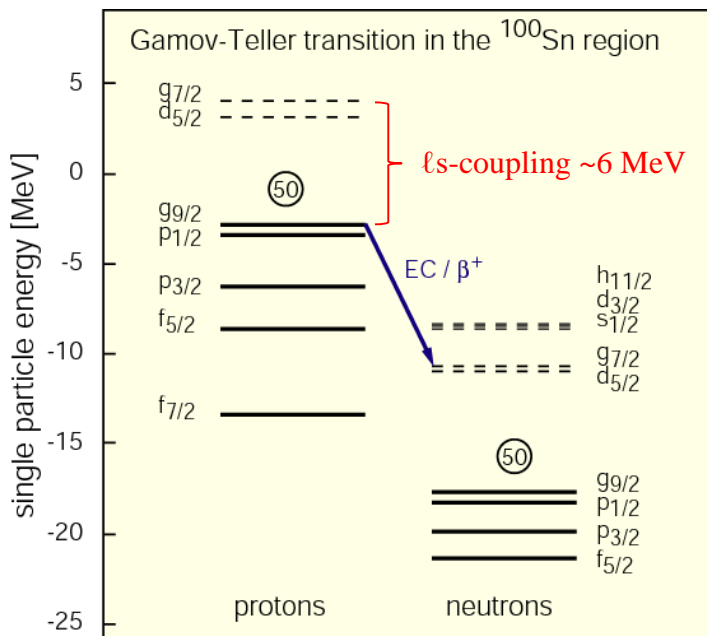
# Spectroscopy of the doubly magic nucleus $^{100}\text{Sn}$ and its decay





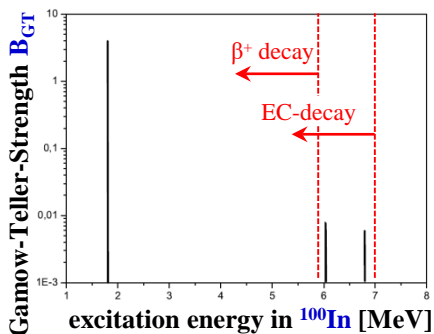
# Gamow-Teller Strength and $Q_{EC}$ value in the $\beta$ -decay of $^{100}\text{Sn}$

Single particle energies for shell model orbitals in  $^{100}\text{Sn}$



$$\beta^+: Q=M(Z+1)c^2-M(Z)c^2-2m_e c^2$$

$$EC: Q=M(Z+1)c^2-M(Z)c^2-BE(K\text{-electron})$$



❖  $^{100}\text{Sn}$  is an ideal testing ground to investigate GT-strength:

pure GT spin-flip transition:  $0^+ \Rightarrow (\pi g_{9/2}^{-1} \nu g_{7/2}) 1^+$

❖ Almost the whole strength of the GT resonance is covered by the energy window of the  $\beta^+$ -decay

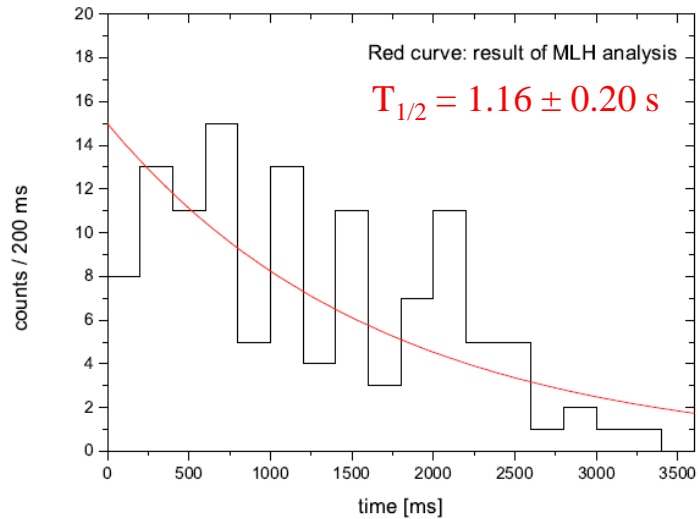
Theoretical calculation of the distribution of the GT-strength:

97% of the whole strength is concentrated in a single state, which is accessible in the  $\beta^+$ -decay

$$B_{GT}(ESM) = \frac{4\ell}{2\ell + 1} \cdot \left(1 - \frac{N_{\nu g_{7/2}}}{8}\right) \cdot N_{\pi g_{9/2}} = 17.78$$

with  $\ell=4$   $N_{\nu g_{7/2}}=0$   $N_{\pi g_{9/2}}=10$

# Gamow-Teller strength and $Q_{EC}$ value in the $\beta$ -decay of $^{100}\text{Sn}$



The **Gamow-Teller Strength**  $B_{GT}$  (only one final state populated) can be calculated from the half life  $T_{1/2}$  and the Fermi Phasespace Integral  $f(Z, E_0)$ :

$$f(Z, E_0) \cdot T_{1/2} = \frac{2\pi^3 \hbar^7}{m_e^5 c^4 G_F^2} \cdot \frac{\ln 2}{g_V^2 \cdot |M_F|^2 + g_A^2 \cdot |M_{GT}|^2}$$

$$G_F/(\hbar c)^3 = 1.16637(1) \cdot 10^{-5} \text{ GeV}^{-2}, \quad g_A/g_V = 1.2695 \pm 0.0029$$

$$f(Z, E_0) \cdot T_{1/2} = \frac{6142.8s}{B_F + (g_A/g_V)^2 \cdot B_{GT}}$$

In the case of a pure Gamow-Teller decay the transition strength can be calculated in the following way:

$$B_{GT} = \frac{3811.5s}{f(Z, E_0) \cdot T_{1/2}} = 9.1^{+4.8}_{-2.3}$$

Fermi-integral with LOGFT program NNDC

