

Gamma-ray spectroscopy IV

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Lectures presented at the
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Outline

First lecture

- Properties of γ -ray transitions
- Fusion-evaporation reactions
- Germanium detector arrays
- Coincidence technique
- Nuclear deformations
- Rotation of deformed nuclei
- Pair alignment
- Superdeformed nuclei
- Hyperdeformed nuclei
- Triaxiality and wobbling

Second lecture

- Angular distribution
- Linear polarization
- Jacobi shape transition
- Charged-particle detectors
- Neutron detectors
- Prompt proton decay
- Recoil-decay tagging
- Rotation and deformation alignment

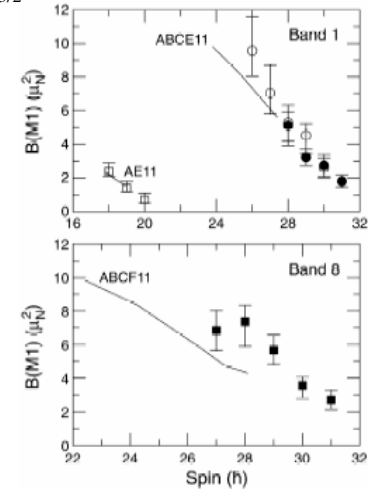
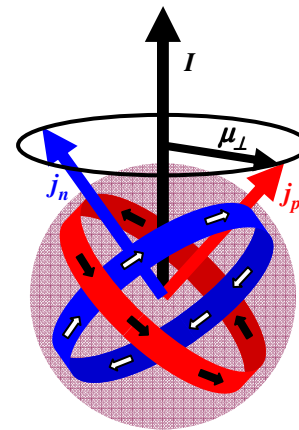
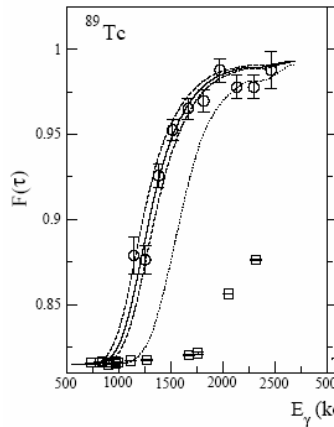
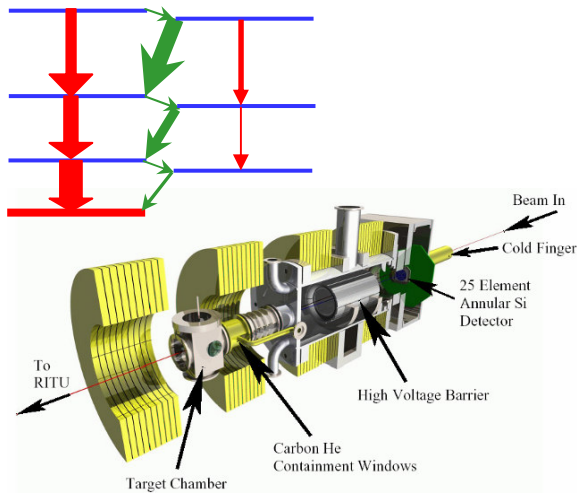
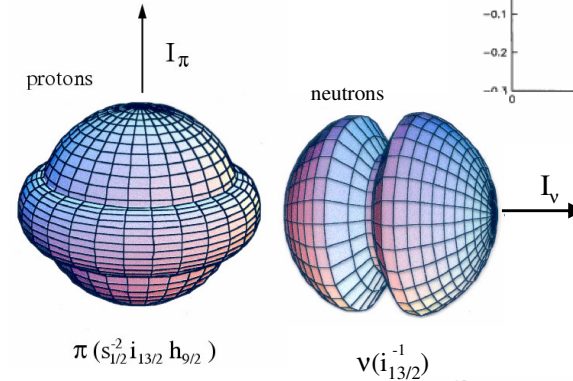
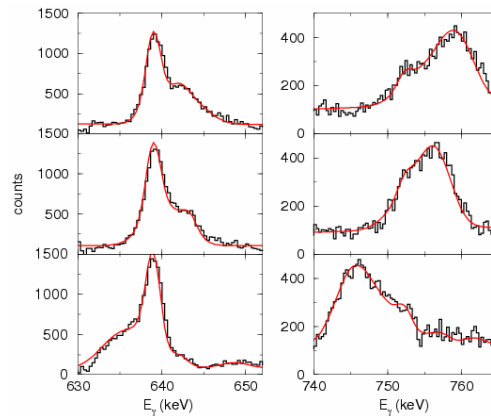
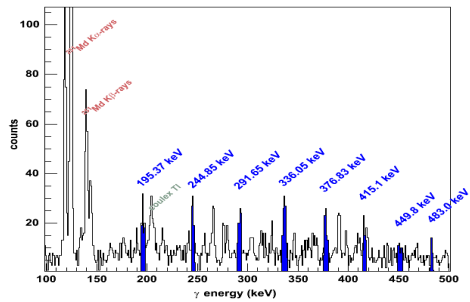
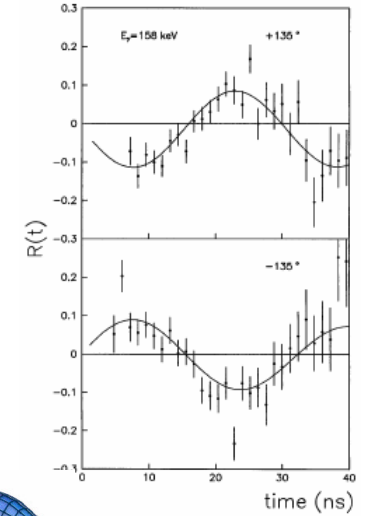
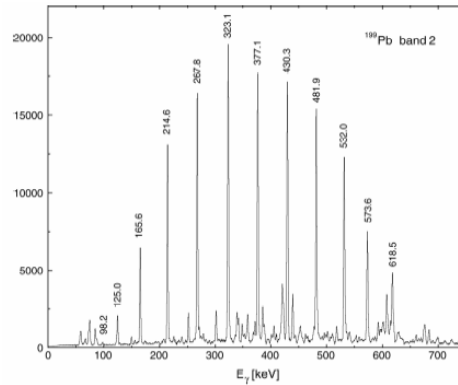
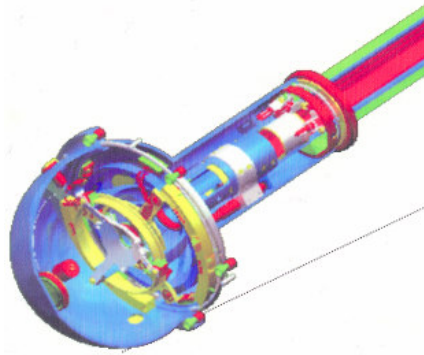
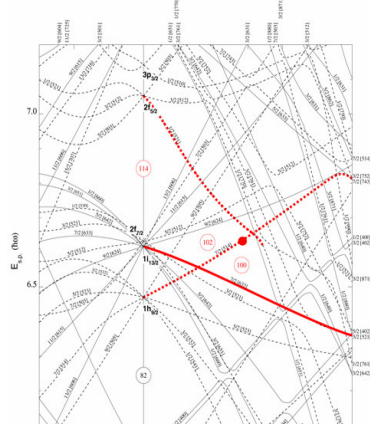
Third lecture

- Spectroscopy of transfermium nuclei
- Conversion-electron spectroscopy
- Quadrupole moments and transition rates
- Recoil-distance method
- Doppler shift attenuation method
- Fractional Doppler shift method
- Magnetic moments
- Perturbed angular distribution
- Magnetic Rotation
- Shears Effect

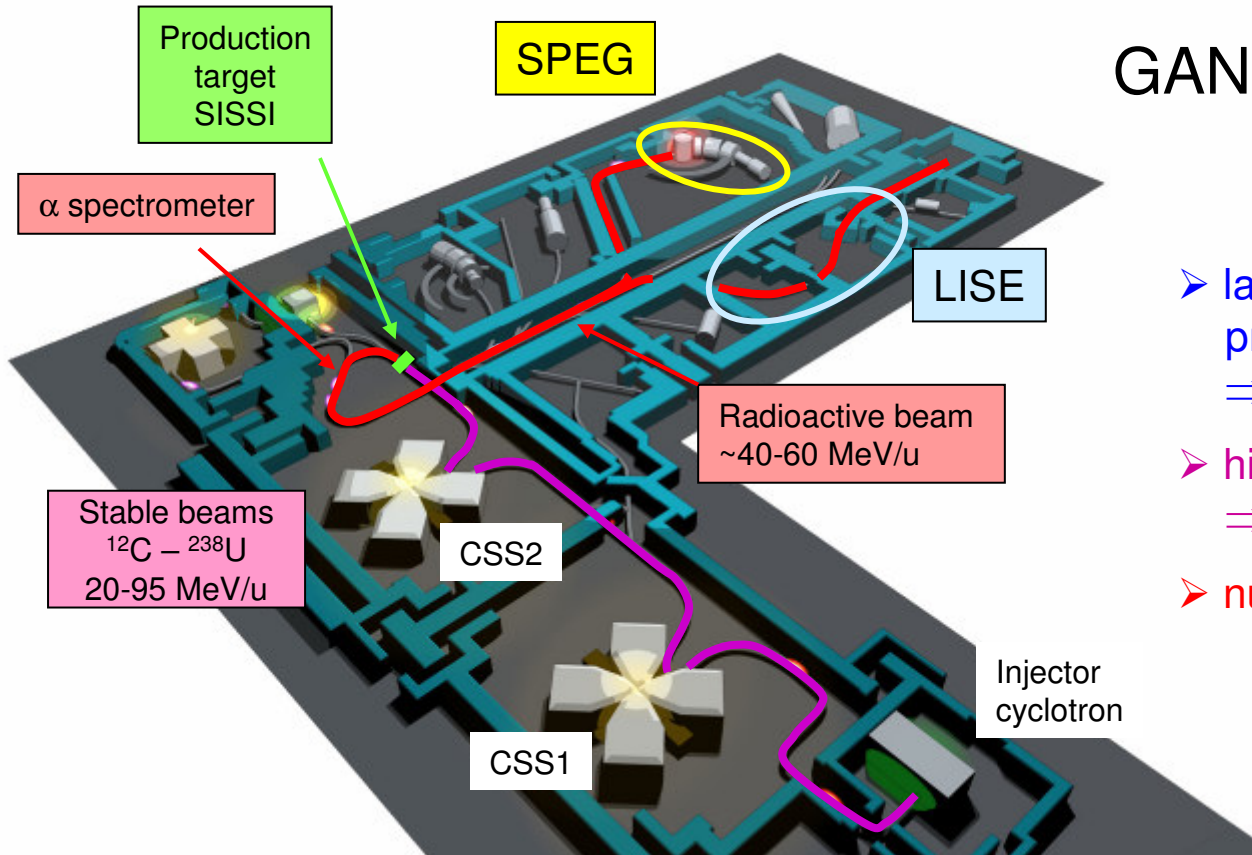
Fourth lecture

- Fast fragmentation beams
- Isomer spectroscopy after fragmentation
- E0 transitions
- Shape coexistence
- Two-level mixing
- Coulomb excitation
- Reorientation effect
- ISOL technique
- Low-energy Coulomb excitation of ^{74}Kr
- Relativistic Coulomb excitation of ^{58}Cr
- Gamma-ray tracking
- AGATA

Summary (III)



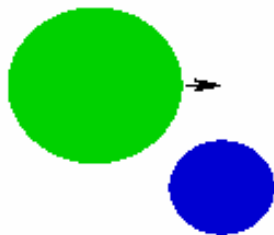
Fast fragmentation beams: production



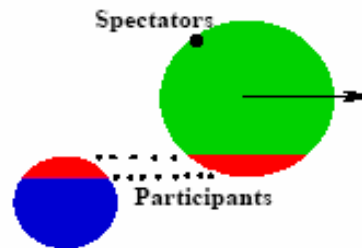
GANIL

- large number of isotopes produced
⇒ need for identification
- high velocities
⇒ strong Doppler effects
- nuclei far from stability

Fragmentation



abrasion

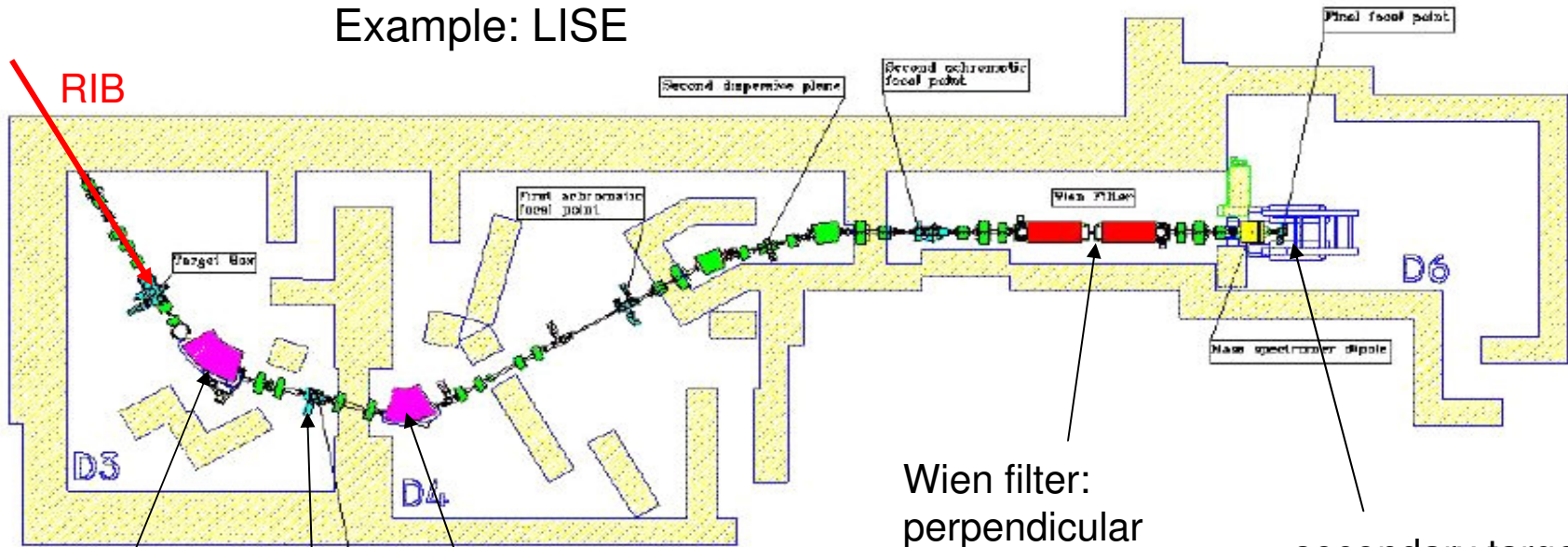


ablation



Fast fragmentation beams: separation

Example: LISE



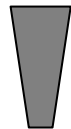
1. Dipole magnet

$$B\rho_1 = \frac{mv}{q}$$

2. Dipole magnet

$$B\rho_2 = \frac{mv}{q}$$

Degrader wedge
different energy loss
for different nuclei



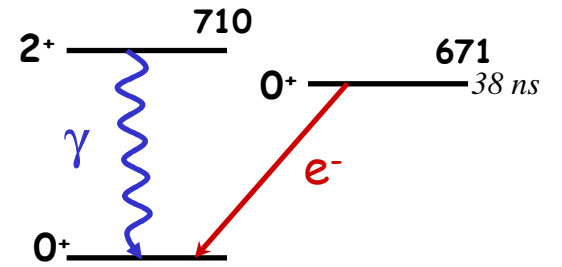
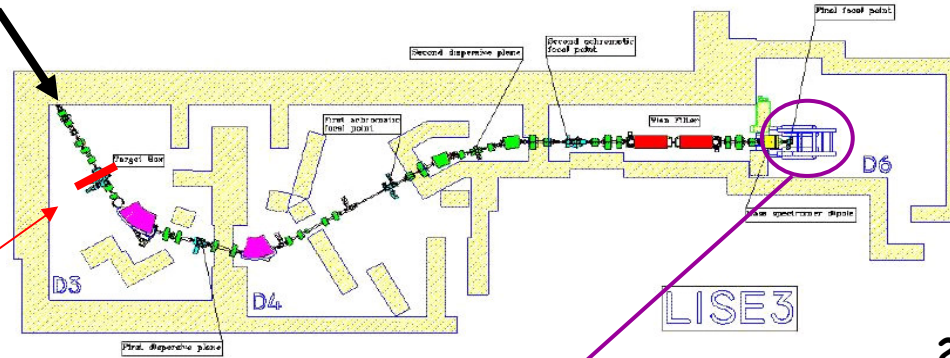
Wien filter:
perpendicular
E and B fields
 $qE = qvB$

secondary target
detectors

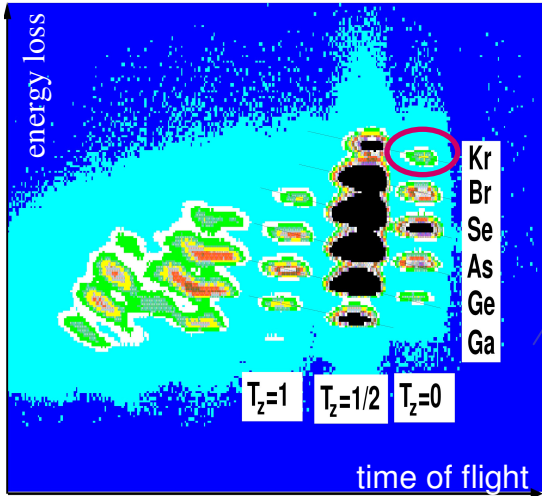
Isomer spectroscopy of ^{72}Kr at LISE

^{78}Kr
70 MeV/u
 $\sim 10^{12}$ pps

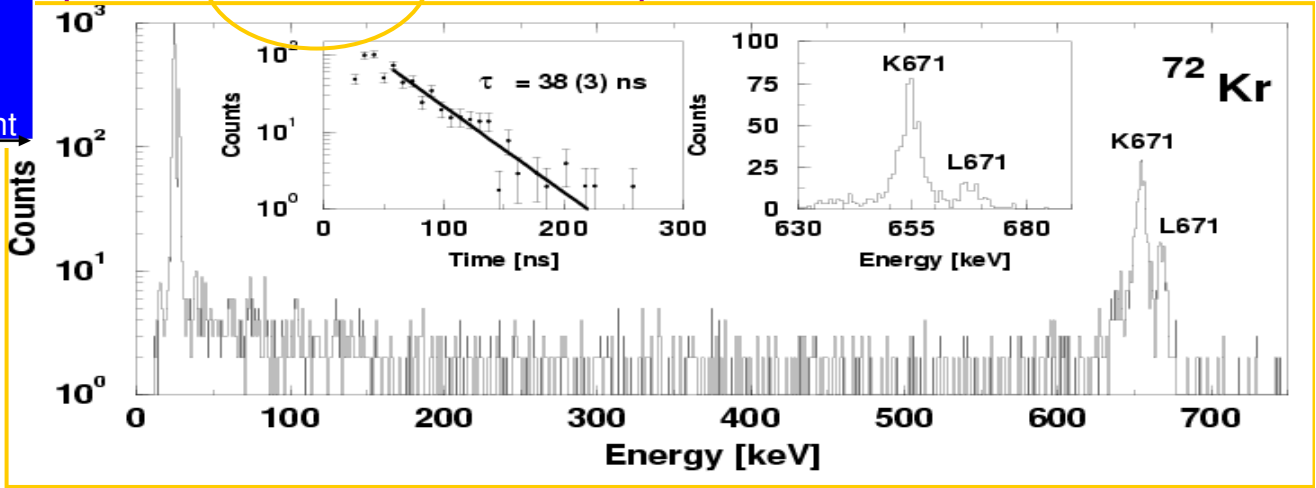
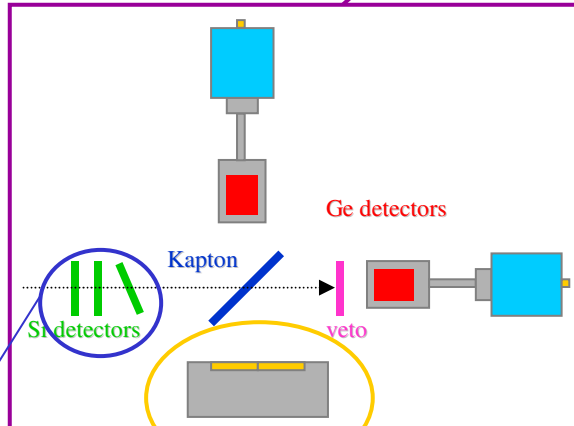
^9Be target



new shape isomer in ^{72}Kr



^{72}Kr : ~ 2 ions/sec



E. Bouchez et al.,
PRL 90, 082502 (2003)

E0 transitions

- electric monopole transitions can occur between states of the same spin and parity in particular $0^+ \rightarrow 0^+$
- E0 transitions are non-radiative: only internal conversion or internal pair creation ($E > 1.022$ MeV) possible
- E0 transitions related to changes in the rms radius of the charge distribution (breathing mode)
- monopole matrix element $\rho = \langle 0_f^+ | \sum_p \frac{r_p^2}{R^2} | 0_i^+ \rangle$ r_p radius vector of the protons
 $R = 1.25 A^{1/3}$ nuclear radius
- example: two 0^+ states of different shapes with mixing

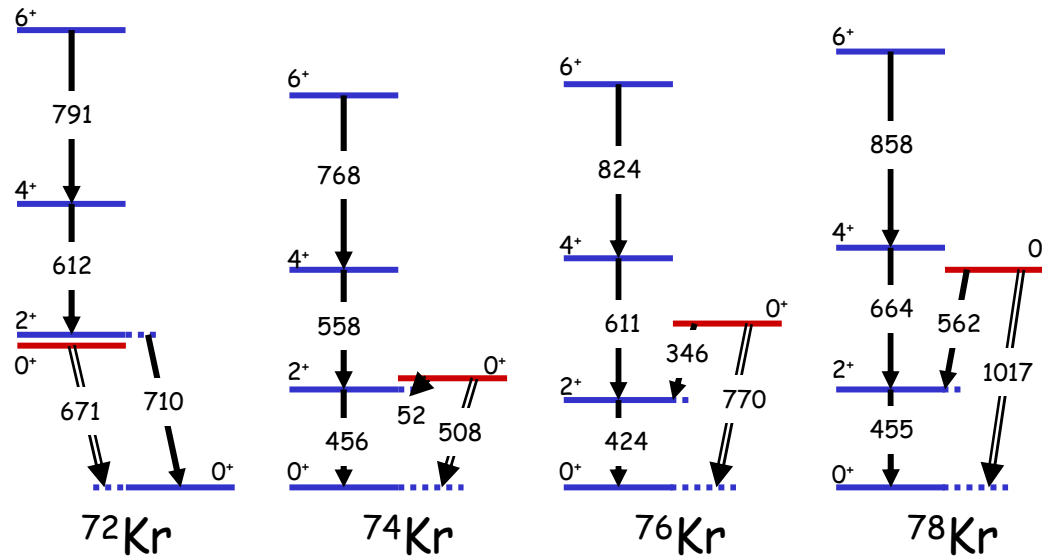
$$|0_i^+\rangle = a|\text{sph}\rangle + b|\text{def}\rangle$$

$$|0_f^+\rangle = -b|\text{sph}\rangle + a|\text{def}\rangle$$

$$\text{E0 transition strength } \rho^2 \propto a^2 b^2 \beta^4 = a^2 (1 - a^2) \beta^4$$

E0 transitions proceed only in the presence of a sizeable deformation and mixing of components with different $\langle r^2 \rangle$

Systematics of the light krypton isotopes



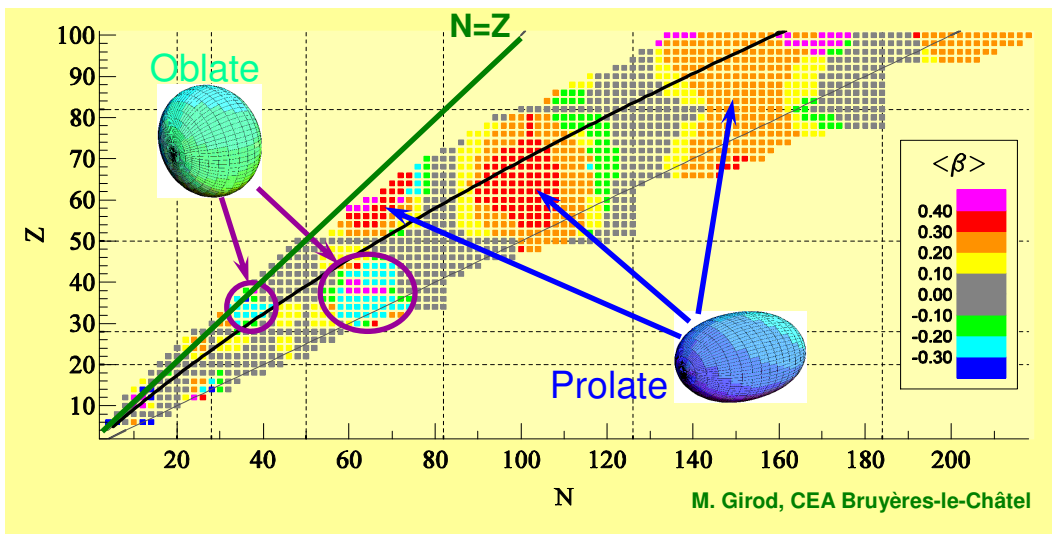
- low-lying 0^+ states
- decay via E0 transitions
- different shapes involved ?

➤ rotational bands at high spin known to be prolate

➤ oblate states predicted at low spin

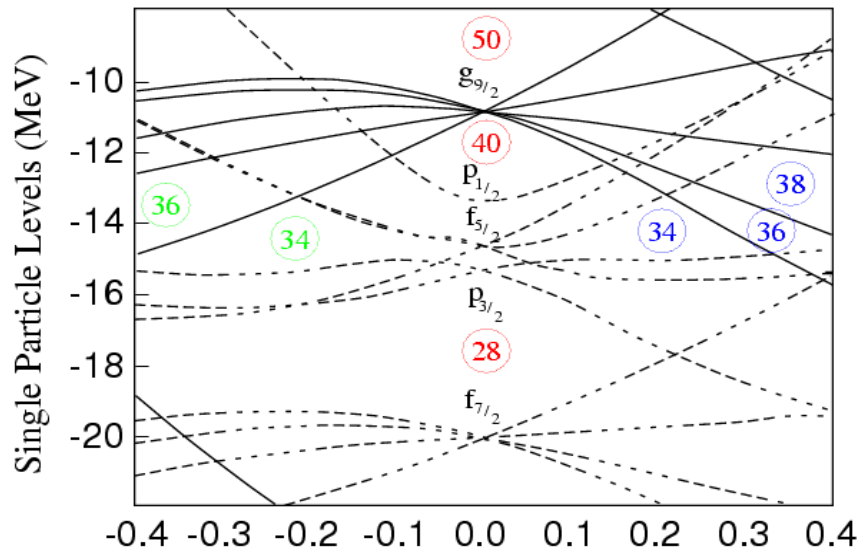
➤ shape coexistence ?

➤ mixing ?

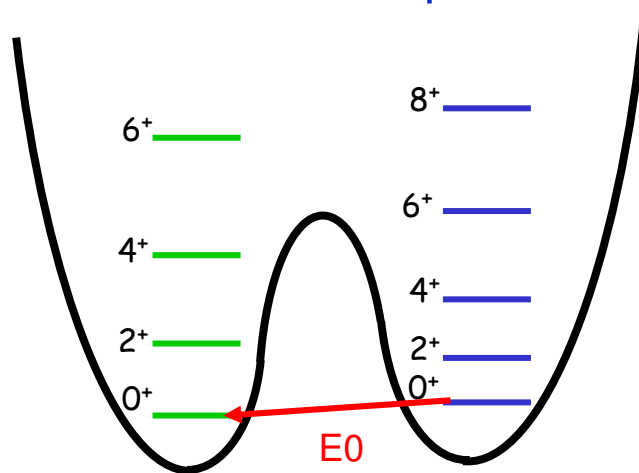


Hartree-Fock-Bogoliubov calculation of ground-state shapes

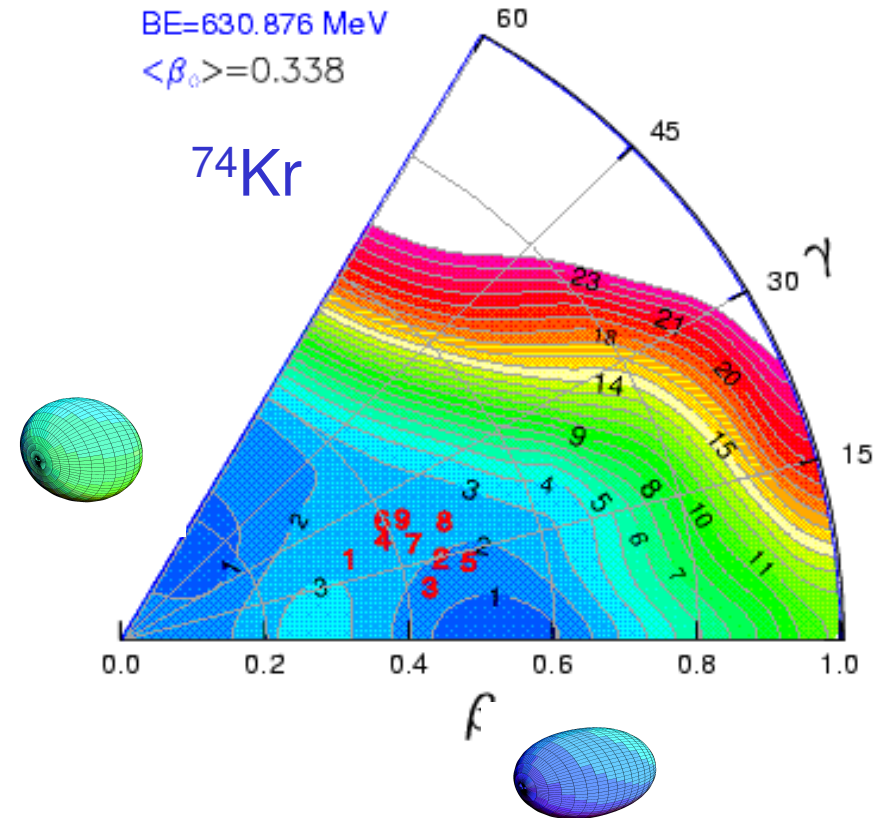
Shape coexistence



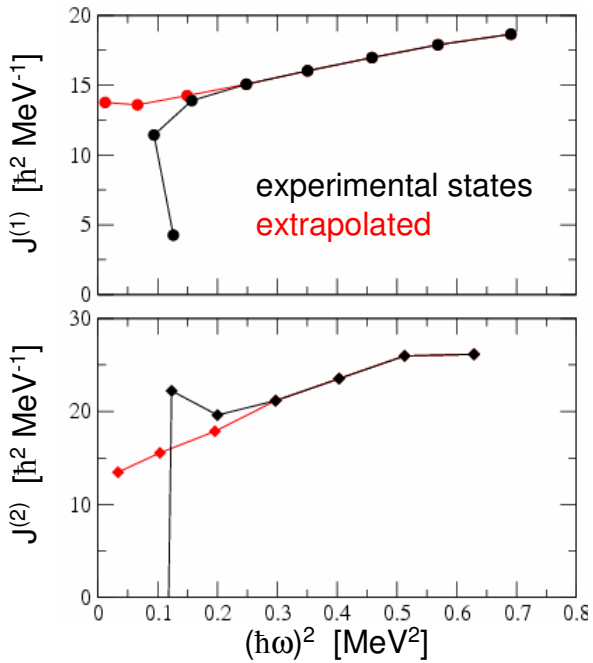
oblate β prolate



competition of shapes expected in



Two-level mixing calculation

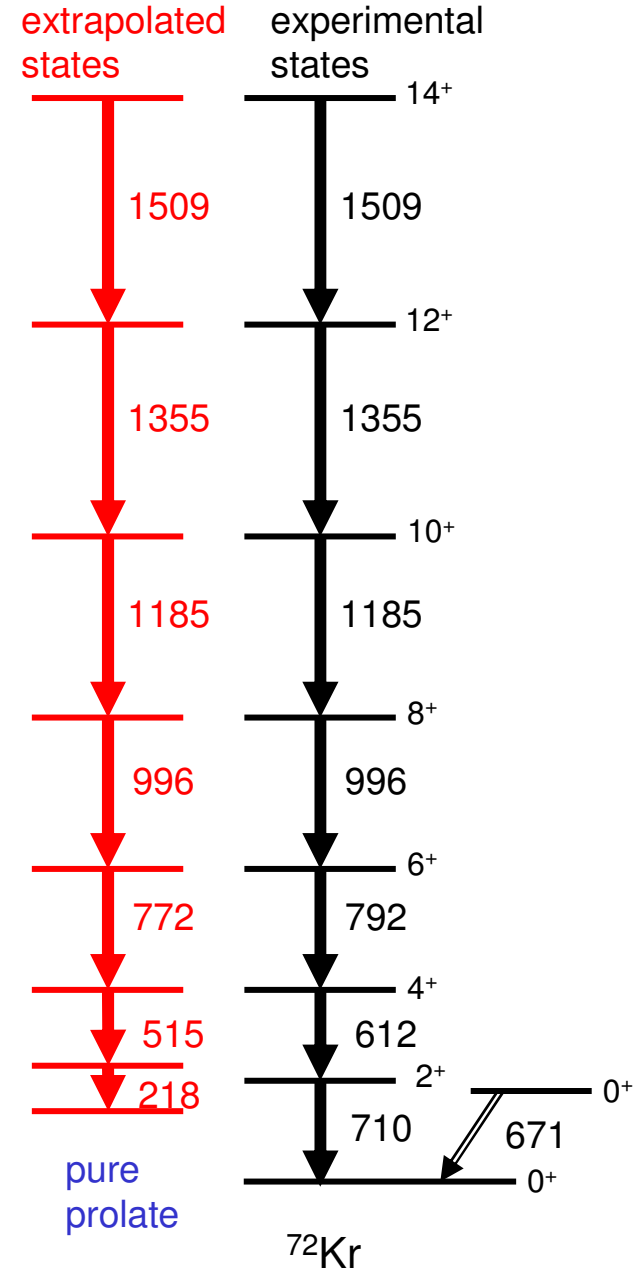
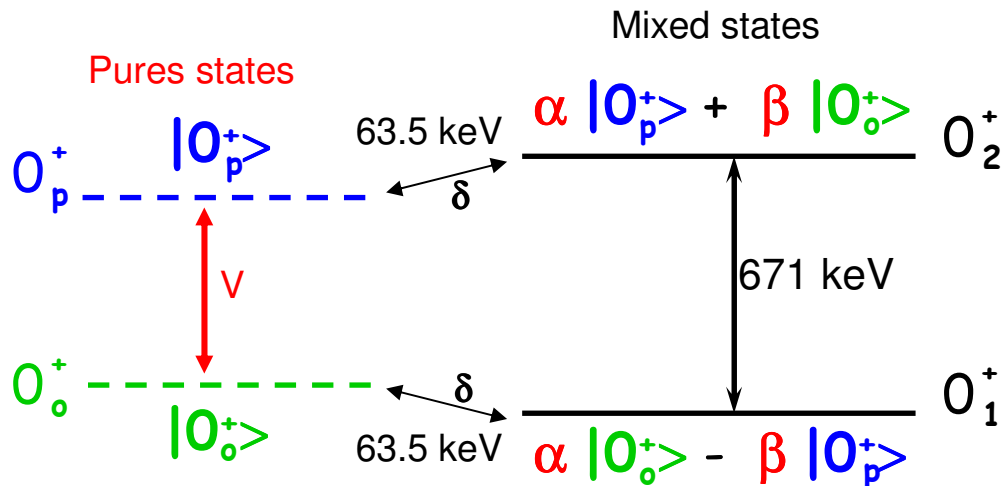


Regular rotational cascade at high spin:

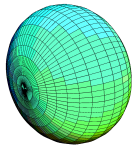
$$E(I) = \frac{\hbar^2}{2\mathcal{J}} I(I+1)$$

Rotational band is distorted at low spin.
 ⇒ influence of mixing

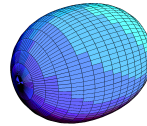
- Interaction V
- mixing amplitudes α, β



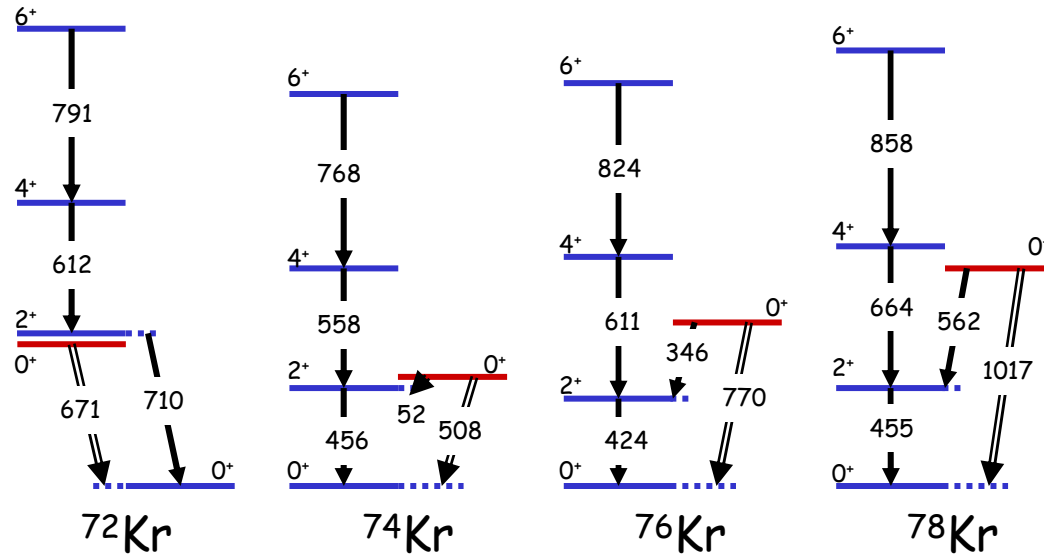
Systematics of the light krypton isotopes



oblate

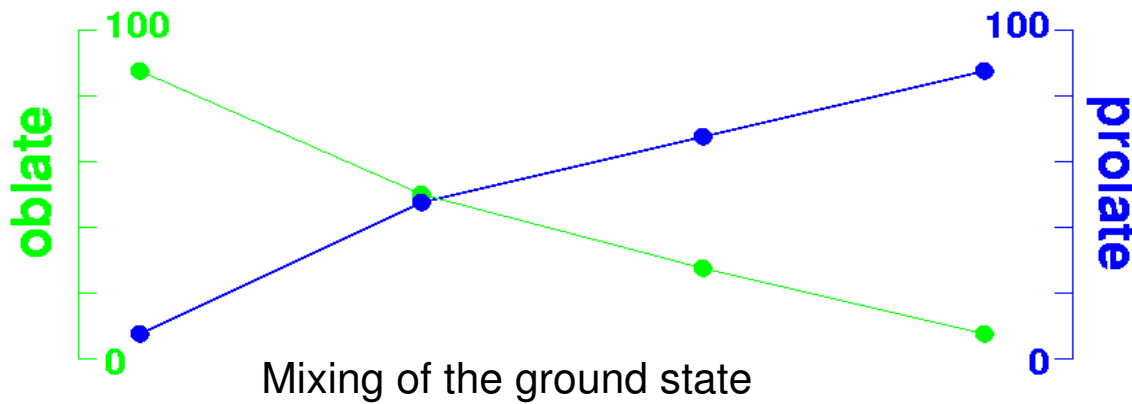


prolate



- energy of excited 0^+ states
- E0 transitions strengths
- mixing amplitudes

Inversion of the ground-state shape for ^{72}Kr



can we prove this scenario directly ?
⇒ Coulomb excitation

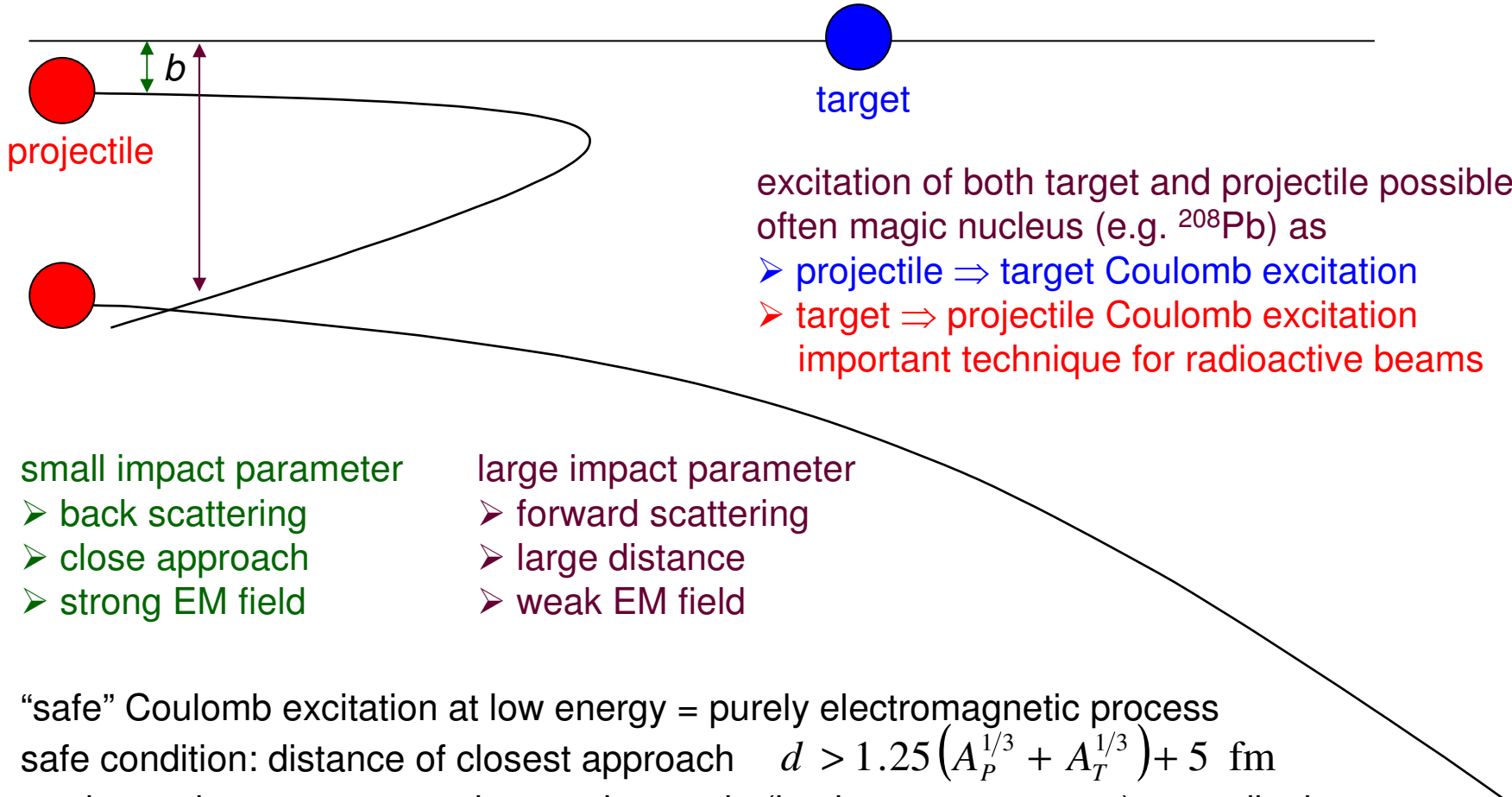
E. Bouchez et al., PRL 90, 082502 (2003)

Coulomb excitation

Nuclear excitation by electromagnetic field acting between nuclei.

Trajectories are hyperbolas $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$
 (Rutherford scattering)

$a \propto$ beam energy
 $b =$ impact parameter



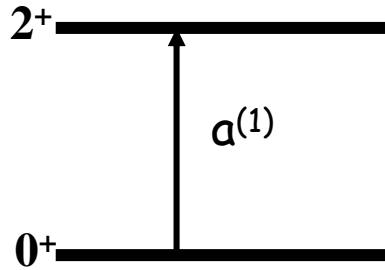
- small impact parameter
- back scattering
 - close approach
 - strong EM field

- large impact parameter
- forward scattering
 - large distance
 - weak EM field

“safe” Coulomb excitation at low energy = purely electromagnetic process
 safe condition: distance of closest approach $d > 1.25(A_P^{1/3} + A_T^{1/3}) + 5$ fm
 \Rightarrow choose beam energy and scattering angle (i.e. impact parameter) accordingly

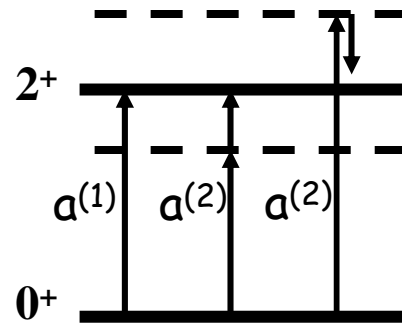
Reorientation effect

1st order:



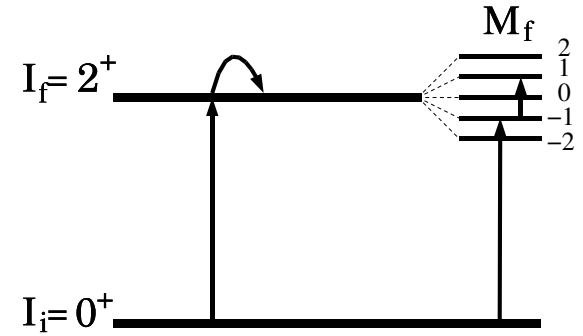
$$P_{i \rightarrow f} = P^{(1)} \propto B(E2) Z_{\text{target}} \propto \beta^2$$

2nd order:



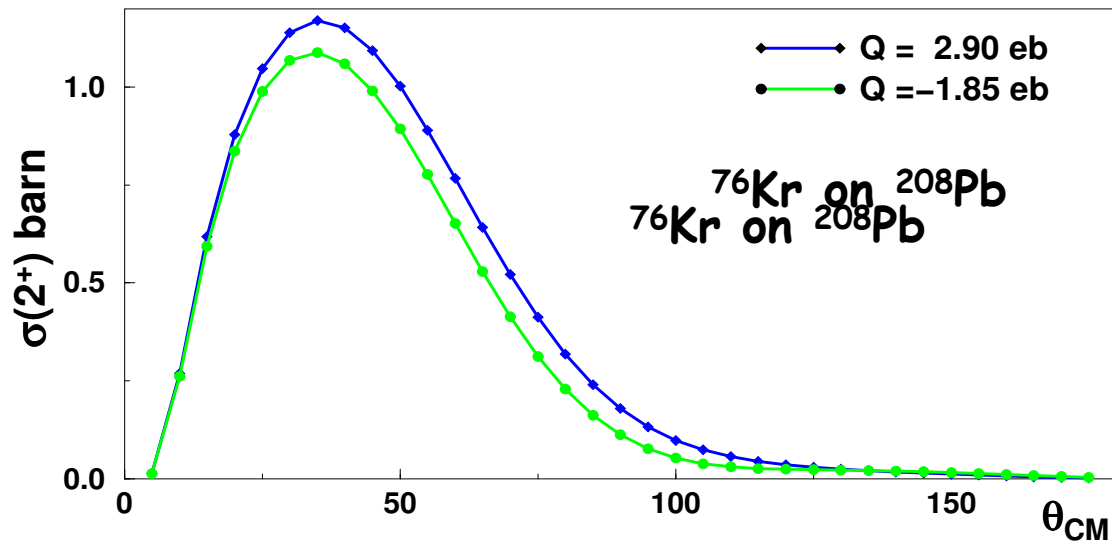
$$P_{i \rightarrow f} = P^{(1)} + P^{(2)} + P^{(1,2)}$$

reorientation effect



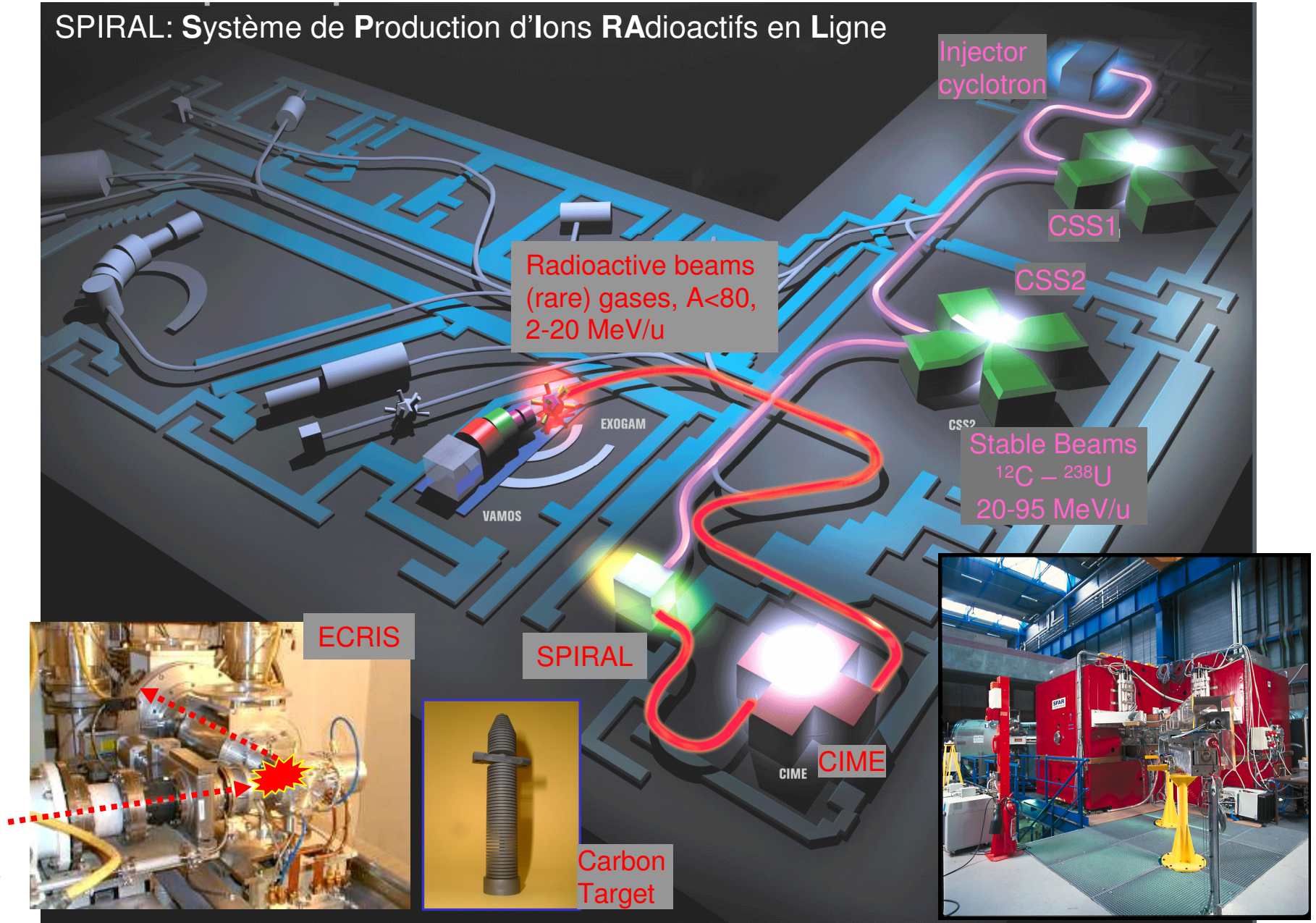
$$P_{i \rightarrow f} = P^{(1)} + P^{(2)} + P^{(1,2)} = f(Q_0)$$

Cross section

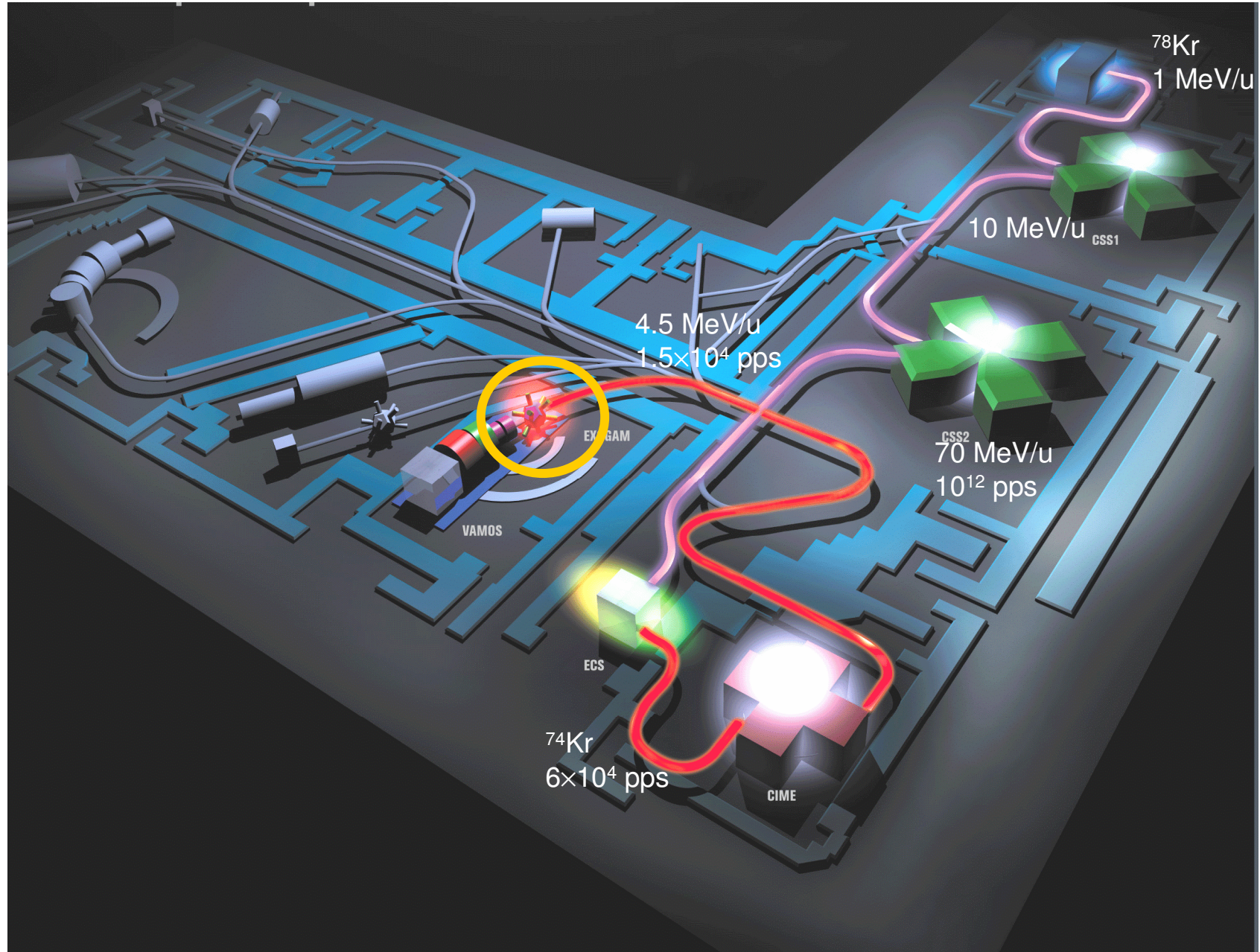


Radioactive ion beams: Isotope separation on-line (ISOL)

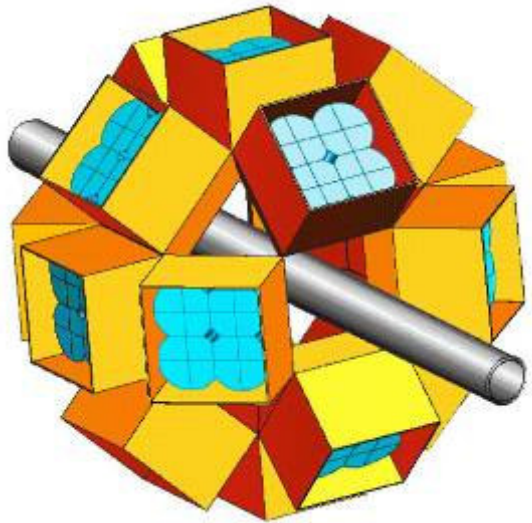
SPIRAL: Système de Production d'Ions RAdioactifs en Ligne



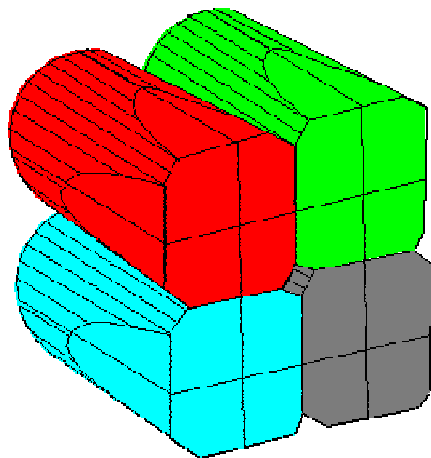
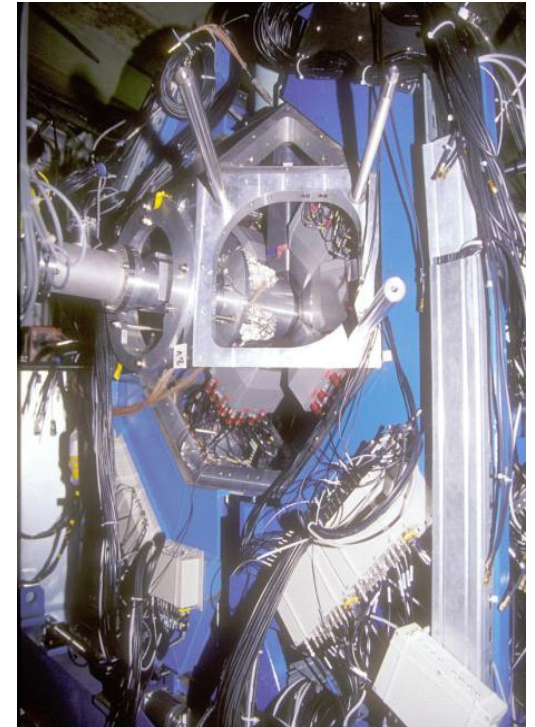
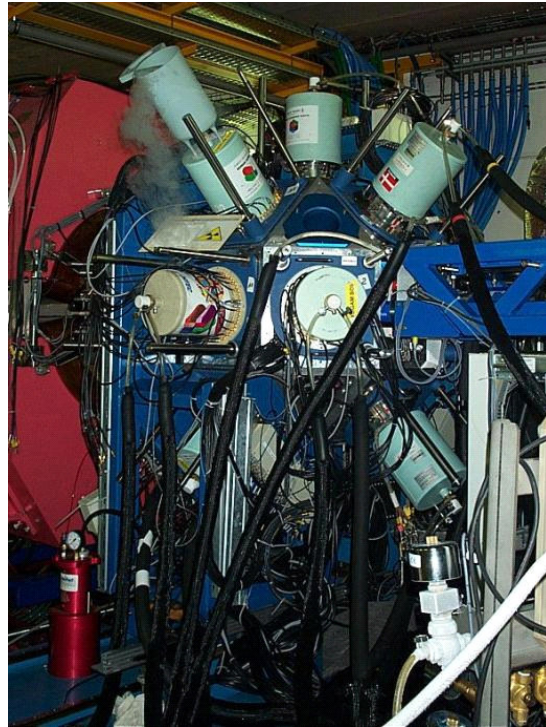
Coulomb excitation of $^{74,76}\text{Kr}$



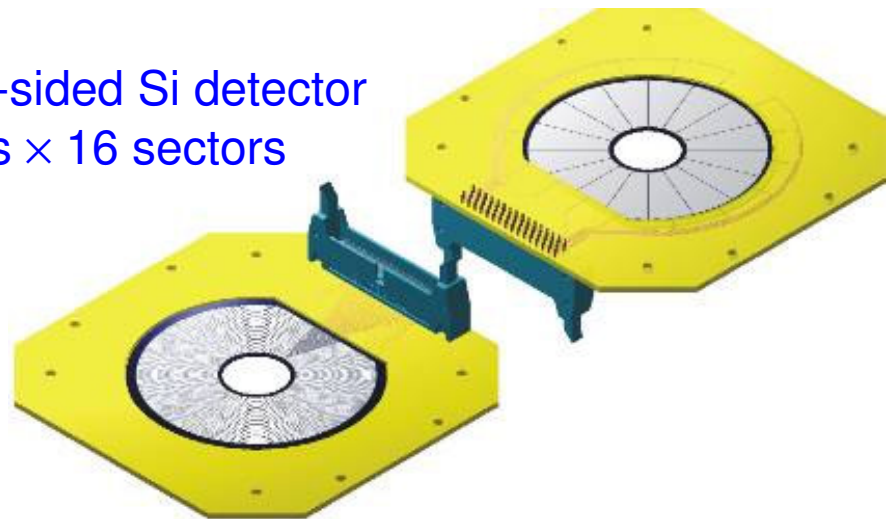
EXOGRAM



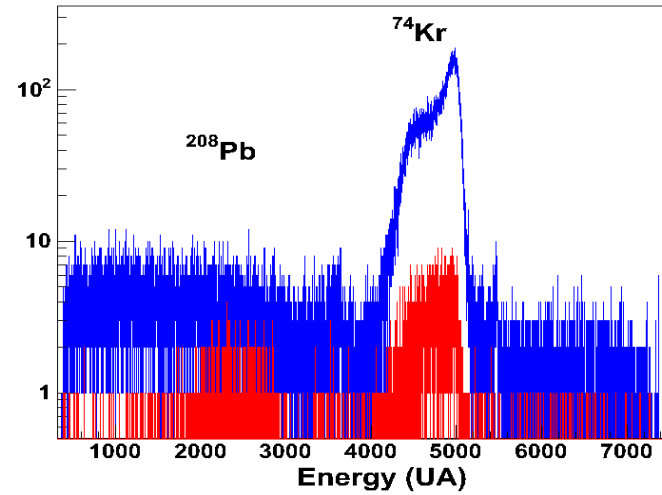
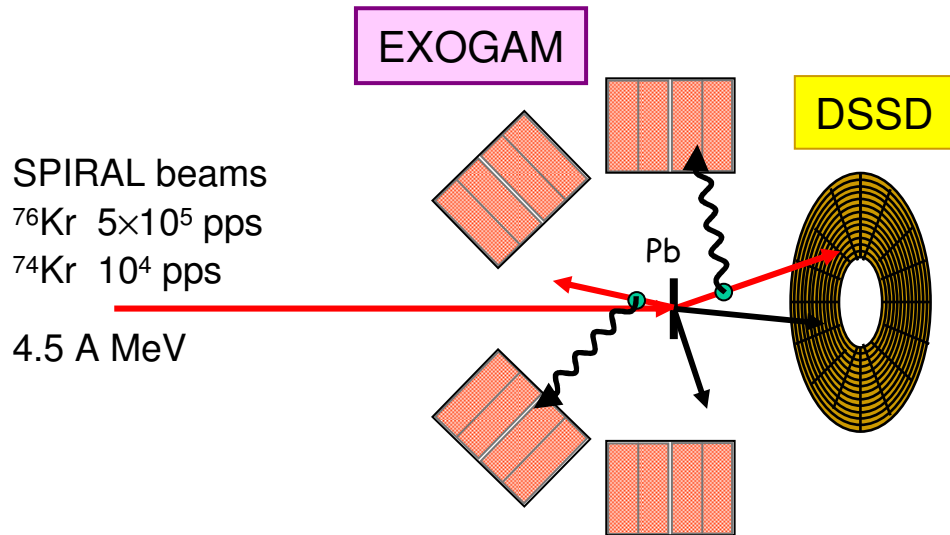
16 large Ge Clover detectors
4 × 4 segmented
photopeak efficiency $\epsilon = 20\%$



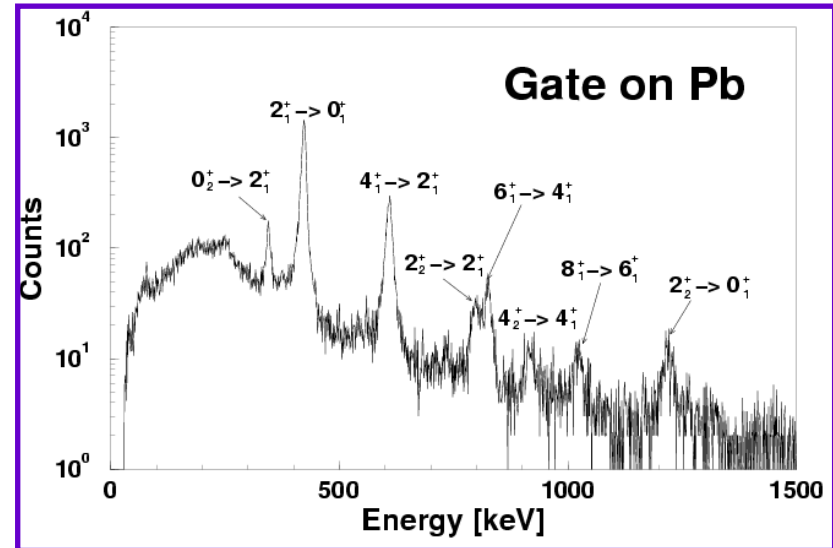
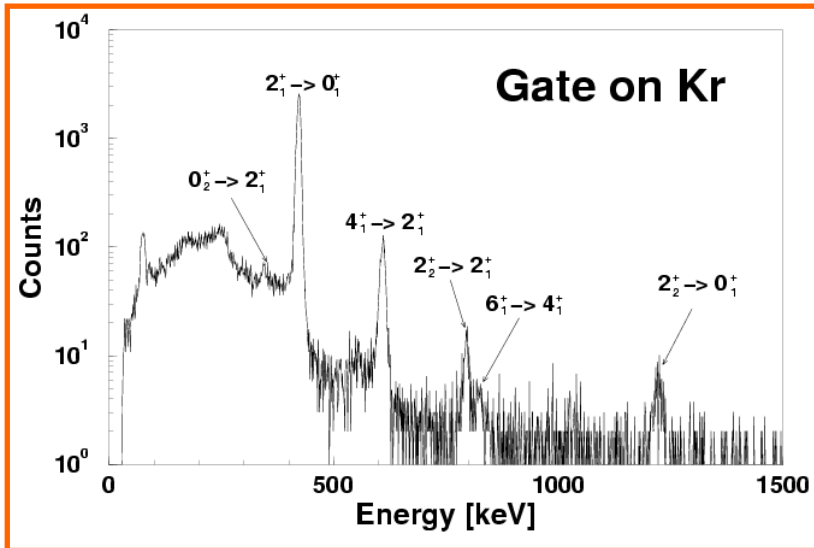
Double-sided Si detector
48 rings × 16 sectors



Coulomb excitation of ^{74}Kr and ^{76}Kr



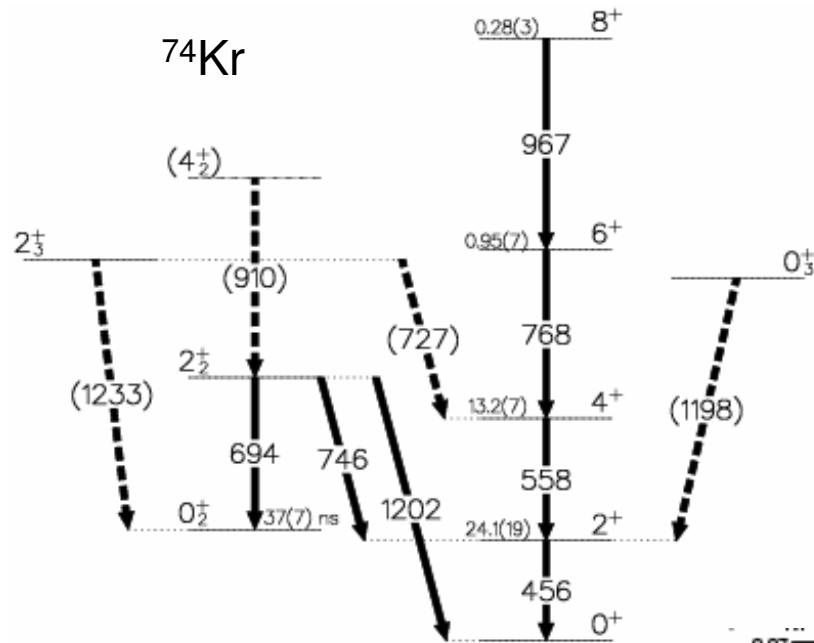
Differential Coulomb excitation cross section for $35^\circ < \theta_{\text{cm}} < 130^\circ$



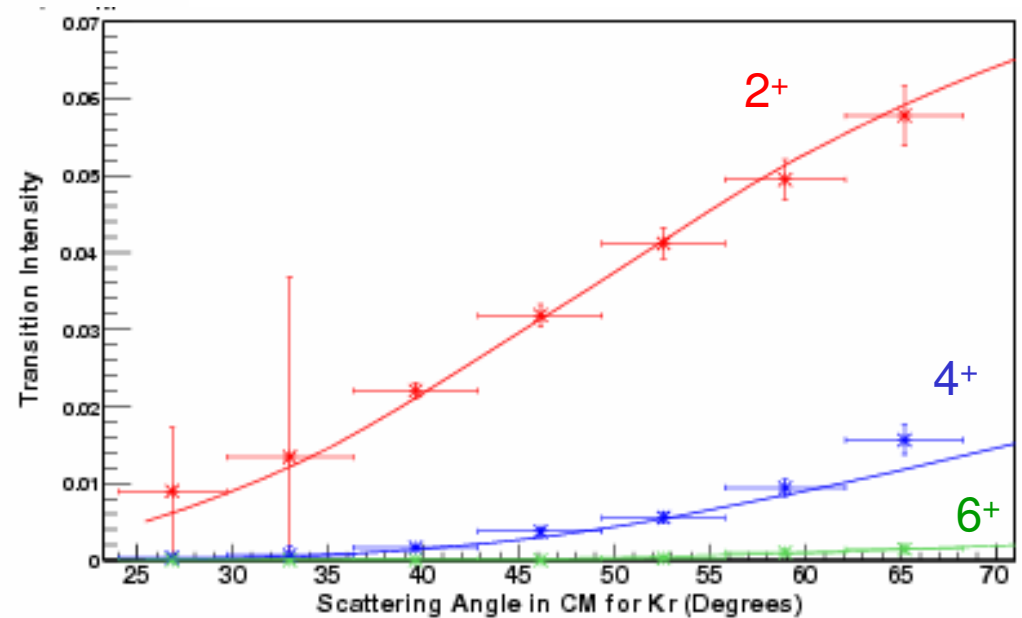
A. G3rgen et al., Acta Phys. Pol. B 36, 1281 (2005)

Coulomb excitation analysis : GOSIA*

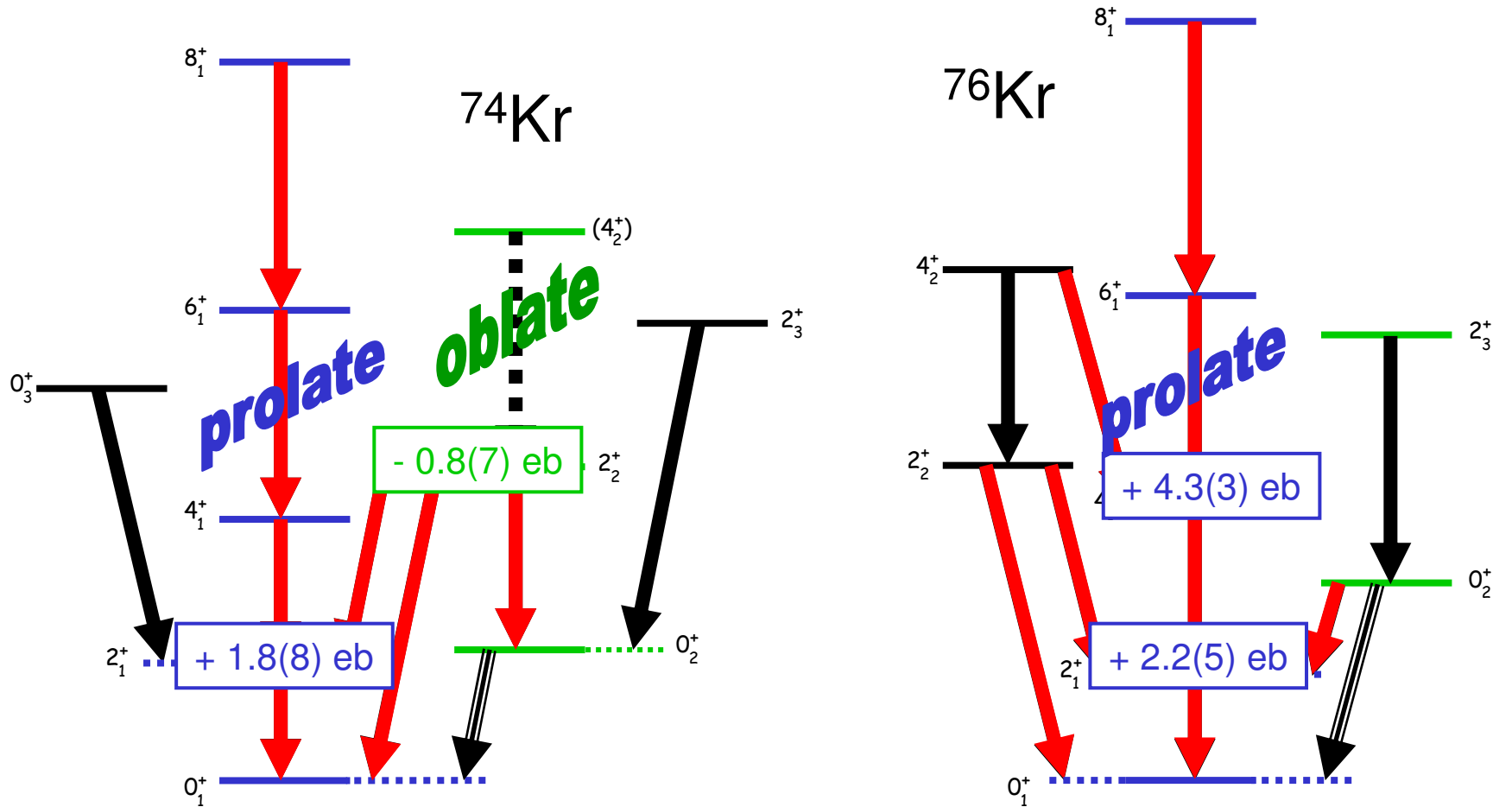
*D. Cline, C.Y. Wu, T. Czosnyka; Univ. of Rochester



- γ yields as function of scattering angle: differential cross section
- least squares fit of ~ 30 matrix elements (transitional and diagonal)
- experimental spectroscopic data
 - lifetimes
 - branching ratios
 - mixing ratios



Quadrupole moments in ^{74}Kr and ^{76}Kr



A. G3rgen et al.,
Acta Phys. Pol. B 36, 1281 (2005)

➤ transitional matrix elements $\rightarrow B(E2)$

➤ diagonal matrix elements \rightarrow static quadrupole moments

Low-energy vs. relativistic Coulomb excitation

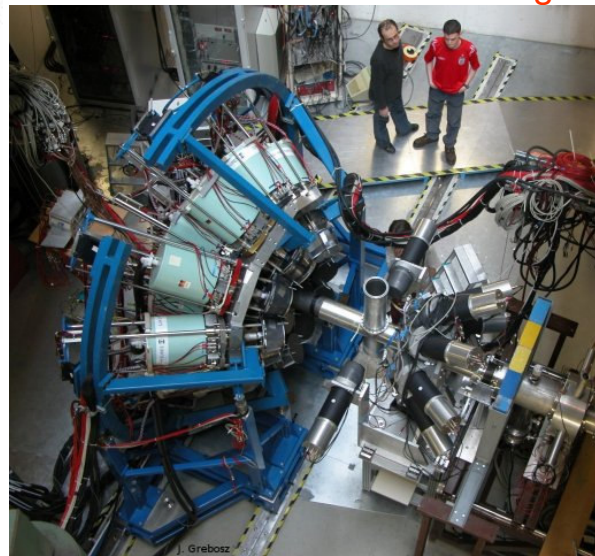
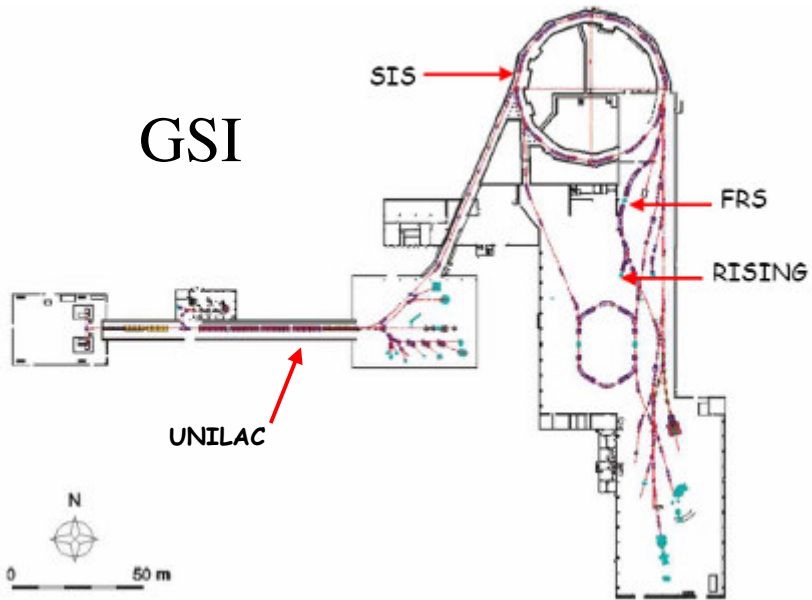
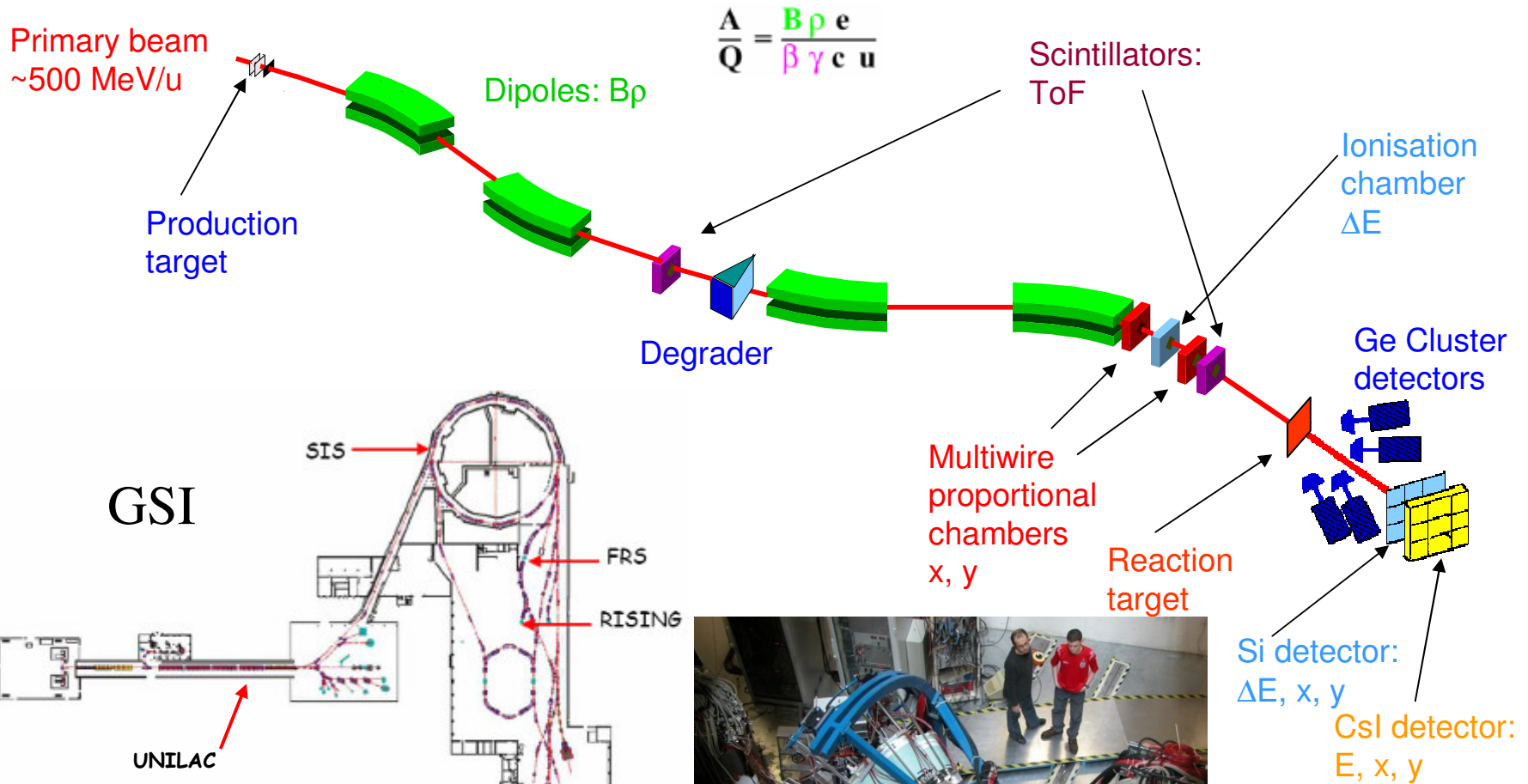
low-energy Coulomb excitation

- energy well below the Coulomb barrier: $< 5\text{MeV/u}$
- purely electromagnetic process
- multiple-step excitation
- can populate high-spin states up to $\sim 30 \hbar$ in actinides
- sensitive to static quadrupole moments (reorientation effect)
- limited to stable and moderately exotic nuclei

relativistic Coulomb excitation

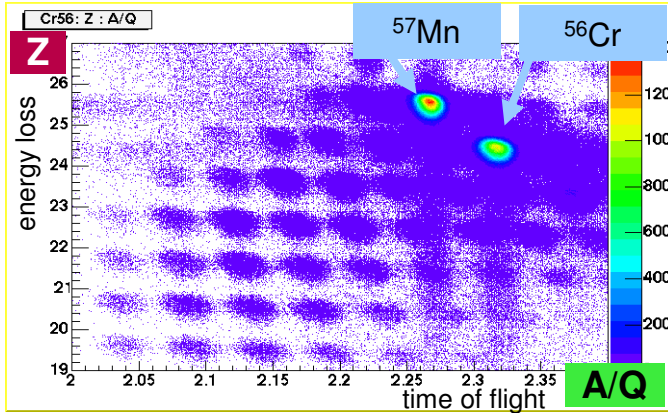
- energy well above the Coulomb barrier: $\sim 50 - 500 \text{ MeV/u}$
- nuclear contribution
- single-step excitation
- populates 2^+ state only
- sensitive to transitional matrix elements (i.e. $B(E2)$ values)
- tool to study very exotic nuclei

RISING at GSI

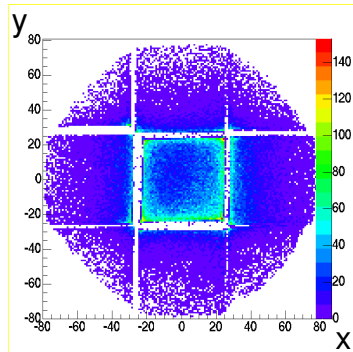
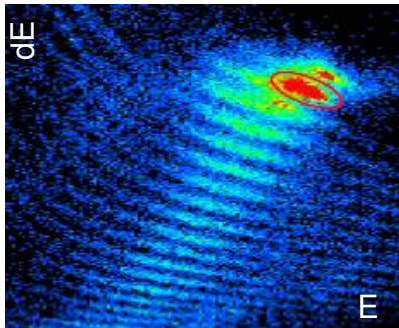


Relativistic Coulomb excitation of $^{54,56,58}\text{Cr}$

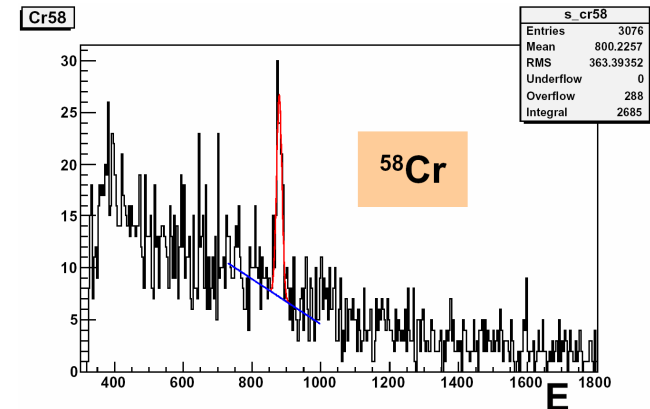
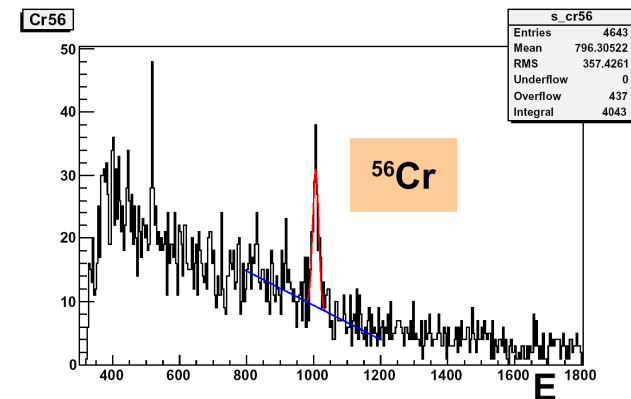
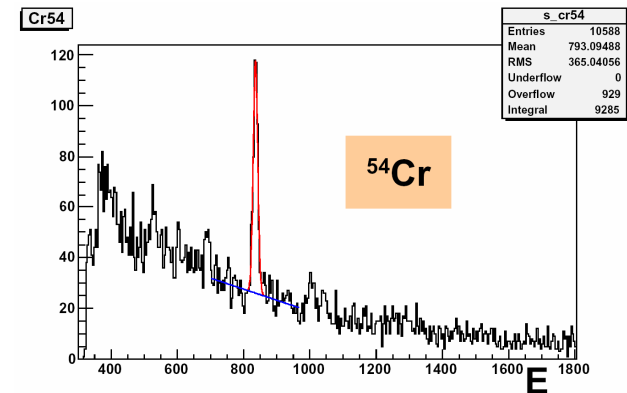
Identification before the secondary target



after secondary target

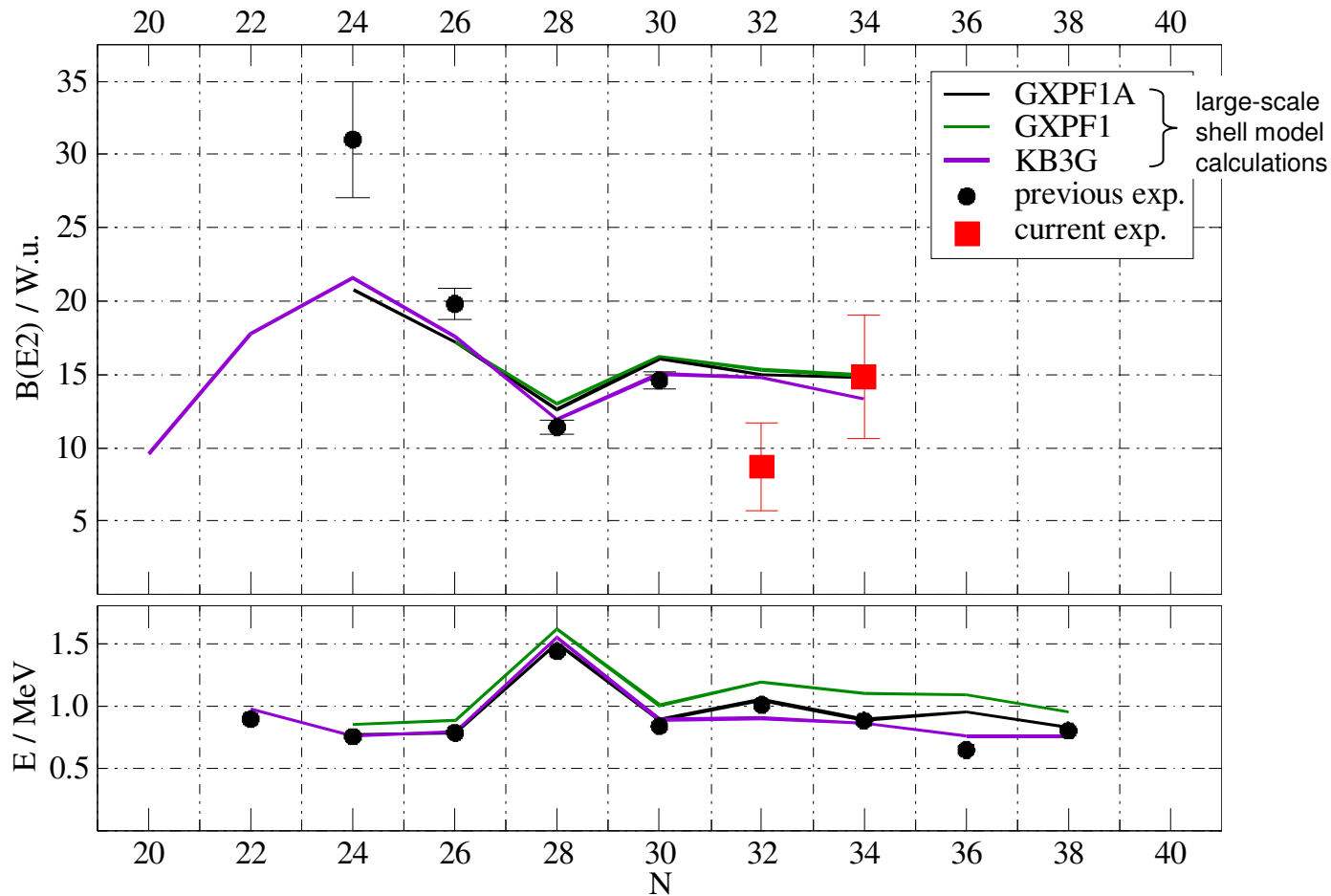


- identification of nuclide before and after the secondary target to select Coulomb excitation events
- tracking of incoming and outgoing particles to determine scattering angle and perform Doppler correction ($v/c=0.43$)



A. Bürger et al., Phys. Lett B 622, 29 (2005)

Systematics of the Cr isotopes



- significant lower collectivity for ^{56}Cr
- sub-shell closure at $N=32$
- evolution of shell structure for exotic nuclei
- new magic numbers for neutron-rich nuclei

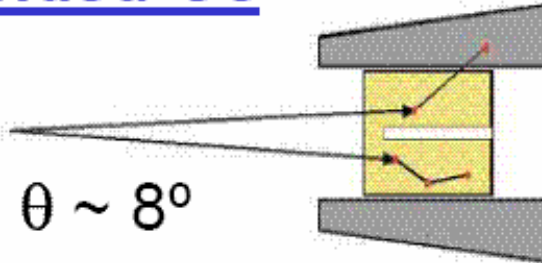
Gamma-ray tracking

Compton Shielded Ge

$$\epsilon_{ph} \sim 10\%$$

$$N_{det} \sim 100$$

$$\Omega \sim 40\%$$

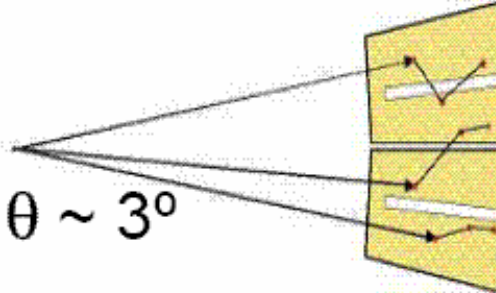


large opening angle
means poor energy
resolution at high
recoil velocity

Ge Sphere

$$\epsilon_{ph} \sim 50\%$$

$$N_{det} \sim 1000$$



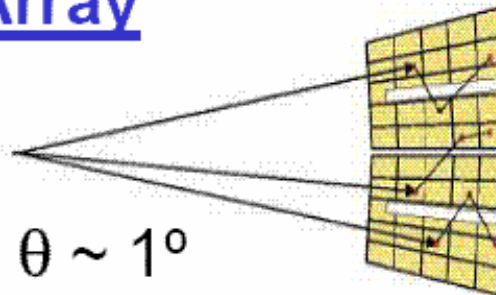
too many detectors
are needed to avoid
summing effects

Ge Tracking Array

$$\epsilon_{ph} \sim 50\%$$

$$N_{det} \sim 100$$

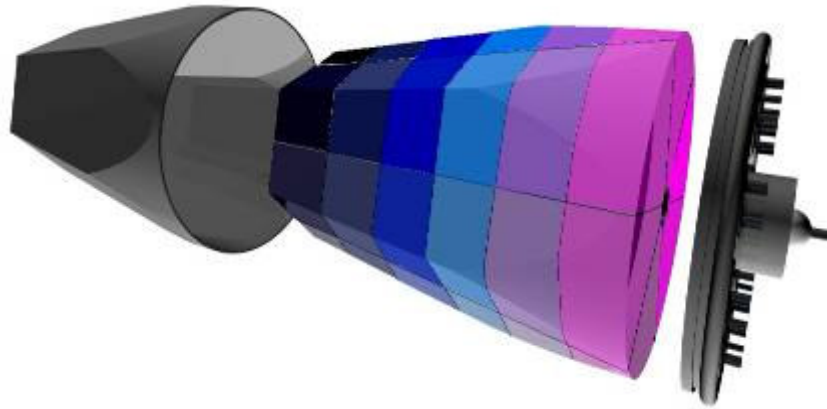
$$\Omega \sim 80\%$$



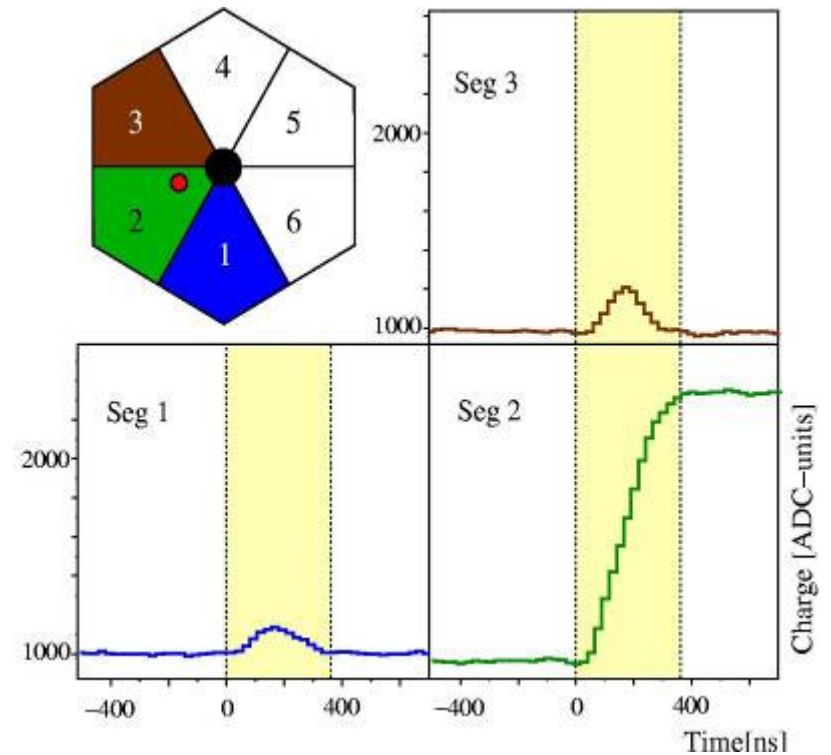
Combination of:

- segmented detectors
- digital electronics
- pulse processing
- tracking the γ -rays

Position-sensitive segmented Ge detector

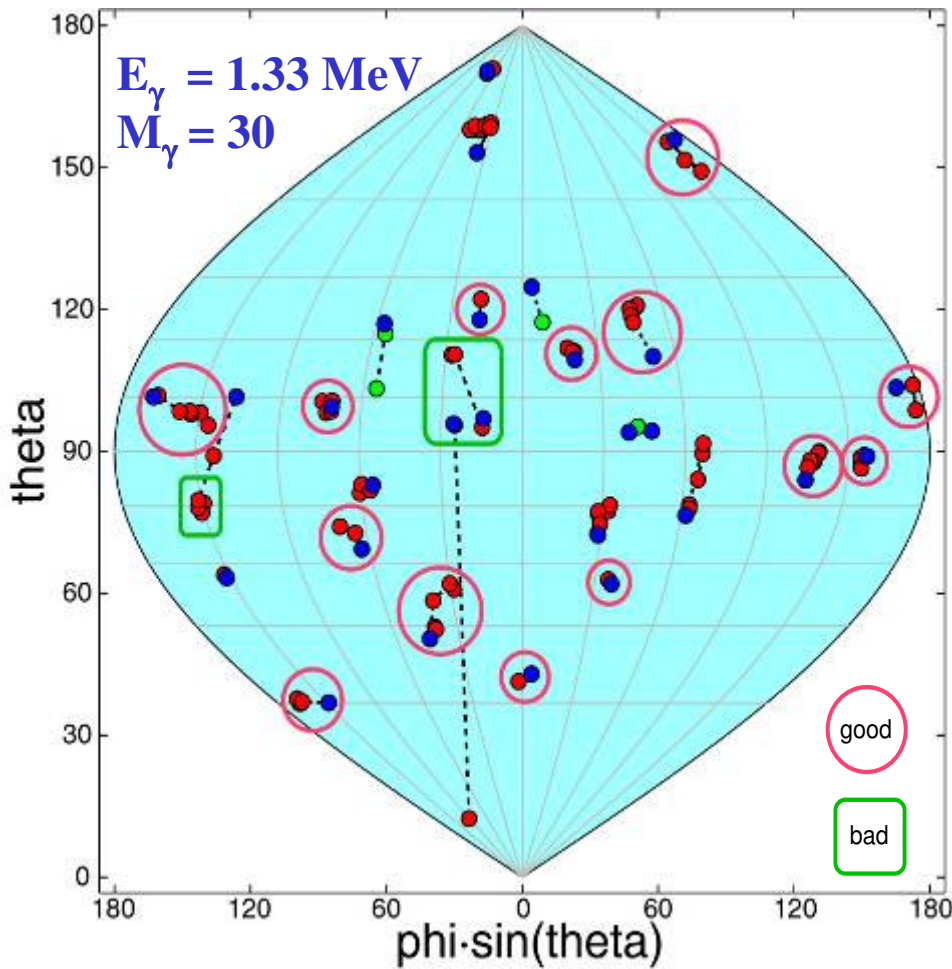


- encapsulated, coaxial Ge monocrystal
- 6 x 6 fold “electrical” segmentation
- “hexaconical” tapered shape



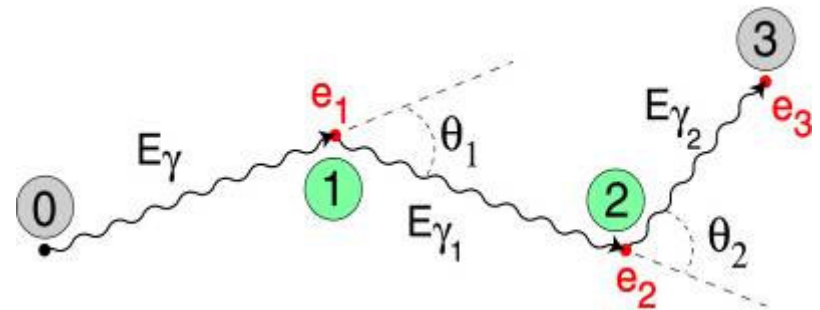
- Position information from pulse-shapes :
- signal rise time → radius
 - “image charges” → azimuth & depth
- ⇒ position determination in 3 dimensions
 $(\Delta x = \Delta y = \Delta z \sim 2-3 \text{ mm})$

Gamma-ray tracking



“Clusterisation” algorithm :

- Identify interaction point clusters
- Validate Clusters using the energy-angle relationship for Compton scattering
- check complete reconstruction

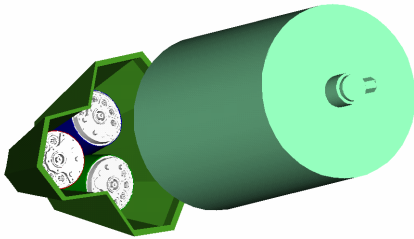
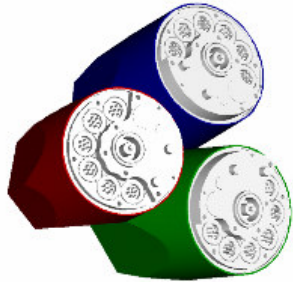


Look for a χ^2 minimum in the $N!$ permutations of the interaction points

- 0123 0132
- 0231 0213
- 0312 0321

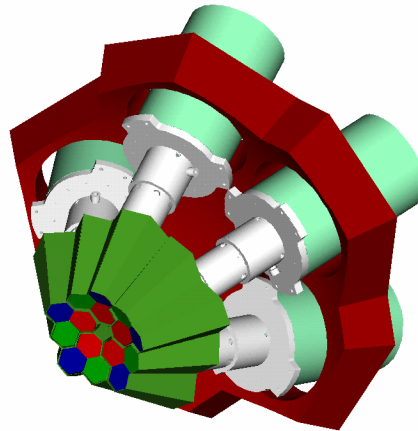
$$E_{\gamma'} = \frac{E_{\gamma}}{1 + \frac{E_{\gamma}}{m_0 c^2} (1 - \cos \vartheta)}$$

AGATA



triple-cluster module:

3 slightly different asymmetric crystals, 36-fold segmented, in a common cryostat (tests Aug./Sept. 2005)



AGATA demonstrator
result of R&D 2003-2008

5 triple-cluster modules

36-fold segmented crystals

540 segments

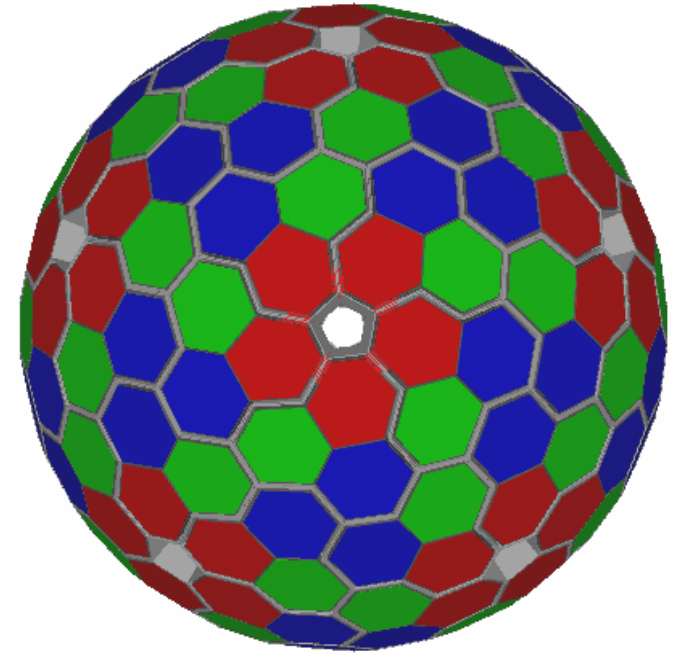
555 digital-channels

Eff. 3 – 8 % @ $M_g = 1$

Eff. 2 – 4 % @ $M_g = 30$

Full ACQ

with on line PSA and γ -ray tracking



Full AGATA (~2015)

180 Ge crystals

82% solid angle coverage

6480 segments

362 kg germanium

inner radius: 23 cm

singles rate ~50 kHz

6660 digital electronics channels

on-line PSA and tracking

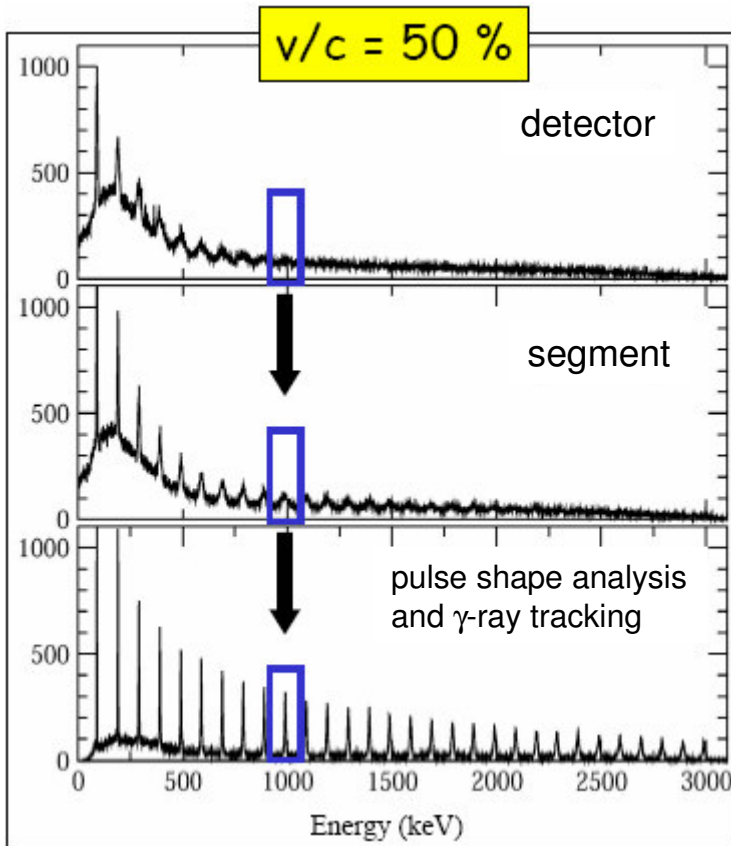
efficiency: 43% ($M_\gamma=1$), 28% ($M_\gamma=30$)

peak/total: 58% ($M_\gamma=1$), 49% ($M_\gamma=30$)

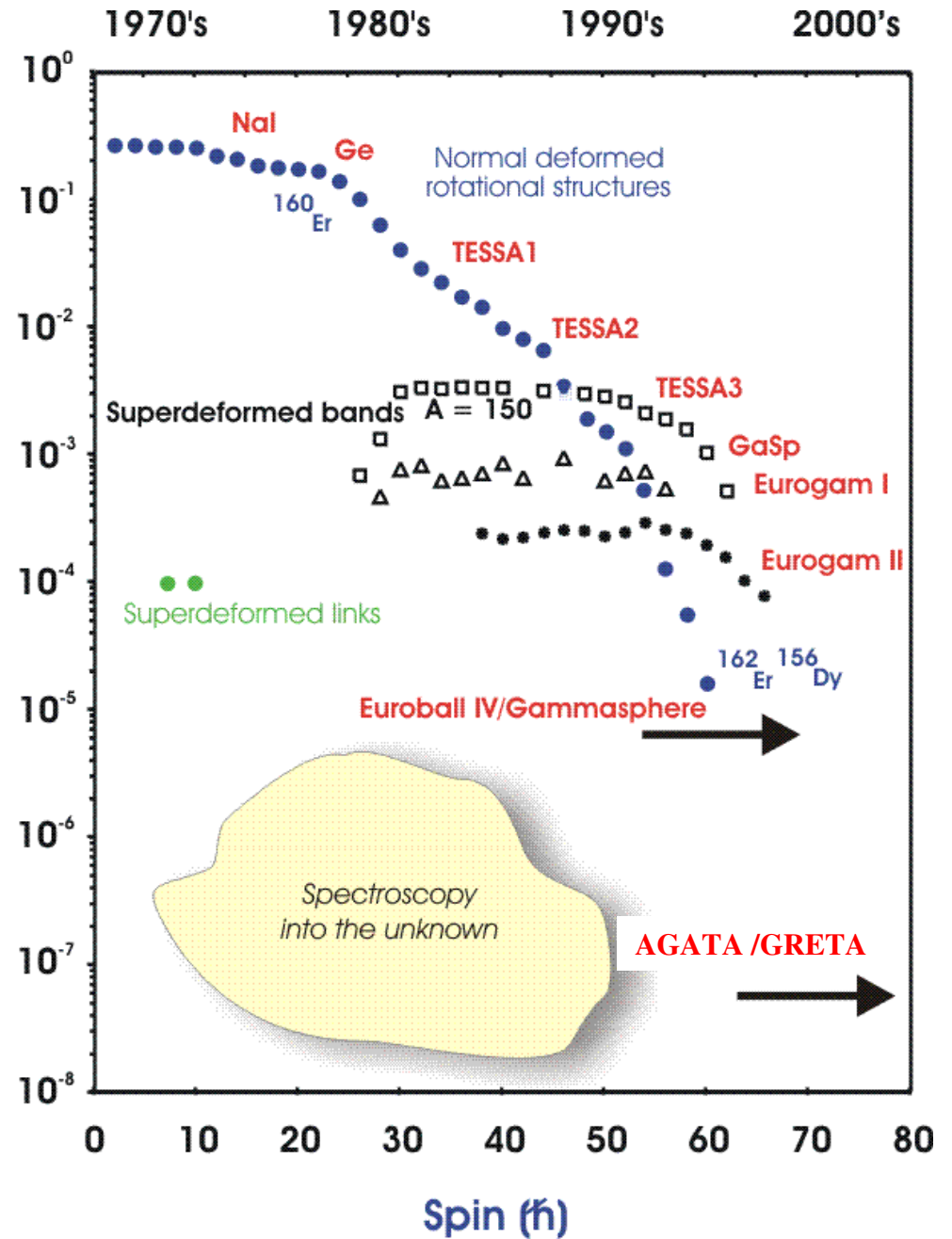
Performance of γ -ray tracking

experimental conditions

- low intensity beam
- high background
- large Doppler broadening
- high counting rates
- high γ -ray multiplicity



Fraction of Reaction Channel



The nucleus is always full of surprises



Instrumentation advances



New Science

fin